# First-Principles Study on Stability and Magnetism of $MAl_n$ (M = Ni, Cu) (n = 1 - 9) Clusters

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# ABSTRACT

We have investigated the structures, stabilities and magnetism of NiAl<sub>n</sub> and CuAl<sub>n</sub> (n = 1 - 9) clusters systematically by using first-principles density functional theory. Our calculated results indicate that most of the ground state structures for the Al clusters doped with one nickel or copper atom are different from those of the corresponding pure Al clusters. NiAl<sub>n</sub> and CuAl<sub>n</sub> (n = 1 - 9) cluster ions have similar geometrical configurations to the corresponding neutral clusters, except for positive NiAl<sub>9</sub> ion. The magnetic moments of NiAl<sub>n</sub> (n = odd number) and CuAl<sub>n</sub> (n = even number) cluster anions, neutrals and cations are 0, 1  $\mu_B$ , and 2  $\mu_B$ , respectively. The magnetic moments of NiAl<sub>4</sub> and NiAl<sub>6</sub> cluster anions, neutrals and cations are associated with 1  $\mu_B$ , 2  $\mu_B$ , and 3  $\mu_B$ , respectively. NiAl<sub>2</sub>, NiAl<sub>8</sub> and CuAl<sub>n</sub> (n = odd number) clusters do not have any net magnetic moment. But, NiAl<sub>2</sub> and NiAl<sub>8</sub> cluster ions have the net magnetic moment of 1  $\mu_B$ .

Keywords: NiAl Cluster; CuAl Cluster; Stable Structure; Magnetism

## 1. Introduction

Transition-metal aluminides [1] and nickel-aluminum alloys [2] have attracted much attention due to their wide applications in advanced material technology. Both Albased compounds of transition-metals (TM) [3] and nickel-based superalloys [4-6] are among the most promising candidates for high-performance structural materials. In the nanoscale regime, the nickel-aluminum bimetallic nanocluster has martensitic transformation as temperature alternation, which aroused many studies [7-10]. Their chemical and physical properties may vary with the composition, atomic ordering and the cluster size.

Wen *et al.* investigated Ni<sub>n</sub>Al (n = 2 - 8) neutral clusters using the density functional theory based on generalized gradient approximation (GGA) with the exchangecorrelation potential (BPW91) [7]. They found that atomization energies per atom for Ni<sub>n</sub>Al (n = 2 - 8) clusters has the same trend as the binding energies per atom for Ni<sub>n</sub> (n = 3 - 9) clusters. Ni<sub>5</sub>Al is the relatively most stable structure in the series. Ni average magnetic moment decreases when alloyed with Al atoms than that in pure Ni clusters. Wang *et al.* [8] calculated the magnetic properties of MAl<sub>n</sub> (M = Cr, Mn, Fe, Co, Ni; n = 1 - 7, 12) clusters using density-functional theory based on generalized gradient approximation. They found that the MAl<sub>n</sub> clusters have similar geometries as that of Al<sub>n+1</sub> clusters. The computed total magnetic moments of the lowest-energy structures oscillate with the cluster size. Deshpande *et al.* reported the magnetic properties of small Ni<sub>13-n</sub>Al<sub>n</sub> clusters with n = 0 - 13 calculated in the framework of density functional theory [9]. The overall magnetic moment of the Ni<sub>13-n</sub>Al<sub>n</sub> cluster decreases as Al atoms increases. Bailey *et al.* presented their research results about nickel and aluminum clusters and nickelaluminum nanoalloy clusters with up to 55 atoms. They investigated the effect of doping Al atoms into pure Ni clusters and *vice versa* [10].

In this paper, we will report our result about investigation on the NiAl<sub>n</sub> and CuAl<sub>n</sub> (n = 1 - 9) clusters by using first-principles calculations. Our calculations were performed with the generalized gradient approximation (GGA) by means of the Becke-Perdew functional, which uses Becke's [11] gradient correction to the local expression for the exchange energy and Perdew's [6] gradient correction to the local expression of the correlation energy, as implemented in the Amsterdam Density Functional (ADF) codes [12,13]. The self-consistent field was converged to a value of  $10^{-6}$ .

Frequencies were computed using numerical different-

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tiation of gradients computed in slightly displaced geometries. The binding energy (BE) for the NiAl<sub>n</sub> cluster is calculated according to the following atomization reaction: NiAl<sub>n</sub>  $\rightarrow$  Ni + nA1. It is defined by the following: BE = E<sub>Ni</sub> + nE<sub>A1</sub> - E<sub>NiAl<sub>n</sub></sub>, where E is the total energy of the system. For the CuAl<sub>n</sub> cluster, similar calculation is made.

#### 2. Results and Discussions

In order to reach the global minimum at energy surface, we chose a random way to produce initial geometrical configurations, and then used the Amsterdam Density Functional (ADF) package for geometrical optimizations. In this way, about one hundred thousand initial geometrical configurations are produced automatically within a three-dimensional box, or a cage, or a ball in real space. The separations of Al-Al, Ni-Al and Ni-Ni atoms are properly chosen to avoid overlapping or loosely packing. After the structural optimization on the initial configuretions is performed, some of them are stable, but some structures are not convergent. In many cases, several different starting configurations are found to give the same structure upon optimization. A frequencies calculation has been performed to ensure that all the imaginary frequencies vanish and the structures are stable. Only the most stable structures for the  $Al_n$  (n = 3 - 10),  $NiAl_n$ ,  $CuAl_n$  (n = 2 - 9) clusters and their ions are presented in Figures 1 and 2. The similar structures for the cluster ions to their neutrals' are not plotted in the figures. But a different structure for NiAl<sub>9</sub> cluster from NiAl<sub>9</sub> cluster's is also presented in Figure 1.

NiAl cluster is a dimer with different atoms. NiAl<sub>2</sub> cluster and its ions have an isosceles triangle with  $C_{2v}$ symmetry as their ground state structures. NiAl<sub>3</sub> cluster, its positive and negative ions have one three-dimensional tetrahedral structure with C3v symmetry as their lowest energy structures, which are different from that of Al<sub>4</sub> cluster. Similarly, the ground state structure for NiAl<sub>4</sub>,  $NiAl_{4}^{-}$  and  $NiAl_{4}^{+}$  clusters is one pentahedral structure with C<sub>4v</sub> symmetry, differing from the planar structure of Al<sub>5</sub> cluster. The most stable structures for NiAl<sub>5</sub> cluster neutral, anion and cation have the same geometric configurations with Cs symmetry, which are obtained from the pentahedral structure of NiAl<sub>4</sub> by putting a surface Al atom. The lowest energy structures of NiAl<sub>6</sub> and NiAl<sub>8</sub> clusters cannot be obtained from Al<sub>7</sub> and Al<sub>9</sub> clusters by substituting one aluminum atom with nickel atom. Both of them have C<sub>s</sub> symmetry. Al<sub>7</sub> cluster is an anti-trigonal prism with a capping atom (C<sub>3v</sub> symmetry), while NiAl<sub>6</sub> cluster is a trigonal prism with a capping atom. The ground state structure for Al<sub>9</sub> cluster is regarded as a bicapped hexagonal bipyramids with a capping atom. But NiAl<sub>8</sub> cluster possesses another different structure. For



Figure 1. The ground state structures of  $Al_n$  (n = 3 - 10),  $NiAl_n$  (n = 2 - 9) and  $NiAl_9^+$  ion clusters. Larger black spheres and smaller gray sphere refer to Ni atom and Al atom, respectively.



Figure 2. The ground state structures of  $CuAl_n$  (n = 2 - 9) clusters. Larger black spheres and smaller gray sphere refer to Cu atom and Al atom, respectively.

NiAl<sub>7</sub> and NiAl<sub>9</sub> clusters, the lowest structures are different from those of pure Al<sub>8</sub> and Al<sub>10</sub> clusters. It is worthy mentioning that positive NiAl<sub>9</sub> cluster ion has a severe distorted ground state structure compared with its neutral and anion (see NiAl<sub>9</sub><sup>+</sup> structure in **Figure 1**). Mulliken population analysis shows that the Al atoms labeled 1, 2 and 3 letters lose 37%, 28%, and 20% elec-

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tron in the  $NiAl_9^+$  structure, respectively. This makes the bond energies among them decrease. The severe structure distortion is mainly resulted from the non-uniform charge lose.

NiAl cluster has a single electron besides the paired electrons. If we add an electron into NiAl cluster, the electron would pair up with the original single electron, producing zero magnetic moment in NiAl<sup>-</sup> cluster. But, the electron removed is from paired electrons in NiAl cluster. Thus, NiAl<sup>+</sup> cluster have two unpaired electrons, showing magnetic moment of 2  $\mu_{\rm B}$ . Loss of an electron weakens the NiAl bond, which makes NiAl<sup>+</sup> cluster unstable due to positive binding energy. All the orbitals in neutral NiAl<sub>2</sub> cluster are doubly occupied. But the ionic clusters have the magnetic moment of 1  $\mu_{\rm B}$  because there is one single-occupied orbital. Interestingly,  $NiAl_4^-$ , NiAl<sub>4</sub>, and NiAl<sub>4</sub><sup>+</sup> clusters have magnetic moments of 1  $\mu_{\rm B}$ , 2  $\mu_{\rm B}$  and 3  $\mu_{\rm B}$ , respectively. It is found from observing Table 1 that NiAl<sub>3</sub>, NiAl<sub>5</sub>, NiAl<sub>7</sub>, NiAl<sub>9</sub> clusters and their ions with odd-aluminum atoms have the same magnetic moments as NiAl cluster and their ions. That is to say, their anions have no magnetic moments, but the cations show the magnetic moment of 2  $\mu_B$ . NiAl<sub>6</sub><sup>-</sup>, NiAl<sub>6</sub>, and NiAl<sub>6</sub><sup>+</sup> clusters have the same magnetic moments of 1  $\mu_B$ , 2  $\mu_B$  and 3  $\mu_B$  as NiAl<sub>4</sub>, NiAl<sub>4</sub>, and  $NiAl_4^+$  clusters, respectively. But, the magnetic properties of  $NiAl_8^-$ ,  $NiAl_8$ , and  $NiAl_8^+$  clusters are the same as those of NiAl<sub>2</sub>, NiAl<sub>2</sub>, and NiAl<sub>2</sub><sup>+</sup> clusters, respecttively.

**Figure 3** presents the calculated total density of states (DOS) for NiAl<sub>4</sub><sup>-</sup>, NiAl<sub>4</sub>, NiAl<sub>4</sub><sup>+</sup>, and NiAl<sub>6</sub> clusters. DOS further provides an explanation of the magnetic behavior of these clusters. The majority spin is contributed by the Ni-d orbitals in the clusters. DOS for spin up

and spin down are asymmetric in the clusters suggesting the systems to be magnetic. Similar situations can be found in other clusters.

The magnetic moments of the Ni-Al clusters are considered to be from the strong sp-d hybridization. The electronic configurations of Ni atom and Al atom are  $3d^84s^2$  and  $3s^23p^1$ , respectively. The Ni 3d orbitals are open shells. For the Ni-Al clusters, we note that the Ni atom obtain charge of about 0.4e from the Al atoms according to Mulliken populations. At the same time, some charge transfers into the 4p and 3d orbitals from the Ni 4s orbitals. For example, NiAl<sub>3</sub><sup>+</sup> cluster has magnetic moment of 2  $\mu_B$ , in which 0.494  $\mu_B$  and 0.502  $\mu_B$  are from the Ni atom and each Al atom, respectively. A part of the Ni 4s, Al 3s and 3p charge goes to the Ni 4p and 3d orbitals to form sp-d hybridization.

In order to better understand the role of the impurity Ni atom in the Al host clusters, we have also investigated the structural and magnetic properties of the copper-doped aluminum clusters by comparative study. The ground state structures for  $CuAl_n$  (n = 2 - 9) clusters are presented in Figure 2. Their magnetic moments, binding energies, energy gaps, electron affinities and ionization potentials are presented in Table 2. Although most of the structures can not be obtained from those of  $Al_n$  (n = 3 -10) clusters either by replacing one Al atom with a Cu atom, more structures are similar to the lowest energy structures of  $Al_n$  (n = 3 - 10) clusters compared with Ni- $Al_n$  (n = 2 - 9) clusters. It is found from observing the structures in Figure 1 that some of the aluminum cluster structures get a cardinal change after doping one impurity nickel atom. But, one substitutional zinc atom only causes some local structural distortion without changing the basic geometrical configurations of the original Al<sub>n</sub>

Table 1. The total magnetic moments (M, in  $\mu_B$ ) and the binding energies (BE, in eV) for NiAl<sub>n</sub> (n = 2 - 9) clusters and their ions. The energy gaps (E<sub>g</sub>, in eV), the electron affinities (EA, in eV) and ionization potentials (IP, in eV) of neutral NiAl<sub>n</sub> (n = 2 - 9) clusters.

	M (in $\mu_{\rm B}$ )			BE (in eV)			E (in aV)	EA (in aV)	ID (in aV)
Clusters	Anionic	Neutral	Cationic	Anionic	Neutral	Cationic	$E_g(\Pi ev)$	EA (III eV)	IP (III ev)
NiAl	0	1	2	-4.82	-3.53	3.47	0.25	1.29	7.00
NiAl <sub>2</sub>	1	0	1	-8.18	-6.94	-0.15	1.06	1.24	6.79
NiAl <sub>3</sub>	0	1	2	-11.31	-9.92	-2.67	0.60	1.39	7.25
NiAl <sub>4</sub>	1	2	3	-14.10	-12.21	-5.17	1.18	1.89	7.04
NiAl <sub>5</sub>	0	1	2	-16.62	-14.59	-8.38	0.52	2.03	6.21
NiAl <sub>6</sub>	1	2	3	-20.10	-17.64	-11.25	0.26	2.46	6.39
NiAl <sub>7</sub>	0	1	2	-23.16	-21.06	-14.50	0.53	2.10	6.56
NiAl <sub>8</sub>	1	0	1	-25.80	-23.56	-17.47	0.73	2.24	6.09
NiAl <sub>9</sub>	0	1	2	-28.81	-26.39	-19.99	0.69	2.42	6.60

	$M$ (in $\mu_{\rm B}$ )			BE (in eV)			E (in all)	EA (in aV)	ID (in aV)
Clusters	Anionic	Neutral	Cationic	Anionic	Neutral	Cationic	$E_g(mev)$	EA (III eV)	IP (III eV)
CuAl	1	0	1	-3.58	-2.89	4.32	1.69	0.69	7.21
CuAl <sub>2</sub>	0	1	2	-6.23	-5.05	2.52	0.38	1.18	7.57
CuAl <sub>3</sub>	1	0	1	-8.91	-6.95	-0.73	0.36	1.96	6.22
CuAl <sub>4</sub>	0	1	2	-12.24	-10.06	-3.71	0.27	2.18	6.35
CuAl <sub>5</sub>	1	0	1	-14.67	-12.54	-6.18	0.65	2.13	6.36
CuAl <sub>6</sub>	0	1	2	-18.60	-15.95	-9.31	0.41	2.65	6.64
CuAl <sub>7</sub>	1	0	1	-20.92	-18.83	-12.75	0.90	2.09	6.08
CuAl <sub>8</sub>	0	1	2	-23.61	-21.32	-15.19	0.64	2.29	6.13
CuAl <sub>9</sub>	1	0	1	-26.88	-24.38	-18.15	0.68	2.50	6.23

Table 2. The total magnetic moments (M, in  $\mu_B$ ) and the binding energies (BE, in eV) for CuAl<sub>n</sub> (n = 2 - 9) clusters and their ions. The energy gaps (E<sub>g</sub>, in eV), the electron affinities (EA, in eV) and ionization potentials (IP, in eV) of neutral CuAl<sub>n</sub> (n = 2 - 9) clusters.

(n = 3 - 10) clusters [14]. This is considered to be related to the electronic configurations of the impurity atoms. As the number of electrons from Cr atom to Zn atom increases, the 3d orbital's hybridization intensity of metal atom with the orbital of Al reduces gradually. In addition, the cohesive energies of Ni, Cu, and Zn are 4.44, 3.49, and 1.35 eV, respectively [15]. Therefore, the influence of the impurity Cu atoms on the structures of the host Al clusters is less than that of the Ni atom. The influence caused by Zn atoms is even less.

Some of the ground state structures of  $\text{CuAl}_n$  (n = 2 - 9) clusters are different from those of NiAl<sub>n</sub> (n = 2 - 9) clusters. They also present different magnetic properties. Note that the magnetic moments of all the anionic, neutral and cationic CuAl clusters with odd Al atoms are of 1  $\mu_B$ , 0, and 1  $\mu_B$ , respectively. But, the corresponding Cu-Al system containing even Al atoms are associated with the magnetic moments of 0, 1  $\mu_B$ , and 2  $\mu_B$ , respectively. The cations have two unpaired electrons, showing the magnetic moment of 2  $\mu_B$ .

Wang *et al.* [8] investigated the properties of  $MAl_n$  (M = Cr, Mn, Fe, Co, Ni; n = 1 - 7, 12) clusters. They found that the  $MAl_n$  clusters have similar structures to  $Al_{n+1}$  clusters. Our calculated ground state structures for  $Al_n$  (n = 2 - 10) clusters are in excellent agreement with the results reported in the Ref. [16], but differing from the structures obtained by Wang [8]. For NiAl<sub>n</sub> (n = 5 - 7) clusters, ours structures. As a result, the structures are unstable. Some of them transfer into our structures. The differences are probably caused by the different choice of the functional and the basis set for the problem under investigation. But, for the magnetic moments from NiAl

cluster to NiAl<sub>7</sub> cluster, our calculated results fully consistent with their results.

**Figure 4** shows the second difference of cluster energies,  $\Delta_2 E(n) = E(NiAl_{n-1}) + E(NiAl_{n+1}) - 2E(NiAl_n)$ , which is a sensitive quantities that reflects the stabilities of clusters. The maxima can be found at n = 2, 3, 7 for NiAl<sub>n</sub> (n = 1 - 9) clusters, implying that the clusters are more stable than their neighboring clusters. But, for CuAl<sub>n</sub> (n = 1 - 9) clusters, the maxima can be found at n = 2, 4, 6, 7. Obviously, different impurity atoms would change their relative stabilities.

The electron affinities (EA) and ionization potentials (IP) of the mixed clusters as the function of the clusters size (shown as Figure 4) are also important quantities that reflect the stability of the clusters. The positive EAs imply that the clusters have a tendency to gain an electron under normal conditions. In the mixed NiAl<sub>n</sub> and  $CuAl_n$  (n = 1 - 9) clusters, all the EAs are positive. Their trend is basically the same. The smaller clusters have a small electron affinity. However, for the ionization potentials, an opposite situation is observed. Generally speaking, the highly stable structure has small electron affinity and large ionization potential. For example, NiAl<sub>3</sub> and NiAl<sub>7</sub> clusters are comparatively highly stable. They have smaller EAs and larger IPs relative to their neighbors. Figure 4 also presents the energy gaps (Eg) between the highest-occupied molecular orbital (HOMO) and the lowest-unoccupied molecular orbital (LUMO). Most of them are less than 1.0 eV.

#### 3. Summary

We optimized the geometric structures of the mixed Ni-Al<sub>n</sub> and CuAl<sub>n</sub> (n = 1 - 9) clusters by using first-principles density functional theory. The ground state structures are obtained, and their relative stabilities are discussed. Most of the Al clusters doped one Ni or Cu atom are different from those of the host Al clusters. NiAl<sub>n</sub> and

 $CuAl_n$  (n = 1 - 9) cluster ions present the similar structures to their neutral clusters. In addition, their magnetic properties are investigated. The magnetic moments of



Figure 3. Total density of states (DOS) for  $NiAl_4^-$ ,  $NiAl_4^+$ ,  $NiAl_4^+$ , and  $NiAl_6^-$  clusters. The Fermi level is given by a vertical line.

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Figure 4. The second difference of cluster energies, the electron affinities, the ionization potentials, and the energy gaps  $E_g$  between the highest-occupied molecular orbital (HOMO) and the lowest-unoccupied molecular orbital (LUMO) of NiAl<sub>n</sub> and CuAl<sub>n</sub> (n = 2 - 9) clusters.

NiAl<sub>n</sub> (n=odd number) and CuAl<sub>n</sub> (n = even number) cluster anions, neutrals and cations are 0, 1  $\mu_B$ , and 2  $\mu_B$ , respectively. Negative, neutral and positive NiAl<sub>4</sub> and NiAl<sub>6</sub> clusters show the magnetic moments of 1  $\mu_B$ , 2  $\mu_B$ , and 3  $\mu_B$ , respectively. NiAl<sub>2</sub>, NiAl<sub>8</sub> and CuAl<sub>n</sub> (n = odd number) clusters do not have any magnetic moments, while NiAl<sub>2</sub> and NiAl<sub>8</sub> cluster ions have the magnetic moment of 1  $\mu_B$ . The magnetic moments of the Ni-Al clusters are from the strong sp-d hybridization.

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