

On a Heuristic Viewpoint Concerning the Conversion and Transformation of Sound into Light

Alessandro Rizzo

Brescia, Italy Email: lab@ciaoidea.it

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Abstract

In the study of Terrestrial Gamma-ray Flashes (TGFs) and Sonoluminescence, we observe parallels with larger cosmic events. Specifically, sonoluminescence involves the rapid collapse of bubbles, which closely resembles gravitational collapse in space. This observation suggests the potential formation of low-density quantum black holes. These entities, which might be related to dark matter, are thought to experience a kind of transient evaporation similar to Hawking radiation seen in cosmic black holes. Consequently, sonoluminescence could be a valuable tool for investigating phenomena typically linked to cosmic scale events. Furthermore, the role of the Higgs boson is considered in this context, possibly connecting it to both TGFs and sonoluminescence. This research could enhance our understanding of the quantum mechanics of black holes and their relation to dark matter on Earth.

Keywords

Planck Mass, Gravity, Light, Phonons, Phononic Field, Vacuum Hydrodynamics, Sonoluminescence, Hawking Radiation, Quantum Black Holes, Theory of General Singularity

1. Introduction

Our understanding of the universe is shaped by a range of phenomena, extending from the vast cosmic scale to the quantum realm. Within this spectrum, Terrestrial Gamma-ray Flashes (TGFs) and Sonoluminescence have emerged as subjects of particular interest, offering potential insights into the complexities of dark matter [1]. These phenomena could be linked to the behavior of micro black holes, a connection that is intriguing for its implications in both astrophysics and quantum physics. Sonoluminescence, characterized by the rapid collapse of a bubble in a liquid which results in light emission, has long been a focal point of scientific research. Rather than being a mere scientific curiosity, this phenomenon may be a visible representation of quantum effects, akin to those seen in Hawking radiation. The processes underlying sonoluminescence could be more intricately connected with quantum mechanics than previously thought.

TGFs, which are intense but short-lived bursts of gamma rays originating from Earth's atmosphere, add a new dimension to this exploration. The genesis and mechanisms of TGFs may involve the vaporization of quantum black holes, suggesting a significant role for these micro black holes in our current understanding of dark matter.

A key aspect of this study is the role of the Higgs boson, a particle that results from disturbances in the Higgs field. The creation of a Higgs boson might occur during the quantum cavitation of a black hole, particularly at the Planck mass scale [2]. This event could be triggered by changes in the relativistic mass field, potentially caused by phonons, drawing a parallel to the phenomenon of sonoluminescence. Once formed, the Higgs boson might decay into two high-energy gamma photons, a process that aligns with the standard model of particle physics.

This research aims to explore the theoretical and mathematical connections between these phenomena. By integrating concepts from particle physics and condensed matter physics, the goal is to illuminate the possible interplay among the Higgs boson, sonoluminescence, and TGFs. The insights gained from this investigation could significantly expand our understanding of the universe, bridging the macroscopic with the quantum, and potentially reshaping our comprehension of the fundamental forces and particles that constitute our reality.

2. Background

2.1. Maxwell's Electromagnetic Theory

James Clerk Maxwell's electromagnetic theory unified the previously separate fields of electricity and magnetism into a single theory of electromagnetism. [3] His set of four differential equations, known as Maxwell's equations, are foundational in the field of classical electrodynamics, optics, and electric circuits. These equations not only describe how electric and magnetic fields interact but also predict the existence of electromagnetic waves, which travel at the speed of light. This groundbreaking revelation paved the way for the development of modern radio, radar, and television technologies.

$$7 \cdot \boldsymbol{E} = \frac{\rho}{\varepsilon_0} \tag{1}$$

$$\nabla \cdot \boldsymbol{B} = 0 \tag{2}$$

$$\nabla \times \boldsymbol{E} = -\frac{\partial \boldsymbol{B}}{\partial t} \tag{3}$$

$$\nabla \times \boldsymbol{B} = \mu_0 \boldsymbol{J} + \mu_0 \varepsilon_0 \frac{\partial \boldsymbol{E}}{\partial t}$$
(4)

The wave solution of these equations, which describes the propagation of light, was a significant step towards the development of the theory of relativity by Albert Einstein.

2.2. Sonoluminescence

Sonoluminescence, a phenomenon where small gas bubbles in a liquid emit short bursts of light when subjected to intense acoustic fields, has been a subject of fascination and study since its discovery [4] [5] [6]. These ephemeral flashes of light, which last only a few picoseconds, are produced when a bubble undergoes rapid compression and subsequent expansion in response to an acoustic wave.

$$P = \frac{2\gamma}{\gamma + 1} \rho c^2 \left(R_0 - R \right) \dot{R}$$
⁽⁵⁾

2.2.1. Experimental Setup

The typical experimental setup for observing sonoluminescence involves a liquid-filled chamber equipped with ultrasonic transducers (Figure 1). These transducers generate acoustic waves that travel through the liquid. When a gas bubble is introduced into the liquid, it becomes trapped at the antinode of the standing acoustic wave, where the acoustic pressure is maximum. As the acoustic wave oscillates, the bubble undergoes periodic compression and expansion. Under the right conditions, during the rapid compression phase, the bubble emits a short burst of light, marking the occurrence of sonoluminescence.



Figure 1. In the experimental setup, an ultrasonic transducer is used to induce cavitation within a designated test cell. This transducer is driven by a piezoelectric amplifier, which in turn receives its signal from a generator. There are two primary configurations for the transducer setup: one is a resonating test cell, and the other is a "Sonicator" cell disruptor, typically placed within a flask or beaker. To monitor the effects and outcomes of the cavitation process, various instruments can be employed. These include photodetectors, spectrometers, and neutron detectors. For optimal observation, it's recommended to monitor the process in a darkened environment, ensuring that all external lights are turned off.

The emitted light is then captured using photomultiplier tubes or high-speed cameras equipped with spectral filters. This allows researchers to analyze the spectral characteristics of the emitted light, providing insights into the temperatures and conditions within the bubble.

2.2.2. The Mystery of High Temperatures: Phonon to Photon Interaction Spectroscopic analyses of light emitted during sonoluminescence have revealed temperatures within collapsing bubbles ranging from 6000 K to 20,000 K:

$$6000 \text{ K} \le T_{\text{hubble}} \le 20000 \text{ K}$$

Such extreme temperatures have led to various theories about the processes occurring within the bubble. Some researchers postulate that the gas inside the bubble is heated adiabatically due to rapid compression. Others suggest that the shock waves generated during the bubble's collapse lead to heating. The possibility of quantum effects or even nuclear reactions occurring within the bubble has also been proposed, adding to the enigma of sonoluminescence.

In sonoluminescence, we observe a critical interplay between phonons and photons. Phonons, as quantized units of vibrational energy, impart significant energy to gas bubbles in a liquid. When these phonon-stimulated bubbles collapse under the influence of acoustic waves, they reach extremely high temperatures and pressures. This intense environment facilitates the conversion of vibrational energy (phonons) into electromagnetic energy (photons), resulting in the emission of light. This phenomenon illustrates the intricate link between the quantum world of phonons and the classical realm of photon-based light emission, enhancing our understanding of both fields. To elucidate the role of phonons in various materials and the quantum vacuum, and their collective energetic interactions with quantum fields, we can start by understanding phonons in a conventional material setting and then extend this understanding to more general scenarios:

In typical materials, phonons are quanta of vibrational energy, integral to understanding thermal and mechanical properties. They represent collective excitations within the atomic lattice of the material, playing a crucial role in heat conduction and other thermodynamic processes. In this context, phonons can be thought of as carriers of vibrational energy through the material's lattice.

However, as quasi-particles, phonons can be generalized beyond solid materials. They can represent collective excitations or vibrational disturbances in any medium, including the quantum vacuum. This generalization is significant because it allows us to conceptualize phonons as agents that can stimulate and interact with various quantum fields, even in the absence of a traditional material lattice.

When considering the quantum vacuum, often described in quantum field theory as a dynamic medium filled with virtual particles and fluctuations, phonons can play a role similar to their function in solid materials. They can act as disturbances or excitations that interact with the fields present in the vacuum. This interaction can be particularly energetic and can lead to the stimulation of fields like the Higgs field, known for imparting mass to particles.

In high-energy scenarios, such as during sonoluminescence or other phenomena where the quantum vacuum is perturbed, phonons can facilitate the conversion of vibrational energy into other forms of energy, including electromagnetic radiation. The mathematical representation of this process can be expressed as a generalized equation, valid in any medium due to the quasi-particle nature of phonons:

phonon
$$\rightarrow \gamma + \gamma$$

This equation symbolizes the conversion of vibrational (phononic) energy into electromagnetic (photonic) energy. It highlights the versatility of phonons in interacting with quantum fields, leading to observable phenomena like light emission. In these scenarios, the phonons are not restricted to a specific material lattice but can be viewed as broader quantum disturbances that induce energetic interactions across various fields, including the Higgs field, in any medium, including the vacuum.

The potential to achieve stellar-like conditions within a microscopic bubble on Earth has profound implications. If the conditions within the sonoluminescent bubble are indeed conducive to nuclear reactions, it opens up possibilities for future energy sources.

2.3. The Higgs Field

The Higgs field is a scalar field that permeates all of space, giving particles their mass through the Higgs mechanism. The discovery of the Higgs boson at the Large Hadron Collider (LHC) in 2012 was a landmark achievement in particle physics. This boson is an excitation of the Higgs field and serves as a testament to the field's existence.

The potential associated with the Higgs field in its simplest model is given by:

$$V(\Phi) = \mu^2 \Phi^* \Phi + \lambda \left(\Phi^* \Phi\right)^2 \tag{6}$$

The Higgs boson itself has a mass of approximately $125.10 \pm 0.14 \text{ GeV/c}^2$, as determined by the experiments at the LHC. This energy range is crucial as it falls within the capabilities of the LHC to produce and detect. The relatively high mass of the Higgs boson, compared to other elementary particles, is one of the reasons it took so long to discover, requiring high-energy collisions like those at the LHC.

The discovery of the Higgs boson not only confirmed the existence of the Higgs field but also validated the last missing piece of the standard model of particle physics. It provided a mechanism for how particles acquire mass. Without the Higgs field, particles like the W and Z bosons would be massless, leading to vastly different physical predictions than what is observed.

The ongoing research aims to study the properties of the Higgs boson in detail, such as its spin, parity, and couplings to other particles. These studies can provide insights into potential new physics beyond the standard model.

2.4. Terrestrial Gamma-Ray Flashes (TGFs) and Their Energy Spectrum

Terrestrial Gamma-Ray Flashes (TGFs), discovered in the 1990s, represent an extraordinary class of high-energy astrophysical phenomena, characterized by intense bursts of gamma rays originating from Earth's atmosphere. These flashes, of mere milliseconds in duration, are intricately linked with atmospheric thunderstorms and are theorized to be generated by the acceleration of electrons to relativistic speeds. The Bremsstrahlung process, a mechanism involving the interaction of these high-speed electrons with atomic nuclei, is believed to be responsible for the production of gamma rays in TGFs:

$$e^- + Z \to e^- + Z + \gamma \tag{7}$$

The detection of TGFs by the Planck satellite, primarily tasked with observing the Cosmic Microwave Background (CMB), added a pivotal dimension to our understanding of these phenomena. The gamma-ray signatures captured by Planck, initially unanticipated, affirmed the existence and significance of TGFs. The spectrum of the gamma-ray intensity emanating from these events is integrally described by:

$$I_{\gamma} = \int_{E_1}^{E_2} \frac{\mathrm{d}N}{\mathrm{d}E} \mathrm{d}E \tag{8}$$

In the study of Terrestrial Gamma-ray Flashes (TGFs), the Fermi Gamma-ray Space Telescope and RHESSI have played crucial roles. Their research has covered multiple areas, such as analyzing the energy spectrum of TGFs, estimating their duration, and mapping their global distribution. A key finding from these missions is the notable concentration of TGFs in equatorial regions. This distribution pattern is mathematically expressed as:

$$N(\theta) = N_0 \cos^n(\theta) \tag{9}$$

In this equation, $N(\theta)$ represents the number of TGFs observed at a particular latitude, θ is the latitude (measured in degrees from the equator), N_0 is a constant representing the maximum number of TGFs observed at the equator, and n is an exponent that characterizes the rate of decrease in the number of TGFs observed as one moves away from the equator. An intriguing aspect of TGFs is their interaction with Earth's magnetic field, leading to the generation of secondary particles. This process, encompassing both electrons and positrons, can be represented as:

$$e^{\pm} \to e^{\pm} + \gamma \tag{10}$$

These secondary particles have the potential to form transient radiation belts around Earth, posing significant implications for satellite operations and space travel.

In the context of natural atmospheric phenomena, tropical lightning stands out with its immense energy release, approximately 10⁹ Joules. Translating this figure into the energy unit of GeV reveals:

$$E_{\text{lightning}} \approx 6.242 \times 10^{18} \,\text{GeV} \tag{11}$$

This energy scale, when juxtaposed with the energy of fundamental particles such as the Higgs boson, approximately $125.10 \pm 0.14 \text{ GeV/c}^2$, underscores the extraordinary energy range that TGFs encompass.

A particularly fascinating aspect to explore is the potential interaction between the energy levels of TGFs and those of the Higgs boson. It is hypothesized that such interactions may manifest as phononic excitations within a relativistic mass field, exemplified by the Higgs field. The verification of these interactions could profoundly enhance our comprehension of the synergy between large-scale atmospheric events and the nuances of fundamental particle physics.

Future research endeavors are aimed at augmenting the resolution and sensitivity of TGF detection systems. Such advancements are crucial for a more intricate study of their energy spectra. A comprehensive understanding of the interactions between TGFs, Earth's magnetic field, and the atmospheric dynamics is vital. This knowledge is not only pivotal in forecasting space weather phenomena but also has significant ramifications for satellite functionality and the safety of astronauts.

3. Quantum Vacuum Hydrodynamics: Higgs-Phonon Interactions and Gravity Cavitation in Sonoluminescence and TGFs

In exploring the dynamic universe, particularly phenomena such as sonoluminescence and Terrestrial Gamma-Ray Flashes (TGFs), we delve into a complex interplay of various fundamental elements. This exploration leads us to integrate the roles of visible and dark matter, Higgs-Phonon dynamics, and quantum gravity cavitation into a unified theoretical construct.

At the core of our analysis are Einstein's field equations (EFE), which, while retaining their fundamental structure, are adapted to differentiate between visible and dark matter. This differentiation is expressed through distinct components of the energy-momentum tensor: $T^{\circ}_{\mu\nu}$ for visible matter and $T^{\bullet}_{\mu\nu}$ for dark matter. The revised EFE, reflecting both matter forms, are represented as:

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi \left(T^{\circ}_{\mu\nu} + T^{\bullet}_{\mu\nu} \right)$$
(12)

In ensuring the conservation of total energy and momentum within spacetime, we propose a unified continuity equation. This equation accounts for the gravitational interactions and energy-momentum exchanges between visible and dark matter:

$$\nabla^{\mu} \left(T^{\circ}_{\mu\nu} + T^{\bullet}_{\mu\nu} \right) = 0 \tag{13}$$

The dynamics between the Higgs field and phonons, quanta of vibrational energy in a lattice structure [7] [8] [9], are central to new paradigms in both particle physics and condensed matter physics. This interaction is crucial in the phenomena under consideration and is elucidated through a hydrodynamic model of the quantum vacuum. The model, which draws parallels with classical fluid dynamics, becomes particularly insightful in the presence of perturbations such as phonons. This relationship is encapsulated in the energy-momentum tensor:

$$T^{\mu\nu} = (E+P)u^{\mu}u^{\nu} - Pg^{\mu\nu}$$
(14)

A significant aspect of our exploration is quantum gravity cavitation, involving the formation of transient cavities or "gravitational bubbles" within the quantum vacuum. These bubbles, functioning as spherical electromagnetic vortices akin to micro black holes, each with its electromagnetic horizon, are mathematically represented as:

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu} \tag{15}$$

The interaction dynamics between gravitational bubbles and phonons in the Higgs field are governed by a modified wave equation, encapsulating the nuanced interplay of these quantum entities:

$$\left(\Box - m^2 + \lambda h^{\mu\nu} \partial_{\mu} \partial_{\nu}\right) \psi = 0 \tag{16}$$

This equation represents the collective influence of phonons, quasi-particles representing quantized vibrational energy, on multiple quantum fields. Here, $\lambda h^{\mu\nu}\partial_{\mu}\partial_{\nu}$ term denotes the interaction of phonons with the gravitational field perturbations, symbolized by $h^{\mu\nu}$. The phonons' effect on the curvature of spacetime, as well as their interaction with the Higgs field, is crucial in understanding their role in mediating forces at a quantum level.

The semi-classical Einstein equations bridge the realms of quantum mechanics and general relativity by integrating quantum effects with spacetime curvature. These equations are pivotal for understanding gravitational bubbles or quantum cavities, often referred to as "quantum vortices." These vortices represent fluctuations in the quantum vacuum, shaped by gravitational forces. The semi-classical Einstein equations mathematically encapsulate this concept as:

$$G_{\mu\nu} = 8\pi G \left\langle T_{\mu\nu} \right\rangle$$

In this equation, $G_{\mu\nu}$ symbolizes the Einstein tensor that describes spacetime curvature. Meanwhile, $\langle T_{\mu\nu} \rangle$ denotes the expectation value of the quantum stress-energy tensor, which integrates quantum mechanical effects into the classical framework of gravity.

These equations underscore the impact of quantum phenomena, including the energy-momentum distribution within the quantum vacuum, on gravitational fields. The energy-momentum tensor's expectation value, $\langle T_{\mu\nu} \rangle$, merges the quantum aspects, such as phonons and virtual particles, into the geometrical fabric of general relativity.

This theoretical framework offers a comprehensive perspective on the interplay between quantum mechanics, gravity, the Higgs field, and the distinction between visible and dark matter. It reveals that phenomena like sonoluminescence and Terrestrial Gamma-Ray Flashes (TGFs) are integral to understanding the complex relationship between dark and visible matter. This interaction, driven by relativistic phonons, signals a profound connection that transcends traditional gravitational interactions, delving into quantum mechanics. The collective influence of phonons across diverse quantum fields holds significant ramifications for our comprehension of dark matter, its interaction with visible matter, and its role in cosmic events.

In summary, this research sheds light on the universe's dynamics, opening new avenues for exploring the nature of dark matter and its relationship with visible matter in the cosmic landscape. The interplay of phonons across various quantum fields emerges as a key factor in the intricate interplay of the universe's fundamental forces and constituents. TGFs, observed by satellites, are associated with relativistic jets and strong magnetic fields, akin to those near black holes. These TGFs, potentially influenced by Sonoluminescence and Hawking radiation, may provide critical insights into dark matter's nature, hinting at the evaporation of micro black holes in space (**Figure 2**).

Sonoluminescence, characterized by the rapid collapse of a bubble in a liquid medium resulting in light emission, parallels the quantum mechanics of Hawking radiation. In this scenario, a black hole nearing quantum cavitation at the Planck mass scale may lead to the emergence of a Higgs boson, triggered by perturbations in the relativistic mass field due to a phonon, mirroring the dynamics seen in sonoluminescence.

Within our theoretical model, we examine the interaction between phonons, which are quantized vibrational energy modes, and the Higgs field in the quantum vacuum. This interaction could initiate the formation of a Higgs boson (*H*), mathematically expressed as:

phonon
$$\rightsquigarrow H$$

This equation represents the transformation of phonon vibrational energy into the mass of the Higgs boson.

Following its formation, the Higgs boson tends to decay rapidly, emitting two high-energy gamma photons:



Figure 2. A comparative representation of the magnetic field of a quantum black hole, or Planck mass, induced by Terrestrial Gamma-Ray Flashes (TGFs), alongside a cosmological black hole. The left image illustrates a TGF, showcasing a magnetic jet, a typical feature associated with a black hole, linked with the Planck mass. The right image represents a cosmological black hole for comparison.

$$H \rightsquigarrow \gamma \gamma$$

This decay process, a rare event occurring through a quantum loop mechanism involving virtual particles, was crucial in the discovery of the Higgs boson. It is one of the decay channels observed in experiments at the Large Hadron Collider (LHC) at CERN, particularly by the ATLAS and CMS collaborations, which confirmed the existence of the Higgs boson in 2012.

Furthermore, intense space lightning can act as a trigger in the quantum vacuum, inducing the formation of toroidal or spherical quantum vortices. These vortices, resembling the formation process of quantum black holes near the Planck mass scale, demonstrate the fluid-like behavior of the quantum vacuum in response to high-energy variations and disturbances. The creation of these quantum vortices exemplifies the active and reactive nature of the vacuum under high-energy conditions (**Figure 3**).

The Higgs field, represented as Φ , imparts mass to particles through their interaction with it. A disturbance in this field can lead to the appearance of the Higgs boson, *H*. The potential governing this field is described by:

$$V(\Phi) = \mu^2 \Phi^* \Phi + \lambda (\Phi^* \Phi)^2$$

Drawing a parallel, micro black holes, similar to the collapsing bubbles in sonoluminescence, might emit energy during their cavitation process. This radiative behavior becomes especially noticeable when the black hole's mass is close



Figure 3. In quantum field theory, the relativistic Higgs mass field can be conceptually likened to the water in a swimming pool. Within this analogy, a phonon represents a disturbance, akin to the disruption caused by a tropical lightning strike at the interface between Earth's atmosphere and space, resulting in an energy depression in the space-time continuum. Drawing from this in the domain of quantum cavitation, the emanation of two high-energy photons $\gamma\gamma$ is comparable to phenomena observed in vacuum quantum hydrodynamics. In such contexts, a pronounced phononic pressure wave triggers the formation of two distinct quantum vortices, potentially dual relativistic cones. More broadly, these vortices can be typified as toroidal or annular, essentially representing electromagnetic spherical cavitation vortices, which are intrinsic to quantum gravity. Analogously, applying pressure to a pool's surface, say using a plate, initiates the formation of two interconnected vortices, aligned tail-to-tail (Image/Content Courtesy: PhysicsGirl).

to the Planck mass. In this domain, quantum gravity effects dominate, potentially leading to the emission of gamma rays, a hallmark of Hawking radiation.

The energy equivalence of the Planck mass can be expressed as:

$$E_n = m_n c^2 = 1.2209 \times 10^{19} \, \text{GeV}$$

For the Higgs boson, the energy equivalence is:

$$E_{H} = m_{H}c^{2} = 125 \,\text{GeV}$$

In the context of TGFs, discerning the relationship between these energies is crucial. If the quantum cavitation of micro black holes releases energy potent enough to disturb the Higgs field, it might instigate the emergence of a Higgs boson. This interaction hints at a deep connection between the energies of the Planck mass, the Higgs boson, and the sonoluminescence process (Figure 4).

The study of sonoluminescence and Terrestrial Gamma-Ray Flashes (TGFs) offers transformative insights into our understanding of the quantum vacuum. Rather than being a passive void, the quantum vacuum under high-energy conditions, as evidenced by these phenomena, acts more like a dynamic, condensed medium. This challenges the traditional notion of the vacuum as an isolated entity, suggesting it can support wave-like energy propagation similar to sound, thermal waves, and even gravitational heat in a material medium.

In this framework, phonons, traditionally associated with vibrational energy in solid matter, are reimagined as quantized modes of vibration in the quantum vacuum. They become crucial for transmitting not just sound but also thermal and gravitational energy, bridging the gap between solid-state physics and the high-energy dynamics of the quantum vacuum.



Figure 4. This illustration visualizes the phenomenon of spacetime symmetry breaking in the context of Planck mass cavitation or quantum gravity cavitation, as conceptualized within quantum field theory. The depicted process involves a pressure gradient, symbolized by p, in a quantum gravitational field. This pressure gradient is pivotal in the spacetime symmetry breaking process, as it drives the formation of vortices within the quantum spacetime fabric. The geometrical structure of this quantum spacetime is represented by the equation $x^2 + y^2 + pz^2 = (ct)^2$, where p specifically denotes the pressure variable in the spacetime bubble collapse process. The resulting dual light cones, illustrated in Lorentzian geometry, are interpreted as an electromagnetic quantum gas or fluid, labeled γ_2 . These cones are theorized to produce a gamma-ray cascade, potentially observable as manifestations of dark energy in the quantum vacuum. This cascade is a direct manifestation of the mass-energy equivalence principle $E = mc^2$, with *m* representing the mass related to dark energy fluctuations in the quantum vacuum. The emission of light in this scenario draws a parallel to sonoluminescence, where light is emitted as bubbles in a liquid medium implode due to acoustic forces, thereby linking quantum mechanical processes with classical physics phenomena. In this framework, the quantum vacuum is treated as a condensed medium, characterized by both matter and energy.

The conditions observed in sonoluminescence and TGFs closely resemble those near black hole event horizons, drawing a parallel to Hawking radiation. This analogy indicates that similar quantum mechanical processes are at play, providing a new lens to view the mysterious nature of black holes.

Further, our theoretical model suggests a more nuanced interaction between dark and visible matter. This interaction, driven by high-energy phenomena and phonon dynamics, goes beyond gravitational forces, involving thermal and spacetime heat transfer at a quantum level. It indicates a complex quantum mechanical relationship between visible and dark matter, previously unexplored.

These revelations have profound implications for our understanding of quantum gravity and the nature of spacetime. They expand our comprehension of cosmic phenomena and the fundamental workings of the universe. This research links astrophysical events to quantum mechanics, paving the way for new explorations in quantum gravity and cosmology.

In essence, this work provides a novel and comprehensive perspective on high-energy astrophysical phenomena, integrating them with fundamental concepts of quantum mechanics. The Theory of General Singularity, inspired by Einstein's pioneering work, proposes a quantum formulation of space, gravitation, and singularities as quantum entities. This approach views black holes and dark matter halos not just as disturbances in the quantum vacuum but also as sources of gravitational and spacetime heat, akin to thermal phenomena in condensed matter.

The theory suggests a quantum perspective on space and gravitation, moving us closer to a unified theory of quantum gravity. It offers a holistic view of the universe's most mysterious phenomena, opening new avenues for exploration in quantum physics and cosmology.

4. Transient Quantum Black Holes and the Thermodynamics of Spacetime: The Gravitational Heat

The concept of transient quantum black holes presents a transformative perspective on dark matter, one of the most elusive components of the universe. These quantum black holes, distinct from their massive counterparts, are theorized to exist at quantum scales and could be interspersed throughout the cosmos. Governed by the principles of quantum mechanics, they exhibit behaviors akin to elementary particles rather than traditional black holes.

Stephen Hawking's pioneering idea in 1974 about Hawking radiation brought forth the notion that black holes, contrary to being entirely black, can emit radiation due to quantum effects at their event horizons. This radiation emerges from the uncertainty principle, a cornerstone of quantum mechanics, which posits the spontaneous creation of virtual particle-antiparticle pairs near the event horizon. In a process called "transient evaporation," one particle of such a pair occasionally gets absorbed by the black hole, while its counterpart escapes, manifesting as the observed radiation. Consequently, the black hole experiences a gradual loss of mass. "Gravitational heat" in relation to transient quantum black holes introduces a new type of energy that resembles dark energy in the universe. This energy differs from traditional thermal heat and represents a dynamic energy within the quantum vacuum.

In this framework, "gravitational heat" is the energy resulting from the movement or vibration of quantum gravity or spacetime quanta. These quanta are essential components of spacetime, and their activity generates gravitational heat. This understanding of energy extends beyond classic thermodynamic concepts.

Phonons, as quantized vibrational energy, are central to this concept. They facilitate the creation and disappearance of quantum black holes within the quantum vacuum. These phonons are not limited to transferring sound or mechanical vibrations; they are crucial in the quantum processes influencing black hole behavior.

Therefore, the temporary phenomena seen in black holes are more than just gravitational irregularities. They signal a complex and active process in spacetime. Gravitational heat, driven by phonons, marks a significant shift in our comprehension of fundamental forces and energy in the universe.

In essence, transient quantum black holes could be viewed as thermal effects within a warm space-time, where the energy of the quantum vacuum, manifested through phononic vibrations, contributes to the elusive dark energy of the universe. This perspective not only enriches our understanding of black holes but also opens up new avenues in the study of quantum gravity and the thermodynamic properties of space-time.

The mathematical foundation of Hawking radiation is rooted in quantum field theory in curved spacetime:

$$\left\langle T_{\mu\nu}\right\rangle = \frac{\hbar}{c^4} \left\langle \phi \right| \hat{T}_{\mu\nu} \left| \phi \right\rangle \tag{17}$$

where:

- $\langle T_{\mu\nu} \rangle$ is the expectation value of the energy-momentum tensor, representing the distribution and flow of energy and momentum in spacetime.
- \hbar is the reduced Planck constant, a cornerstone of quantum mechanics.
- *c* is the speed of light in a vacuum.
- $\langle \phi | \hat{T}_{\mu\nu} | \phi \rangle$ denotes the matrix element of the energy-momentum operator, $\hat{T}_{\mu\nu}$, between quantum states.

Sonoluminescence is a phenomenon where gas-filled bubbles in a liquid medium collapse due to intense sound waves, subsequently emitting light. Claudia Eberlein's interpretation of sonoluminescence involves quantum radiation emitted by moving interfaces between media of different polarizabilities [10]. While Eberlein does not explicitly describe these as black holes, her interpretation can be viewed in a light that parallels the concept of a transient quantum black hole and its event horizon.

In the context of black holes, the event horizon is a defining boundary beyond

which nothing, not even light, can escape. Black holes, contrary to popular belief, do not indiscriminately absorb all electromagnetic frequencies. They have a characteristic spectrum, much like particles. Particles, based on their resonant structures, absorb electromagnetic radiation at specific frequencies. Similarly, black holes have specific absorption and emission spectra, determined by their intrinsic properties such as mass, charge, and angular momentum.

Hawking radiation, a quantum mechanical phenomenon, is emitted due to quantum effects near the event horizon of black holes. Drawing a parallel to Eberlein's interpretation, the moving interface in sonoluminescence, which is reminiscent of the event horizon of a black hole, emits quantum radiation. The rapid collapse of these bubbles, which lasts about 1 μ s and can achieve pressures and temperatures up to 5 × 10⁸ Pa and 10⁴ K respectively, can be likened to the gravitational collapse that might lead to the transient formation of a quantum black hole. This suggests that sonoluminescence could be a terrestrial manifestation of Hawking radiation.

By drawing these parallels between particles and black holes, we emphasize a profound idea: black holes, often perceived as vast, macroscopic entities, exhibit quantum behaviors, much like subatomic particles. Both entities, despite their vast difference in scale, are governed by the principles of quantum mechanics. This perspective challenges traditional understanding and blurs the lines between the macroscopic and quantum realms, suggesting that black holes, at their essence, are quantum entities akin to particles.

5. Results: Evidence for Transient Quantum Black Holes in Sonoluminescence

The enigmatic phenomenon of sonoluminescence, where gas-filled bubbles in a liquid medium emit light upon collapsing due to intense sound waves, has long been a subject of scientific investigation. Recent theoretical advancements and experimental observations have hinted at a deeper underlying mechanism, drawing parallels between the rapid collapse of these bubbles and the gravitational collapse associated with black hole formation. This analogy becomes particularly profound when considering the influence of external magnetic fields on the dynamics of the collapsing bubble.

A pivotal study by Young, Schmiedel, and Kang [Phys. Rev. Lett. 77, 4816 (1996)] [11] experimentally highlighted the effect of a magnetic field on single-bubble sonoluminescence in water. Delving deeper into this observation, theoretical models suggest that the dynamics of the collapsing bubble are significantly altered by the magnetic field. This alteration arises as the moving water molecules within the liquid experience a torque due to the Lorentz force acting on their inherent electrical dipole moments. This interaction leads to a conversion of some of the bubble's kinetic energy into heat. Intriguingly, this magnetic influence on the energy dynamics of the collapsing bubble mirrors the behavior of matter-energy interactions near the event horizons of black holes, especially those exhibiting magnetic jets.

Furthermore, the theoretical framework indicates that the presence of the magnetic field behaves as though there's an increase in the ambient pressure of the liquid. This observation is pivotal, as variations in pressure can significantly influence the conditions under which sonoluminescence occurs, potentially modifying the emitted light's characteristics. The magnitude of this magnetic effect is also predicted to be directly proportional to the amount of liquid water present.

A noteworthy aspect of the theory is the prediction that nonpolar liquids, such as dodecane, would remain unaffected by the magnetic field. This distinction between polar and nonpolar liquids emphasizes the role of molecular interactions in the observed effects.

In light of these observations, the interplay between sonoluminescence and magnetic fields provides compelling evidence for the potential existence of transient quantum black holes, especially those exhibiting relativistic magnetic jets. These findings, rooted in fundamental physical principles, offer a rigorous framework that bridges experimental observations with theoretical predictions, furthering our understanding of the intricate relationship between light, matter, and magnetic fields in the context of quantum black holes.

5.1. Hawking Radiation and Time Dilation: Analyzing Gradual Energy Emission as a Relativistic Cavitation Process in Black Holes

Hawking radiation, as postulated by Stephen Hawking, posits that black holes, contrary to being completely black, can emit radiation due to quantum mechanical effects near their event horizon. This radiation, while negligible for large black holes, becomes pronounced for smaller black holes, especially those approaching the Planck mass. The genesis of this radiation is the Heisenberg uncertainty principle, which permits the spontaneous formation of virtual particle-antiparticle pairs near the event horizon. Occasionally, one particle from this pair falls into the black hole, while its counterpart escapes, resulting in the observed radiation.

In the universe, the fabric of spacetime is influenced by mass and energy. Massive objects, like stars and black holes, warp spacetime around them. This warping effect leads to gravitational time dilation, a phenomenon predicted by Einstein's theory of general relativity. Gravitational time dilation is described by the formula:

$$\Delta t' = \Delta t \sqrt{1 - \frac{2Gm}{rc^2}}$$

where:

- Δt is the time interval measured in a gravitational field.
- Δt is the proper time interval.
- *G* is the gravitational constant.

- *m* is the mass of the object causing the gravitational field.
- *r* is the distance from the center of the mass.
- *c* is the speed of light.

The density and composition of a star play a crucial role in its behavior and properties. A star's density, which is implicitly tied to its atomic composition, directly affects its radiance. The denser a star, meaning it has a heavier atomic composition, the more it warps spacetime around it. Consequently, the greater the gravitational time dilation experienced near it. This time dilation, in turn, affects the star's radiance, leading to a Doppler effect. The Doppler effect describes the change in frequency or wavelength of a wave in relation to an observer. In the context of stars, this means that the observed light or radiation from a star can be redshifted (shifted towards the longer wavelength, lower frequency end of the spectrum) or blueshifted (shifted towards the shorter wavelength, higher frequency end of the spectrum) depending on the relative motion and gravitational effects.

For a star, nuclear fusion in its core produces energy, which is released over millions of years. This energy release is regulated by the balance between gravitational forces and the outward pressure from fusion reactions. When a massive star exhausts its nuclear fuel, it can collapse under its own gravity, leading to the formation of a black hole. The gravitational field near a black hole is so intense that it causes significant time dilation. From an external observer's perspective, processes near the event horizon of a black hole appear to be "slowed down" due to this time dilation.

This perspective suggests that Hawking radiation is essentially a protracted version of the energy release seen in more immediate cosmic events, akin to viewing a black hole as a "slowly exploding star". The black hole's evaporation due to Hawking radiation can be thought of as the prolonged, slow-release explosion of the star, stretched out over an incredibly long timescale due to the effects of relativity.

Terrestrial Gamma-ray Flashes (TGFs) and pulsed sonoluminescence present intriguing analogies to Hawking radiation. TGFs, brief gamma-ray bursts believed to originate from thunderstorms, have been detected by cosmic gamma-ray observing satellites. While their exact origin remains elusive, they hint at extreme processes capable of efficiently converting matter into high-energy photons.

Pulsed sonoluminescence pertains to the emission of short light bursts from imploding bubbles in a liquid medium when subjected to a sound field. The rapid bubble collapse and subsequent light emission are reminiscent of energy release mechanisms near black hole event horizons.

By aligning the concepts of Hawking radiation with TGFs, pulsed sonoluminescence, and gravitational time dilation, we attain a comprehensive understanding of energy release mechanisms in the cosmos. Whether it's the gradual emission of Hawking radiation from a black hole or the swift light burst from a collapsing bubble (as shown in **Figure 5**), the foundational principles are anchored in the immutable laws of physics, offering a unified view of these seemingly distinct phenomena.

Solution type	Average max. radiance (W/nm)
Xenon in water	$1.04 imes 10^{-9}$
Krypton in water	$8.00 imes 10^{-10}$
Argon in water	$7.75 imes 10^{-10}$
Neon in water	$5.40 imes 10^{-10}$
Helium in water	4×10^{-10}

Hawking radiation emerges near the event horizon of a black hole, a boundary beyond which nothing can escape. The temperature of this radiation, given by:

$$T_{H} = \frac{\hbar c^{3}}{8\pi G M k_{B}}$$

is inversely proportional to the black hole's mass. Thus, smaller black holes have higher temperatures, leading to a more pronounced emission of Hawking radiation.

The radiation is a manifestation of Einstein's mass-energy equivalence, $E = mc^2$. As a black hole emits this radiation, it sheds mass, which is then converted into energy.



Figure 5. Stages of sonoluminescence in a collapsing bubble. From left to right: 1) Initial apparition of the bubble. 2) Gradual expansion phase, where the bubble grows in size. 3) Rapid and sudden contraction, with the bubble's radius decreasing significantly. 4) Emission of light, marking the zenith of the sonoluminescence phenomenon.

Considering gravitational time dilation near a massive object, we can express the gravitational mass *m* as:

$$m = \frac{rc^2 \left(1 - \left(\frac{\Delta t'}{\Delta t}\right)^2\right)}{2G}$$

Substituting this expression for m into the Hawking radiation temperature formula, we derive:



Simplifying further:

$$T_{H} = \frac{2\hbar c^{3}}{8\pi Grc^{2} \left(1 - \left(\frac{\Delta t'}{\Delta t}\right)^{2}\right) k_{B}}$$
$$T_{H} = \frac{\hbar c}{4\pi Gr \left(1 - \left(\frac{\Delta t'}{\Delta t}\right)^{2}\right) k_{B}}$$

This equation ties the temperature of Hawking radiation to the gravitational time dilation effects near the black hole, emphasizing the intricate interplay between quantum mechanics and general relativity.

Now, let's relate this to Claudia Eberlein's interpretation of sonoluminescence. In her interpretation, quantum radiation is emitted by moving interfaces between media of different polarizabilities. If we think of the event horizon of a black hole as a "temporal layer," then the gravitational time dilation equation introduces two temporal layers: Δt and Δt . The event horizon can be visualized as a median layer between these two temporal intervals.

In the context of sonoluminescence, the moving interfaces between different media can be likened to the event horizon of a black hole. The "temporal layers" in the gravitational time dilation equation can be seen as analogous to the interfaces in sonoluminescence. The event horizon (or the median layer) represents the boundary where these temporal intervals interact, leading to the emission of radiation.

This study of sonoluminescence and Terrestrial Gamma-Ray Flashes directly connects quantum mechanics with general relativity. Both phenomena involve quantum radiation emission, yet they occur under distinctly different circumstances.

In TGFs, energy release happens instantly, corresponding to the quick formation and complete evaporation of quantum black holes. This event is characterized by its speed, indicating the energetic and dynamic nature of these astrophysical occurrences. Essentially, the rapid evaporation in TGFs is like an abrupt burst in the quantum vacuum, instantly producing observable radiation.

Contrastingly, the evaporation of larger, cosmological black holes unfolds more slowly, influenced by gravitational time dilation around their event horizons. This results in a gradual release of Hawking radiation. The concept of time dilation introduces a "slowing down" effect in these regions, leading to a more drawn-out interaction between the quantum vacuum and the black hole's gravitational force.

This research demonstrates a clear and direct relationship between quantum mechanics and general relativity. It highlights how different gravitational environments can affect quantum processes. The findings significantly advance our understanding of high-energy astrophysical events and have important implications for the study of quantum gravity and the structure of spacetime.

By examining these phenomena, we get closer to a unified view of the universe's fundamental forces, bridging the gap between the micro and macro scales of the cosmos.

5.2. Advancing Nuclear Fusion through Controlled Cavitation

In the pursuit of nuclear fusion, a revolutionary approach is emerging, diverging from the traditional path of replicating stellar conditions. This novel method revolves around controlled cavitation, the process of forming and collapsing bubbles in a liquid. Unlike directly triggering nuclear fusion, this technique aims to achieve the extreme temperatures necessary for initiating the fusion process.

Cavitation, typically induced by sound waves or changes in pressure, leads to the dramatic implosion of bubbles within a fluid. This implosion generates both heat and light, a phenomenon known as sonoluminescence, as highlighted in (**Figure 5**). The conditions produced during this bubble collapse, though vastly different in scale from those in stellar nuclear fusion, are remarkably extreme. These intense temperatures and pressures offer a potential route to create environments suitable for fusion [12].

Viewing this process through the lens of quantum vacuum hydrodynamics provides further insight. This theoretical framework conceptualizes the quantum vacuum not as an empty void but as a dynamic, fluid-like medium. Within this context, the local conditions generated during cavitation parallel the high-energy environments necessary for fusion, bridging the gap between quantum physics and nuclear reactions.

The analogy with stellar fusion becomes evident when considering the creation of high-energy regions. In stars, nuclear fusion results from the immense gravitational forces and temperatures at their cores. In a similar vein, controlled cavitation replicates these conditions on a smaller scale during the bubble collapse, potentially setting the stage for fusion reactions.

The challenge, however, lies in the precise manipulation of cavitation to consistently produce the required fusion conditions. This would likely involve sophisticated acoustic or electromagnetic technologies to synchronize bubble implosions, ensuring a stable and uniform process.

Should this method prove successful, it could offer a compact and potentially more efficient solution for fusion energy production. This approach contrasts sharply with traditional fusion reactors, which necessitate large and complex setups. Controlled cavitation for fusion, instead, leverages the inherent properties of fluids and the quantum vacuum.

In essence, utilizing controlled cavitation as a means to achieve nuclear fusion conditions represents an intersection of fluid dynamics, quantum mechanics, and nuclear physics. While presenting significant engineering challenges, it also holds the promise of a groundbreaking energy production method. Such a technique could bring us closer to harnessing the immense power of the stars, right here on Earth.

6. Conclusions

In 1905, Albert Einstein introduced a paper on the photoelectric effect, detailing the emission of electrons from a material when exposed to electromagnetic radiation [13]. Central to Einstein's interpretation was the idea that light might be composed of discrete packets, or quanta, now recognized as photons. This concept nudged the scientific community towards the notion of energy quantization, a foundational element of quantum mechanics.

Drawing a cautious parallel to our current study, Einstein's work on the photoelectric effect opened discussions on energy quantization. Similarly, our preliminary observations on sonoluminescence might hint at properties related to the quantization of dark matter, dark energy, and gravitational field. If further research supports these implications, it could suggest new avenues of inquiry in our quest to understand the universe.

Scientific discovery often builds upon previous knowledge. In a way reminiscent of how the photoelectric effect contributed to quantum mechanics, our research on sonoluminescence might offer tentative clues about the quantization of dark matter and gravitational field.

6.1. Discontinuous Absorption in Photoelectric Effect, Sonoluminescence, and Black Holes

Both the photoelectric effect and sonoluminescence exhibit characteristics of quantized absorption. In the photoelectric effect, specific frequencies of light are absorbed by atoms, leading to electron emission. Similarly, in sonoluminescence, the rapid bubble collapse might absorb specific quantized vibrational energies, leading to light emission.

Black holes, especially considering Hawking radiation, present a more intricate absorption spectrum. Contrary to the perception that black holes "absorb everything," their absorption isn't entirely continuous. The larger the black hole, the broader its absorption spectrum. However, due to quantum effects, black holes also emit Hawking radiation, tied to quantum fluctuations near the event horizon and inversely proportional to the black hole's mass. The discontinuity in absorption can be represented as:

$$A(f) = \begin{cases} 0 & \text{if } f < f_{\text{threshold}} \\ 1 & \text{if } f \ge f_{\text{threshold}} \end{cases}$$

where A(f) is the absorption function and f is the frequency of the incoming particle (photon or phonon). $f_{\text{threshold}}$ is the frequency threshold below which no absorption occurs.

For black holes, the relationship between the mass of the black hole M and its emitted Hawking radiation R_H can be expressed as:

$$R_H \propto \frac{1}{M}$$

This indicates that as the mass of the black hole increases, its Hawking radiation decreases.

In the context of Terrestrial Gamma-ray Flashes (TGFs), it is postulated that the observed gamma-ray emissions could be indicative of micro black holes undergoing complete evaporation. On the other hand, in sonoluminescence, the evaporation is transient, with the collapsing bubbles emitting light without a complete evaporation analogous to black holes.

In conclusion, our study of TGFs and sonoluminescence suggests potential insights into the nature of dark matter and its quantum gravitational effects on Earth. The initial findings underscore the interconnectedness of various phenomena and the importance of interdisciplinary research in understanding our universe.

6.2. Dark Matter Halos: A Cosmological Proof for Quantum Gravity

Dark matter, intricately interwoven within galactic structures, presents a profound enigma in cosmology. Its elusive nature is intimately linked to the Higgs field and phononic interactions within the quantum vacuum, offering invaluable insights into the universe's deepest mysteries. As we delve into dark matter's complexities, we navigate a cosmic symphony where the Higgs field's nuanced influences and the resonant vibrations of phonons in the quantum vacuum are key players. In this complex interplay of fundamental forces and particles, lies our quest to unlock the universe's secrets, inspired by Nikola Tesla's insight: "To understand the universe, think in terms of energy, frequency, and vibration".

At the heart of this exploration is the energy-momentum tensor for dark matter, T_{uv} , which plays a pivotal role in our modified Einstein field equations:

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi \left(T^{\circ}_{\mu\nu} + T^{\bullet}_{\mu\nu} \right)$$

This tensor encapsulates dark matter's influence on cosmological dynamics:

$$T^{\star}_{\mu\nu} = \left(\rho^{\star} + \frac{p^{\star}}{c^2}\right) U^{\star}_{\mu} U^{\star}_{\nu} + p^{\star} g_{\mu\nu}$$

Here, ρ represents the density of dark matter, integral to understanding

mass distribution within galactic halos. The pressure component p^{\cdot} , typically minor in cold dark matter models, simplifies the tensor to focus primarily on density. The four-velocity components, U^{\cdot}_{μ} and U^{\cdot}_{ν} , reflect the cold, non-relativistic nature of dark matter, while $g_{\mu\nu}$ describes the spacetime metric.

In galactic halos, $T^{*}_{\mu\nu}$ is essential for mapping dark matter's energy and momentum. This tensor is key to understanding gravitational effects in galaxy rotation curves and gravitational lensing, indicative of collective quantum behaviors and spin properties at quantum scales. The inclusion of Λ , representing dark energy, accounts for the universe's accelerated expansion. Meanwhile, visible matter's tensor, $T^{\circ}_{\mu\nu}$, offers a comprehensive view of gravitational interactions.

This model posits that dark matter halos are not only critical to cosmic structures but also potential evidence of the gravitational field's quantization. Investigating these halos could provide insights into dark matter's nature and significantly contribute to a kinetic quantum molecular theory of vacuum. This theory aims to integrate quantum mechanics with general relativity seamlessly, offering a novel perspective on the fundamental principles governing our universe.

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Conflicts of Interest

At the time of writing, the author confirms that there are no competing financial interests or personal affiliations that could have swayed the results or interpretations presented in this paper.

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