

Thermal Analysis of Laser Chemical Machining: Part I: Static Irradiation

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Abstract

The laser chemical machining is a non-conventional substractive processing method. It is based on the laser-activation of a material dissolution of metals in electrolyte ambient via local-induced temperature gradients and allows a gentle and smooth processing of especially temperature-sensitive metals. However, the material removal is characterized by a narrow process window and is restricted by occurring disturbances, which are supposed to be related to the localized electrolyte boiling. In order to control the removal quality and avoid disturbances, the correlation between the laser-induced temperatures and the resulting removal geometry has to be better understood. In this work an analytical modeling of the laser-induced temperatures at the surface of titanium based on a Green-function approach is presented. The main influencing factors (laser, electrolyte, material) as well as possible heat transfer into the electrolyte are included and discussed. To verify the calculated temperatures, single spot experiments are performed and characterized for titanium in phosphoric acid solution within laser irradiation of 1 s. The correlation between the temperature distribution and the resulting removal geometry is investigated based on a spatial superposition. Thereby, the bottom limit temperature is found to range between 63°C and 70°C whereas the upper limit is related to the nucleate boiling regime. Based on the performed correlation an indicator is identified to predict the ruling removal regime and thereby to reduce the experimental expenditure.

Keywords

Laser Micro Machining, Laser Chemical Removal, Modeling, Temperature, Process Stability, Titanium

1. Introduction

Within the ever-increasing trend of miniaturization, traditional mechanical machining reaches more and more its performance limits due to the enhanced complexity and amount of micro-components as well as occurring size effects [1]. At the same time, non-conventional machining is quickly taking root in the production of especially metallic micro tools and components [2].

Among others, these include the laser chemical machining (LCM) that unifies the advantages of laser machining with its precise and localized energy deposition and the electrochemical machining with its smooth processing without significant thermal impacts [3]. Laser chemical machining is a further development of the hybrid laser-assisted electrochemical machining, in which the laser beam is coaxially positioned to the electrolyte jet [4]. Within this process the laser beam heats up the workpiece, which is immerged in a continuously pumped electrolyte [5]. Depending on the laser parameters such as the laser power and spot diameter, the induced temperature fields at the workpiece surface can change the electrochemical potential in a range within it the anodic material dissolution is activated and results thereby in the removal of the base material [6]. This laser-activated chemical dissolution was observed for different self-passivating metals, e.g. stainless steel and titanium alloys [7]. Within suitable process windows a gentle removal occurs without significant heat affected zones or a recast formation. This gentle processing represents the main advantage compared with the laser machining, in which micro-cracks, distortion and stress can result when using short laser pulses [8].

However, the dynamics of the laser light absorption, heat, chemical reactions, hydrodynamics and transport phenomena causes within a certain range of parameters a disturbance of material removal [9]. As Laser chemical machining is mainly a temperature-driven process, it was experimentally demonstrated that occurring disturbances are strongly related to the electrolyte boiling and the ensuing gas bubble formation [9] as well as to the electrolyte-metal combination [10]. Nevertheless, it is still a lack of knowledge about the direct correlation between the laser-induced temperatures and the resulting removal geometry.

Within this work, an analytical modeling of the laser-induced surface temperatures is presented based on a Green-function approach. It takes into account the main influencing factors (laser, electrolyte and material) as well as possible heat transfer into the electrolyte and is used to identify the influence of single process parameters on the temperature distribution. In addition, the removal properties are experimentally characterized in order to validate the modeling results. Therefore, single spot experiments are performed for titanium in phosphoric acid solution within laser irradiation of 1 s. The correlation between the temperature distribution and the resulting removal geometry is investigated based on a spatial superposition. In dependence of laser power and beam diameter the starting temperature for a laser chemical removal as well as its upper limit temperature are determined. Furthermore, it is shown that once validated the presented model can be used to predict the process window for a disturbance-free LCM-process and there by helps reducing the experimental expenditure.

2. Process Fundamentals

The laser irradiation is used in laser chemical machining as a localized and selective heat source that can induce suitable thermal impact for the activation of heterogeneous chemical reaction between a liquid ambient and a metallic surface and results in a temperature-induced electrochemical etching [6]. At suitable parameter settings the metal dissolution occurs under the formation of hydrogen and water soluble metallic salts following the chemical reaction (see Figure 1):

$$Me + 2H^+ \rightarrow Me^{2+} + H_2 \uparrow$$
(1)

In laser chemical machining, the workpiece surface is in a direct contact to the electrolytic solution. In consequence of its heat impact the laser beam can induce or enhance reactions at the metal-liquid interface via changes in the electrochemical Nernst potential. The locally induced temperature gradients result in the generation of a thermobattery allowing a current flow within the metal between the center of the incident laser light and its periphery. Despite the low generated electromotive forces (some 0.1 V for a temperature rise of 100 K) the electric field strengths are very high due to the small battery dimensions [6]. Thus, self-passivating metals lose their natural passivation property allowing then the dissolution of the base material [3].

Within the LCM-process the laser induced-temperatures define both, the proton activity within the redox-reaction and the electrochemical potential at the workpiece surface [11]. It is therefore plain that certain threshold temperatures are required in order to realize a material removal above the background etching rate (some 10^{-9} m/s). Thereby, the laser-induced temperatures depend on different factors that can be divided in:

1) Laser characteristics: laser power, irradiation duration, intensity distribution, spot size and feed velocity.





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Figure 1. Schematic illustration of the principles of the laser chemical removal of metals. Here, phosphoric acid is taken exemplarily as the electrolyte solution.

2) Material properties: wavelength-dependent absorption coefficient, chemical composition, thermal diffusivity, specific heat, density...

3) Electrolyte properties: acidic/basic solution, concentration, layer thickness, wavelength-dependent transmission coefficient.

Beside the temperature, the electrochemical potential is also depending on the chemical activity of the dissolved metal ions and on the mass transport limitation [3]. Latter one is mainly determining the removal speed within the aqueous electrolytes. Further, the convective flow represents also an important factor by determining the transport of reaction products as well as the provision and exchange of reactants. An increased convection can enhance the reaction rates by several orders of magnitude. At high laser intensities an electrolyte boiling can occur resulting on the formation of vapor gas bubble. Among others, Mehrafsun *et al.* [9] and Yavas *et al.* [12] have reported that the formed bubbles result in removal disturbances that impede the controllability of the LCM process. Therefore, it is recommended to avoid electrolyte boiling.

3. Methodology

3.1. Model Assumptions

As already mentioned, the laser irradiation has the function of thermally activate the chemical etching reaction. Because of the high number of influence factors as well as the complex interaction nature (chemically, physically and flow dynamics) it is still a lack of knowledge about the mechanisms occurring during LCMprocess.

The laser radiation propagates throughout the etchant solution, is absorbed at the workpiece surface, induces a temperature distribution that define the area and properties of the chemical dissolution reaction and thereby the quality of the material removal. Therefore, a determination of the temperature distribution over the workpiece surface would help to understand the influences of the main process parameters. To build up a theoretical description of the surface temperature following assumptions have been made:

1) The laser beam—as the heat source—is a TEM_{00} -mode with a Gaussian intensity distribution

$$I(x, y) = I_0 \cdot e^{\left[\left(\frac{x}{r_x}\right)^2 + \left(\frac{y}{r_y}\right)^2\right]}$$
(2)

where $I_0 = P_{abs}/A$ with P_{abs} is the absorbed laser power and A is the laser beam area at the workpiece surface, $A = \pi r_x r_y$ and $r_x = r_y$.

2) The workpiece/laser beam is moving with a constant speed v and in x-direction. In this work the feed velocity v = 0, as only the case of a static irradiation is studied.

3) The material is supposed to be isotropic with temperature-independent properties.

4) Phase changes do not occur. On the one hand laser melting cannot occur at the applied laser powers and on the other hand the formation of metallic salt lay-

ers is neglected.

5) The laser power is affected by the transmission coefficient τ_E that describes the power loss during the propagation throughout the etchant solution and by the absorption coefficient α_{abs} of the metallic material. Both coefficients are assumed to be constant and temperature-independent. The absorbed laser power P_{abs} is then described as:

$$P_{abs} = P_L \cdot \alpha_{abs} \cdot \tau_E \tag{3}$$

6) The thermal interaction takes place only between laser beam and workpiece. Additional contributions, such as the heat of reaction, are neglected.

7) Heat transfer into the etchant solution is considered. The heat equation includes heat loss rates dependent on constant heat transfer coefficients of the electrolyte.

8) For the description of the heat equation a rectangular coordinate system is used. This is fixed in the workpiece, where the origin is directly beneath the beam center, *x*-*y*-plane is the workpiece surface and the positive *z*-axis points into the workpiece. The laser beam interacts with the workpiece at z = 0. All relevant modeling parameters are listed in Table A1 (see Supplementary Material).

3.2. Green's Function Based Model

The interaction between laser irradiation and metallic surface is assumed to be dominated by conduction during the electron-lattice heating. The conduction is related to the thermal diffusivity D, the volumetric heat capacity C_p and the material density ρ . The resulting temperature distribution T in the material is associated to the power density Q through the diffusion equation:

$$\frac{\partial T}{\partial t} = D \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) - \frac{Q}{\rho C_p}$$
(4)

Here, *Q* represents the contribution of the heat source (laser beam) and can be described as:

$$Q = \frac{P_{abs}}{2\pi r^2} \cdot e^{\frac{(x-vr)^2 + y^2}{2r^2}} \cdot e^{-\alpha z}$$
(5)

The temperature rise T(x, y, z, t) is valid for $x > -\infty$, $y < \infty$, $0 \le z \le \infty$ and t > 0 and follows the boundary conditions (see Figure 2):

T = 0 at t = 0, $T \to 0$ for $x, y \to \pm \infty$

$$T \to 0 \text{ for } z \to \infty, \ \frac{\partial T}{\partial t} = \frac{H}{\kappa} T \text{ at } z = 0$$

For a simplified mathematical treatment a dimensionless formulation of Equation (4) has to be provided. Therefore, following dimensionless variables were defined:

$$X = \frac{x}{r}, Y = \frac{y}{r}, Z = \frac{z}{r}, \tau = \frac{2Dt}{r^2}, \mu = \frac{v \cdot r}{D}, \alpha = \frac{r}{l}, \Theta = \frac{H \cdot r}{\kappa}$$



Figure 2. Schematic of the laser heating with the related boundary conditions. For a simplified illustration only the x-z-plane is shown.

and

$$\Psi = \frac{T}{\Delta T'} \quad \text{with} \quad \Delta T = \frac{P_{abs}}{4\sqrt{\pi\kappa r}}$$

The dimensionless heat equation can be then formulated as [13]:

$$\frac{\partial \Psi}{\partial t} = \frac{\partial^2 \Psi}{\partial X^2} + \frac{\partial^2 \Psi}{\partial Y^2} + \frac{\partial^2 \Psi}{\partial Z^2} - \mu \frac{\partial \Psi}{\partial X} - \frac{2\alpha}{\sqrt{\pi}} e^{-X^2 - \gamma^2 - \alpha Z}$$
(6)

where following boundary conditions are valid:

$$\Psi = 0 \text{ at } \tau = 0 , \quad \Psi \to 0 \text{ for } X, Y \to \pm \infty$$
$$\Psi \to 0 \text{ for } Z \to \infty , \quad \frac{\partial \Psi}{\partial \tau} = \Theta \Psi \text{ at } Z = 0$$

The solution of the dimensionless temperature distribution at the workpiece surface (Z = 0) is given by:

$$\Psi(X,Y,0,\tau) = \int_0^\tau \int_{-\infty}^\infty \int_{-\infty}^\infty \int_0^\infty G(X,Y,0,\tau,X',Y',Z',\tau')$$

$$\times \frac{2\alpha}{\sqrt{\pi}} e^{-X'^2 - Y'^2 - \alpha Z'} dZ' dY' dX' d\tau'$$
(7)

Here, the general solution of the Green-function $G(X,Y,0,\tau,X',Y',Z',\tau')$ is:

$$G = \frac{1}{4\left[\pi\left(\tau - \tau'\right)\right]^{3/2}} e^{\frac{-(X - X')^2 + (Y - Y')^2 + (Z - Z')^2}{4(\tau - \tau')}}$$
(8)

.

In accordance with Carslaw and Jaeger [14], the Green-function for the 3D-case can be described as follows:

$$G = \frac{1}{\left[4\pi(\tau-\tau')\right]^{\frac{3}{2}}} e^{-\left[\frac{(X-X'-\mu(\tau-\tau'))^{2}+(Y-Y')^{2}}{4(\tau-\tau')}\right]} \times \left\{ e^{\frac{-(Z-Z')^{2}}{4(\tau-\tau')}} + e^{\frac{-(Z+Z')^{2}}{4(\tau-\tau')}} -\sqrt{4\pi(\tau-\tau')} \theta \cdot e^{\theta^{2}(\tau-\tau')+\theta(Z+Z')} \cdot \operatorname{erfc}\left[\frac{Z+Z'}{2\sqrt{\tau-\tau'}} + \theta\sqrt{\tau-\tau'}\right] \right\}$$
(9)

Using the substitution $\phi = \tau - \tau'$ and taking into account the velocity related term μ ; the dimensionless Equation (Equation (7)) at Z = 0 can be transformed into:

$$\Psi = \frac{2\alpha}{\sqrt{\pi}} \int_{0}^{r} \int_{-\infty}^{\infty} \int_{0}^{\infty} \int_{0}^{\infty} \frac{1}{[4\pi\phi]^{\frac{3}{2}}} e^{-\left[\frac{(X-X'-\mu\phi)^{2}+(Y-Y')^{2}}{4\phi}\right]} \cdot e^{\frac{-(Z-Z')^{2}}{4\phi}} \cdot e^{-X'^{2}-Y'^{2}-\alpha Z'} dZ' dY' dX' d\phi + \frac{2\alpha}{\sqrt{\pi}} \int_{0}^{r} \int_{-\infty}^{\infty} \int_{0}^{\infty} \frac{1}{[4\pi\phi]^{\frac{3}{2}}} e^{-\left[\frac{(X-X'-\mu\phi)^{2}+(Y-Y')^{2}}{4\phi}\right]} \cdot e^{\frac{-(Z+Z')^{2}}{4\phi}} \cdot e^{-X'^{2}-Y'^{2}-\alpha Z'} dZ' dY' dX' d\phi - \frac{2\alpha}{\sqrt{\pi}} \int_{0}^{r} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{0}^{\infty} \frac{1}{[4\pi\phi]^{\frac{3}{2}}} e^{-\left[\frac{(X-X'-\mu\phi)^{2}+(Y-Y')^{2}}{4\phi}\right]} (10) \cdot e^{-X'^{2}-Y'^{2}-\alpha Z'} dZ' dY' dX' d\phi - \frac{2\alpha}{\sqrt{\pi}} \int_{0}^{r} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{0}^{\infty} \frac{1}{[4\pi\phi]^{\frac{3}{2}}} e^{-\left[\frac{(X-X'-\mu\phi)^{2}+(Y-Y')^{2}}{4\phi}\right]} \cdot \left\{ e^{\frac{-(Z-Z')^{2}}{4\phi}} + e^{\frac{-(Z+Z')^{2}}{4\phi}} - \sqrt{4\pi\phi}\theta \cdot e^{\theta^{2}\phi + \theta(Z+Z')} \cdot \operatorname{erfc}\left[\frac{Z+Z'}{2\sqrt{\phi}} + \theta\sqrt{\phi}\right] \right\} \cdot e^{-X'^{2}-Y'^{2}-\alpha Z'} dZ' dY' dX' d\phi$$

In Equation (10) the first two integrals represent the lossless heat equation, whereas the third term includes the heat losses when considering heat transfer into the electrolyte (*i.e.* H > 0). This formulation is in good agreement with the work of Yung *et al.* [15], in which a similar approach was used.

With help of the closed-form approximation of the error function, described in [16]:

$$e^{x} \cdot \operatorname{erfc}(x) \approx \frac{a}{(a-1)\sqrt{\pi x^{2}} + \sqrt{\pi x^{2} + a}}$$
(11)

where $a = \pi/(\pi - 2)$, the surface temperature rise T(x, y, 0, t) can be finally simplified and described as:

$$T = \frac{P \cdot \alpha_{Abs} \cdot \tau_E}{4\pi \cdot \kappa \cdot l} \cdot \int_0^\tau \frac{1}{1 + 4\phi} \cdot \frac{a}{(a - 1)\sqrt{\pi\alpha^2\phi} + \sqrt{\pi\alpha^2\phi + a^2}} \cdot e^{\left[\frac{(X - \mu\phi)^2 + Y^2}{1 + 4\phi}\right]} d\phi$$

$$- \frac{P \cdot \alpha_{Abs} \cdot \tau_E}{4\pi \cdot \kappa \cdot l} \cdot \theta \int_0^\tau \frac{1}{1 + 4\phi} e^{-\left[\frac{(X - \mu\phi)^2 + Y^2}{1 + 4\phi}\right]}$$

$$\cdot \int_0^\infty \frac{a}{(a - 1)\sqrt{\pi\left(\frac{Z'}{4\phi} + \Theta^2\phi + \Theta Z'\right)}} + \sqrt{\pi\left(\frac{Z'}{4\phi} + \Theta^2\phi + \Theta Z'\right)} + a^2$$

$$\cdot e^{\frac{Z'^2}{4\phi}} \cdot e^{-\alpha Z'} dZ' d\phi$$
(12)

3.3. Experimental

As laser source a cw-fiber laser JK400 (from JK Lasers) was used. Its TEM_{00} cw-laser radiation of 1080 nm is focused by a telecentric f-theta optic and guided using the galvanometer scanning system Raylase Superscan III-15 to the surface.

Using an inverse telescope, the laser beam diameter and thus the focal spot size can be varied. Within the performed investigations the laser spot diameters 30.5 μ m and 109 μ m were applied. As sample material rolled titanium (Ti 3.7024) with a thickness of 0.8 mm was used. The Ti-workpiece was placed in a closed liquid-phase etching chamber, where a 5 molar (28.7% vol.) phosphoric acid (H₃PO₄) was pumped as a cross-jet through a 25 mm × 2 mm cross-section with velocity v_f of 2 m/s. The electrolyte layer between workpiece and protective glass has a thickness of 2 mm. A detailed description of the used setup can be found in [17].

Depending on laser power and spot diameter arrays of 4×4 single irradiation spots were structured, while the irradiation time was kept constant at 1 s. The main process parameters as well as the properties of the used material and electrolyte are listed in **Table 1**. The removal cavities (depth and diameters) were recorded and characterized using a 3D-laser confocal microscope (VHX970-Keyence). For a statistic evaluation five different irradiations spots per used laser power were measured, while 3 to 5 height profiles were captured for every single cavity.

4. Results

4.1. Modeled Influence of Laser Parameters

To study the influence of laser parameters we consider the case of an absent heat transfer into the etchant solution. Here, $\Theta = 0$ and $\partial \psi / \partial z = 0$ at Z = 0. Thus, the temperature rise in Equation (12) can be reduced to its first term:

$$T(X,Y,0,\phi) = \frac{P \cdot \alpha_{Abs} \cdot \tau_E}{4\pi\kappa l} \int_0^{\tau} \frac{1}{1+4\phi} e^{\frac{X^2 + Y^2}{1+4\phi}} \frac{a}{(a-1)\sqrt{\pi\alpha^2\phi} + \sqrt{\pi\alpha^2\phi + a^2}} d\phi \quad (13)$$

Table 1. List of process parameters used for both, modeling and experimental investigation.

	Properties	Unit	Value
	Thermal diffusivity D	m²/s	$6.8 imes 10^{-6}$
Titanium (3.7024)	Thermal conductivity κ	W/(m·K)	21
	Absorption coeff. at NIR a_{abc}	-	0.4
	Wavelength λ	nm	1080
T 1	Focus spot diameter $d_{\rm spot}$	μm	30.5, 68, 109
Laser beam	Irradiation time t_L	s	1
	Laser power P_L	W	0 … 20
	Solution	-	H_3PO_4
	Concentration	mol/l	5
	Boiling temperature T_{Boiling}	°C	104
Electrolyte	Layer thickness	Mm	1
	Transmission coefficient τ_E	-	0.96
	Flow speed	m/s	2

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4.1.1. Influence of Laser Power

In **Figure 3** the resulting temperatures at the surface of titanium around the laser spot center are shown exemplarily for $d_{\text{spot}} = 30.5 \,\mu\text{m}$. As expected from Equation (13), the surface temperature is mainly determined by the laser power.

For a beam diameter of 30.5 μ m, the peak temperature as well as the width of distribution increase linearly with the laser power. Thereby, the boiling temperature of the used phosphoric acid ($T_{\text{Boiling}} = 104^{\circ}$ C) can be achieved at laser powers of about 1 W. Thus, higher laser powers are not recommended as the electrolyte boiling is assumed to affect the quality of LCM because of occurring gas bubble formation [9].

4.1.2. Influence of Laser Spot Size

Figure 4(a) shows the influence of focus beam diameter d_{spot} on the resulting temperature distribution at a constant laser power of 2 W. Here, the increase in d_{spot} from 30.5 µm to 109 µm results in a decrease of the peak temperature rise from 190°C down to 67°C. This is due to the lower power density at a bigger spot area (274 kW/cm² vs 21.5 kW/cm²). In **Figure 4(b)** it can be seen that the temperature rise becomes faster when increasing the laser spot diameter. For a power density of 50 kW/cm², the peak temperatures amount 51°C, 88°C and 130°C with spot diameters of 30.5 µm, 68 µm and 109 µm, respectively. Moreover the electrolyte boiling ($T_{Boiling} = 104$ °C), as an assumed critical temperature, can be achieved at a power density of 137 kW/cm² with $d_{spot} = 30.5$ µm and 38 kW/cm² with $d_{spot} = 109$ µm. Thus, it is recommended to avoid exceeding these laser power densities in order realize a disturbance-free LCM.

4.2. Modeled Influence of Heat Transfer into the Electrolyte

Within the LCM process occurring heat losses are mainly related to the heat transfer into the electrolyte. It has to be noticed that the presented modeling



Figure 3. Temperature distribution on the surface of titanium at a distance x_0 from the center of a laser spot ($d_{spot} = 30.5 \ \mu m$) calculated using Equation (13).



Figure 4. Calculated influence of the laser beam diameter on surface temperature distribution on titanium at a constant laser power $P_L = 2$ W (a) and on the peak surface temperature $T_{\text{model,peak}}$ in dependence of the applied laser power density (b).

enables a simplified consideration of heat transfer using constant heat transfer coefficients. As the laser spot size, which defines the width of the interaction zone, ranges between 30.5 μ m and 109 μ m in diameter, we have to consider heat transfer coefficients representing enforced heat convection in the micro range. Thereby, the case of water flows in a micro pipe has been chosen as a reference. Depending on the electrolyte temperature two different heat transfer coefficients *H* were defined [18]:

- $H = 50.000 \text{ W/(m^2 \cdot K)}$ for the case water boiling. It was applied for temperature distributions with $T_{\text{model,peak}} > 90^{\circ}\text{C}$. This is based on the work of De Silva *et al.* [5], in which it was shown that the risk of an electrolyte boiling is extremely enhanced for surface temperatures greater than 90°C.
- $H = 3.000 \text{ W/(m^2 \cdot \text{K})}$ representing an enforced convection within a moderate water flow. This value was applied for temperature distributions with $T_{\text{mo-}}_{\text{del,peak}} < 90^{\circ}\text{C}$.

Figure 5 shows the influence of considered heat transfer on the modeled peak temperature line for different laser spot diameters. Here, it can be distinguished between the heat transfer before and after the electrolyte boiling. The heat transfer caused by a moderate flow for temperatures < 90 °C is negligible. The temperature differences compared to the lossless case ($H = 0 \text{ W/m}^2 \cdot \text{K}$) amount between 0.1 K and 0.4 K. In contrast, for the case of occurring electrolyte boiling (assumed for $T > 90 ^{\circ}$ C) the heat transfer into the etchant solution increases. With the change of heat transfer coefficient from 3.000 to 50.000 W/m²·K for $T_{\text{model,peak}} > 90 ^{\circ}$ C the deviation from the lossless case becomes clear. Thereby, it can be seen in **Figure 5** that heat losses increase with the applied laser power density and the laser spot diameter. For peak temperatures up to 200 °C, the measured decrease ranges between 1.5 K and 3 K at a spot diameter of 30.5 µm, whereas this decrease lies between 4 K and 10 K at $d_{\text{spot}} = 109 \text{ µm}$.

In general, it can be stated that for surface temperatures between 20°C and 100°C the heat transfer into the electrolyte during the LCM can be neglected.



Figure 5. Peak surface temperature line in dependence of considered heat losses into the electrolyte for different laser beam spot diameters.

4.3. Experimental Verification

4.3.1. Removal Characteristics

The influence of the laser power on the resulting surface modification on titanium after an irradiation time of 1 s is exemplarily illustrated in **Figure 6** for $d_{\text{spot}} = 30.5 \ \mu\text{m}$. The surface modification obtained with $d_{\text{spot}} = 109 \ \mu\text{m}$ are included within the supplementary material (**Figure A1**).

As can be seen, a detectable material removal (depth > 1 µm) occurs first at laser power of around 0.65 W. For 0.7 W< P_L < 1.1 W the removal rates increase with the laser power. Here, a bell-like removal shape is observed, which indicates a disturbance-free processing and suitable induced surface temperatures. From P_L > 1.1 W the cavity profile changes to a W-like shape, in which the maximum removal depth is shifted from the center to the outer flanks. A further increase of laser power (especially from P_L > 1.4 W) leads to a change of the removal behavior. In this regime an additional material deposition, as seen in the height profiles in **Figure 6**, can be observed in the disturbance region.

Because of occurring electrolyte turbulences these mushroom-like structures are sometimes locally shifted from the cavity center. The same three regimes were also observed with $d_{spot} = 109 \ \mu\text{m}$. Here, a detectable removal in titanium was obtained first at $P_L = 2.6 \ W$. The removal retains its bell-like shape up to laser powers of 4.6 W. At higher laser power the removal is then disturbed as the mushroom-like structures appear.

In a previous work a detailed EDX-analysis of the chemical composition of the different cavities was performed [17]. While only the K_a and K_β peaks of titanium were detected within the disturbance-free removal regime, the occurring removal disturbances were characterized by the appearance of additional phosphor



Figure 6. Microscopic images of the removal spots and their height profiles in dependence of the applied laser power after a 1 s-irradiation with a $30.5 \,\mu\text{m}$ laser spot.

and oxygen peaks. The formation of both titanium oxide and titanium phosphate is supposed to be strongly related to the thermal interaction of a formed boiling gas bubble with the laser-induced convection dynamic in the removal cavity, so that an intense deposition of titanium-phosphate is located more at the cavity center than at the outer flanks. A detailed discussion of the appearance of the mushroom-like structures can be found in [17].

4.3.2. Removal Depth

With respect to the ruling process regime the resulting removal depths were measured at the center of the removed cavity in the disturbance-free regime and at the flanks of the W-like cavity in the disturbed regime. Figure 7 depicts the removal depths obtained with both spot diameters 30.5 μ m and 109 μ m in dependence of the applied laser power. The results reveal that the removal depths can be assigned directly to the different removal regimes. During the disturbance-free regime (Regime II) the removal depth increases linearly with the laser power up to values of 11 μ m (with $d_{spot} = 30.5 \mu$ m) and 7 μ m (with $d_{spot} = 109 \mu$ m), whereby the deviations were measured to range between 0.1 μ m and 0.7 μ m. In contrast, the transition to the disturbed regime is characterized in the one hand by a shifting of the removal depth from the center to the outer sides (see Figure 6). In the other hand the occurring disturbances are reflected on the enhanced deviations of the measured depth. These lie between 1.2 μ m and 2.5 μ m.



Figure 7. Measured removal depth in dependence of the applied laser power (density) obtained with both laser spot diameters $30.5 \ \mu m$ and $109 \ \mu m$. The deviation in power is due to the measurement uncertainty of the powermeter, while the deviation in depth is related to the experimental and analysis methods.

Moreover, it is observed that the depth is briefly reduced before it continues to grow with a slower slope. At the same time the width as well as the volume of the accumulated metallic salts increase. **Figure 7** depicts clearly that the formed mushroom-like structures (within regime III) grow linearly with the laser power.

4.3.3. Cavity Diameters

To enable a direct correlation between the resulting removal geometry and the laser-induced temperature distribution at the workpiece surface a spatial superposition of both is required. Therefore, the diameter of the observed removal cavities, referred to as D_{outer} , was measured for the disturbance-free regime. Here, the center of the incident laser beam represents the origin of the coordinate system at workpiece surface. Besides, the diameter of the disturbed region, referred to as D_{inner} , was also characterized.

Figure 8 shows that the evolution of both diameters D_{outer} and D_{inner} is similar to the removal depth and can be assigned directly to the removal regime. Within the regime II (disturbance-free removal) the cavity diameter D_{outer} increases linearly with the laser power. For $d_{spot} = 30.5 \,\mu\text{m}$ the diameter D_{outer} rises from (18 \pm 0.2) μm up to (56 \pm 2.6) μm within a laser power increase of 0.4 W, while D_{outer} increases from (55 \pm 1.2) μm to (140 \pm 4.5) μm with $d_{spot} = 109 \,\mu\text{m}$. Moreover, the transition to the disturbed removal regime III is characterized by a change in the slope increase of D_{outer} . Both, D_{outer} and D_{inner} continue then growing with a linear trend indicating thereby that the growth in width of the mushroom-like structures is also linear to a further increase of laser power.

5. Discussion

5.1. Limit Temperatures of Laser Chemical Removal

As mentioned before, the laser chemical machining is a temperature-driven



Figure 8. Measured characteristics diameters D_{outer} and D_{inner} in dependence of the applied laser power in titanium. D_{outer} and D_{inner} represent respectively the diameters of the removal cavity and the disturbed zone.

process, for which it is still a lack in understanding the direct correlation between the resulting removal geometry and the laser-induced temperatures.

From the validation of the model presented in Section 3 with the experimental results it is expected to open up the opportunity to:

1) Determine the required limits surface temperatures for a disturbance-free material removal.

2) Predict the resulting removal quality in dependence of the main process parameters, which can help to reduce the experimental expenditure.

Therefore, the temperature distribution has to be correlated spatially with the removal profiles of machined cavities, respectively with both distinctive diameters D_{outer} and D_{inner} (see the schematic diagram in **Figure 9**). It has to be noticed that $T_{R,min}$ and $T_{R,max}$ correspond to the bottom and upper limit temperatures at a defined parameter combination resulting in a successful material removal. At the regime II (disturbance-free removal) $T_{R,min}$ represents the surface temperature at the distance $D_{\text{outer}}/2$, whereas $T_{R,max}$ is equal to the modelled peak laser induced surface temperature $T_{\text{model,peak}}$. Within the regime III (disturbed removal) $T_{R,min}$ and $T_{R,max}$ correspond to the surface temperatures at the distances $D_{\text{outer}}/2$ and $D_{\text{inner}}/2$, respectively.

In Figure 10 the characteristic limits temperatures related to both diameters D_{outer} and D_{inner} are illustrated as a result of a laser irradiation ($t_L = 1$ s) with $d_{spot} = 30.5 \ \mu\text{m}$ and $d_{spot} = 109 \ \mu\text{m}$. It is observed that the laser chemical removal in the disturbance-free regime starts at a nearly constant temperature. With $d_{spot} = 30.5 \ \mu\text{m}$ the $T_{R,min}$ -plateau was found to range between 63°C and 66°C, whereas this plateau lies between 68°C and 70°C with $d_{spot} = 109 \ \mu\text{m}$. As the titanium



Figure 9. Schematic illustration of the spatial correlation between removal profile and temperature distribution at the workpiece surface. Using the geometric parameters D_{outer} and D_{inner} the temperature range for a disturbance-free laser chemical removal can be defined. Changes of the temperature distribution due to occurring disturbances in regime III are not taken into account.



removal regime: I no removal II non disturbed III disturbed

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Figure 10. Defined bottom and upper limit surface temperatures $T_{R,min}$ and $T_{R,max}$ required for the laser chemical removal in titanium with a laser spot diameter of 30.5 µm (left) and 109 µm (right). The dashed lines depict the modeled peak surface temperature with consideration of heat losses into the electrolyte.

surface cannot undergo an interaction with the electrolyte at room temperature ($T \approx 20$ °C) it becomes clear that the activation of the anodic dissolution reaction requires a minimum limit temperature.

Within the regime II it can be observed that the peak surface temperature represents the upper limit for the laser chemical removal. This is reflected on the linear increase of the temperature range with respect to the laser power. Moreover, as seen in **Figure 10**, the removal disturbances occur first at temperatures of about 108°C and 125°C with spots diameters of 30.5 µm and 109 µm, respectively. In contrast to De Silva *et al.* [5], which have declared that the highest removal efficiency is achieved at surface temperatures \approx 90°C, the here defined upper limit temperatures $T_{R,max}$ are higher. As discussed in [19], the water vaporization is mainly responsible for the primary bubble formation when water is irradiated by a micrometic heat source. The subsequent bubble expansion is then caused by the diffusion of dissolved gases. This confirms that the bubble formation and attachment, which characterize the disturbed regime, are strongly initiated by the electrolyte boiling.

The defined temperatures $T_{R,max}$ in the regime III (108°C and 125°C) are higher than the given boiling temperature of 104°C under 1 atm. When considering the Nukiyama boiling curve it can be stated that these temperatures are related to the nucleate boiling. For aqueous solutions, this boiling regime extends from 5 K to about 30 K above the saturation temperature (here 104°C) and is characterized by an enhanced bubble formation and an increasing heat flux [20]. Thus, taking the boiling temperature of the electrolyte as the upper limit guaranties a disturbance-free removal.

With a further increase of laser power in the removal regime III it can be seen that the upper limit temperature $T_{R,max}$ achieve its maximum at 137°C ± 5°C. With respect to the boiling regime, this temperature range fits well to the transition boiling, in which the rate of bubble formation exceeds the rate of bubble detachment at the heated surface. Within this boiling regime a combined unstable vapor film with partial-nucleate boiling can be formed [20]. This leads to a decreased contact between the heated surface and the liquid solution and provides the evidence of the shielding model [9] that described the effect of an attached gas bubble on the quality of laser chemical machining of metals.

However, it has to be noticed that the presented model considers only constant heat transfer coefficient and does not reflect the temperature dependent heat flux within the different boiling regimes.

5.2. Correlation between Surface Temperatures and Material Removal

In Figure 11, the direct correlation between the defined limit temperatures and the removal characteristics (depth and diameter D_{outer}) is illustrated. Within the disturbance-free removal (regime II) a linear dependence on the applied laser powers is observed. As the upper limit temperature $T_{R,max}$ and thereby the temperature range increases, the removal depth as well as the cavity diameter follow this trend and grow linearly. The observed maximum removal depths amount between 8 µm and 11 µm with both laser spot diameters. This is in accordance



Figure 11. Direct correlation between the LCM-temperature range (blue color for $T_{R,min}$ and red color for $T_{R,max}$) and the removal dimensions (cavity depth and diameter) after a 1 s-laser irradiation with $d_{spot} = 30.5 \ \mu m$ and $d_{spot} = 109 \ \mu m$.

with the maximum removal rate of 10 μ m/s that was identified by Nowak *et al.* for the purely laser chemical machining of metals [6].

Furthermore, within the transition to the disturbed removal (formation of the mushroom-like structures) the slope-increase of $T_{R,max}$ changes. As depicted in **Figure 11**, $T_{R,max}$ switches to lower values than the expected peak temperatures $T_{model,peak}$. This affects directly the removal depth and cavity diameter. These show also a different growth slope when disturbances occur. Similar is observed also within the removal regime III. The formed mushroom-like structures follow the linear trend of the limit temperatures $T_{R,max}$ until an observed maximum temperature plateau about 137°C ± 5°C is achieved (see **Figure 10**). In contrast, the removal depth and cavity diameter remain increasing. For that reason, the removal rate cannot be anymore correlated to the surface temperatures. The occurring mechanisms in this regime are mainly dominated by the formation and attachment of gas bubbles.

Another interesting feature is the similar maximum values of the upper limit temperature $T_{R,max}$ obtained with both laser spot diameters. This indicates the direct correlation between the surface temperatures, the laser power as well as the laser spot diameter. Taking into account Equation (13) it can be noted that the surface temperature is proportional to the ratio P_L/d_{spot} . To verify this relation, the modeled peak surface temperatures as well as the experimentally identi-

fied limit temperatures $T_{R,min}$ and $T_{R,max}$ are plotted as function of P_L/d_{spot} for both laser spot diameters, as illustrated in Figure 12.

Thereby, a quasi-invariant evolution trend is observed with both spot diameters. $T_{\text{model,peak}}$, $T_{R,min}$ and $T_{R,max}$ show a characteristic and unique trend regardless the heated area. The observed deviation in $T_{\text{model,peak}}$ at temperatures greater than 100°C can be explained by the included heat losses when considering an enforced water boiling ($H = 50.000 \text{ W/m}^2$ ·K for $T_{\text{model,peak}} > 90°$ C), which become more significant with an increased laser spot diameter (see Figure 5). In contrast, the deviations in $T_{R,min}$ and $T_{R,max}$ are related to the characterized diameters (see Figure 8) and range between $< \pm 5°$ C in the removal regime II and < 20°C in the disturbed removal regime.

From Figure 12 it can be stated that the laser chemical machining is governed by a two-dimensional heating process as the surface temperature is the determinant factor. Regardless the laser spot diameter the thermal evolution of the LCM-limit temperature is unique for a defined electrolyte-metal combination. Similar has been observed for the case of a cw laser heating of water in the front of a glass substrate containing gold nanoparticles. Here, Baffou *et al.* have reported that the gas bubble formation is generated in the superheating regime at temperatures of about 220°C independent of the applied laser spot diameter [21].

Thus, the quotient P_L/d_{spot} can be used as an indicator to predict the removal quality. In **Table 2**, the LCM-removal regimes of titanium in a 5 mol/l are illustrated. Thereby, a disturbance-free removal is assured regardless the laser spot size at P_L/d_{spot} ranging between 23 mW/µm and 40 mW/µm.



Figure 12. LCM-limit temperatures $T_{R,min}$ and $T_{R,max}$ and modeled peak surface temperature $T_{\text{model,peak}}$ as a function of the ratio P_L/d_{spot} obtained with both laser spot diameters 30.5 µm and 109 µm. The correlation shows a quasi-invariant evolution trend.

Removal regime	(regime I)	(regime II)	(regime III)
	No removal	Disturbance-free removal	Disturbed removal
$P_L/d_{\rm spot} [{\rm mW}/{\rm \mu m}]$	<23	23 … 40	>40

Table 2. Removal quality of titanium in H_3PO_4 in dependence of the quotient P_I/d_{spot^*}

It has to be noticed that the influence of the reaction time, which is also an important factor, is not studied in this work. This will be included in a following second part, in which the laser chemical removal will investigated under consideration of a moving laser beam with different feed velocities.

6. Conclusions

In this work a Green-function based modeling of the laser-induced temperatures at the workpiece surface during the laser chemical machining was presented. From its correlation with resulting removal geometry following conclusions can be drawn:

1) The initiation of a laser chemical removal requires a minimum threshold temperature. This ranges between 63° C and 70° C when processing titanium in phosphoric acid.

2) The enhanced gas bubble formation within the nucleate boiling of the electrolyte defines the upper limit of the laser chemical removal. This is in line with the experimental observations.

3) Within the disturbance-free processing regime the material removal show a linear behavior. Both, removal depth and cavity diameter follow the linear increase of the surface temperature with respect to the applied laser power.

4) The limit surface temperatures of a laser chemical machining follow a unique and invariant evolution regardless the size of the heated area. This is only dependent on the material-electrolyte-combination.

In a next step the thermal modeling will be extended to the case of a moving laser beam, in which the influence of the reaction time will be investigated depending on the feed velocity. The provision of a temperature-dependent formulation of the material load will open up the opportunity of comparing the laser chemical machining with other thermal- and chemical-based processes such as electrochemical and electro discharge machining.

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Supplementary Materials

Table A1. List of used symbols.

Symbol	Description	Unit
A	Laser beam area at the surface	m ²
а	Approximation constant [16]	-
C_p	Specific heat capacity	kJ/(kg K)
D	Thermal diffusivity	m²/s
D_{inner}	Inner removal diameter	μm
$D_{\rm outer}$	Outer removal diameter	μm
$d_{ m spot}$	Laser spot diameter	μm
G	Green function	-
Н	Heat transfer coefficient	W/(m ² ·K)
Ι	Laser power density	W/cm ²
1	Absorption depth	nm
P_L	Laser power	W
P_{abs}	Absorbed laser power	W
r	Laser beam radius	μm
Т	Temperature rise	°C
T_{Boiling}	Electrolyte boiling temperature	°C
$T_{ m model,peak}$	Peak surface temperature (Model)	°C
$T_{R,max}$	Upper limit temperature for a material removal	°C
$T_{R,min}$	Bottom limit temperature for a material removal	°C
t	Time	s
t_L	Irradiation time	s
V	Feed velocity	m/s
XYZ	Dimensionless coordinates	-
xyz	Dimensional coordinates	m
а	Dimensionless quantity (r/l)	-
α_{abs}	Wavelength related absorption coefficient of T_i	%
θ	Dimensionless quantity $(H \cdot r/\kappa)$	-
к	Thermal conductivity	W/(m K)
λ	Laser wavelength	nm
ϕ	Integration variable/substitution quantity ($ au$ - $ au$)	-
ρ	Density	Kg/m³
τ	Dimensionless time coordinate	-
$ au_E$	Transmission coefficient of the electrolyte	%
Ψ	Dimensionless temperature rise	-



Figure A1. Microscopic images of the removal spots and their height profiles in dependence of the applied laser power after a 1 s-irradiation with a 109 µm laser spot.

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