

The Impact of a Heterogeneous Surface on Spatiotemporal Uncertainties of Sensible Heat, Latent Heat, and CO₂ Flux Measured over the Secondary Forest

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Abstract

The turbulent fluxes, such as sensible and latent heat fluxes and CO₂ flux, are globally observed over various terrestrial areas in order to understand the interaction between biosphere and atmosphere. Although the turbulent flux observations are generally performed on a horizontally homogeneous surface, the spatial distribution of the soil moisture is not homogeneous even on cultivated land with homogeneous vegetation, indicating that the development of each plant would be different and that the plant physiology, such as photosynthesis and growth, would be heterogeneous. In this study, to clarify the impact of a heterogeneous surface on spatiotemporal uncertainty of turbulent fluxes, a simultaneous flux observation experiment was conducted at different heights (20 m and 30 m) above the ground surface in a secondary seasonal tropical forest located in the Tak Province, Thailand. We defined ε as the spatial uncertainty of the turbulent flow flux, as proposed by Kim *et al.* (2011b) [1], and observed that ε of CO₂ flux was high, whereas ε of sensible and latent heat fluxes were low. This is likely to be caused by spatial uncertainty such as a heterogeneous surface. The CO₂ environment was heterogeneous; however, sensible and latent heat environments were homogeneous because the source area received insolation uniformly. Therefore, the analytical results for the CO₂ flux presented a different pattern from those exhibited by the analytical results of the latent and sensible heat fluxes.

Keywords

Eddy Covariance, Fractional Uncertainty, Monin-Obukhov Similarity Theory, Simultaneous Flux Observation

1. Introduction

Studies on turbulent diffusion have considerably progressed after Kolmogorov (1941) [2] derived a theoretical interpretation for the turbulent energy spectrum and after Obukhov (1946) [3] discovered that there was a scaling parameter for turbulent diffusion. Thereafter, Monin and Obukhov (1954) [4] derived a similarity theory based on the vertical wind speed in the surface boundary layer on a homogeneous surface, which can be referred to as the Monin-Obukhov similarity theory (MOST). The devices that can directly measure the turbulent diffusion, such as a sonic anemometer, were developed during the 1970s, with these devices initially being used for performing field-based flux experiments during the late 1980s. Various studies have focused on the interaction between the biosphere and atmosphere because of growing concerns over the impact of climate change on the terrestrial ecosystem. For example, the “FLUXNET” international network was established to monitor the heat, water, and CO₂ fluxes between the atmosphere and the land surface (Baldocchi *et al.* 2001 [5]). Further, the turbulence data are currently being collected at more than 500 flux observation sites from various vegetation zones, such as cultivated land and forests, across the world. Using these data, studies are being conducted to quantify the spatiotemporal variations in the global carbon stock and to estimate the global potential evapotranspiration based on biometeorology (Saegusa *et al.* 2008 [6]; Fisher and Baldocchi 2008 [7]). In addition, the collected heat, water, and CO₂ fluxes are extremely important for studies on the response of the terrestrial ecosystem to the regional differences in global climate change and for the development of models that are necessary to predict these responses.

The turbulent flux observations are generally performed on a horizontally homogeneous surface. There are two reasons for this observational constraint. First, because the eddy covariance method is used to calculate the fluxes from the observations, it can be assumed that material transport via advection can be ignored, and the vertical material transport is solely based on transport via turbulent flow. Second, the observed value is the weighted average of the material transported from the upwind source area via turbulent flow. Based on the wind direction and speed at the time of the observation, the impact on the source area may vary. If a surface area outside the study area is included in the source area, its impact will be included; therefore, the observation is conducted on a horizontally homogeneous surface.

However, the spatial distribution of the soil moisture is not homogeneous even on cultivated land with homogeneous vegetation, indicating that the development of each plant would be different and that the plant physiology, such as photosynthesis and growth, would be heterogeneous. Forests comprising diverse trees and forest floor vegetation are also heterogeneous in terms of plant physiology. The turbulent flux observations obtained from a heterogeneous surface exhibit different source areas based on the wind direction and speed, denoting that such a surface is theoretically unsuitable for obtaining such observa-

tions. However, there has been little discussion on the heterogeneity of the source areas despite considerable improvements in the performance and theoretical accuracy of the observational instruments over the previous three decades. Schmid and Lloyd (1999) [8] reported that it is important to conduct footprint analysis considering the observation altitude and atmospheric stability because the flux data obtained from a heterogeneous surface do not represent the footprint of the source area. In previous flux observations, in cases in which it was qualitatively confirmed that the MOST was established for analyzing the spectra of turbulent flow data for each time scale (30 minutes to two hours) without any issue, flux observation was empirically performed on the heterogeneous surfaces (Foken, 2006 [9]). However, even forest canopies that were considered to be homogeneous were reported to have spatiotemporal uncertainties in their sensible heat, latent heat, and CO₂ fluxes because of the impact of the ecosystem, and Oren *et al.* (2006) [10] showed that spatiotemporal uncertainty could lead to an error of a maximum of approximately 50% over a year while estimating the pure ecosystem CO₂ exchange using homogeneous vegetation. Therefore, it is important to quantitatively, rather than qualitatively, evaluate the impact of a heterogeneous surface on flux observations because the theoretical reliability of the flux observations is only valid up to a certain level of heterogeneity in the ground surface.

The eddy covariance method is the most extensively used method to measure the flux by directly measuring the turbulent diffusion. Recent studies have evaluated the spatiotemporal uncertainty (δ) generated during a flux analysis that uses the eddy covariance method. When the spatiotemporal uncertainty of the measured flux was initially discussed, it was suggested that δ comprised two elements. One element was the random error (δ_r), which was dependent on the stochastic nature of turbulent flow (Wesely and Hart, 1985 [11]) and was estimated from the standard deviation of a probability density function that followed a normal distribution centered on the true value when measured repeatedly. The other element was the systematic error (δ_s), which exhibited a certain impact on measurements (Abernethy *et al.* 1985 [12]). Therefore, majority of the studies on spatiotemporal uncertainty focused on both δ_r and δ_s .

However, Vickers and Mahrt (1997) [13] proposed that unsteady fluctuations in data are another element of δ , which was later recognized as the illegitimate error (δ_i). Therefore, it is assumed that δ includes δ_r , which is derived from the limitations of the measurement devices and the unpredictable fluctuations in the measurement conditions, δ_s , which is derived from the allowable error of the observational instruments and fundamental theory, and δ_i , which is derived from the human error and incorrect instrument operation (Figure 1, Kim *et al.* (2011b)) (Bevington and Robinson, 2003) [14].

Finkelstein and Sims (2001) [15] derived a method for estimating δ as the sampling error based on statistical analysis. As the most recent study that estimated δ using such statistical analysis, Kim *et al.* (2011b) evaluated the fractional uncertainty (ε), which can be obtained by dividing δ with the flux at

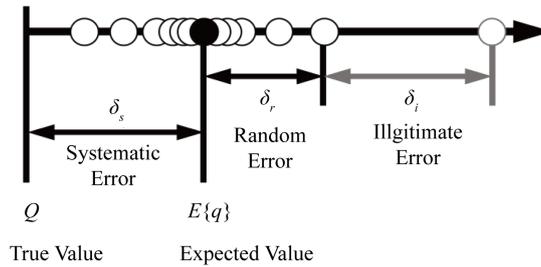


Figure 1. Schematic of the manner in which the true and expected values are related with the associated errors. The expected value that is obtained from the observations (open circles) is indicated by the black circle (Kim *et al.*, 2011b).

the time scale of the turbulent flow data. They further comparatively analyzed ε in various vegetation zones and denoted the potential of the ε -values for the sensible heat, latent heat, and CO₂ fluxes to converge to a same value irrespective of the spatiotemporal scale and the vegetation type.

The index (ε) that quantifies δ , which has been proposed by Kim *et al.* (2011b), is defined in Equation (1).

$$\varepsilon = \frac{\delta}{|F|} = \frac{\delta_r + \delta_s + \delta_i}{|F|} \approx \frac{\delta_r + \delta_i}{|F|} \tag{1}$$

δ_s approaches zero for well calibrated instruments.

$$\delta = \sqrt{\text{Var}\{q\}} \tag{2}$$

$$\text{Var}\{q\} = E\{(q - E\{q\})^2\} = E\{q^2\} - E^2\{q\} \tag{3}$$

$$E\{q\} = \lim_{N \rightarrow \infty} \frac{1}{N} \sum_{t=1}^N q_t \tag{4}$$

where F denotes the flux, q denotes the observation (where q_t ($t = 1, 2, \dots, N$) is the number of samples for a given observation at each time increment), E is the expected value. δ holds on Equation (2). According to Kim *et al.* (2011a [16] and 2015 [17]), δ_r is similar to white noise and is therefore considered constant (≈ 0.07 , dashed line Fig.1 in Kim *et al.*, 2011a), and ε combines δ_r with δ_i , which is irregular and produced by deviations from an illegitimacy of the EC measurement assumption. Additionally, Kim *et al.* (2011b) proposed that ε would be proportional to δ_i which is the degree of the ground surface heterogeneity and atmospheric stationary. Therefore, a heterogeneous surface can be inferred by ε .

The objective of this study is clarifying the impact of a heterogeneous surface on spatiotemporal uncertainty of sensible heat, latent heat, and CO₂ fluxes. In this study, a simultaneous flux observation experiment was conducted at different heights (20 m and 30 m) above the ground surface in a secondary seasonal tropical forest located in the Tak Province, Thailand, to use theoretical analysis using the MOST and ε .

2. Dataset and Methods

2.1. Dataset

The observational data were collected from an observation tower located in the Tak, Thailand (N16.56.24, E99.25.48). It is surrounded by a secondary seasonal tropical forest with heterogeneous vegetation, including deciduous trees and evergreens (refer to Kim *et al.* (2014) [18] for further site details and aerial photo).

We installed a three-dimensional (3D) sonic anemometer (CSAT3; Campbell Scientific, Utah, USA) and an open path CO₂/H₂O analyzer (LI7500; LI-COR, Nebraska, USA) at 20- and 30-m heights, respectively, on the observation tower and collected the vertical and horizontal wind speeds, temperature, and CO₂ and H₂O concentrations at a 10-Hz sampling frequency from June 5 to August 26, 2010. The vegetation height surrounding the observation tower was 7 m. We calculated the hourly sensible heat, latent heat, and CO₂ fluxes from the observational data using the eddy covariance method.

2.2. Method 1: Evaluation of Consistency of Surface Homogeneity

The vertical wind speed profile in the surface boundary layer can be obtained using Equation (5), which is based on the MOST.

$$\frac{d\bar{u}}{dz} = \frac{u_*}{\kappa z} \cdot \phi_m \left(\frac{z}{L} \right) \quad (5)$$

$$\phi_m = \left(1 - 16 \cdot \frac{z}{L} \right)^{-\frac{1}{4}} \quad (6)$$

where \bar{u} denotes the hourly averaged horizontal wind speed, z denotes the height above the surface, u_* denotes the friction velocity, κ denotes the von Kármán constant, L denotes the Obukhov length, and ϕ_m denotes the non-dimensional shear function (Dyer and Hicks, 1970) [19], which is obtained using Equation (6). We calculated F_* to evaluate the consistency between the magnitudes of the turbulent flow observations at 20 and 30 m using the MOST.

$$F_* = \frac{F}{\phi_m} \quad (7)$$

where the fluxes at 20 and 30 m are denoted as F_{*20m} and F_{*30m} , respectively. If the magnitudes of the turbulent flow observations at 20 m and 30 m were from source area with similar heterogeneity, F_{*30m} and F_{*20m} should be same values. In addition, impact of atmospheric stationarity on F_{*30m} and F_{*20m} should be also same on the simultaneous flux observation experiment at 20 and 30m. Therefore, we state that the differences of source areas for F_{*20m} and F_{*30m} can be expressed increasingly consistent as F_{*30m}/F_{*20m} approaches 1 in this study. Note that in terms of consistency, F_{*30m}/F_{*20m} approaches 1 when the source areas of F_{*20m} and F_{*30m} have similar heterogeneity. We calculated F_{*30m}/F_{*20m} for the CO₂, latent heat, and sensible heat fluxes (F_{*30m}/F_{*20m} (CO₂),

F_{*30m}/F_{*20m} (IE), and F_{*30m}/F_{*20m} (H), respectively).

Method 2: Calculation of the spatiotemporal uncertainty for the turbulent flow fluxes

In accordance with the method proposed by Kim *et al.* (2011b), we calculated F and δ to determine ε using Equation (1). Further, we calculated ε for the CO₂, latent heat, and sensible heat fluxes ($\varepsilon_{\text{CO}_2}$, ε_{IE} , and ε_{H} , respectively). Please refer to Kim *et al.* (2011b) for further details.

2.3. Data Selection

Only the optimal data examined by Methods 1 and 2 can be used for this research. Therefore, data was strictly selected by the following processes:

1) Because a stable atmosphere inhibits the development of the turbulent flow, we excluded the data where the atmospheric stability was greater than 1.

2) We also excluded the observations where simultaneous sensible heat, latent heat, and CO₂ fluxes were not obtained for Method 1. In addition, temporal uncertainties were same because we only used the flux data observed simultaneously. It means that ε represents the spatial uncertainty where each ε were different.

3) Further, because the consistency of surface homogeneity, F_{*30m}/F_{*20m} , was compared examined with the spatiotemporal uncertainty of the turbulent flow observations at 20 m, ε_{20m} , we only selected the data where the $\varepsilon_{30m}/\varepsilon_{20m}$ ratio was close to 1 ($0.9 < \varepsilon_{30m}/\varepsilon_{20m} < 1.1$), which means spatiotemporal uncertainty were similar at 20 and 30 m heights.

Table 1 presents the number of analyzed data during each step of the data selection process. Finally, the number of optimal data for this research was 48 which weren't included δ_i excluding surface heterogeneity. In addition, because the surface heterogeneity isn't instantly changed, many and/or continuous data isn't necessary in this research.

3. Results

Figure 2 depicts the relation between $\varepsilon_{\text{CO}_2(20m)}$ (spatiotemporal uncertainty) obtained via the 2-(3) method 2 and F_{*30m}/F_{*20m} (CO₂) (consistency of the surface heterogeneity) obtained via the 2-(2) method 1. The following three key groups are observed in the data: large F_{*30m}/F_{*20m} (CO₂) values (>2.0 ; triangles), small F_{*30m}/F_{*20m} (CO₂) values (≤ 2.0) with $\varepsilon_{\text{CO}_2(20m)} < 0.15$ (circles), and smaller F_{*30m}/F_{*20m} (CO₂) values (≤ 2.0) with $\varepsilon_{\text{CO}_2(20m)} \geq 0.15$ (crosses). **Figure 3** and **Figure 4** denote the relation between ε and F_{*30m}/F_{*20m} for the sensible and latent heat fluxes, respectively. Further, we used the same symbols for the sensible and latent heat fluxes measured at the same time as the CO₂ flux in **Figure 2** to compare the relation between ε and F_{*30m}/F_{*20m} for each flux.

Figure 5 was divided into four sectors to delineate the observed heterogeneities in the CO₂ environment. The upper left sector ($F_{*30m}/F_{*20m} > 2.0$ and $\varepsilon_{\text{CO}_2(20m)} < 0.15$) is given an A classification and corresponds to the area denoted

Table 1. Number of data for each selection stage.

Number of data where each flux was observed at the same time	Number of data where each flux was observed at the same time and where $0.9 < \varepsilon < 1.1$
67	48

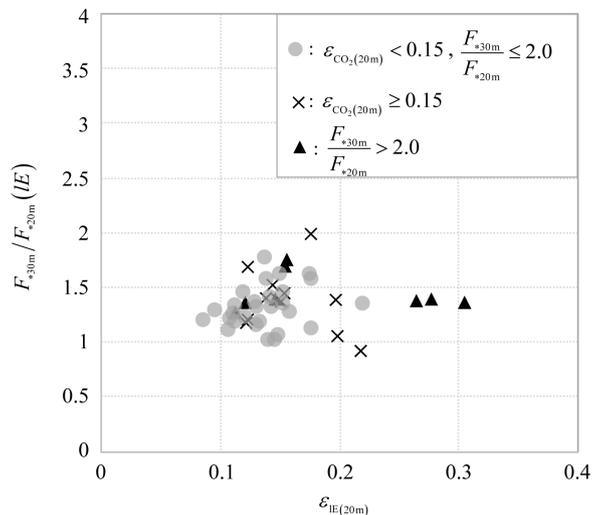


Figure 2. Relation between $\varepsilon_{CO_2(20m)}$ and $F_{*30m}/F_{*20m} (CO_2)$.

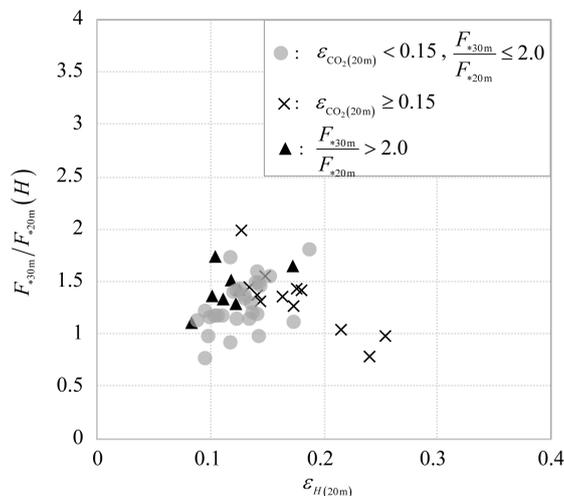


Figure 3. Relation between $\varepsilon_{H(20m)}$ and $F_{*30m}/F_{*20m} (H)$.

by the triangles in **Figure 2**. The upper right sector ($F_{*30m}/F_{*20m} > 2.0$ and $\varepsilon_{CO_2(20m)} \geq 0.15$) is given a B classification. The lower left sector ($F_{*30m}/F_{*20m} \leq 2.0$ and $\varepsilon_{CO_2(20m)} < 0.15$) is given a C classification and corresponds to the area denoted by circles in **Figure 2**. The lower right sector ($F_{*30m}/F_{*20m} \leq 2.0$ and $\varepsilon_{CO_2(20m)} \geq 0.15$) is given a D classification and corresponds to the area denoted by crosses in **Figure 2**. As presented in **Table 2**, the CO_2 fluxes in the A classification sector in **Figure 5** exhibit a relatively low consistency with a low spatiotemporal uncertainty, whereas those in the B classification sector also exhibit

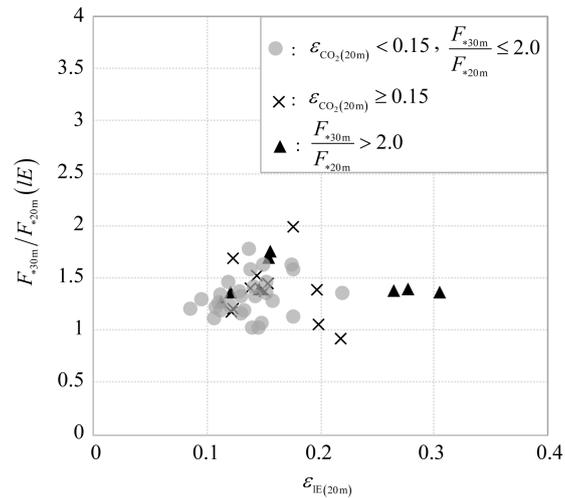


Figure 4. Relation between $\epsilon_{IE(20m)}$ and $F_{*30m}/F_{*20m}(IE)$.

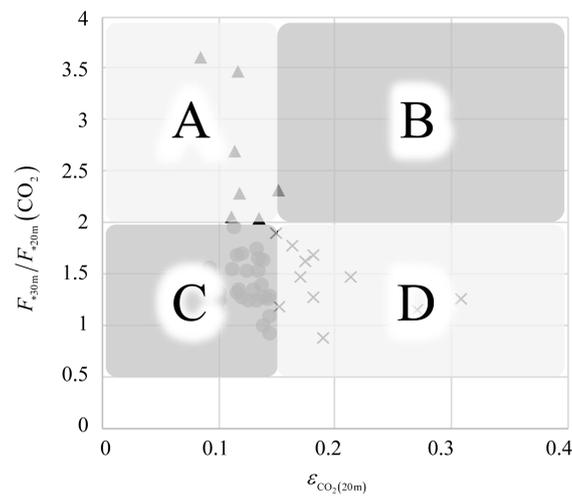


Figure 5. Classification. In this study, upper limit of vertical axis was 4.0, lower limit of vertical axis was 0.5 (vertical axis decrease inversely when it less than 1).

Table 2. Classification methods and characteristics.

Classification	A	B	C	D
Consistency	Low	Low	High	High
Spatiotemporal Uncertainty	Low	High	Low	High

a relatively low consistency with a high spatiotemporal uncertainty. Regarding CO₂ fluxes in the A classification, the heterogeneities of source areas at 20 and 30 m were different but the spatiotemporal uncertainties of both source areas were low (observed values were close to Q (true value)).

It means that the surface heterogeneity of source area at 20 and 30 m were different but both of surface heterogeneity have little impact on $\epsilon_{CO_2(20m)}$. Here,

we only selected the optimal data during the 2-(4) data selection process, CO₂ fluxes in the B classification sector were excluded. CO₂ fluxes in the C classification exhibit a high consistency (source area at 20 and 30 m have same heterogeneity) with low spatiotemporal uncertainty. Namely, it means the source area at 20 and 30 m were homogeneous. On the other hand, those in D classification also exhibit a high consistency (source area at 20 and 30 m have same heterogeneity) but high spatiotemporal uncertainty. Namely, it means that source area at 20 and 30 m were heterogeneous.

As depicted in **Figures 2-4**, some of the CO₂ flux results were assigned a D classification (crosses in **Figure 2**), whereas some were assigned a C classification due to ε_H and ε_{IE} for the sensible and latent heat environments. Furthermore, an analysis based on the MOST denoted that the CO₂ fluxes with an A classification (triangles in **Figure 2**) were assigned either C or D classifications for the sensible and latent heat fluxes (triangles in **Figure 3** and **Figure 4**), indicating high consistencies in the sensible and latent heat environments. However, there were also latent heat fluxes with a D classification and a relatively high spatiotemporal uncertainty (triangles in **Figure 4**). The source areas for the latent heat fluxes at 20 and 30 m exhibited similarly high spatiotemporal uncertainty, leading to high consistencies. However, the source areas for the sensible heat fluxes at both 20 and 30 m have low spatiotemporal uncertainty, because all the sensible heat fluxes were assigned a C classification, with high consistencies and low spatiotemporal uncertainties.

4. Discussion

The CO₂ flux results were assigned a D classification (crosses in **Figure 2**), whereas the corresponding sensible heat and latent heat flux results were assigned a C and D classification (crosses in **Figure 3** and **Figure 4**). It means that sensible heat and latent heat fluxes tended to have low spatial uncertainty compare with CO₂ flux because we only used the optimal data which temporal uncertainty were same. Some of sensible heat and latent heat flux results which were assigned a D classification in **Figure 3** and **Figure 4** had same temporal uncertainty as CO₂ flux results. However, those in a C classification in **Figure 3** and **Figure 4** had different spatial uncertainty from CO₂ flux results. It is able to be considered that different spatial uncertainty was attributed to a heterogeneous surface. The surface heterogeneity on the sensible heat and latent heat flux are homogeneous but not on CO₂ flux.

The CO₂ flux results were assigned an A classification (triangle in **Figure 2**), whereas the corresponding sensible heat flux results were assigned a C classification (triangle in **Figure 3**). It means that the source area at 20 and 30 m of sensible heat was similarly homogeneous. In addition, almost all latent heat flux results were also assigned a C classification (triangle in **Figure 4**). It means that the source area at 20 and 30 m of latent heat had same surface heterogeneity and some of them were heterogeneous but some of them were homogeneous.

One of reasons why the analytical results for the CO₂ flux presented a different pattern from those exhibited by the analytical results of the sensible and latent heat fluxes was considerable from the different impact of the insolation on sensible, latent, and CO₂ fluxes. The degree of ground surface heating is proportional to the insolation, which indicates that the increase in sensible and latent heat fluxes are strongly proportional to the insolation. Although latent heat and CO₂ fluxes, namely transpiration and photosynthesis, are also corresponding to the insolation, these are also regulated with the amount of water in the plant body, and photosynthesis is constant (saturated) under the fine insolation as described by many previous researches (cf. light response curve of photosynthesis (Monsi and Saeki, 1953) [20]).

For the above reasons, the amount of water in the plant body and some other factors (cf. stomatal conductance, vegetation, etc.) increase the spatial uncertainties of CO₂ flux; and the surface heterogeneity of source area of CO₂ flux was higher than source area of latent heat and sensible heat fluxes. In addition, although $\varepsilon_{\text{CO}_2(20\text{m})} < 0.15$ and $F_{*30\text{m}}/F_{*20\text{m}} > 2.0$ were empirically used for the data classification in this study, further investigations of the physical meaning of these value would be needed.

5. Conclusion

We defined ε as the spatial uncertainty of the turbulent flow flux, as proposed by Kim *et al.* (2011b), and observed that $\varepsilon_{\text{CO}_2}$ was high, whereas ε_{IE} and ε_{H} were low. This is likely to be caused by spatial uncertainty such as a heterogeneous surface. The CO₂ environment was heterogeneous; however, sensible and latent heat environments were homogeneous because the source area received insolation uniformly. Therefore, the analytical results for the CO₂ flux presented a different pattern from those exhibited by the analytical results of the latent and sensible heat fluxes.

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Conflicts of Interest

The authors declare no conflicts of interest regarding the publication of this paper.

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