Design of a Co-Digestion Biogas Plant to Curb Deforestation-Case Study of Phalombe Secondary School in Malawi

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Abstract

Biogas technology is one of the renewable technologies that use biodegradable waste such as human waste (HW), agricultural waste, animal and food waste. Over 90% of the population in Malawi is heavily reliant on firewood as their primary source of energy for cooking. This results in deforestation, pollution of the environment, and great monetary expenditure to buy firewood, more especially by boarding schools. A co-digestion biogas plant that uses human, animal, agriculture, and canteen food waste has been designed. This study design was based on the use of HW and canteen food wastes (CFW) as the substrate for the biodigester to produce methane (CH₄) gas that could be used for cooking and lighting at Phalombe Secondary School in Malawi to replace firewood. With a school population of 757 people, design calculations/stimations were performed to find out the amount of HW and CFW required per day. A field survey at the school was carried out to appreciate the problem the school is facing so that a solution could be found. Based on factors such as energy demand at the school, availability of feedstock, size of the digester, biogas yield, life span of the biodigester, and availability of construction materials, the type of biogas plant suitable for this purpose has been selected and designed. A computer-aided design (Auto CAD) software was used for the drawing. These design parameters were arrived at through a baseline survey, observation methods, and literature reviews. Through a questionnaire, a detailed energy demand analysis was carried out from whose results a fixed
dome biogas plant of digester size 62 m$^3$, gasometer of size 19 m$^3$, and digestate collection tank size of 61 m$^3$ has been designed. The design came up with an amount of HW and CFW of 286 and 60 kg per day respectively making total organic raw materials of 346 kg per day. The macromolecular composition of the HW, CFW, and mixture of HW and CFW in terms of dry matter (DM) was 11%, 45% and 56% of carbohydrate, 3%, 15%, and 18% of protein, 15%, 40%, and 30% lipids, and 15%, 0%, and 15% of ash respectively. The substrate showed a high degradability of 90%. The simulation analysis showed that HW produced 185 m$^3$ per kg of biogas which represented 64% and 35.9% CH$_4$ and carbon dioxide (CO$_2$), CFW produced 58.9 m$^3$ per kg that represented 61.1% and 38.4% of CH$_4$ ad CO$_2$, and mixture produced 265 m$^3$ per kg contained 59% and 41% of CH$_4$ and CO$_2$ in 40 days respectively. A cost estimate of the design has been carried out to appreciate the economic viability of the biogas technology and is estimated at the US$5277. The cost of constructing a biogas plant at the school is less than what the school is spending currently on firewood and electricity, a recommendation has been made to adopt the technology to reduce the financial burden the school is facing.

**Subject Areas**
Renewable

**Keywords**
Biodigester, Co-Digestion, Phalombe, Human Waste, Curb Deforestation

**1. Introduction**
Biogas has been used in most parts of the world for cooking, heating, and lighting. In Africa, countries such as Kenya, Uganda, Ethiopia, Tanzania, Rwanda, Cameroon, Burkina Faso, and Benin have benefited from this technology through National Biogas programs initiated by their governments [1]. In Malawi, little has been done to promote this technology. Since access to electricity is still very low (10.8% in 2018 and projected to 12.7% in 2020) [2] [3]. Malawi’s main source of energy for cooking is firewood. Over 90% of the population in Malawi is heavily reliant on firewood as their primary source of energy for cooking. Most boarding secondary schools in Malawi depend on firewood as their main source of energy for cooking and heating water. This results in deforestation, pollution of the environment, and great monetary expenditure to buy firewood, more especially by boarding schools. Moreover, this places a financial burden on these schools due to the ever-increasing prices of firewood. One amongst such schools is Phalombe Boarding Secondary School. It is against this background that it was proposed to design a co-digestion biogas plant for use at Phalombe Boarding Secondary School. To generate more biogas, the temperature in the biodigester must be increased [4]. Methane-producing bacteria will operate most efficiently if temperatures in the biodigester are in the range of
30°C - 40°C for the mesophilic bacterial activity and 50°C - 60°C for the thermophilic bacterial activity [5]. The thermophilic temperature is responsible for methane production and is reached after a longer HRT (40 - 60 days). A longer HRT is favourable for the production of more methane gas than a shorter HRT which produces more hydrogen gas than methane [6]. A pH of 7.8 to 8.2 is preferred for methanogenic bacteria to digest the waste for the production of methane gas [7]. It is against this background that the simulation used a temperature of 55°C and pH of 7.8 (neutral) to calculate biogas production.

Phalombe district is located in a moderate to hot zone which has very good weather conditions for biogas production. Its monthly temperatures ranging from 25°C to 28°C but temperatures of more than 30°C are obtained in the hot summer season. The school enrolls 562 students and has around 195 members of staff including their dependents. This brings to a total number of 757 people. This number of people is enough to produce the human waste (HW) necessary to sustain the project. Furthermore, there are always a lot of food leftovers at the students’ canteen which can be used to co-digest with HW. The school is surrounded by three villages that are engaged in agricultural activities such as cattle and rice farming; from which we can also obtain daily feeding materials for this biogas plant. This biogas plant will use HW and canteen food wastes (CFW). To supplement these daily feeding materials, it will also use cow manure and agricultural wastes such as rice bran from the surrounding villages. Once the plant is installed at the school, it will curb deforestation and reduce the amount of money the school spends on cooking and lighting. Biogas offers a great alternative for fuel for cooking, heating, and lighting. It also addresses the issues of HW disposal [8]. It reduces the impacts on the environment which are mostly caused by deforestation and greenhouse gas emissions into the atmosphere. Biogas is a combustible mixture of gases that primarily consists of Methane (CH₄), Carbon dioxide (CO₂), and other trace elements [9] [10]. These gases are produced from the decomposition of organic wastes through anaerobic digestion (AD) [11]. There are several designs of biogas plants across the world and the designs depend on geographical location, availability of substrate, and climatic conditions [12]. Some biogas plants are fixed underground while others are constructed above the ground. Out of the different biogas digesters, the fixed dome model developed by China and the floating drum model developed by India has continued to perform well until today [1] [13].

The size of the digesters depends on the location, the number of households, and the amount of substrate available every day. Biogas plant models can be modified to suit the conditions of Malawi and Phalombe Secondary School in particular. This research is therefore aimed at seeking to modify the available performing biogas designs in Malawi that only use one type of substrate for digestion. The designed biogas plant will make use of HW and CFW to co-digest them to produce biogas for cooking and lighting at the school to replace firewood. Mzuzu University in Malawi under the faculty of Renewable Energy has been implementing fixed dome biogas projects in rural areas of Malawi using
sing digestion to preserve the carbon sink and switch to a cleaner and more ef-
cient alternative to firewood. One of the beneficiaries of this project is Ruguwa
Mhlanga Village, a rural village North East of Mzuzu [1]. Similarly, tubular po-
lyethylene biogas digesters have been developed and tested in Zomba in Malawi by
the Swedish University of Agricultural Sciences in conjunction with the University
of Malawi (Chancellor College) to cut back deforestation and support global cli-
mate change mitigation and adaptation. Waste management and agricultural
productivity can even be improved as a result of biogas technology. Further, the
event and promotion of biogas within the energy sector can propel the estab-
lishment of the latest enterprises thereby creating a full range of opportunities
for jobs and tiny and medium enterprises both in urban and rural areas [13].

With all the advantages above in mind, the construction of a biogas plant at
Phalombe Boarding Secondary School will be very vital. The biogas plant will
use HW from school toilets and CFW from student’s canteen as feedstock (sub-
strate) for co-digestion. The biogas plants that are currently in use in Malawi use
single digestion (only one type of feedstock). This research study aims at ad-
ressing this gap by introducing co-digestion. To supplement the feedstock, it
will also be using animal manure and crop residues such as rice straw/bran from
the surrounding communities. Phalombe is one of the highest rice-producing
districts in Malawi but does not make use of rice bran after rice milling. Millions
of tons of rice bran are not used and are either burned into ashes or just thrown
away. The district is also engaged in animal farming which includes goats, cows,
and pigs. From these farm animals, farm manure can be collected and used as a
daily feeding material/feedstock for the biogas plant. Therefore, the general ob-
jective of this study is to design an affordable co-digestion biogas plant for use at
Phalombe Secondary School in Malawi.

2. Materials and Methods

This study was carried out at Phalombe Secondary school. The school is 1 km
away from the central district of Phalombe and is situated 0.5 km away from
Michesi Hill Forest which is the other source of firewood for the school’s kitchen
activities. The researcher engaged the school head and its members of staff to
come up with the total energy demand (TED) at the school. The researcher also
engaged village heads to establish the availability of livestock that would provide
daily feeding material (substrate) for the biodigester at the school to supplement
the already available daily feeding material at the school. The village heads en-
gaged were Mbodi, Bokosi, and Seven. Also interviewed were owners of rice
mills around Phalombe Secondary School who could provide rice husks/bran for
free to be used for co-digestion.

2.1. Data Collection Methods

The data collection has been done through various methods including literature
reviews concerning biogas plant designs and biogas production using different
biodegradable wastes either as a single substrate or co-digested with other wastes,
questionnaires, interviews, and observation. Primary data was collected through a baseline survey that included a questionnaire and personal observations in and around Phalombe secondary school where the study was carried out.

Secondary data was collected through literature reviews that included books, journals/articles, and websites. Data gathered from the literature review was used to determine the type of biogas plant to be used at Phalombe Secondary School. The Floating drum, Fixed dome, and the Polythene tube biodigester are three main digesters used worldwide. Each type of the three biogas plants mentioned above was thoroughly evaluated and the best design suitable for use at Phalombe Secondary school was selected using the Ranking method. Data for daily feeding material (DFM) was collected from both surrounding households and the administrator of the school. Also collected were data on the number of times of cooking per day at the school, number of staff and students at the school, disposal of kitchen waste, and annual temperatures of Phalombe district. All this data was required to come up with an appropriate design of a biogas plant that could supply Phalombe Secondary School with the right amount of gas for cooking and lighting. Other design considerations were based on the hydraulic retention time (HRT) and total solids (TS) content in the manures. From the literature review, the TS value desired is 8% and HRT is greater than 20 days. From this information, a TS value of 8% and HRT of 40 days was used in the design calculations for the biogas plant to be constructed at Phalombe Secondary School.

2.2. Energy Demand Assessment

The energy demand assessment has been done through a questionnaire, interviews, and site visit, therefore, data for energy demand (ED) for cooking and lighting was also collected. This helped to know how much electrical energy (EE) per day was being used by the school for lighting in the school classrooms, staff houses, kitchen, laboratories, and hostels. Also collected were data on the amount of firewood the school was using per school term. The electrical energy demand (EED) and the ED for firewood were then summed up and converted into biogas equivalence. It was from this sum of ED that the calculations for the size of the biogas plant were based. The respondents of the questionnaire on EED at the school for lighting were the head teacher of the school and other members of staff on duty during evening study times at the school. On the demand for firewood, the respondent of the questionnaire was the head cook. The respondents for ED for lighting at staff houses of the school were the head teacher and his fellow members of staff who are housed in the school compound.

The EED requirement was based on EE used by the staff members for lighting in their houses, EE used in the classrooms and offices for lighting during study times, EE used in the laboratories, student hostels, student kitchen, dining hall/canteen, and storeroom where kitchen facilities are kept. The EED in kilowatt-hour (kWhr) was summed up and converted to ED in Joules per day. This was then being converted to biogas flow rate per day (m³ per day) as biogas equivalent from ED. Wood energy demand was calculated based on the amount
of firewood the school is using in an academic term or year. This was then converted to the amount of firewood the school uses per day. Using the firewood to biogas-equivalent conversion, it came up with the amount of biogas in cubic meter (m³) required per day (m³ per day) for cooking in the kitchen as an alternative source of energy. The total amount of biogas required per day at the school for cooking and lighting was calculated by summing up the biogas equivalence for electrical lighting and firewood to biogas equivalent in m³ per day. Using the sum of biogas equivalence per day required at the school for cooking and lighting, the amount of HW required per day to be fed into the digester was determined. Based on the total amount of substrate to be fed into the biodigester (HW and CFW) and an estimated HRT of 40 days, the sizing of the biodigester, Gasometer, and the Digestate Collecting Tank was carried out. Detailed calculations are shown in the next section (section 2.5.3).

2.3. Selection of the Type of Biogas Plant

The tool used for this method was literature reviews on the common types of biogas plants in use globally for biogas production namely the Floating drum, Fixed dome, and the Polythene tube biodigester. The information of these types of biogas plants was gathered in terms of construction methods, availability of materials used in construction, the durability of materials, gas pressure holding ability, gas leakage through walls, gas pressure capacity, their life span, gas holding capacity, maintenance costs, their versatility in terms of construction (in high or low weather conditions), methane emission from each type, and other factors that should be considered when designing a biogas plant were sourced through this literature search. Each type of the three biogas plants mentioned above was thoroughly evaluated and the best design suitable for use at Phalombe Secondary school was selected. Based on literature detailed information about each of the three types of biogas plants, the fixed dome was selected [12] [14]. Although high skilled labor is required in the construction of a fixed dome biodigester, it has several advantages over the other types of biodigesters in AD [15]. Therefore, it was the preferred choice in the design selection. It consists of a digester with a fixed, non-movable gas holder that sits on top of the digester. When gas production starts, the slurry is displaced into the overflow tank. Gas pressure increases with the volume of the gas stored and the height of the difference between the slurry level in the digester and the slurry level in the compensation tank. There are no rusting steel parts in its construction hence long life (20 years or more). The plant is constructed underground, protecting it from physical damage and saving space. The underground digester is protected from low temperatures at night and cold seasons [12] [16].

2.4. Statistical Analyses of Results

A Biogas software called Online Biogas App (OBA) was used to simulate biogas production from the amount of substrate that was calculated/estimated in the
design. The biogas yield was calculated from stoichiometry calculation, based on substrate compositions using OBA. Graphical presentations were drawn from the averaged results. All statistical work was done in Microsoft Excel 2016 (Microsoft Corporation, USA) and Past statistical software (version 4.03).

2.5. System Analysis and Design

2.5.1. Design of the Biogas Plant

Calculations for the sizing of the Biodigester tank, Gasometer, Digestate collection tank, and mixing tank were performed based on ED and available substrate at the school. These calculations were based on the fixed dome biogas plant which was selected as the best design suitable for use at Phalombe Secondary School. The information used in the design was taken from the following literature [12] [16]-[21].

2.5.2. Designing the Size of a Biogas Plant

All biogas plants have two useful parts that help to design the size of biogas plants. These parts are the digester which is the tank body and the gasometer which is commonly known as the dome. So for design calculations, these two main parts are considered. Other parts that have to be calculated are the sizing of the mixing tank and the digestate tank. The volume/size/capacity of a biogas plant depends on the HRT and the DFM. The DFM consists of organic biodegradable materials and water to be mixed with it. In this research, DFM includes HW, cow dung, FCW, and wastewater. Rice bran/straw was used for improving the C/N ratio of HW [8] [11]. Phalombe secondary school has an enrolment of 562 students and 195 members of the staff including their dependents. According to literature research, one adult human produces an average of 0.5 kg of HW [22]. For a simple biogas digester, the HRT is at least 40 days. But practical experience has shown that HRT can reach as far as 60 to 100 days if there is a shortage of daily feeding material. However, long HRT can increase the amount of gas produced by the biodigester by 40% of the initial production [23]. Since this study’s main objective was to come up with a big plant required to produce a large quantity of biogas to satisfy the needs of the school, and HRT was to be estimated at 40 days (minimum).

2.5.3. Design Calculations

1) Energy demand calculations

To come up with the correct size of the biogas plant that can serve the two purposes of cooking and lighting at the school, detailed calculations were carried out to determine the ED at the school as follows:

a) Classroom demand (for studies)

Number of classrooms = 8.

Number of 22 watts (W) fluorescent bulbs per classroom = 2.

Lighting time (from 6 pm to 10 pm) = 4 hours (h).

Therefore, energy (E) required in kilowatt-hour (kWh) during study time
\[ E = 8 \times 2 \times 4 \times 22 / 1000 = 1.4 \text{kWh} \]  \hspace{1cm} (1)

b) Laboratories

Biology, Physics, and Chemistry labs 2 \times 22 \text{ W} fluorescent tubes each.
Lighting time (from 6 pm to 10 pm) = 4 h

\[ E = 3 \times 2 \times (22 \text{ W}) / 1000 = 0.4 \text{kWh} \]  \hspace{1cm} (2)

c) Student hostels

Number of hostels = 12.
Number of rooms per hostel = 10.
Each room uses 1 \times 22 \text{ W} fluorescent tube for 5 hours lighting (6 - 10 pm, 03:00-04:00 am). Therefore, the energy required in the student hostels, \( E \) is given by Equation (3)

\[ E = 12 \times 10 \times 5 \times (22 \text{ W}) / 1000 = 13.2 \text{kWh} \]  \hspace{1cm} (3)

Each hostel uses a 2 \times 22 \text{ W} security light (one inside and one outside). Therefore, the energy required for security lighting at the hostels is given by Equation (4)

\[ E = 2 \times 12 \times 10 \times (22 \text{ W}) / 1000 = 5.3 \text{kWh per day} \]  \hspace{1cm} (4)

Subtotal = (13.2 + 5.3)kWhr = 18.5 kWhr  \hspace{1cm} (5)

d) Staff houses

40 houses, 3 bulbs per house, 10 W with an average lighting period of 6 hours, \( E \) is given by Equation (6)

\[ E = 40 \times 3 \times 6 \times (10 \text{ W}) / 1000 = 7.2 \text{kWh per day} \]  \hspace{1cm} (6)

One security light of 22 W per house with a lighting period of 10 hours, \( E \) is given by Equation (7)

\[ E = 1 \times 40 \times 10 \times (22 \text{ W}) / 1000 = 0.8 \text{kWh per day} \]  \hspace{1cm} (7)

Subtotal = (7.2 + 0.8)kWhr = 8.0 kWhr  \hspace{1cm} (8)

e) Students Kitchen

Energy required for 3 \times 22 \text{ W} fluorescent tubes for 6 hours lighting and 2 \times 22 \text{ W} fluorescent tubes security lights for 10 hours is calculated using Equation (9) and (10)

\[ E = 3 \times 6 \times (22 \text{ W}) / 1000 = 0.4 \text{kWh per day} \]  \hspace{1cm} (9)

\[ E = 2 \times 10 \times (22 \text{ W}) / 1000 = 0.4 \text{kWhr per day} \]  \hspace{1cm} (10)

Subtotal = (0.4 + 0.4)kWhr per day = 0.8 kWhr  \hspace{1cm} (11)

f) Dining Hall

The energy required for 8 \times 22 \text{ W} fluorescent tubes for 2 hours is calculated as follow (12)

\[ E = 8 \times 2 \times (22 \text{ W}) / 1000 = 0.4 \text{kWh per day} \]  \hspace{1cm} (12)
g) Storeroom

The energy required for a 1 × 22 W fluorescent tube for 6 hours is given by Equation (13)

\[ E = 1 \times 6 \times (22 \text{ W}) / 1000 = 0.1 \text{ kWh per day} \]  

(13)

The total lighting energy required per day is summarized in Table 1.

2) Energy conversion

\[ 1 \text{ kWh} = 3.6 \times 10^6 \text{ Joules} \]  

(14)

Therefore,

\[ E = 30 \text{ kWh} = 3.6 \times 10^6 \text{ joules} \times 30 \text{ kWh} / 1 \text{ kWh} = 108 \text{ MJ per day} \]  

(15)

According to [14], a mixture of human and kitchen waste produce 0.15 m³ per kg of biogas.

Assuming that this is possible with an HRT of 40 days as per the researcher’s design and using the calorific value of biogas is 20 MJ per m³ (MJ: megajoule), then the daily biogas flow rate can be calculated as follows:

\[
\text{Daily Biogas flow rate} = \frac{\text{daily energy requirement}}{\text{calorific value of fuel}} \\
= \frac{108 \text{ MJ}}{20 \text{ MJ}} = 5.40 \text{ m³ per day}
\]  

(16)

3) Firewood to biogas equivalent

Phalombe Secondary School uses 52 tons of firewood in a school calendar. The school runs on three terms of 12 weeks each on average. 12 weeks is equal to 84 days.

Therefore, the number of tons of firewood required per day is given by Equation (17)

\[ 52 \times \frac{1}{(3 \times 84)} = 0.206 \text{ ton per day} \]  

(17)

\[ \text{but } 1 \text{ ton} = 1000 \text{ kilogram (kg)} \]  

(18)

Therefore, 0.206 ton per day = 1000 × 0.206 kg per day = 206 kg per day.

Table 1. Summary of energy demand at phalombe boarding secondary school.

<table>
<thead>
<tr>
<th>Section of School</th>
<th>ED (kWhr per day)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Classrooms</td>
<td>1.4</td>
</tr>
<tr>
<td>Laboratories</td>
<td>0.4</td>
</tr>
<tr>
<td>Student hostels</td>
<td>18.5</td>
</tr>
<tr>
<td>Staff houses</td>
<td>8.0</td>
</tr>
<tr>
<td>Students kitchen</td>
<td>0.8</td>
</tr>
<tr>
<td>Dining hall</td>
<td>0.4</td>
</tr>
<tr>
<td>Storeroom</td>
<td>0.1</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>29.6 ≈ 30</strong></td>
</tr>
</tbody>
</table>
According to Biogas Digest Volume III, Biogas applications and product development, biogas costs and benefits, ISAT, GTZ [24].

\[ 1 \text{ m}^3 \text{ biogas} = 5.5 \text{ kg of firewood} \]  \hspace{1cm} (19)

\[ \text{So if} \quad 5.5 \text{ kg} = 1 \text{ m}^3 \text{ of biogas} \]  \hspace{1cm} (20)

Therefore, 206 kg of firewood = 1 × 2065.5 m³ of biogas = 37.45 m³ per day.

Therefore, the total amount of biogas (Y) required at Phalombe Secondary School for lighting and cooking is calculated using Equation (21)

\[ Y = \left( 5.40 \text{ m}^3 + 37.45 \text{ m}^3 \right) \text{per day} = 42.85 \text{ m}^3 \text{ per day} \]  \hspace{1cm} (21)

The quantity of HW (Q_{HW}) required is given by the amount of gas produced per day over gas production per kg from HW [25].

\[ Q_{HW} = \frac{42.85}{0.15} \text{ kg} = 286 \text{ kg per day} \]  \hspace{1cm} (22)

With the number of people at Phalombe secondary being 757 and on average a human being produces 0.5 kg of HW, we expect the amount of HW produced in a day to be

\[ 0.5 \times 757 \text{ kg} = 378.5 \text{ kg per day} \]  \hspace{1cm} (23)

This amount of HW exceeds the requirement per day. Therefore, Phalombe Secondary School has enough HW to supply the digester to be constructed at the school.

From this organic material (ORM) will be added CFW of 60 kg per day, therefore,

\[ \text{ORM} = (286 + 60) \text{ kg per day} = 346 \text{ kg per day} \]  \hspace{1cm} (24)

Add 1:1 ratio of ORM to Water becomes

\[ 346 \text{ kg per day} \times 2 = 692 \text{ kg per day substrate} \]  \hspace{1cm} (25)

And according to [18], TS = 16% of the mass of substrate

\[ = 16\% \times 692 \text{ kg per day} = 110.72 \text{ kg per day} \]  \hspace{1cm} (26)

Quantity (Q) of the substrate is given by Equation (27)

\[ Q = \text{TS}/8\% \]  \hspace{1cm} (27)

Therefore, the required Q = 110.72/0.08 kg per day = 1384 kg per day.

2.5.4. Sizing of the Digester, Gasometer, Digestate Collection Tank, and Mixing Tank

1) Sizing of the Digester

Given \( Q = 1384 \text{ kg per day} \), \( \text{HRT} = 40 \text{ days} \) and density of slurry = 1000 kg per m³.

The operating volume of the digester (\( V_0 \)) is calculated using Equation (28),

\[ V_0 = Q \times \text{HRT}/1000 \text{ m}^3 = 1384 \times 40/1000 \text{ m}^3 = 55.36 \text{ m}^3 \]  \hspace{1cm} (28)

But \( V_0 = 90\% \) of \( V_T \) where \( V_T \) is the total volume of the digester [25].

Therefore \( V_T = V_0/90\% = 55.36/0.9 \text{ m}^3 = 61.51 \text{ m}^3 \)
According to [18], the height of a digester is 4 times its radius \( r \) i.e. \( h = 4r \), but

\[
V_g = \pi r^2 h = \pi r^2 \times 4r = 4\pi r^3
\]

(29)

\[
V_g = \pi r^3 + 4\pi = r^3
\]

(30)

\[
r = \sqrt[4]{61.51/4\pi} = 1.698 \text{ m} = 1.7 \text{ m}
\]

Diameter of the digester becomes \( 2r = 2 \times 1.7 \text{ m} = 3.4 \text{ m} \)

Height of the digester becomes \( 4r = 4 \times 1.7 \text{ m} = 6.8 \text{ m} \)

2) Sizing the Gasometer

According to [15] the volume of biogas from cow dung per kg = 0.000616 m\(^3\). According to [26] biogas yields (m\(^3\) per kg daily solids) for cow manure and HW are 0.3 and 0.4 respectively. The difference between the two yields is very small. The yield from HW will be improved by the addition of CFW as per the researcher’s design of the biogas plant. For this reason, a value of 0.000616 m\(^3\) is used to calculate the volume \( V_g \) of the gasometer as follows:

\[
V_g = \text{Volume of biogas per day} \times \text{DFM} \times \text{HRT}
\]

(31)

where Volume of biogas per day = 0.000616 m\(^3\), DFM = 692 kg per day and HRT = 40 days, then

\[
V_g = 0.000616 \text{ m}^3 \text{ per kg} \times 692 \text{ kg per day} \times 40 \text{ days} = 17.05 \text{ m}^3
\]

An allowance of 10% is given.

Therefore,

\[
V_g = V_g' + \left( 0.1 \times V_g \right) = 17.05 + \left( 0.1 \times 17.05 \right) \text{ m}^3 = 18.76 \text{ m}^3
\]

(32)

In practice, the ratio \( V_g : V_0 \) where \( V_0 \) is the operating volume of the digester, which is commonly used is between 1:3 and 1:5 [18] [27] [28]. According to this design, the ratio is 18.76:55.36 = 1:3, so the design is feasible.

Taking the height, the gasometer to be 4 times its radius, the diameter, and height of the gasometer can be calculated as follows:

\[
V_g = \pi r^2 h \quad \text{where} \quad h = 4r
\]

(33)

\[
V_g = \pi r^2 \times 4r = 4\pi r^3
\]

(34)

\[
r = \sqrt[4]{V_g/4\pi} = \sqrt[4]{18.75/4\pi} = 1.14 \text{ m}
\]

\[
D = 1.14 \text{ m} \times 2 = 2.28 \text{ m}
\]

\[
H = 1.14 \text{ m} \times 4 = 4.56 \text{ m}
\]

3) Sizing the Digestate collection Tank (Overflow tank)

The Digestate tank can take the shape of a rectangle, square, or circle. For the digestate collection tank, a 10% allowance is given for mixing.

a) Circular tank sizing

The volume of collection tank (\( V_c \)),

\[
V_c = V_o + \left( 0.1 \times V_o \right) = 55.36 + \left( 0.1 \times 55.36 \right) = 60.89 \text{ m}^3
\]

(35)
The height of the tank is 1.5 times its radius [18], but
\[ V_c = \pi r^2 h \]  
(36)

Therefore,
\[ V_c = \pi r^2 \times 1.5r \]  
(37)
\[ V_c = \pi r^3 \times 1.5 \]
\[ 60.89 = 1.5\pi r^3 \]
\[ r^3 = 40.597 \text{ m} \]
\[ r = 3.44 \text{ m} \]
\[ D = 6.88 \text{ m} \]
\[ h = 1.5r = 1.5 \times 3.44 \text{ m} \]
\[ h = 5.16 \text{ m } \approx 5.0 \text{ m} \]

b) For a square base tank, the volume (V) will remain the same \textit{i.e.} 60.89 m$^3$ and height of 5.0 m

\[ V = L^2 \times H \]  
(38)

Therefore,
\[ 60.89 \text{ m}^3 = 5.0L^2 \]
\[ L^2 = 60.89/5.0 = 12.178 \text{ m}^2 \]
\[ L = \sqrt{12.178} \text{ m}^2 = 3.5 \text{ m} \]

4) **Sizing mixing tank for kitchen wastes/agriculture waste/cow dung**

Since the tank will be accommodating 60 kg of kitchen wastes per time, the following dimensions have been suggested to be reasonable:

- Depth of mixing tank = 1.0 m
- The diameter of mixing tank = 0.9 m

The volume of the mixing tank = \( \pi r^2 h = \pi \times (0.3 \text{ m})^2 \times 1.0 \text{ m} = 0.28 \text{ m}^3 \)  
(39)

**Table 2** shows a summary of the sizing of the designed Fixed Dome Biogas plant.

2.5.5. Development of a Detailed Biogas Plant Drawing

Detailed drawings were produced to be used by the masonry builders when constructing the biogas plant. A computer-aided design (Auto CAD) software was used for the drawing biogas plant layout out Phalombe Boarding Secondary School as shown in **Figure 1** while **Figure 2** was sourced from Rwandan Standards Board. This is the standard fixed dome biogas plant that is used worldwide. The major dimensions in **Table 3** are from the calculations in the sizing of the Digester tank, Gasometer, Digestate tank, and the Mixing tank.

The detail drawing in **Figure 2** will be used by the masonry builders to construct a biogas plant at Phalombe Secondary School. The Mixing and Biodigester (digester) tanks are cylindrical while the Digestate tank is square.
Figure 1. Biogas plant layout.

Figure 2. Detail drawing of fixed dome biogas plant. Source: [16] [27] [28].
Table 2. Summary of sizing of the fixed dome biogas plant.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Volume (m³)</th>
<th>Height (m)</th>
<th>Radius (m)</th>
<th>Diameter (m)</th>
<th>Thickness (m)</th>
<th>Length (m)</th>
<th>Width (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Biodigester</td>
<td>61.51</td>
<td>6.80</td>
<td>1.70</td>
<td>3.40</td>
<td>0.32</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Gasometer</td>
<td>18.76</td>
<td>4.56</td>
<td>1.14</td>
<td>2.28</td>
<td>0.32</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Mixing tank (CFW)</td>
<td>0.57</td>
<td>0.90</td>
<td>0.45</td>
<td>0.90</td>
<td>0.15</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Digestate Tank</td>
<td>60.89</td>
<td>5.00</td>
<td>3.44</td>
<td>6.88</td>
<td>0.032</td>
<td>3.50</td>
<td>3.50</td>
</tr>
</tbody>
</table>

Table 3. Major dimensions of the fixed dome biogas plant.

<table>
<thead>
<tr>
<th>Component</th>
<th>Dimension (m)</th>
<th>Component</th>
<th>Dimension</th>
<th>Component</th>
<th>Dimension</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>3.50</td>
<td>E</td>
<td>6.80</td>
<td>J</td>
<td>6.80</td>
</tr>
<tr>
<td>B</td>
<td>3.50</td>
<td>F</td>
<td>1.70</td>
<td></td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>1.70</td>
<td>G</td>
<td>2.62</td>
<td></td>
<td></td>
</tr>
<tr>
<td>D</td>
<td>5.00</td>
<td>H</td>
<td>5.66</td>
<td></td>
<td></td>
</tr>
<tr>
<td>E</td>
<td></td>
<td>I</td>
<td>5.86</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

2.5.6. Design Cost Estimates

The size of the designed biogas plant was used to estimate the cost of building this biogas plant at the school. The costs of using firewood for cooking and electricity for lighting at the school were compared with that of building the designed biogas plant. Bills of quantities for the sized biogas plant were used to come up with the cost of constructing the biogas plant at the school. The bill of quantities for the 62 m³ biogas digester is shown in Table 4. Exchange rate: MK800 = US$1.

2.5.7. Simulation of Biogas Production Using Quantities of the Substrate in the Design

A Biogas software called Online Biogas App (OBA) was used to simulate biogas production from the amount of substrate that was calculated in the design. Three biogas production simulations were run (Figures 3-5) using:

1) HW only as a substrate
2) CFW only as a substrate and
3) Co-digestion of HW and CFW

The results for each simulation were then analyzed.

1) Design Simulation

This design simulation was based on the type of biomass, amount of biomass, the molecular composition of the biomass, PH in the biodigester, and the temperature required for methane gas production. This Biogas Simulation software was written and developed by [29] with assistance from Jon Katz.
Table 4. Bill of quantities for a 62 m³ biodigester.

<table>
<thead>
<tr>
<th>Item</th>
<th>Description</th>
<th>Qty</th>
<th>Unit</th>
<th>Unit Price ($)</th>
<th>Amount ($)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Accessories</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Black enamel paint</td>
<td>15</td>
<td>Liter</td>
<td>20.0</td>
<td>300.00</td>
</tr>
<tr>
<td></td>
<td>110 mm PVC Pipe</td>
<td>20</td>
<td>length</td>
<td>8.75</td>
<td>175.00</td>
</tr>
<tr>
<td></td>
<td>Watering can</td>
<td>3</td>
<td>NA</td>
<td>5.0</td>
<td>15.00</td>
</tr>
<tr>
<td></td>
<td>Flexible hose</td>
<td>600</td>
<td>m</td>
<td>0.38</td>
<td>228.00</td>
</tr>
<tr>
<td></td>
<td>Wheelbarrow heavy duty</td>
<td>2</td>
<td>NA</td>
<td>50.00</td>
<td>100.00</td>
</tr>
<tr>
<td></td>
<td>Thread tapes</td>
<td>12</td>
<td>NA</td>
<td>0.044</td>
<td>0.53</td>
</tr>
<tr>
<td></td>
<td>Shovels (excavation work)</td>
<td>4</td>
<td>NA</td>
<td>10.00</td>
<td>40.00</td>
</tr>
<tr>
<td></td>
<td>Hoes/handles (excavation work)</td>
<td>6</td>
<td>NA</td>
<td>4.38</td>
<td>26.28</td>
</tr>
<tr>
<td></td>
<td>Pails</td>
<td>3</td>
<td>NA</td>
<td>6.25</td>
<td>18.75</td>
</tr>
<tr>
<td></td>
<td>Black plastic sheet</td>
<td>2</td>
<td>NA</td>
<td>4.38</td>
<td>8.76</td>
</tr>
<tr>
<td></td>
<td>Butterfly valves</td>
<td>6</td>
<td>NA</td>
<td>6.88</td>
<td>41.28</td>
</tr>
<tr>
<td></td>
<td>G.I. Union</td>
<td>10</td>
<td>NA</td>
<td>0.63</td>
<td>6.30</td>
</tr>
<tr>
<td></td>
<td>G.I. Elbow</td>
<td>10</td>
<td>NA</td>
<td>0.63</td>
<td>6.30</td>
</tr>
<tr>
<td></td>
<td>G.I. Tee joint</td>
<td>10</td>
<td>NA</td>
<td>0.63</td>
<td>6.30</td>
</tr>
<tr>
<td></td>
<td>G.I. Socket</td>
<td>12</td>
<td>NA</td>
<td>0.63</td>
<td>7.56</td>
</tr>
<tr>
<td></td>
<td>G.I. Nipple</td>
<td>12</td>
<td>NA</td>
<td>0.63</td>
<td>7.56</td>
</tr>
<tr>
<td></td>
<td>G.I. Pipes</td>
<td>14</td>
<td>length</td>
<td>8.75</td>
<td>122.5</td>
</tr>
<tr>
<td></td>
<td>G.I. R. Bush</td>
<td>20</td>
<td>NA</td>
<td>0.63</td>
<td>12.60</td>
</tr>
<tr>
<td></td>
<td>Lime</td>
<td>10</td>
<td>kg</td>
<td>0.75</td>
<td>7.50</td>
</tr>
<tr>
<td></td>
<td>Paintbrush</td>
<td>4</td>
<td>NA</td>
<td>4.38</td>
<td>17.52</td>
</tr>
<tr>
<td></td>
<td>Wire brush</td>
<td>2</td>
<td>NA</td>
<td>4.38</td>
<td>8.76</td>
</tr>
<tr>
<td></td>
<td><strong>Subtotal</strong></td>
<td></td>
<td></td>
<td></td>
<td><strong>1156.50</strong></td>
</tr>
<tr>
<td>2</td>
<td>Building Materials</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Bricks</td>
<td>20,000</td>
<td>NA</td>
<td>0.025</td>
<td>500.00</td>
</tr>
<tr>
<td></td>
<td>Transport</td>
<td>NA</td>
<td>NA</td>
<td>50.00</td>
<td>50.00</td>
</tr>
<tr>
<td></td>
<td>Cement (50kg)</td>
<td>60</td>
<td>Bags</td>
<td>10.00</td>
<td>600.00</td>
</tr>
<tr>
<td></td>
<td>Transport</td>
<td>NA</td>
<td>NA</td>
<td>50.00</td>
<td>50.00</td>
</tr>
<tr>
<td></td>
<td>Quarry stones</td>
<td>12</td>
<td>Tons</td>
<td>10.63</td>
<td>127.56</td>
</tr>
<tr>
<td></td>
<td>Transport</td>
<td>NA</td>
<td>NA</td>
<td>10.00</td>
<td>10.00</td>
</tr>
<tr>
<td></td>
<td>Fine Sand</td>
<td>4</td>
<td>Tons</td>
<td>2.50</td>
<td>10.00</td>
</tr>
<tr>
<td></td>
<td>Transport</td>
<td>NA</td>
<td>NA</td>
<td>18.75</td>
<td>18.75</td>
</tr>
<tr>
<td></td>
<td>Course sand</td>
<td>10</td>
<td>Tons</td>
<td>6.25</td>
<td>62.50</td>
</tr>
<tr>
<td></td>
<td>Transport</td>
<td>NA</td>
<td>NA</td>
<td>10.00</td>
<td>10.00</td>
</tr>
<tr>
<td></td>
<td><strong>Subtotal</strong></td>
<td></td>
<td></td>
<td></td>
<td><strong>1388.81</strong></td>
</tr>
</tbody>
</table>
### Other Costs

<table>
<thead>
<tr>
<th>Description</th>
<th>Qty</th>
<th>Unit</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Shuttering materials</td>
<td>60</td>
<td>pcs</td>
<td>75.00</td>
</tr>
<tr>
<td>Transport</td>
<td></td>
<td></td>
<td>37.50</td>
</tr>
<tr>
<td>Outlet covers (student and staff kitchens)</td>
<td>2</td>
<td>NA</td>
<td>8.76</td>
</tr>
<tr>
<td>Training of biogas users</td>
<td>2</td>
<td>days</td>
<td>125.00</td>
</tr>
<tr>
<td><strong>Subtotal</strong></td>
<td></td>
<td></td>
<td>246.26</td>
</tr>
</tbody>
</table>

### Labour

<table>
<thead>
<tr>
<th>Description</th>
<th>Qty</th>
<th>Unit</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mason (skilled)</td>
<td>2</td>
<td>NA 5.00 per day for 30 days</td>
<td>300.00</td>
</tr>
<tr>
<td>Casual labour (water/construction)</td>
<td>6</td>
<td>NA 37.5</td>
<td>225.00</td>
</tr>
<tr>
<td>Plumber</td>
<td>2</td>
<td>NA 5.00 per day for 10 days</td>
<td>100.00</td>
</tr>
<tr>
<td><strong>Subtotal</strong></td>
<td></td>
<td></td>
<td>625.00</td>
</tr>
</tbody>
</table>

### Administration

<table>
<thead>
<tr>
<th>Description</th>
<th>Qty</th>
<th>Unit</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Board &amp; Lodgings</td>
<td>1</td>
<td>NA 25.00 per day for 30 days</td>
<td>750.00</td>
</tr>
<tr>
<td>Communication</td>
<td>1</td>
<td>NA 1.45 per day for 30 days</td>
<td>43.50</td>
</tr>
<tr>
<td>Consultation, reporting, supervision fee</td>
<td>1</td>
<td>NA 21.00 per day for 30 days</td>
<td>630.00</td>
</tr>
<tr>
<td>Transport/fuel</td>
<td>1</td>
<td>NA 12.50 per day for 30 days</td>
<td>375.00</td>
</tr>
<tr>
<td>Survey</td>
<td>1</td>
<td>NA 31.25 per day for 2 days</td>
<td>62.50</td>
</tr>
<tr>
<td><strong>Subtotal</strong></td>
<td></td>
<td></td>
<td>1861.00</td>
</tr>
</tbody>
</table>

**Grand Total** 5277.57

NA: not applicable, Qty: quantity, $: USA dollar, MK: Malawian Kwacha, GI: Galvanized Iron.

### 2) Inputs and outputs for OBA simulation Software

The inputs for this simulation process are as follows:

a) Substrate composition (%)

b) Mass of the substrate (kg)

c) Substrate biodegradability (%DM)

d) Substrate partitioning to cell synthesis (%)

e) Reactor pH and

f) Reactor temperature (˚C)

The outputs are as follows:

a) Methane production

b) Carbon dioxide production

c) Nitrogen production and other impurities

d) Total Biogas production

This biogas plant uses HW as well as CFW as biomass material for feeding the biodigester. The parameters for each type of biomass are tabulated in Table 5.
Table 5. Parameters for simulation of biogas production.

<table>
<thead>
<tr>
<th>Biomass</th>
<th>Quantity in kg</th>
<th>Macromolecular composition (%DM)</th>
<th>The temperature in the digester with HRT of 40 days</th>
<th>pH in the digester</th>
</tr>
</thead>
<tbody>
<tr>
<td>CFW</td>
<td>60</td>
<td>Carbohydrate (45%)</td>
<td>55°C</td>
<td>7.5</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Proteins (15%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Lipids (40%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>HW</td>
<td>286</td>
<td>Carbohydrates (11%)</td>
<td>55°C</td>
<td>7.5</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Water (65%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Ash (15%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Fats (15%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Nitrogen (3%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Protein (3%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Co-digestion</td>
<td>346</td>
<td>Carbohydrate (56%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Protein (18%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Ash (15%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>Lipids (30%)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

3) Results of simulation

a) Simulation of biogas production from HW

The amount of HW whose mass was 286 kg as the amount of organic material in the design was used as input into the digester. The macromolecular composition (%DM) of the HW was 11% carbohydrate, 3% protein, 15% lipids, and 15% ash (Figure 3). Since HW are highly biodegradable, the substrate degradability was at 90%. The digester pH was 7.5 with a mesophilic temperature of 55°C. Figure 3 shows the results of theoretical gas production using HW.

b) Simulation of biogas production from CFW

The amount of CFW whose mass was 60 kg as the amount of organic material in the design was used as input into the digester. The macromolecular composition (%DM) of the CFW was 45% carbohydrate, 15% protein, 40% lipids, and 0% ash (Figure 4). Since CFW are highly biodegradable, the substrate degradability was at 90%. The reactor pH was 7.5 with a mesophilic temperature of 55°C. Figure 4 shows the results of theoretical gas production using CFW.

c) Simulation of biogas production using co-digestion of HW and CFW

The amount of CFW whose mass was 60 kg was mixed with 286 kg of HW making a total co-digestion substrate of 346 kg as amount of organic material in the design was used as input into the digester. The macromolecular composition of the mixture was 56% carbohydrate, 18% protein, 30% lipids, and 15% ash. Since both HW and CFW are highly biodegradable, the substrate degradability was estimated at 90%. The reactor pH was 7.5 with a mesophilic temperature of 55°C. Figure 5 shows the results of theoretical gas production using co-digestion of HW and CFW.
Figure 3. Theoretical biogas production from HW.

Figure 4. Theoretical biogas production from CFW.

Figure 5. Theoretical biogas production from co-digestion of HW and CFW.
3. Results and Discussions

This section presents the results of the design including simulation of biogas production, comparison of the results with existing literature, discussion of the feasibility of the design, cost comparison between the design, and the continued use of firewood as the source of energy for cooking at Phalombe Secondary School. The study design was based on the use of HW and CFW as the substrate for the biodigester to produce methane gas that could be used for cooking and lighting at Phalombe Secondary School to replace firewood. With a school population of 757 people, design calculations/estimations were performed to find out the amount of HW required per day. The design came up with an amount of HW as 286 kg per day. An estimated 60 kg of CFW per day was used, making a total ORM of 346 kg per day. These wastes were co-digested for biogas production. Based on the ED at the school, a 61 m³ biogas plant that could co-digest these wastes was designed using theories from the literature [18] [19] [20] [21] [30] [31].

3.1. Simulation of the Design

Using HW and CFW separately as substrates and then using the mixture as substrate simulations were run (Figures 3-5). The results were as follows Simulation 1: Theoretical biogas production from HW, Simulation 2: Theoretical biogas production from CFW, and Simulation 3: Theoretical biogas production from co-digestion of HW and CFW as shown in Table 6, Table 7, and Table 8 respectively.

Table 6. Results of Simulation 1 from HW.

<table>
<thead>
<tr>
<th>Input</th>
<th>Quantity (kg)</th>
<th>Macromolecular composition (%DM)</th>
<th>Substrate degradability (%)</th>
<th>The temperature in the digester with HRT of 40 days</th>
<th>pH in the digester</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>HW</td>
<td>286</td>
<td>Carbohydrates 11% Ash 15% Lipids 15% Protein 3%</td>
<td>90</td>
<td>55°C</td>
<td>7.5</td>
<td>The standardized volume of CH₄ was 118,000 L per kg (18 m³ per kg) A fraction of CH₄ produced was 64% Mole fraction of CH₄ in dry biogas was 64% The volume of CO₂ was 66,400 L per kg (66.4 m³ per kg) The volume of biogas produced was 185,000 L per kg (185 m³ per kg)</td>
</tr>
</tbody>
</table>

Table 7. Results of Simulation 2 from CFW.

<table>
<thead>
<tr>
<th>Input</th>
<th>Quantity (kg)</th>
<th>Macromolecular composition (%DM)</th>
<th>Substrate degradability (%)</th>
<th>The temperature in the digester with HRT of 40 days</th>
<th>pH in the digester</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>CFW</td>
<td>60</td>
<td>Carbohydrates 45% Ash 0% Lipids 40% Protein 15%</td>
<td>90</td>
<td>55°C</td>
<td>7.5</td>
<td>The standardized volume of CH₄ was 36,300 L per kg (36.3 m³ per kg) A fraction of CH₄ produced was 61.6% Mole fraction of CH₄ in dry biogas was 61.6% The volume of CO₂ was 22,600 L per kg (22.6 m³/kg) The volume of biogas produced was 58,900 L per kg (58.9 m³ per kg)</td>
</tr>
</tbody>
</table>
Table 8. Results of Simulation 3 from co-digestion of HW and CFW.

<table>
<thead>
<tr>
<th>Input</th>
<th>Quantity (kg)</th>
<th>Macromolecular composition (%DM)</th>
<th>Substrate degradability (%)</th>
<th>pH in the reactor</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>HW + CFW</td>
<td>346</td>
<td>Carbohydrates 56% Ash 15% Lipids 30% Protein 18%</td>
<td>90 55˚C 7.5</td>
<td>The temperature in the reactor with HRT of 40 days</td>
<td>The standardized volume of CH₄ 157,000 L per kg (157 m³ per kg)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>The fraction of CH₄ produced 59% Mole fraction of CH₄ in dry biogas 59%</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>The volume of CO₂ 109,000 m³ per kg (109 m³ per kg)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>The volume of biogas produced 265,000 L per kg (265 m³ per kg)</td>
</tr>
</tbody>
</table>

As described from the above tables, in simulation 1, the macromolecular composition of HW is 11%, 15%, 15%, and 3% for carbohydrates, Ash, Lipids, and Protein respectively. The total volume of biogas produced was 185,000 L per kg (185 m³ per kg) from which the amount of CH₄ produced was 118,000 L per kg (118 m³ per kg) representing 64% CH₄ from the total biogas produced. The amount of CO₂ produced was 66,400 L per kg (66.4 m³ per kg) representing 35.9% of the total gas produced. In simulation 2, the macromolecular composition of CFW is 45%, 0%, 40%, and 15% for carbohydrates, Ash, Lipids, and Protein respectively. The total volume of biogas produced was 58,900 L per kg (58.9 m³ per kg) from which the amount of CH₄ produced was 36,300 L per kg (36.3 m³ per kg) representing 61.6% CH₄ from the total gas produced. The amount of CO₂ produced was 22,600 L per kg (22.6 m³ per kg) representing 38.4% of the total biogas produced. In simulation 3, the macromolecular composition of the mixture was 56%, 15%, 30%, and 18% for carbohydrates, Ash, Lipids, and Protein respectively. The biogas production from co-digestion was high compared to HW and CFW digestion alone. However, the %CH₄ was low compared to them. The total volume of biogas produced was 265,000 L per kg (265 m³ per kg) from which the amount of CH₄ produced was 157,000 L per kg (157 m³ per kg) representing 59% CH₄ from the total gas produced. The amount of CO₂ produced was 109,000 L per kg (109 m³ per kg) representing 41% of the total biogas produced. All digesters presented high degradability with 90%.

3.2. Graphical Presentation and Analysis of the Results

Figure 6 and Figure 7 show pie charts and bar charts for the mole fraction of methane in dry biogas produced from co-digestion of HW and CFW.

The two graphs above show that single digestion of HW and CFW gives results of 64% and 61.6% respectively. When the two types of wastes are co-digested, they also give a fairly good result of 59%; a figure which is within the bracket of 55% - 65% CH₄ composition [30] [32]. From the simulation results 1 and 2, it can be seen that both substrates (HW and CFW) have the potential of producing enough biogas, with gas constituent compositions well comparable [33] [34]. Similarly, if the two substrates are co-digested, it can also be seen that enough CH₄ is well comparable to the constituent compositions presented by [32] [35].
The study [36] reported that the quantity and quality of biogas produced from biodegradable wastes largely depend on the nature and composition of the digester feedstock, temperature, organic loading rate, HRT, and C/N ratio. Proper management of the production process is also of great importance. This simulation exercise did not show the C/N ratio. In general, anaerobic microbes utilize carbon 25 - 30 times faster than nitrogen. So for efficient biogas production, the C/N ratio in the feedstock should be maintained at 20 - 30:1 [9] [37] [38]. This is the optimal value that can give out enough CH₄ gas. However, the designer of this study will use rice straw/bran to improve the C/N ratio during the anaerobic co-digestion of these wastes. Plants such as rice straw have a high percentage of carbon. For example, rice straw has a C/N ratio of 70:1 [39] such that it can be mixed with materials of low C/N ratio such as HW to maintain this optimum C/N ratio thereby increasing the CH₄ yield.

In the study of co-digestion of food waste and human excreta for biogas production [40], the value of biogas generated from a 40-liter laboratory-scale AD was 84,750 cm³ (0.08475 m³) comprising 58% CH₄ and 24% CO₂ with a mesophilic temperature range of 22°C - 30.5°C throughout the study. The simulated results of this design study obtained a CH₄ value of 59% which is slightly higher than what was found in this laboratory experiment. However, it was argued that
if a higher temperature, in this case, 50°C - 60°C was reached during the AD process a higher percentage value of CH₄ yield would have been maintained because methane methanogenic bacteria which is responsible for CH₄ production work efficiently at a mesophilic temperature of 30°C - 40°C and thermophilic temperature of 50°C - 60°C.

The study suggested the temperature of below 30°C slowed the development of methanogenic bacteria responsible for CH₄ production, hence low yield. In the study of [41] which was done to find out the yield of CH₄ when fruit vegetable waste and food wastes were digested separately in anaerobic conditions, methane yields for fruit vegetable waste and food waste in m³ per kg-VS were 35% and 60% respectively. This shows that there is potential in food wastes for CH₄ production. The results are also very comparable with the value obtained through simulation of biogas production in CFW (61.6%). A study of [42] reported that with a proper organic loading rate into the biodigester, the highest CH₄ production yield was 64%. Therefore, the simulation results of this design agree with those of this study. In the study of [18], a biodigester of volume 2.5 m³, gasometer volume of 0.7 m³, and digestate volume of 2.5 m³ were designed. With an HRT of 30 days, the total gas produced was 0.6108 m³, with maximum gas production of 0.037 m³ per day while the maximum biogas potential was 0.771 m³. This study has designed a biogas of volume 62 m³. Mathematically it can be proved that if a 2.5 m³ biodigester produces 0.037 m³ per day of biogas, then a 61 m³ biodigester will produce

\[
\left(\frac{0.037}{2.5}\right) m^3 \times \frac{62}{day} = 0.9176 m^3 \text{ per day of biogas} \quad (40)
\]

We can assume that with an HRT of 40 days as per this design, the volume of biogas produced in the digester will be more than 0.9176 m³ per day. Taking this value of 0.9176 m³ per day of biogas production, it means that to satisfy the demand of biogas at Phalombe secondary school which is currently at 42.85 m³ per day as per the researcher’s calculations, then this demand will be met within 47 days. But this is when the HRT is 30 days. Therefore, with an HRT of 40 days as per this design and the addition of rice straw to the substrate to improve the C/N ratio, then the demand can be met in less than 47 days. Therefore, this is a viable design. It must also be mentioned here that proper management of the whole biogas production process is very vital to achieve good results. Table 9 shows standard sizes (models) of fixed dome biogas plants used in Bangladesh.

According to Table 9 from these articles, we can compare the effective digester volumes and their respective rated biogas production with the new design. It can be seen that if a digester of volume 11.8 m³ produces 4.8 m³ of biogas per day, then from the new design of 62 m³ digester we can get:

\[
4.8 \text{ m}^3 \text{ per day} \times \left(\frac{62}{11.8}\right) = 25.2 \text{ m}^3 \text{ per day of biogas} \quad (41)
\]

The energy demand at Phalombe Boarding School is found to be 42.85 m³ per day. So at the rate of 25.2 m³ per day of biogas, this demand can be meet within a very short period.
3.3. Use of Conversion Factors for Biogas

If we use conversion factors in Figure 8 we can calculate \( \text{CH}_4 \) production from the biogas energy demand in this design.

From the table in Figure 8, 1 m\(^3\) of biogas = 0.65 m\(^3\) of CH\(_4\). Therefore the 25.2 m\(^3\) per day of biogas, CH\(_4\) produced will be 0.65 m\(^3\) \times 25.2 m\(^3\) per day = 16.38 m\(^3\) per day

From this value, it can be assumed that meeting the demand of 42.85 m\(^3\) per day can be achieved in 3 days after the HRT which in this design is 40 days. A study [45] proved that the best HRT is below 44 days because after this day biogas production becomes stable for some time and then drops. Also, studies [23] [25] showed the same effect of HRT. So, an HRT of 40 days for this design is a good time for digestion since by the time this day is reached production of biogas will be at its peak and the yield will be stable from the 44th day. Using the value of 25.2 m\(^3\) per day of dry biogas, the Mole fraction of CH\(_4\) in dry biogas can be calculated as follows:

Amount of dry biogas production per day = 25.2 m\(^3\).

Amount of Methane production per day = 16.38 m\(^3\).

Then the Mole fraction of CH\(_4\) in dry biogas will be \((16.38 \div 25.2) \times 100\% = 65\%\).

This value of the mole fraction of CH\(_4\) is approximately the same as the values found in the simulation results. Therefore, the volume of this biogas plant designed in this study will be able to meet energy demand at Phalombe Boarding Secondary school.

Table 9. Standard sizes of fixed dome biogas plants used in Bangladesh.

<table>
<thead>
<tr>
<th>Rated biogas production (m(^3)/day)</th>
<th>Effective digester volume (m(^3))</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Cow</td>
</tr>
<tr>
<td>1.2</td>
<td>3.0</td>
</tr>
<tr>
<td>1.6</td>
<td>3.8</td>
</tr>
<tr>
<td>2.0</td>
<td>4.8</td>
</tr>
<tr>
<td>2.4</td>
<td>5.8</td>
</tr>
<tr>
<td>3.2</td>
<td>7.8</td>
</tr>
<tr>
<td>4.8</td>
<td>11.8</td>
</tr>
<tr>
<td></td>
<td>Poultry</td>
</tr>
<tr>
<td>1.2</td>
<td>2.3</td>
</tr>
<tr>
<td>1.6</td>
<td>3.0</td>
</tr>
<tr>
<td>2.0</td>
<td>3.9</td>
</tr>
<tr>
<td>2.4</td>
<td>4.5</td>
</tr>
<tr>
<td>3.2</td>
<td>6.0</td>
</tr>
<tr>
<td>4.8</td>
<td>9.3</td>
</tr>
</tbody>
</table>

Source: study Article [43] [44].

Figure 8. Conversion factors for Biogas [43].
3.4. Economic Viability of the Design

Initial investment costs for a fixed dome biogas digester may seem to be high. However, it has more advantages than the other types of biogas plants namely. The amount of firewood used by Phalombe Secondary school per term is 60 tons. In three terms it uses 180 tons of firewood. One ton costs US$16.67. Therefore 180 tons cost US$3000. The school spends US$344 on electricity per month. A school term is approximately 4 months. This means that the school spends a total of US$1032 per term. The school has three academic terms, so the total amount of money spent on electricity in one academic year is approximately US$3096.

If these two expenditures are summed up (firewood plus electricity), the total expenditure in one academic year is approximately US$6096. The cost of installing a biogas plant at the school is approximately US$5277.57. This amount is less than the amount of money the school spends on firewood only in one academic year and it can be used to construct the biogas plant at the school. Therefore, the use of a biogas plant will not only curb deforestation in the district but also make great savings on the money the school is currently spending on firewood and electricity. This money can be used for other school requirements. Moreover, according to the Indian Agriculture Research Institute (ICAR), a single biogas plant with a capacity of 2.8 m$^3$ can save a woodland area of 0.12 ha per year. Therefore, with this designed biogas plant whose capacity is 62 m$^3$, it can save a forest area of 2.66 ha of woodland per year in the Phalombe district.

4. Conclusion

This research study has reviewed the common types of biogas plants that are used worldwide. There are several factors to be looked into when designing the type of biodigester to be used in a particular area. The choice of the right biodigester to be used in a particular area is of crucial importance when designing biogas plants. The design stage should take into consideration very important factors such as the type of substrate to be used, the continued availability of the substrate, availability of low-cost construction materials, the shape of the biodigester, weather conditions of the area where the biogas plant is going to be installed, the life span of the biogas plant which depends on the quality of the materials used in the construction and masonry skills. The results of this study have shown that human and canteen food wastes are good substrates to be co-digested in a biodigester to produce biogas which can be used for cooking and lighting hence the need to promote co-digestion biogas technology. In Malawi, there are no recycling technologies that can convert these wastes to something that does not pose health risks to humans once the wastes are disposed of. The use of clean technologies such as biogas for cooking and heating has been undermined by most developing countries. According to 2018 World Health Organization (WHO) report 3.8 million people, a year die prematurely from illness attributed to household air pollution which is caused by the inefficient use
of solid fuels such as firewood crop wastes, charcoal, coal, and kerosene in open fires for cooking and heating. Therefore, this premature death could be avoided if the use of methane gas for cooking is encouraged and adapted by governments because it is a clean, cheap, and renewable source of energy.

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**Competing Interests**

Authors have declared that no competing interests exist.

**References**


