

Cosmic Dark Energy Density from Classical Mechanics and Seemingly Redundant Riemannian Finitely Many Tensor Components of Einstein's General Relativity

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Received 16 March 2014; revised 15 April 2014; accepted 12 May 2014

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Abstract

We determine the limit of the ratio formed by the independent components of the Riemann tensor to the non-zero component as space dimensionality tends to infinity and find it to be 12. Subsequently we use this result in conjunction with Newtonian classical mechanics to show that the ordinary measurable cosmic energy density is given by $E(O) = \left(\frac{1}{2}\right)\left(\frac{1}{12-1}\right)mc^2$ while the dark energy density is obviously the Legendre transformation dual energy $E(D) = 1 - E(O)$. The result is in complete agreement with the COBE, WMAP and type 1a supernova measurements.

Keywords

Semi Classical Quantum Systems, Dark Energy, Accelerated Cosmic Expansion, Riemannian Tensor, Infinite Dimensional Topology, Nonlocal Elasticity

1. Introduction

The present analysis, although quite short and straight forward, is never the less of considerable importance to the understanding of arguably one of the most difficult questions presently facing both theoretical physics and cosmology, *i.e.*, the meaning and nature of dark energy [1]-[8]. Unlike previous publications we concentrate here on taking the limit of infinite dimensional geometry and proceed from there, using Newtonian mechanics only, to show that the analysis and results are consistent with a physical truly fractal and Cantorian spacetime [4]-[10]. Finally we hint at a connection to nonlocal elasticity [11]-[13].

How to cite this paper: El Naschie, M. (2014) Cosmic Dark Energy Density from Classical Mechanics and Seemingly Redundant Riemannian Finitely Many Tensor Components of Einstein's General Relativity. *World Journal of Mechanics*, 4, 153-156. <http://dx.doi.org/10.4236/wjm.2014.46017>

2. Analysis

In the following short communication we employ what is essentially a fractal spacetime picture to compute the dark energy density [1]-[10] via the ratio of non-zero components [1] to the total number of independent components in n dimensions when we let n tend to infinity. We recall that voids in spacetime are essentially empty sets with a negative Menger-Uhryson topological dimension while ordinary spacetime are zero sets [10]. Said in the language of fractals, empty regions are fat fractals while non-empty regions of spacetime are thin fractals [4]-[10]. Translated to the algebraic geometry of a Riemannian tensor, the ordinary spacetime regions are represented by the non-zero component of the tensor in n dimensions which are given as is well known by [1]:

$$N_1 = N(\text{non-zero component}) = n^2 (n-1)^2 \quad (1)$$

On the other hand the total numbers of independent components are given by the well known Formula:

$$N_2 = N(\text{independent component}) = n^2 (n^2 - 1)/12 \quad (2)$$

Following what we reasoned earlier on then we can regard the sparsity ratio N_2/N_1 as essentially the Lorentzian factor in Einstein's Formula [7]-[10]. That means we regard $E = \gamma mc^2 = mc^2$ as the regular hundred percent total energy density which is a basic tacit assumption in all our non-fractal theories in high energy physics and cosmology. Consequently Newton's kinetic energy [4]-[10]:

$$E_N = \frac{1}{2}mv^2 \quad (3)$$

could be thought of as a generalization of Einstein's energy when $v \rightarrow c$ and $\frac{1}{2} \rightarrow 1$ [10]. This limit corresponds in set theoretical formulation to when the zero set $d_c^{(0)} = \phi$ changes its average value $\langle d_c^{(0)} \rangle = \frac{1}{2}$ and tends to the unitary set $\langle d_c^{(0)} \rangle = 1$ [10]. Following this transfinite set theoretical logic we can write [5]-[8]:

$$E = (\gamma) \left[\frac{1}{2} m (v \rightarrow c)^2 \right] = (\gamma/2) mc^2 \quad (4)$$

On the other hand for a Cantorian fractal formal dimensionality is intrinsically $n \rightarrow \infty$. Therefore by letting n go to infinity and using the role of de L'Hopital we have [1]:

$$\gamma(n \rightarrow \infty) = \left[n^2 (n^2 - 1)/12 \right] / \left[n^2 (n-1)^2 \right] = \frac{1}{12} \left[\frac{(n-1)(n+1)}{(n-1)^2} \right] = \frac{1}{12} \frac{n+1}{n-1} = \frac{1}{12} \quad (5)$$

Inserting in E we find the following slightly inaccurate result as will be explained later [4]-[10]:

$$E = \left(\frac{1}{2} \right) \frac{1}{12} m (v \rightarrow c)^2 \quad (6)$$

Now a direct comparison between $E = mc^2$ and $E(0)$ could not be made unless we become completely aware that $E = mc^2$ was tacitly based on a one degree of freedom Lagrangian which Einstein never wrote down. This is of course the U(1) single photon degree of freedom leading to $E = mc^2$. The above formula however has taken on board also indirectly 12 degrees of freedom $\lambda = 1/\gamma = 12$ representing the 12 messenger photons of the standard model, *i.e.*, $|\text{SU}(3)| = 8$ gluons, $|\text{SU}(2)| = 3$ (W^+ , W^- , Z^0) and $|\text{U}(1)| = 1$ photon [10]. Consequently consistency requires us to subtract the ordinary photon from our 12 messenger particles so that we do not double count it. In other words we have the following consistent limits:

$$d_c^{(0)} = \phi \rightarrow \langle d_c^{(0)} \rangle = \frac{1}{2} \quad (7)$$

$$\langle d_c^{(0)} \rangle = \frac{1}{2} \rightarrow d_c^{(0)} = d_c^{(1)} = 1 \quad (8)$$

$$v \rightarrow c \quad (9)$$

$$\frac{1}{12} \rightarrow \frac{1}{12-1} = \frac{1}{11} \quad (10)$$

$$\gamma = 1 \rightarrow \gamma = \left(\frac{1}{2}\right)\left(\frac{1}{11}\right) = \frac{1}{22} \quad (11)$$

That way we find the correction $\gamma = \left(\frac{1}{2}\right)\left(\frac{1}{12-1}\right)$ and thus:

$$E = mc^2 \rightarrow E(0) = mc^2/22 \quad (12)$$

From the above the dark energy density is easily deduced to be [4]-[10]:

$$E(D) = mc^2 - (mc^2/22) = mc^2 (21/22) \quad (13)$$

which is 95.5% of the total energy in full agreement with measurements as well as previous theoretical derivations. We could validate the preceding result in virtually one line of analysis when we consider that the only non-zero components of the Riemann tensor of general relativity is 24 [1] and compare that with the maximal possible of symmetries as given by the killing vector fields of Witten's 5 Brane theory in eleven dimensions, namely 528. The ratio γ is then given in a trivial straight forward way by [4]-[10]:

$$\gamma = \frac{24}{528} = \frac{1}{22} \quad (14)$$

exactly as shown above. Dark energy density is consequently [5]-[8]:

$$E(D) = mc^2 \frac{528-24}{528} = \frac{504}{528} mc^2 = mc^2 (21/22) \quad (15)$$

also as shown above.

3. Conclusion

In the present short analysis we started from an infinite dimensional geometry and topology and ended with a finite expression for both the ordinary and the dark energy density of the cosmos. The result, as expected, is in full agreement with measurements but we gained additional evidence for the true physical fractality of spacetime at both the quantum as well as the cosmological level [1]-[10]. It is crucial to appreciate the deep meaning and implications of obtaining a quantum gravity result in agreement with cosmic measurements using essentially Newtonian classical mechanics and without involving quantum mechanics. We stress that this is only possible because of our use of nonclassical fractal-Cantorian spacetime geometry and infinite dimensional topology [4]-[10]. We note on passing that we have very recently discovered that all the above results could also be obtained using the nonlocal elasticity theory of A. C. Eringen [6] [11]-[14] which is a welcome confirmation of the basic philosophy of the present work, namely the unity of physics, mathematics, engineering and philosophy [14].

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