

The First Principle Study of β -CuAgSe Subcells

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Abstract

CuAgSe has been considered as a promising thermoelectric material because of its high mobility and low thermal conductivity. The superior performance of CuAgSe is closely related to its crystal structure and electric properties. In this work, the stabilities and electronic structures of different three CuAgSe subcells have been theoretically investigated using Vienna Ab initio Simulation Package (VASP) with DFT calculations. We found that the different occupations of copper atoms would affect the stability and electronic structures of CuAgSe subcells. The various directions of Cu-Se chain in neighbor layers will result in different stabilities and electronic properties.

Keywords

CuAgSe, Subcells, Stability, Electronic Property

1. Introduction

Copper chalcogenides have been regarded as promising functional materials for their application in thermoelectrics [1] [2] [3], photovoltaics [4] [5], superconductivity [6] [7], sensors [8] and solar cell applications [9] [10] [11]. Among these copper chalcogenides, CuAgSe is a promising thermoelectric material because it has extremely high carrier mobility and relatively low thermal conductivity [12] [13] [14].

The superior performance of CuAgSe is closely related to its crystal structure and electric properties [15]. It had been reported that CuAgSe has two phases: low temperature β -phase and high temperature α -phase, which is similar to Cu₂Se [16] [17]. At low temperature, CuAgSe has a tetragonal or orthorhombic unit cell (with little difference of lattice parameter in b axis, listed in **Table 1**). Both of these two symmetries had been found in experimental works [18] [19]. In a unit cell of LT structure, two Ag atoms located in positions: (1/4, 1/4, 0.551), (3/4, 3/4, 0.449) and two Se atoms in positions: (1/4, 1/4, 0.127), (3/4, 3/4, 0.873),

respectively. Besides, there are four equivalent positions for two Cu atoms, namely $(1/4, 3/4, 0.105)$, $(3/4, 1/4, 0.895)$, $(3/4, 1/4, 0.105)$ and $(1/4, 3/4, 0.895)$.

Typically, Cu atoms will occupy the two positions in diagonal positions in a unit cell [20]. That is to say, one Cu atom in position: $(1/4, 3/4, 0.105)$ and another in position: $(3/4, 1/4, 0.895)$. In this case, chains will be formed by Cu atoms and their nearest Se atoms. As shown in **Figure 1(a)**, these chains have the same direction and are connected as CuSe layers. Ag atoms take the places between CuSe layers to form a layered structure of β -CuAgSe (This subcell structure will be called S1 for short below).

Moreover, the equivalent positions for Cu atoms are not fully occupied, there are many vacancies for Cu to diffuse. In this way, Cu atoms can diffuse between the nearest Cu-Se layers to form other two sublattice structures. In one subcell, Cu atoms will locate at the positions $(1/4, 3/4, 0.105)$ and $(3/4, 1/4, 0.105)$, as shown in **Figure 1(b)**. In this structure, Cu atoms will get together in the same Cu-Se layers. In their neighbor layers, there are only Se atoms (This subcell structure will be called S2 for short below). The third subcell structure contains two Cu atoms in positions $(1/4, 3/4, 0.105)$ and $(1/4, 3/4, 0.895)$. In this case, Cu atoms will also be chained with their nearest Se atoms. Different from the subcell above, these Cu-Se chains have different directions with their neighbor layers, as shown in **Figure 1(c)** (This subcell structure will be called S3 for short below).

In this work, we will firstly discuss total energies of the mentioned low temperature CuAgSe subcells, to have a theoretical understanding of the stabilities of them. And then, the electronic band structures and projected density of states will also be discussed. Besides, DFT + U works are included to reveal the contributions from d electrons as well.

Table 1. The lattice parameters of orthorhombic structure and tetragonal structure of β -CuAgSe.

Structure	Space Group	Lattice Parameter (Å)		
		a	b	c
orthorhombic	Pmmn	4.105	4.07	6.31
tetragonal	P4/nmm	4.105	4.105	6.31

a, b, c are the lattice parameters of a unitcell in three directions. The directions can be seen in **Figure 1**.

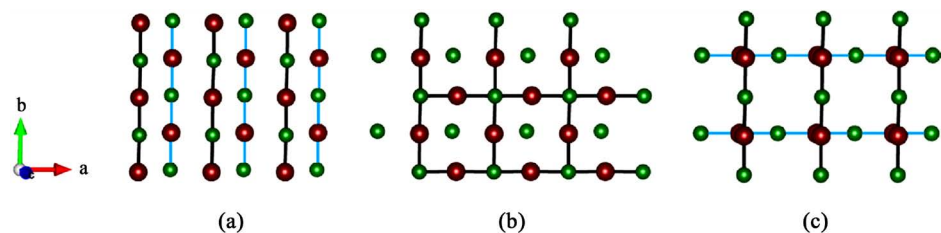


Figure 1. The top view of (a) S1, (b) S2 and (c) S3. Green, silvery and deep red spheres are respectively Se, Ag and Cu atoms. The occupancy of the Cu site is 0.5. The crystal structures are visualized in VESTA [21]. For convenient observation, Cu-Se bond in different layers is colored with color darkgray and color blue, respectively.

2. Computational Details

The calculation of this work is based on density functional theory (DFT) [22] and implemented in the Vienna Ab initio Simulation Package (VASP) [23] [24]. We use the Perdew-Burke-Ernzerhof (PBE) type of generalized gradient approximation (GGA) as the exchange-correlation functional [25] [26] [27]. The valence electron configurations employed in our calculations are Cu (3d10, 4s1), Ag (4d10, 5s1) and Se (4s2, 4p4). The interaction between the core electrons and the valence electrons is included by the standard frozen-core projector augmented-wave (PAW) potentials provided within the VASP package [28] [29] [30]. The plane-wave cutoff energy is set to 600 eV in this calculation. Because Cu atom and Ag atom belong to transition metal elements, in order to verify the results of electronic structures, we also use PBE + U method to calculate the energy structures and density of states. The calculation use the PBE + U method with $U = 4.0$ eV to approximately describe the Cu-3d electrons, and we also use $U = 2.0$ eV to approximately describe the Ag-4d electrons [31] [32] [33]. During the optimization, in consideration of dimensions of the structure and the convergence of the forces, we adopt the Monkhorst-Pack scheme k-point mesh [34] [35] from gamma to the $21 \times 21 \times 21$ point and use finer k-points to further calculate the electronic structures. The relaxation of the electronic degrees of freedom stops when both the total energy and the band structure energy variations between two steps are smaller than 10^{-6} eV. When we do a static calculation, we use ISMEAR = -5 and ionic relaxation goes on as long as any force is larger than 0.0001 eV/Å, but it will immediately stop when the force is larger than 0.02 eV/Å. The detailed atomic coordinates are listed in **Table 2**. We construct three subcell through VESTA to concretely show these three configurations (as shown in **Figure 1**).

3. Results and Discussion

Before reporting the electronic structures of the mentioned subcells, we will firstly discuss the stability of them. The stability of a material can be characterized by the total energy. The total energy, E_{tot} can be expressed by Equation (1):

$$E_{\text{tot}} = E_{\text{energy without entropy}} + T \times S \quad (1)$$

where E_{tot} is the total energy, $E_{\text{energy without entropy}}$ is the energy without entropy. In this work, $T \times S$ is set to be 0, so that E_{tot} is equal to $E_{\text{energy without entropy}}$. Therefore, we calculated the total energies of three CuAgSe subcells with various lattice

Table 2. The detailed atomic coordinates of the three sub-lattices structures of CuAgSe [20].

Structure	Ag1	Ag2	Se1	Se2	Cu1	Cu2
S1					(1/4, 3/4, 0.105)	(3/4, 1/4, 0.895)
S2	(1/4, 1/4, 0.551)	(3/4, 3/4, 0.449)	(1/4, 1/4, 0.127)	(3/4, 3/4, 0.873)	(1/4, 3/4, 0.105)	(1/4, 3/4, 0.895)
S3					(1/4, 3/4, 0.105)	(3/4, 1/4, 0.105)

parameters, to determine the influence of copper occupation on the stabilities and electronic structures to all mentioned subcells above.

3.1. The Stabilities

The calculated total energies with various scaled lattice parameters have been shown in **Figure 2**. Where the scaled 1.00 refers to the lattice parameter reported in experimental works [20] [36]. Both orthorhombic and tetragonal structures are plotted together for convenient comparison. For these two symmetries, the relationship between total energies and scaled lattice parameters are very similar, the little differences in b-axis do not have significant effect on the total energies.

For S1 and S2, their total energy plots have very similar trends. Although there is a little difference in the plots of orthorhombic and tetragonal symmetries, they have the same lowest positions of the total energy, which located at 0.99, very closely to former experimental works [37] [38]. As listed in **Table 3**, for S1 and S2, the lowest energies are -23.0682 eV (ortho) and -23.0548 eV (tetra) for S1 and -23.0684 eV (ortho) and -23.0550 eV (tetra) for S2, respectively. These locations of lowest total energies match well with former experimental works, which revealed the coexistence of these two symmetries [16] [39].

The total energy plot of S3 is quietly different from those of S1 and S2. As shown in **Figure 2(c)**, the lines oscillate firstly and then go down to smaller values.

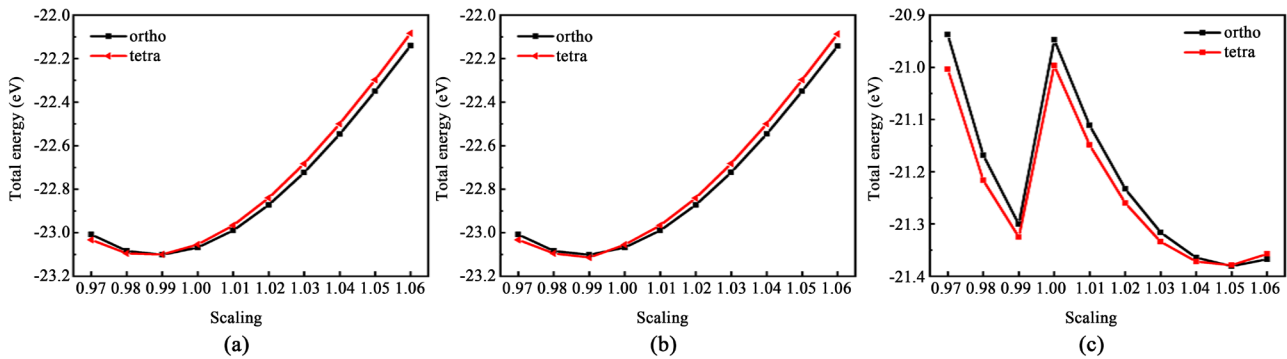


Figure 2. The total energies of S1, S2 and S3 with scaling the lattice parameters. (a)-(c) results using PBE recipe. From left to right are S1, S2 and S3, respectively. The black line represents orthogonal structure and the red line represents tetragonal structure.

Table 3. The total energy of orthorhombic and tetragonal phase of S1, S2, S3 at the equilibrium lattice constants in using PBE recipe.

Structure	Phase (space group)	Total Energy (eV) PBE
S1	Orthorhombic (Pmmn)	-23.0682
		-23.0548
S2	Orthorhombic (Pmmn)	-23.0684
	Tetragonal (P4/nmm)	-23.0550
S3		-20.9473
		-20.9965

The lowest total energies located at 1.05, which is a bit far from those in experimental works [38]. Besides, the lowest energy of S3 is much higher than those of S1 and S2. In the considerations of above, we think S3 is relatively unstable subcell.

3.2. The Electronic Properties

3.2.1. Band Structures

We first carry out the electronic band structures of S1, S2 and S3. For a direct comparison, tetragonal and orthorhombic structures are plotted together with the same path: Γ -X-M- Γ -Z [40], since they have nearly the same lattice constant (so the reciprocal lattice). It can be seen that the plotted bands for tetragonal and orthorhombic structures are almost overlapped, which means that the symmetry has little effect on the electronic structure, so our discussions will focus on the differences between different subcells.

In **Figure 3(a)**, S1 is predicted to be a semimetal with the Fermi level crossing bands along Γ -X and Γ -Z lines. There is a peak at Fermi level in the total density of states for S1. While for S2 and S3 (shown in **Figure 3(b)** and **Figure 3(c)**), they are predicted to be semimetals as well (but smaller peak at Fermi level), according to the total density of states. Early experimental works [12] had reported CuAgSe is a semimetal. As mentioned above, the total energy of S1 and S2 are nearly the same. Besides, the total energy of S3 is relatively high. If so, S1 and S2 are more like to exist and contribute to the electronic properties of CuAgSe. That is to say, the semimetal behavior of CuAgSe may result from the contributions of both S1 and S2.

3.2.2. DFT + U

Recently, Råsander *et al.* studied the electronic properties of fluorite Cu₂Se using the DFT + U approaches. The results obtained by LDA + U show that a adequately high U opens up a gap [41]. Moreover, Yb Zhang *et al.* using the mBJ + U approach investigated Cu₂X (X = S, Se, Te), and found impose different U

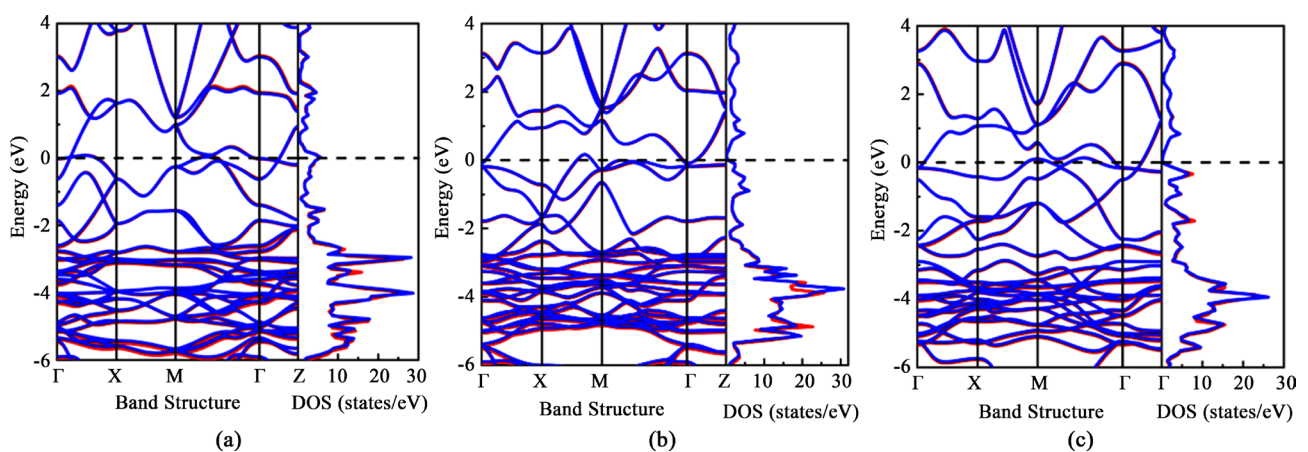


Figure 3. The band structures and total DOS of S1, S2, S3 under PBE. The red lines represent orthogonal structure and the blue lines are tetragonal structure. The dash lines are Fermi level.

values on the 3d orbital of Cu, and the band gap gradually increases with increasing U [33]. Hence, we introduced DFT + U to further study the electronic band structures of CuAgSe. We use the PBE + U method with $U = 4.0$ eV to approximately describe the Cu-3d electrons, and we also use $U = 2.0$ eV to approximately describe the Ag-4d electrons. The calculated band structures are shown in **Figure 4**, the plotted bands for tetragonal and orthorhombic structures are almost overlapped. Their band structures have little difference compared with them without U indicating CuAgSe in low temperature still is a metal conductor and the application of U has little effect on the electronic band structures of CuAgSe.

3.2.3. Density of States

Then we investigate the projected density of states of CuAgSe with different Cu positions. The calculated DOS of tetragonal subcells and orthorhombic subcells are very similar, so only the DOS of tetragonal subcells are shown in **Figure 5**.

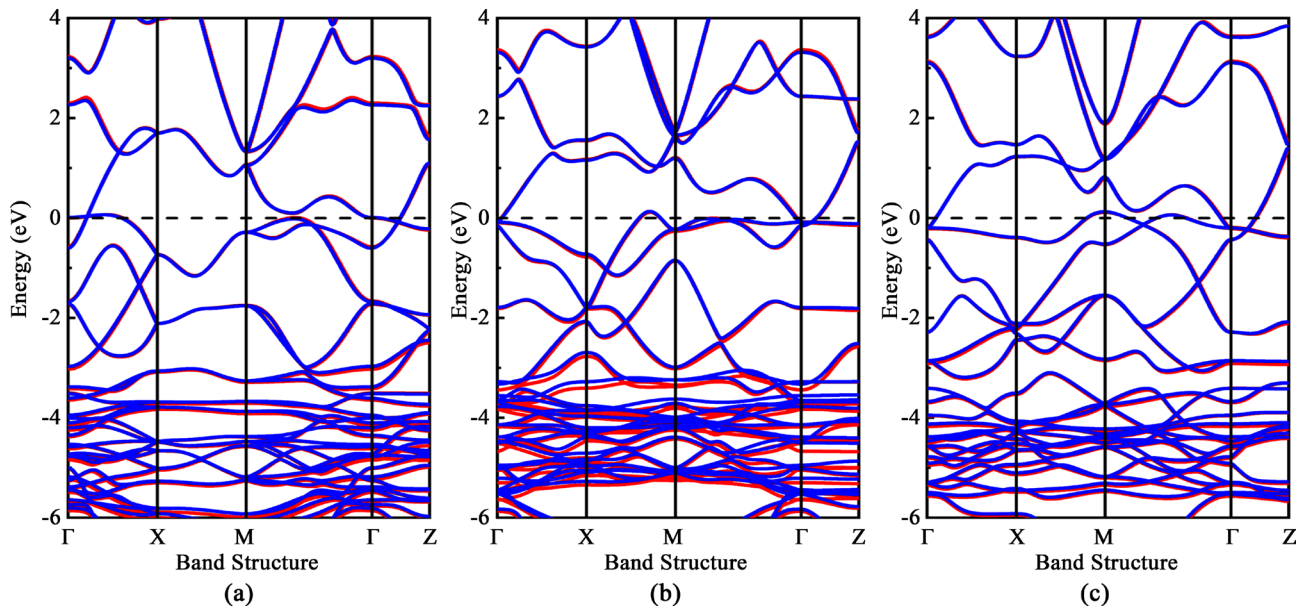


Figure 4. The Band structures of S1, S2 and S3 with DFT + U (we use $U = 4.0$ eV to approximately describe the Cu-3d electrons, and we also use $U = 2.0$ eV to approximately describe the Ag-4d electrons.). The red lines represent the orthorhombic structure of S1, S2 and S3, the blue lines are the tetragonal structure of S1, S2 and S3.

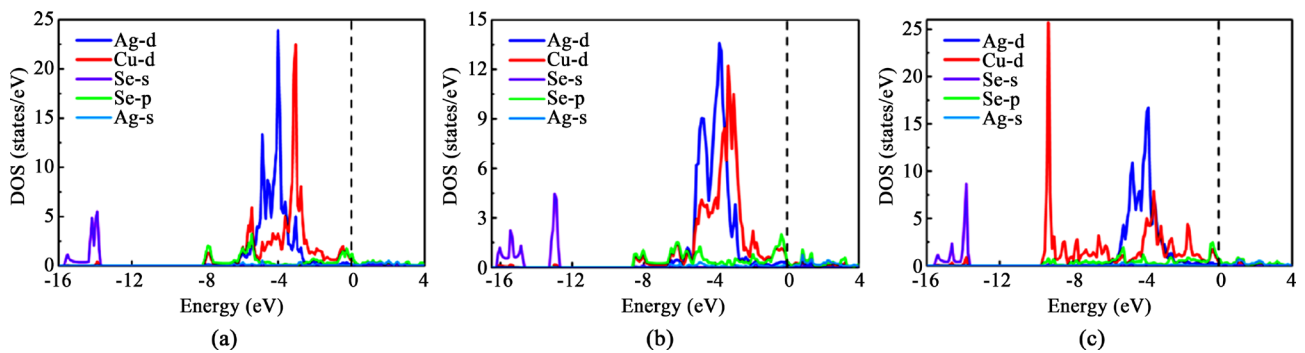


Figure 5. The DOS of tetragonal symmetry structures of S1, S2 and S3 with using PBE recipe, respectively. The dotted lines represent the Fermi levels.

For S1 (**Figure 5(a)**), the lowest band located at -16 eV to -13.5 eV is derived from Se 4s states and the semimetal behavior is mainly contributed by Cu 3d electrons and Se 4p electrons. The hybridization of Cu 3d electrons and Se 4p electrons can also be found in -8 eV to -7.5 eV and -6 eV to -5 eV. Besides, comparable Ag 4d states are found in -6 eV to -5.3 eV as well. The region from -5 eV to -2.5 eV is mainly built up by Cu 3d states and Ag 4d states. The Cu 3d peak and Ag 4d peak lie between the energy level discussed above. This indicates the hybridization below Fermi level are anti-bonding states and bonding states lie below -5 eV, respectively.

The Cu 3d and Se 4p hybridization of S2 is similar to S1. We can see in **Figure 5(b)**, the bands of S2 located -16.5 eV to -14.5 eV and -13.5 eV to -12.5 eV are also derived from Se 4s states. Nevertheless, the mixing states of Cu 3d and Se 4p lie at lower energy level, just below the Fermi level. For S2, the overlap of Ag 4d states and Cu 3d states from -5 eV to -3 eV is much larger than that of S1, indicate a stronger correlation of Cu 3d electrons and Ag 4d electrons.

The calculated DOS of S3 (as shown in **Figure 5(c)**) is very different from S1 and S2. Between -16 eV and -13.5 eV, the lowest band is contributed by Se 4s states, and S3 has higher states than the other two structures. The pd hybridization of Cu 3d electron and Se 4p electron becomes much weaker. Moreover, at the region from -10 eV to -6 eV, the DOS is almost composed by Cu 3d states, in contrast to S1 and S2, there are small Cu 3d peaks refer to the pd hybridization. Comparable Cu 3d states and Ag 4d states are found in -3.5 eV to -3 eV, indicate a correlation of them.

As discussed above, S1 and S2 have nearly the same total energies. The difference of their crystal structures is attributed to the directions of Cu-Se chains. The Cu-Se chains are parallel in S1 and perpendicular in S2, respectively. Because of the layered structure, the bonding states are basically composed by Cu-Se layers. Thus, the differences of electronic structures between S1, S2, and even S3, are contributed by the pd hybridizations of Cu and Se. Since the total energy of S3 is much higher than S1 and S2, the observed behavior of CuAgSe may contributed from a mixing of the feature of S1 and S2, *i.e.*, the directions of Cu-Se chains.

4. Conclusion

In this work, the total energies, electronic structures and density of states of three different CuAgSe subcells have been systematically studied by first principle calculations. Tetragonal and orthorhombic CuAgSe has nearly the same total energies, for both S1 and S2. The observed results that located at 0.99 S1 and S2 have the lowest total energies matched well with former experimental works. However, S3 has its lowest total energy located at 1.05, which is a bit far from experimental results. The calculated electronic structures show that all the three CuAgSe subcells are semimetals, and the little differences in b-axis do not have significant effect on the total energies and electronic properties. Moreover, DFT

+ U works were adopted to reveal the contributions from d electrons as well, but there was little effect on the electronic band structures. The projected density of states shows that the semimetal behavior of β -CuAgSe is mainly contributed by Cu 3d electrons and Se 4p electrons, and the differences of electronic structures between S1, S2, and even S3, are contributed by the pd hybridizations of Cu and Se. The observed electronic structures and behaviors of CuAgSe may be attributed from the different Cu-Se chain directions. Study on the layered structures and subcells will help understand copper chalcogenides with Cu vacancies [42] [43].

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Conflicts of Interest

The authors declare no conflicts of interest regarding the publication of this paper.

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