# A Fine-Structure Constant Can Be Explained Using the Electrochemical Method 

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How to cite this paper: Miyashita, T. (2023) A Fine-Structure Constant Can Be Explained Using the Electrochemical Method. Journal of Modern Physics, 14, 160-170.
https://doi.org/10.4236/jmp.2023.142011
Received: December 21, 2022
Accepted: January 28, 2023
Published: January 31, 2023

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## Abstract

We proposed an empirical equation for a fine-structure constant:
$137.0359991=136.0113077+1+\frac{1}{3 \times 13.5}$. Then,
$13.5 \times 136.0113077=1836.152654=\frac{m_{p}}{m_{e}}$. where $m_{p}$ and $m_{e}$ are the rest mass of a proton and the rest mass of an electron, respectively. In this report, using the electrochemical method, we proposed an equivalent circuit. Then, we proposed a refined version of our own old empirical equations about the electromagnetic force and gravity. Regarding the factors of $9 / 2$ and $\pi$, we used 3.132011447 and 4.488519503 , respectively. The calculated values of $T_{c}$ and $G$ are 2.726312 K and $6.673778 \times 10^{-11}\left(\mathrm{~m}^{3} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~s}^{-2}\right)$.

## Keywords

Fine-Structure Constant, Electrochemical Method

## 1. Introduction

The symbol list is shown in Section 2. We discovered Equation 1 [1] [2] and [3], which appeared very simple. Equations (1)-(3) were mathematically connected [3]. However, we could not establish the background theory. Furthermore, there appeared to be dimension mismatch problems.

$$
\begin{gather*}
\frac{G m_{p}^{2}}{h c}=\frac{4.5}{2} \times \frac{k T_{c}}{1 \mathrm{~kg} \times c^{2}}  \tag{1}\\
\frac{G m_{p}^{2}}{\left(\frac{e^{2}}{4 \pi \varepsilon_{0}}\right)}=\frac{4.5}{2 \pi} \times \frac{m_{e}}{e} \times h c \times\left(1 \frac{\mathrm{C}}{\mathrm{~J} \cdot \mathrm{~m}} \times \frac{1}{1 \mathrm{~kg}}\right) \tag{2}
\end{gather*}
$$

$$
\begin{equation*}
\frac{m_{e} c^{2}}{e} \times\left(\frac{e^{2}}{4 \pi \varepsilon_{0}}\right)=\pi k T_{c} \times\left(1 \frac{\mathrm{~J} \cdot \mathrm{~m}}{\mathrm{C}}\right) \tag{3}
\end{equation*}
$$

These equations have small errors of approximately $10^{-3}$ and $10^{-4}$ [3]. We attempted to reduce the errors in the previous reports by changing the factors of 4.5, $\pi$ and $T_{c}$ [4] [5]. Regarding the factors of $9 / 2$ and $\pi$, we used 4.48870 and 3.13189 , respectively. Then, the errors became smaller than $10^{-5}$.

Then, 4.48870 and $3.13189 \Omega$ are connected as follows.

$$
\begin{equation*}
\frac{m_{p}}{m_{e}}=\frac{1}{4.4887 \times 3.13189 \Omega} \frac{q_{m}}{e} \tag{4}
\end{equation*}
$$

Next, we discovered the empirical equation for a fine-structure constant [6].

$$
\begin{align*}
& 137.0359991=136.0113077+\frac{1}{3 \times 13.5}+1  \tag{5}\\
& 13.5 \times 136.0113077=1836.152654=\frac{m_{p}}{m_{e}} \tag{6}
\end{align*}
$$

To explain 136.0113077, we proposed the following values.

$$
\begin{align*}
& 3.131777037(\Omega)=\frac{R k}{(3 \times 136.0113077)^{1.5}}  \tag{7}\\
& 4.488855463=\sqrt{\frac{136.0113077 \times 4}{27}} \tag{8}
\end{align*}
$$

However, Equations (7) and (8) cannot be compatible with Equations (5) and (6). Main purpose of this report is to improve the compatibility between these equations.

The remainder of the paper is organized as follows. In Section 2, we show the symbol list. In Section 3, we reconsider the deviation from the factors of 9/2 and $\pi$. In Section 4, using the electrochemical method, we propose the equivalent circuit for the fine structure constant. In Section 5, we refine our three equations. In Section 6, general discussions are presented, which are mainly about the UNIT.

## 2. Symbol List (These Values Were Obtained from Wikipedia)

$G$ gravitational constant: $6.6743 \times 10^{-11}\left(\mathrm{~m}^{3} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~s}^{-2}\right)$
(we used the compensated value $6.673778 \times 10^{-11}$ in this report)
$T_{c}$ temperature of the cosmic microwave background: 2.72548 (K)
(we used the compensated value 2.726312 K in this report)
$k$ Boltzmann constant: $1.380649 \times 10^{-23}\left(\mathrm{~J} \mathrm{~K}^{-1}\right)$
c speed of light: 299,792,458 (m/s)
$h$ Planck constant: $6.62607015 \times 10^{-34}$ (Js)
$\varepsilon_{0} \quad$ electric constant: $8.8541878128 \times 10^{-12}\left(\mathrm{~N} \cdot \mathrm{~m}^{2} \cdot \mathrm{C}^{-2}\right)$
$\mu_{0} \quad$ magnetic constant: $1.25663706212 \times 10^{-6}\left(\mathrm{~N} \cdot \mathrm{~A}^{-2}\right)$
$e \quad$ electric charge of one electron: $-1.602176634 \times 10^{-19}(\mathrm{C})$
$q_{m}$ magnetic charge of one magnetic monopole: $4.13566770 \times 10^{-15}(\mathrm{~Wb})$
(this value is only a theoretical value, $q_{m}=h / e$ ) $m_{p}$ rest mass of a proton: $1.6726219059 \times 10^{-27}(\mathrm{~kg})$
(we used the compensated value $1.672621923 \times 10^{-27} \mathrm{~kg}$ in this report)
$m_{e}$ rest mass of an electron: $9.1093837 \times 10^{-31}(\mathrm{~kg})$
$R k$ von Klitzing constant: $25812.80745(\Omega)$
$Z_{0}$ wave impedance in free space: $376.730313668(\Omega)$
a fine-structure constant: 1/137.035999081

## 3. Reconsideration for the Deviation from 4.5 and $\pi$

In this section, we reconsider the deviation from 4.5 and $\pi$. We notice that 4.48870 and 3.1319 can be rewritten as follows.

$$
\begin{equation*}
4.48870=\frac{q_{m} c}{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{3.854377987}\right) m_{p} c^{2}} \tag{9}
\end{equation*}
$$

For example, Equation (9) can be made sure as follows.

$$
\begin{gather*}
4.48870=\frac{4.13567 \times 10^{-15} \times 299792458}{\left(1836.15+1+\frac{1}{3.854377987}\right) \times 1.50328 \times 10^{-10}}  \tag{10}\\
3.13189 \Omega=\frac{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{3.854377987}\right) m_{e} c^{2}}{e c} \tag{11}
\end{gather*}
$$

Next, the deviation from 4.5 and $\pi$ can be explained as follows.

$$
\begin{equation*}
\frac{4.5}{\pi} \times \frac{3.13189}{4.48870}=0.999421207 \doteq 1 \tag{12}
\end{equation*}
$$

Regarding the values for 3.131777037 and 4.88855463 ,

$$
\begin{align*}
& 4.488855463=\frac{q_{m} c}{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{5.106991198}\right) m_{p} c^{2}}  \tag{13}\\
& 3.1317770 \Omega=\frac{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{5.106991198}\right) \times m_{e} c^{2}}{e c} \tag{14}
\end{align*}
$$

Next, the deviation from 4.5 and $\pi$ can be explained as follows.

$$
\begin{equation*}
\frac{4.5}{\pi} \times \frac{3.1317770}{4.488855463}=0.999350548 \doteq 1 \tag{15}
\end{equation*}
$$

Therefore, using $X$, the deviation should be rewritten as follows.

$$
\begin{equation*}
3.1317770=\frac{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{X}\right) \times m_{e} c^{2}}{e c} \tag{16}
\end{equation*}
$$

$$
\begin{equation*}
4.488855463=\frac{q_{m} c}{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{X}\right) m_{p} c^{2}} \tag{17}
\end{equation*}
$$

The value of 4.5 is from the degree of freedom as $9 / 2$. Therefore, 4.488855 should be dimensionless.

$$
\begin{equation*}
\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{X}\right)=\frac{q_{m} c}{4.488855463 \times m_{p} c^{2}}=\frac{\mathrm{Wb} \cdot \mathrm{~m} / \mathrm{s}}{\mathrm{~J}}=\frac{\mathrm{Wb} \cdot \mathrm{~m}}{\mathrm{~J} \cdot \mathrm{~s}}=\frac{\mathrm{m}}{\mathrm{C}} \tag{18}
\end{equation*}
$$

The correct value of $X$ and the UNIT will be discussed in detail in a later section.

## 4. Equivalent Circuit of the Fine Structure Constant with the Electrochemical Method

### 4.1. Explanation Using the Transference Number

For convenience, Equations (5) and (6) are rewritten as follows:

$$
\begin{align*}
& 137.0359991=136.0113077+1+\frac{1}{3 \times 13.5}  \tag{19}\\
& 13.5 \times 136.0113077=1836.152654=\frac{m_{p}}{m_{e}} \tag{20}
\end{align*}
$$

We strongly believe that the fine structure constant should be explained by the transference number [7]. According to Rickert [8],

$$
\begin{align*}
& J_{1}=L_{11} \operatorname{grad} \frac{\eta_{1}}{T}+L_{12} \operatorname{grad} \frac{\eta_{2}}{T}  \tag{21}\\
& J_{2}=L_{21} \operatorname{grad} \frac{\eta_{1}}{T}+L_{22} \operatorname{grad} \frac{\eta_{2}}{T} \tag{22}
\end{align*}
$$

where $J_{1}$ and $J_{2}$ are the current densities of two different carriers; $\eta_{1}$ and $\eta_{2}$ are the electrochemical potentials of the two different carriers; $L_{11}, L_{12}, L_{21}$, and $L_{22}$ are Onsagar coefficients.

In the area of solid-state ionics, Rickert proposed the following equation.

$$
\begin{equation*}
L_{12}=L_{21}=0 \tag{23}
\end{equation*}
$$

Then, the transference number ( $t_{1}$ and $t_{2}$ ) can be explained as follows.

$$
\begin{align*}
& t_{1}=\frac{R_{2}}{R_{1}+R_{2}}  \tag{24}\\
& t_{2}=\frac{R_{1}}{R_{1}+R_{2}} \tag{25}
\end{align*}
$$

where $R_{1}$ and $R_{2}$ are different resistance values. Next, we consider the following equation.

$$
\binom{V_{1}}{V_{2}}=Z_{1} \times\left(\begin{array}{cc}
1 & -\frac{1}{81}  \tag{26}\\
-\frac{1}{81} & 136.0113077
\end{array}\right)\binom{I_{1}}{I_{2}}
$$

where $V_{1}$ and $V_{2}$ are the voltage losses due to different carriers; $I_{1}$ and $I_{2}$ are the currents due to different carriers; $Z_{1}$ is the resistance, which will be explained later. In Equation (26), using an inverse of the matrix, Onsager coefficients can be obtained. Because the derivation is too complex to show here, we have:

$$
\begin{gather*}
V_{1}=Z_{1} \times I_{1}-\frac{Z_{1}}{81} \times I_{2}  \tag{27}\\
V_{2}=-\frac{Z_{1}}{81} \times I_{1}+Z_{1} \times 136.0113077 \times I_{2} \tag{28}
\end{gather*}
$$

Next, we consider the following situation, which implies the open circuit condition.

$$
\begin{equation*}
I_{1}=-I_{2} \tag{29}
\end{equation*}
$$

Therefore, the theoretical voltage $\left(V_{t h}\right)$ is,

$$
\begin{equation*}
V_{t h}=V_{1}-V_{2}=Z_{1} \times\left(136.0113077+1+\frac{1}{3 \times 13.5}\right) \times I_{1} \tag{30}
\end{equation*}
$$

In Equation (30), $-V_{2}$ is the voltage loss due to the opposite drift (not diffusion) current $\left(I_{2}\right)$. Thus, in Equation (30), we obtained the value of a fine-structure constant. For convenience, Equation (5) is rewritten as follows.

$$
\begin{equation*}
137.0359991=136.0113077+1+\frac{1}{3 \times 13.5} \tag{31}
\end{equation*}
$$

Next, we define the interaction voltage ( $V_{3}$ ) as follows.

$$
\begin{equation*}
V_{3}=\frac{Z_{1}}{81} \times I_{1} \tag{32}
\end{equation*}
$$

The transference number for the small voltage loss $\left(V_{1}\right)$ is

$$
\begin{equation*}
t_{1}=\frac{V_{3}-V_{2}}{V_{1}-V_{2}}=\frac{Z_{1} \times\left(136.0113+\frac{1}{3 \times 13.5}\right) \times I_{1}}{Z_{1} \times\left(136.0113+1+\frac{1}{3 \times 13.5}\right) \times I_{1}}=\frac{136.0359991}{137.0359991} \tag{33}
\end{equation*}
$$

Therefore, the interaction coefficient is

$$
\begin{equation*}
1-t_{1}=1-\frac{136.0359991}{137.0359991}=\frac{1}{137.0359991}=\frac{1}{\alpha} \tag{34}
\end{equation*}
$$

The transference number for the large voltage loss $\left(V_{2}\right)$ is

$$
\begin{equation*}
t_{2}=\frac{V_{1}-V_{3}}{V_{1}-V_{2}}=\frac{Z_{1} \times I_{1}}{Z_{1} \times\left(136.0113+1+\frac{1}{3 \times 13.5}\right) \times I_{1}}=\frac{1}{137.0359991} \tag{35}
\end{equation*}
$$

Equation 35 means the strong interaction. From Equations 33 and 35, $V_{3}$ should be transferred from the carriers with a large voltage loss $\left(V_{2}\right)$ to those with the small voltage loss ( $V_{1}$ ). From Equations (33) and (35),

$$
\begin{equation*}
t_{1}+t_{2}=\frac{136.0359991}{137.0359991}+\frac{1}{137.0359991}=1 \tag{36}
\end{equation*}
$$

### 4.2. Determination of the Important Resistance

The total resistance is $Z_{0}$, so the large resistance $\left(Z_{2}\right)$ should be

$$
\begin{equation*}
Z_{2}=Z_{0} \times 137.035999081=2 R k \tag{37}
\end{equation*}
$$

The small resistance is

$$
\begin{equation*}
Z_{1}=Z_{0} \times \frac{137.035999081}{136.0113077}=\frac{2 R k}{136.0113077}=379.5685505 \Omega \tag{38}
\end{equation*}
$$

We discover $Z_{1}$ as follows:

$$
\begin{equation*}
Z_{1}=3^{3} \times \frac{q_{m}}{e} \times \frac{m_{e}}{m_{p}}=27 \times \frac{25812.807459}{1836.152654}=379.5685505 \Omega \tag{39}
\end{equation*}
$$

Therefore, our argument is not a coincidence. From Equation (32), the interaction resistance $\left(Z_{3}\right)$ should be

$$
\begin{equation*}
Z_{3}=\frac{Z_{1}}{81}=\frac{1}{3} \times \frac{q_{m}}{e} \times \frac{m_{e}}{m_{p}}=4.686031487 \Omega \tag{40}
\end{equation*}
$$

Consequently, Equation (26) can be rewritten as follows,

$$
\binom{V_{1}}{V_{2}}=\left(\begin{array}{cc}
Z_{1} & -Z_{3}  \tag{26b}\\
-Z_{3} & Z_{2}
\end{array}\right)\binom{I_{1}}{I_{2}}
$$

### 4.3. Suitable Charge and Equivalent Circuit

We are discussing the equivalent circuit at the quantum level. Clearly, one charge is an electron. However, it is difficult to search for the other charge. The suitable charge is

$$
\begin{equation*}
\frac{q_{m}}{Z_{1}}=1.08957070 \times 10^{-17}(\mathrm{C})=68.00565 \times e \tag{41}
\end{equation*}
$$

Because $q_{m}$ has never been observed, the charge $+\frac{q_{m}}{Z_{1}}$ should be the set of an antiparticle $-\frac{q_{m}}{Z_{1}}$, which may be related to quarks. Then, we propose the equivalent circuit in Figure 1. The total charge is

$$
\begin{equation*}
\frac{2 q_{m}}{Z_{1}}=136.0113 \times e \tag{42}
\end{equation*}
$$

When the charge $+\frac{q_{m}}{Z_{1}}$ cannot be realized at the low energy level, it cannot be observed as the mass.

The direction of $+\frac{q_{m}}{Z_{1}}$ is opposite to the electrical field, which may prevent the increase of the electrical field.


Figure 1. Equivalent circuit to explain the fine-structure constant.

## 5. Our Refined Three Empirical Equations

### 5.1. The Most Suitable Value for $X$

For convenience, Equations (5) and (6) are rewritten as follows:

$$
\begin{align*}
& 137.0359991=136.0113077+1+\frac{1}{3 \times 13.5}  \tag{43}\\
& 13.5 \times 136.0113077=1836.152654=\frac{m_{p}}{m_{e}} \tag{44}
\end{align*}
$$

For convenience, Equations (16) and (17) are rewritten as follows:

$$
\begin{align*}
& 3.1317770 \Omega=\frac{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{X}\right) \times m_{e} c^{2}}{e c}  \tag{45}\\
& 4.488855463=\frac{q_{m} c}{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{X}\right) m_{p} c^{2}} \tag{46}
\end{align*}
$$

Then, we notice that $X$ should be 3 . Therefore,
$3.132011447 \Omega=\frac{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{3}\right) m_{e} c^{2}}{e c}=\frac{\left(\frac{m_{p}}{m_{e}}+\frac{4}{3}\right) m_{e} c^{2}}{e c}=\frac{1837.48599 \times m_{e} c^{2}}{e c}$

$$
\begin{equation*}
4.488519503=\frac{q_{m} c}{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{3}\right) m_{p} c^{2}}=\frac{q_{m} c}{\left(\frac{m_{p}}{m_{e}}+\frac{4}{3}\right) m_{p} c^{2}}=\frac{q_{m} c}{1837.48599 \times m_{p} c^{2}} \tag{48}
\end{equation*}
$$

Here, $4 / 3 m_{e} c^{2}$ is well known and has been discussed by Feynman. Next, the deviation from 4.5 and $\pi$ can be explained as follows.

$$
\begin{equation*}
\frac{4.5}{\pi} \times \frac{3.132011447}{4.488519503}=0.999500154 \doteq 1 \tag{49}
\end{equation*}
$$

### 5.2. Determination of the Important Resistance

$\frac{1}{\frac{m_{p}}{m_{e}}+1+\frac{1}{3}}=\frac{1}{1837.485988}$ appears to be a transference number. The total resistance $\left(Z_{5}\right)$, small resistance $\left(Z_{6}\right)$, large resistance $\left(Z_{7}\right)$ and interaction resistance $\left(Z_{8}\right)$ can be defined.

$$
\begin{gather*}
Z_{5}=2 \times \frac{q_{m}}{e} \times \frac{1}{\frac{m_{p}}{m_{e}}+\frac{4}{3}}=28.095787 \Omega  \tag{50}\\
Z_{6}=2 \times \frac{q_{m}}{e} \times \frac{m_{e}}{m_{p}}=\frac{2 R k}{1836.152654}=28.11618892 \Omega  \tag{51}\\
Z_{7}=2 \times \frac{q_{m}}{e}=2 R k \tag{52}
\end{gather*}
$$

$$
\begin{equation*}
Z_{8}=\frac{13.5}{81} \times Z_{6}=\frac{13.5}{81} \times 2 \times \frac{q_{m}}{e} \times \frac{m_{e}}{m_{p}}=\frac{1}{3} \times \frac{q_{m}}{e} \times \frac{m_{e}}{m_{p}}=4.686031487 \Omega=Z_{3} \tag{53}
\end{equation*}
$$

Consequently, $Z_{8}$ is equal to $Z_{3}$.

### 5.3. Our Refined Three Empirical Equations

We use 2.726312143 K instead of 2.72548 K . We use $6.6737778665 \times 10^{-11}$ $\mathrm{m}^{3} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~s}^{-2}$ instead of $6.6743 \times 10^{-11} \mathrm{~m}^{3} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~s}^{-2}$. Equation (1) is refined as follows:

$$
\begin{gather*}
\frac{G m_{p}^{2}}{h c}=\frac{4.488519503}{2} \frac{k T_{c}}{1 \mathrm{~kg} \times c^{2}}  \tag{54}\\
\frac{G m_{p}^{2}}{h c}=\frac{6.6737778665 \times 10^{-11} \times\left(1.6726219 \times 10^{-27}\right)^{2}}{6.626070 \times 10^{-34} \times 2.9979246 \times 10^{8}}=9.39919318 \times 10^{-40}  \tag{55}\\
\frac{4.488519503}{2} \frac{k T_{c}}{1 \mathrm{~kg} \times c^{2}}=\frac{4.488519503}{2} \times \frac{1.3806490 \times 10^{-23} \times 2.726312143}{\left(2.9979246 \times 10^{8}\right)^{2}}  \tag{56}\\
=9.39919318 \times 10^{-40}
\end{gather*}
$$

Equation (55) is equal to Equation (56). Therefore, the compensation method is perfect. Next, Equation (2) is refined as follows:

$$
\begin{align*}
&\left(\frac{e^{2}}{4 \pi \varepsilon_{0}}\right) \frac{4.488519503}{2 \times 3.132011447 \Omega} \times \frac{m_{e}}{e} \times h c \times\left(1 \frac{\mathrm{C} \cdot \Omega}{\mathrm{~J} \cdot \mathrm{~m}} \times \frac{1}{1 \mathrm{~kg}}\right)  \tag{57}\\
& \frac{G m_{p}^{2}}{\frac{e^{2}}{4 \pi \varepsilon_{0}}}=\frac{6.6737778665 \times 10^{-11} \times\left(1.672621923 \times 10^{-27}\right)^{2}}{\frac{\left(1.60217663 \times 10^{-19}\right)^{2}}{4 \pi \times 8.8541878 \times 10^{-12}}}=8.0929175 \times 10^{-37}  \tag{58}\\
& \frac{4.488519503}{2 \times 3.132011447} \times \frac{m_{e}}{e} \times h c=\frac{4.488519503 \times 9.10938 \times 10^{-31} \times 1.986446 \times 10^{-25}}{2 \times 3.132011447 \times 1.602177 \times 10^{-19}}  \tag{59}\\
&=8.0929175 \times 10^{-37}
\end{align*}
$$

Equation (58) is equal to Equation (59). Therefore, the compensation method is perfect. Next, Equation (3) is refined as follows:

$$
\begin{align*}
& \frac{m_{e} c^{2}}{e} \times\left(\frac{e^{2}}{4 \pi \varepsilon_{0}}\right)=3.132011447 \Omega \times k T_{c} \times\left(1 \frac{\mathrm{~J} \cdot \mathrm{~m}}{\mathrm{C} \cdot \Omega}\right)  \tag{60}\\
& \frac{m_{e} c^{2}}{e} \times\left(\frac{e^{2}}{4 \pi \varepsilon_{0}}\right)= \frac{9.10938 \times 10^{-31} \times\left(2.9979246 \times 10^{8}\right)^{2} \times\left(1.60217663 \times 10^{-19}\right)^{2}}{1.60217663 \times 10^{-19} \times 4 \pi \times 8.8541878 \times 10^{-12}}  \tag{61}\\
&=1.1789142 \times 10^{-22} \\
& 3.132011447 \times k T_{c}=3.132011447 \times 1.3806490 \times 10^{-23} \times 2.726312143  \tag{62}\\
&= 1.1789142 \times 10^{-22}
\end{align*}
$$

Equation (61) is equal to Equation (62). Therefore, the compensation method is perfect.

## 6. Discussion

### 6.1. Dimension Mismatch Problem

For convenience, Equation (54) is rewritten as follows:

$$
\begin{equation*}
\frac{G m_{p}^{2}}{h c}=\frac{4.488519503}{2} \frac{k T_{c}}{1 \mathrm{~kg} \times c^{2}} \tag{63}
\end{equation*}
$$

The value of 4.488519503 is the deviation from the degree of freedom 9/2, which is dimensionless.

Therefore, there are no dimension mismatch problems. For convenience, Equation (56) is rewritten as follows:

$$
\begin{equation*}
\frac{m_{e} c^{2}}{e} \times\left(\frac{e^{2}}{4 \pi \varepsilon_{0}}\right)=3.132011447 \Omega \times k T_{c} \times\left(\frac{\mathrm{J} \cdot \mathrm{~m}}{\mathrm{C} \cdot \Omega}=A m\right) \tag{64}
\end{equation*}
$$

In Equation (64), there remains the unexplained UNIT as "Am".

$$
\begin{equation*}
\frac{m_{e} c^{2}}{4 \pi \varepsilon_{0} c}=3.132011447 \Omega \times k T_{c} \times \frac{A m}{e c} \tag{65}
\end{equation*}
$$

Therefore,

$$
\begin{equation*}
\frac{Z_{0} \times m_{e} c^{2}}{3.132011447 \Omega \times 4 \pi}=k T_{c} \times \frac{A m}{e c} \tag{66}
\end{equation*}
$$

In Equation (66), the UNITs of 1 J and 1 C can be separately defined. However,

$$
\begin{equation*}
1 \mathrm{~J}=6.241509 \times 10^{18} \mathrm{eV}=6.241509 \times 10^{18} e c \times \frac{V}{c} \tag{67}
\end{equation*}
$$

where $\frac{V}{c}$ is the unit of the electromagnetic four potential. Therefore, $\frac{A m}{e c}$ may be Faraday constant at the quantum level. The proof is difficult and will be published in a future report. From Equations (47) and (65), we have

$$
\begin{equation*}
\frac{k T_{c}}{\frac{e^{2} c}{4 \pi \varepsilon_{0}}} \times(A m)=\frac{1}{\left(\frac{m_{p}}{m_{e}}+\frac{4}{3}\right)}\left(\frac{\mathrm{C}}{\mathrm{~m}}\right)=\frac{1}{1837.485988}\left(\frac{\mathrm{C}}{\mathrm{~m}}\right) \tag{68}
\end{equation*}
$$

Next, the fine structure constant $(\alpha)$ is

$$
\begin{equation*}
\frac{e^{2}}{4 \pi \varepsilon_{0}}=h c \times \frac{\alpha}{2 \pi} \tag{69}
\end{equation*}
$$

From Equations (68) and (69),
$\frac{k T_{c}}{h c^{2}}=\frac{1}{\left(\frac{m_{p}}{m_{e}}+\frac{4}{3}\right)} \times \frac{\alpha}{2 \pi} \times\left(\frac{1}{A m}\right)=\frac{1}{1837.485988} \times \frac{\alpha}{2 \pi} \times\left(\frac{\mathrm{s}}{\mathrm{m}^{2}}\right)=6.3206454 E-07$ (70)
In Equations (68) and (70), from different coordinate systems, $k T_{c}$ should be changed because the unit $\mathrm{C} / \mathrm{m}$ is not Lorentz invariant. Therefore, from Equation (63), $G$ is not Lorentz invariant.

### 6.2. Yukawa Potential

According to the advanced Wagner model, the diffusion time for mixed elec-
tronic and ionic currents should exponentially decrease with distance [9]. When the diffusion time for mixed electrons and quark flux should exponentially decrease with distance, the Yukawa potential can be explained.

### 6.3. Consideration of the Degree of Freedom inside Electrons

We have never discussed the spin of electrons. In Equation (64), the number $3.132011447 \Omega$ is the deviation from $\pi$. We believe that $\pi$ is related to the spin of the electron. Angrick et al. have confirmed that the spin of electrons cannot be thermodynamically ignored [10]. Furthermore, Aquino et al. discovered a new method for vector analysis [11]. We hope that the degrees of freedom in electrons will be clarified in detail.

## 7. Conclusions

We proposed an empirical equation for a fine-structure constant: $137.0359991=136.0113077+1+\frac{1}{3 \times 13.5}$. We proposed several empirical equations to describe the relationship between an electromagnetic force and $T_{c}$ Three equations were explained by the factors of $9 / 2$ and $\pi$. We attempted to improve the accuracies by changing the values of $9 / 2$ and $\pi$. For this purpose, using the electrochemical method, we proposed the equivalent circuit. Then, we proposed the following two values,

$$
3.132011447 \Omega=\frac{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{3}\right) m_{e} c^{2}}{e c}, \quad 4.488519503=\frac{q_{m} c}{\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{3}\right) m_{p} c^{2}}
$$

The calculated values of $T_{c}$ and $G$ are 2.726312 K and $6.673778 \times 10^{-11}$ $\left(\mathrm{m}^{3} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~s}^{-2}\right) .\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{3}\right)$ appears to be related to the transference number. However, there should be the UNIT (m/C) in $\left(\frac{m_{p}}{m_{e}}+1+\frac{1}{3}\right)$. Therefore, the values of $T_{c}$ and $G$ should not be Lorentz invariant.

## Conflicts of Interest

The author declares no conflicts of interest regarding the publication of this paper.

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