

A Study on Ranged-Gated Lidar System with Linear Plus

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Abstract—According to the study of super-resolution range-gated system, we proposed an improved system with linear plus detects. And a range function is derived by considering the shot effect noise and dark current noise. The simulation shows that the improved system has a good range accuracy capability.

Keywords—lidar ; range-gated ; linear plus ; range accuracy

1. Introduction

Non-scanning imaging lidar is among the most popular development laser radar systems. The range-gated technology and device in the system have been very mature[1]. In the study of laser radar, range accuracy is an important indicator of appraising a laser radar system, so how to improve the range accuracy has become a very important issue that all researchers chasing for[2]. There are two range-gated laser radar systems which can achieve high range accuracy. The first one is centroid algorithm that 3D images can be derived from an sequence of 2D images[3]. However it costs a lot of time to calculate which slows down the 3D imaging speed. In 2007, French scientist Martin *et al*, presented a super-resolution range-gated technique that only two 2D images are needed to create a 3D image which speeds up the calculation with a higher range accuracy[4]. Based on the super-resolution system this paper presented an improved system which replace the constant plus of the receiver with linear plus, and results show that it has a better SNR and range accuracy capability[5].

2. Range function of range-gated system with linear plus

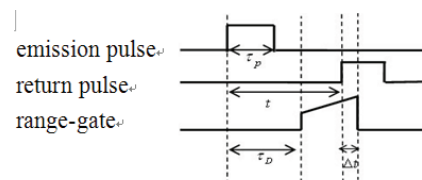


Figure 1. Sequence diagram of laser pulse and gate during falling ramp

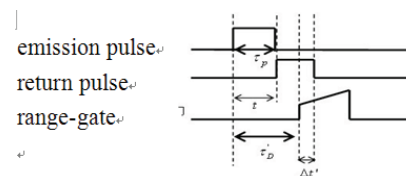


Figure 2. Sequence diagram of laser pulse and gate during rising ramp

Assuming the power and width of the laser pulse is P_0, t_p .

So the function of laser pulse can be written:

$$P(t) = P_0/t_p \text{ rect}(t/t_p) \quad (1)$$

The initiated linear plus of the range-gated receiver is b , the slope is k . Assuming the width of range gate and laser pulse is equal as t_p . Then the linear plus function can be written:

$$G_1(t) = (kt + b)\text{rect}(t/t_p) \quad (2)$$

There are two intensities of images to calculate. Firstly, we derive the intensity when only the front part of the pulse received by the range gate, the Sequence diagram of laser pulse and gate during falling ramp is shown in figure 1. The distance between the target and the detector is z , and the time that the laser pulse travels is $t = 2z/c$. The delay time between the pulse starting transmitting and the range gate getting open is τ_D . The width of the pulse which received by range gate when it is open can be written:

$$\Delta t = \tau_D + \tau_p - t = \tau_D + \tau_p - \frac{2z}{c} \quad (3)$$

The intensity of the image is:

$$I_1 = R \int_{t_p - \Delta t}^{t_p} dt P(t) G_1(t) \quad (4)$$

We can get another intensity function in the same way, the delay time is $\tau_D' = \tau_D + \tau_p$. The Sequence diagram of the pulse and gate during falling ramp is shown in figure 2.

The width of the pulse which received by range gate is:

$$\Delta t' = t + t_p - \tau_D' = \frac{2z}{c} - \tau_D \quad (5)$$

The intensity function can be written:

$$I_2 = R \int_0^{\Delta t'} dt P(t) G_1(t) \quad (6)$$

From equation (1)~(7), we can get the range function:

$$z = \frac{c}{2} \left(\tau_D + t_p - \frac{kt_p + b}{k} + \sqrt{\frac{(kt_p + b)^2}{k^2} - \frac{M(kt_p^2 + 2bt_p)}{k(M+1)}} \right) \quad (7)$$

While M is:

$$M = \frac{I_1}{I_2} = \frac{\left[\frac{(kt_p + b)^2}{k^2} - \left(\frac{2z}{c} - \tau_D + \frac{b}{k} \right)^2 \right]}{\left(\frac{kt_p^2 + 2bt_p}{k} \right) - \left[\frac{(kt_p + b)^2}{k^2} - \left(\frac{2z}{c} - \tau_D + \frac{b}{k} \right)^2 \right]} \quad (8)$$

3. SNR and range accuracy

The differential coefficient of equation (9) can be written:

$$dz = A \frac{dI_1}{I_1} + A \frac{dI_2}{I_2} + B dt_p + C dk + D db \quad (9)$$

Then the range accuracy of the system is:

$$\delta z = \frac{c}{2} \sqrt{A^2 \frac{1}{SNR_1^2} + A^2 \frac{1}{SNR_2^2} + B^2 (\delta t_p)^2 + C^2 (\delta k)^2 + D^2 (\delta b)^2} \quad (10)$$

We only consider the first and second term approximately as the affection of other terms is small. Then the range accuracy of the linear plus system can be written:

$$\delta z = \frac{c}{4} \frac{kt_p^2 + 2bt_p}{k \sqrt{\frac{(kt_p + b)^2}{k^2} - \frac{M(kt_p^2 + 2bt_p)}{k(M+1)}}} \times \frac{M}{(M+1)^2} \sqrt{\frac{1}{SNR_1^2} + \frac{1}{SNR_2^2}} \quad (11)$$

If the shot effect noise and dark current noise are independent, then the total noise of the system can be presented as:

$$\begin{aligned} \sigma_{all} &= F_{iccd} \sqrt{\sigma_s^2 + G^2 \sigma_d^2} \\ &= F_{iccd} \sqrt{N + G^2 \frac{I_d t_i}{e}} \end{aligned} \quad (12)$$

While F_{iccd} is noise factor (usually is $\sqrt{2}$), N is the number of photoelectrons, G is the plus of the system, I_d is the dark current of ICCD, t_i is the integral time of ICCD, e is the charge of an electronic.

Then the SNR of the system can be written:

$$\begin{aligned} SNR_{out} &= \frac{N}{\sigma_{all}} = \frac{N}{F_{iccd} \sqrt{N + \frac{G^2 I_d t_i}{e}}} \\ &= \frac{G \frac{\eta_{pc}}{w} \int_t p_r(t) dt}{F_{iccd} \sqrt{G \frac{\eta_{pc}}{w} \int_t p_r(t) dt + \frac{G^2 I_d t_i}{e}}} \end{aligned} \quad (13)$$

The SNR of the two images with linear plus are respectively:

$$SNR_1 = \frac{\eta_{pc} \left(\frac{w\rho\eta\tau^2 D^2 \Delta t_1}{4t_p z^2} + p_0 t_g \right)}{FG \sqrt{\eta_{pc} \left(\frac{w\rho\eta\tau^2 D^2 \Delta t_1}{4t_p z^2} + p_0 t_g \right) + \frac{G^2 I_d t_i}{e}}} \quad (14)$$

$$SNR_2 = \frac{\eta_{pc} \left(\frac{w\rho\eta\tau^2 D^2 \Delta t_2}{4t_p z^2} + p_0 t_g \right)}{FG \sqrt{\eta_{pc} \left(\frac{w\rho\eta\tau^2 D^2 \Delta t_2}{4t_p z^2} + p_0 t_g \right) + \frac{G^2 I_d t_i}{e}}} \quad (15)$$

While $P_r(t)$ is the power irradiating at the detector, η_{pc} is the quanta efficiency, w is energy of single photonics, ρ is the reflection of target, η is the efficiency of the optics system, τ is the transmission of atmosphere, D is the diameter of the receiver optics system. Δt is the width of pulse received by the range gate.

Then the range accuracy of system can be rewritten as :

$$\delta z_{lin} = \frac{c}{4} \frac{kt_p^2 + 2bt_p}{k \sqrt{\left(\frac{(kt_p + b)^2}{k^2} - \frac{M(kt_p^2 + 2bt_p)}{k(M+1)} \right)}} \times \frac{M}{(M+1)^2} \sqrt{\frac{1}{SNR_{out1}^2} + \frac{1}{SNR_{out2}^2}} \quad (16)$$

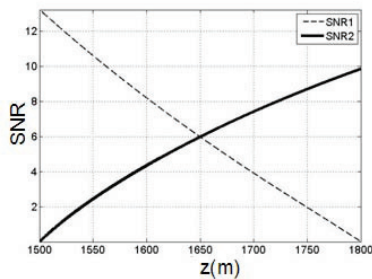


Figure 3. Curve of SNR with linear plus

The curve of SNR with linear plus are shown in fig 3. The SNR of two images are quite different: grown and fallen as distance increased respectively. Because when the distance between the target and detector is increased, the width of the pulse that received by the detector is augmented and reduced

respectively. This results their intensities quite different which make their SNR curves have different shapes.

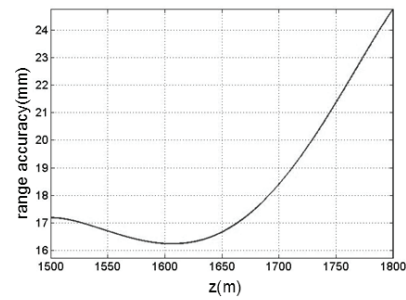


Figure 4. Curve of range accuracy with linear plus vs distance

Fig.4 shows the curve of range accuracy with linear plus vs distance. During the distance when the pulse can be received by range gate, firstly the range accuracy is increased when the target gets away from the detector, and it decreases as the distance continues growing.

4. Conclusion

This article presented a new type of range gated laser radar system which uses linear plus ICCD receiver instead of constant plus. Further more we derived the range function from the intensity of two images by changing the time-delay. Then the range accuracy expressed by SNR is derived from the range function. The dark current and shot noise is considered. At last the curves of SNR and accuracy is given to show the performance of the improved system.

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