

Developing a Model for Controlling Internal Corrosion in Water Supply System

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Abstract

A model was developed to generate charts that fit the conditions as diverse temperatures and ionic strengths, and that estimate the diversified state of water. The chart can be used as a tool for controlling corrosive waters resulted in internal corrosion and the model producing charts composed of a number of sub modules, and each module incorporated parameters including acidity, alkalinity, pH, and calcium ion. Utilizing the chart water quality of the raw water in G water purification works was estimated to be unsaturated and Langelier index becomes -1.4 which means that the water is highly corrosive and calcium carbonate would not be precipitated. Thus, the water requires treatment as the injection of water stabilizing chemicals to promote an oversaturated (protective) condition. As a result of adding 5 mg/L of lime, it is possible to be precipitated with 5 mg/L, and the water becomes noncorrosive. In addition, when 5 mg/L of caustic soda is added as a conditioning chemical, it signifies to be precipitated with 9 mg/L, and the water also turns out to be largely noncorrosive. Both chemicals are possible to use for the water to be favorable for the formation of a protective film. Optimum injection rate for controlling corrosion can be found by repeating the procedures until the well-conditioned water criteria are satisfied.

Keywords

Model, Sub Module, Corrosive, Water Stabilization Chemicals, Langerlier Index

1. Introduction

Nevertheless for the last several decades aged water supply pipes and rust irresistible material pipes had been replaced for rust resistible pipes such as stainless pipe, PE pipe, and PVC pipe and also continuous effort including flushing pipes to supply a safe drinking water has been conducted, a number of the complaints have been continuously increased from drinking water users due to rust stains

found in the pipes. One of the largest complaints for drinking water is caused by rust stains being generated by internal corrosion of water supply pipeline [1] [2].

In Korea, as the corrosiveness of water quality has increased due to the low alkalinity and hardness of raw water, and excessive quantities of injection of chlorine and coagulants in the process of water treatment [3] [4], it is required to introduce an effective water treatment method that can control the corrosive water.

Controlling internal corrosion in water service pipelines is to change the quality of raw water, which includes pH control and injection of corrosion inhibitor that is utilized in existing water purification facilities for controlling water quality [2] [5].

In order to control effectively the corrosive water quality, it is necessary not only to evaluate the quality of raw water accurately, but also to predict and estimate the changes in water quality in case of injection of calcium hydroxide, caustic soda, or soda ash to change the corrosive water into a noncorrosive water, provided that the raw water has been evaluated as having corrosive water qualities. Caldwell Lawrence chart [6] [7] [8] has been widely utilized in practice to achieve the goal, which is complicated in the procedures of use; and also, restricted charts are only available so that it does not reflect diversified water quality characteristics.

This study aimed to develop a model that can generate diversified charts conforming to the water quality characteristics and to make the program able to be processed simply and conveniently in practice by an operator, so that it would be a useful tool to help making decision for controlling water quality in water supply pipeline system.

2. Study Contents and Methods

2.1. Overview

The model developed in this study represents the correlations between alkalinity, acidity, pH, and calcium with the coordinates of parameters of acidity and (alkalinity-calcium) in graph. The coordinate system is set up so that alkalinity minus calcium increases on the positive direction of horizontal axis, and acidity increases on the negative direction of vertical axis. In the Cl and C2 co-ordinate system Cl is defined as negative Acidity and increases in the positive Y direction. while the parameter C2 increase in the positive X direction as C1 = -Acidity and C_2 = Alkalinity-calcium, where

Alkalinity =
$$\begin{bmatrix} HCO_3^- \end{bmatrix} + \begin{bmatrix} CO_3^- \end{bmatrix} + \begin{bmatrix} OH^- \end{bmatrix} - \begin{bmatrix} H^+ \end{bmatrix}$$

and

Acidity =
$$\left[HCO_3^* \right] + \left[HCO_3^- \right] + \left[H^+ \right] - \left[OH^- \right]$$

2.2. Model Setup

Each of the parameters pH, calcium (Ca) and Alkalinity (Alk) can be expressed in terms of the co-ordinate parameters as pH = F1(C1,C2), Alk = F2(C1,C2),



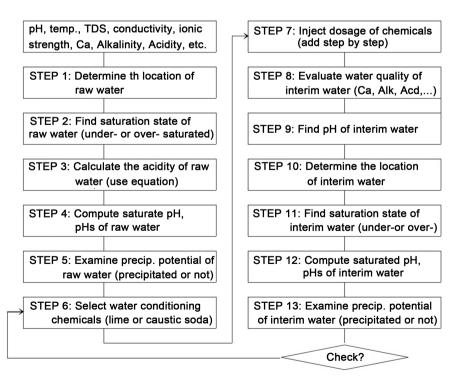
and Ca = F3(C1,C2). Lines representing saturated equilibrium values for these parameters can be found by solving these equations and are plotted in the diagram. Choosing a series values for *C*1 the corresponding values of *C*2 for each expression can be found. Repeating this procedure for a number of Ca, Alk, pH values the diagram composed of a number of lines can be plotted. In the diagram, the intersection point of the lines representing the values of any two of these parameters defines the equilibrium value of the third parameter.

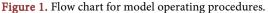
3. Numerical Modeling

Equations for plotting the parameters as alkalinity, pH and calcium were used to relate each of the parameters to the co-ordinate parameters *C*1 and *C*2. They are derived from equilibrium conditions for water conditioning from previous studies [9] [10] [11]. The model incorporating those equations are composed of several submodels: XLN_PH, computes pH lines; XLN_CA, generates calcium lines; YLN_ALKH, produces alkalinity horizontal lines; YLN_ALKV, determines alkalinity vertical lines; XY_PLOT, combines output files from the four submodels and plots lines. The engine used to develop the model is MATLAB, which is a computer program that provides the user with a convenient environment for performing many types of calculations and having graphical capabilities, and offers a tool to implement numerical methods. The model operating procedures are summarized in the flow chart shown in **Figure 1**.

3.1. Submodel for pH Lines

Equations were arranged for HCO_3^- to determine pH lines as below:





$$C1 = K'_{cW} / \mathrm{H}^{+} - \mathrm{HCO}_{3}^{-} - \mathrm{H}^{+} \bullet \mathrm{HCO}_{3}^{-} / K'_{c1} - \mathrm{H}^{+}$$
(1)

$$\left(-1 - K_{c2}'/\mathrm{H}^{+}\right) \left[\mathrm{HCO}_{3}^{-}\right]^{2} + \left(C2 - K_{cW}'/\mathrm{H}^{+} + \mathrm{H}^{+}\right) \left[\mathrm{HCO}_{3}^{-}\right] + K_{cS}' \bullet \mathrm{H}^{+}/K_{c2}' = 0 \quad (2)$$

where:

$$\frac{\left[\mathrm{H}^{+}\right]\left[\mathrm{HCO}_{3}^{-}\right]}{\left[\mathrm{H}_{2}\mathrm{CO}_{3}^{*}\right]} = \frac{K_{1}}{f_{m}^{2}} = K_{1}'; \quad \frac{\left[\mathrm{H}^{+}\right]\left[\mathrm{CO}_{3}^{-}\right]}{\left[\mathrm{HCO}_{3}^{-}\right]} = \frac{K_{2}}{f_{d}} = K_{2}';$$
$$\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right] = \frac{K_{w}}{f_{m}^{2}} = K_{W}'; \quad \left[\mathrm{Ca}^{++}\right]\left[\mathrm{CO}_{3}^{-}\right] = \frac{K_{s}}{f_{d}^{2}} = K_{s}'$$

where K_1 = first dissociation constant for carbonic system; K_2 = second dissociation constant for carbonic acid; K_w = dissociation constant for water; K_s = solubility product constant for carbonic system.

The fundamental equilibria equations for the calcium-carbonic system can be written with species concentrations expressed in ppm as $CaCO_3$ by modifying the equilibrium constants as follows:

$$K'_1 \times 2.5 \times 10^4 = K'_{c1}; \quad K'_2 \times 10^5 = K'_{c2}; \quad K'_1 \times 10^{10} = K'_{cS}; \quad K'_w \times 25 \times 10^8 = K'_{cW}$$

It is difficult to solve Equations (1) and (2) directly so that numerical integrating should be adopted. The value of HCO_3^- can be found while changing C2 with a constant interval for one fixed value of H^+ , and then the obtained value substituted into equation of C1 to obtain one line for pH. It is possible to obtain multi lines conforming to the fixed values of H^+ in diverse range.

3.2. Submodel for Ca Lines

Equations were arranged for HCO_3^- to determine calcium lines as below:

$$C2 = \text{HCO}_{3}^{-} + K_{cS}^{\prime} / \text{Ca}^{++} + \frac{K_{cW}^{\prime} \bullet K_{cS}^{\prime}}{\text{HCO}_{3}^{-} \bullet K_{c2}^{\prime} \bullet \text{Ca}^{++}} - \text{Ca}^{++} - \text{HCO}_{3}^{-} \bullet K_{c2}^{\prime} \bullet \text{Ca}^{++}$$
(3)
$$\frac{K_{c2}^{\prime} \bullet \text{Ca}^{++}}{K_{cS}^{\prime} \bullet K_{c1}^{\prime}} \Big[\text{HCO}_{3}^{-} \Big]^{3} + \left(1 + \frac{K_{c2}^{\prime} \bullet \text{Ca}^{++}}{K_{cS}^{\prime}} \right) \Big[\text{HCO}_{3}^{-} \Big]^{2}$$
(4)
$$+ C1 \Big[\text{HCO}_{3}^{-} \Big] - \frac{K_{cW}^{\prime} \bullet K_{cS}^{\prime}}{K_{c2}^{\prime} \bullet \text{Ca}^{++}} = 0$$

Laguerre method and Muller method [12] [13] can be utilized for obtaining a multinomial solution. The solution generates three roots, incorporating with 1 real root and 2 conjugation imaginary roots from the characteristics of correlation equation. In case of substituting the real root in the equation, one line is obtained for the fixed value of Ca^{++} . Further changing the value of Ca^{++} for 2, 5, 10 and then from 20 to 100, the corresponding lines are produced.

3.3. Submodel for Alkalinity Lines

Alkalinity lines plot in the diagram as curves each with two horizontal limbs joined by a vertical section of curve. To plot the horizontal section of curve, for some chosen Alkalinity *C*1 values are calculated for corresponding *C*2 values. For the vertical section of curve *C*2 values are calculated for corresponding *C*1



values. An alkalinity line becomes a curve by adding up two horizontal lines and one perpendicular line.

1) Alkalinity horizontal lines

To obtain the horizontal line for alkalinity, equations were arranged for H^+ and could be expressed as:

$$C1 = K'_{cW} / \mathrm{H}^{+} - \left[\mathrm{H}^{+}\right]^{2} \bullet X / K'_{c1} \bullet K'_{c2} - \mathrm{H}^{+} \bullet X / K'_{c2} - \mathrm{H}^{+}$$
(5)

$$\left(\frac{K'_{cS}}{K'_{c2}(\text{Alk}-C_2)}-1\right)\left[H^+\right]^2 - \left(\frac{K'_{cS}}{\text{Alk}-C_2}-\text{Alk}\right) \bullet H^+ + K'_{cW} = 0$$
(6)

where $X = K'_{cS}/(Alk - C2)$. Pursuant to the characteristics of equation, two real roots were obtained, one of those is a negative root that draws the horizontal line on the lower part and the other draws the horizontal line on the upper part, respectively. Each of the lines produces regions where a value is suddenly increased larger than a constant horizontal value before connecting to the perpendicular line. At this stage, the angle was restricted to less than 45°, an angle being increased more than the angle 45° was prohibited by treating to generate an error [7].

It is designed to obtain the value of C1 while increasing the value of C2 with a constant interval within the range for the fixed value of alkalinity. When connecting a series of obtained C1 and C2 coordinate values each together, one line is found, and further corresponding lines are explored while changing the value of alkalinity in wide range.

$$C1 = \frac{K_{cW}^{\prime} \left(\text{Alk} - \text{HCO}_{3}^{-} \right)}{K_{c2}^{\prime} \bullet \text{HCO}_{3}^{-} + K_{cW}^{\prime}} + \frac{\text{HCO}_{3}^{-} \left(K_{c2}^{\prime} \bullet \text{HCO}_{3}^{-} + K_{cW}^{\prime} \right)}{K_{c1}^{\prime} \left(\text{Alk} - \text{HCO}_{3}^{-} \right)} + \text{HCO}_{3}^{-} + \frac{K_{c2}^{\prime} \bullet \text{HCO}_{3}^{-} + K_{cW}^{\prime}}{\text{Alk} - \text{HCO}_{3}^{-}}$$
(7)

$$C2 - \text{Alk} - \frac{K'_{cS}}{K'_{c2} \bullet \text{HCO}_3^-} \bullet \frac{K'_{c2} \bullet \text{HCO}_3^- + K'_{cW}}{\text{Alk} - \text{HCO}_3^-} = 0$$
(8)

The solution was found by integrating the equations and could be classified into two categories: in one case three roots were all real ones, the smallest value was used; in other case roots including an imaginary root were found, the smallest value was used among the value of real number of a complex root and real roots. The value of HCO_3^- was obtained while increasing the value of *C*1 for the fixed value of alkalinity with a constant interval; *C*2 was determined by substituting the value in Equations (7) and (8), and then one alkalinity line was found, and in addition corresponding lines are produced while changing the value of alkalinity in diverse range.

4. Results and Discussion

The physical and chemical characteristics of the raw water sampled from G water purification facility of Nakdong River water system are shown in Table 1. The current state of water quality was evaluated step by step by utilizing the

Physical and chemical parameters	Raw water	Chemicals added	
		Ca(OH) ₂	NaOH
Physical properties	<i>T</i> = 25C; TDS = 40 mg/L; <i>I</i> = 0.001		
pH	7.2	9.0	9.0
Calcium mg/L as CaCO ₃	40	45	40
Alkalinity mg/L as CaCO ₃	42	47	47
Acidity mg/L as CaCO ₃	47	42	42
C2 mg/L as CaCO ₃	2	2	7
pHs	8.60	8.45	8.50
Saturation state	under	over	over
[Ca] _{sat} mg/L as CaCO ₃	-	40	36
CaCO ₃ precip. potential	-4	5	9
Langelier's index	-1.4	0.55	0.50

Table 1. Results of water quality changes by injection of water conditioning chemicals.

chart developed in this study, and the results are summarized in the table. In order to evaluate the state of raw water, the chart corresponding to temperature 25° C, and ionic strength, I = 0.001 was selected. The lines corresponding to alkalinity 42 mg/L (as CaCO₃), calcium 40 mg/L (as CaCO₃), pH 7.2 from the chart were connected, and let the intersections as A, B, and C, and then it was represented by the three-sided envelope ABC as shown in Figure 2, which represents that the water is not saturated, since the three lines do not meet at a single point.

Because the raw water is not saturated from the results of step 1, the value of calcium concentration was read out from the calcium line, passing the intersection between the alkalinity line and the pH line in order to determine whether it is over-saturated or under-saturated; this became $\left[\text{Ca}\right]_{\text{sat}}=90\,\,\text{mg/L}$ as a saturated calcium concentration, and because the value exceeded the measured calcium concentration $[Ca]_i = 40 \text{ mg/L}$, it signifies that the raw water becomes under-saturated. Hence, the water requires treatment to promote an oversaturated (protective) condition.

The acidity of the raw water was obtained from the value of Y-axis where it met the horizontally extended line at the intersection between the alkalinity line and the pH line, and the acidity was 47 mg/L. In cases of low calcium concentration and low concentration of alkalinity, because the intersection between the calcium line and the alkalinity line is located outside the left boundaries of the chart, it is not able to calculate the acidity. In such a case, it could calculate the acidity directly by utilizing the equations suggested from previous studies [9] [10] [11].

The saturated pH concentration, pH, 8.6 was obtained by reading out the pH value at the intersection of the calcium and alkalinity lines. Langelier Saturation Index [8] [14], LSI of -1.4 was obtained by utilizing the parameter, signifying that the water is corrosive.



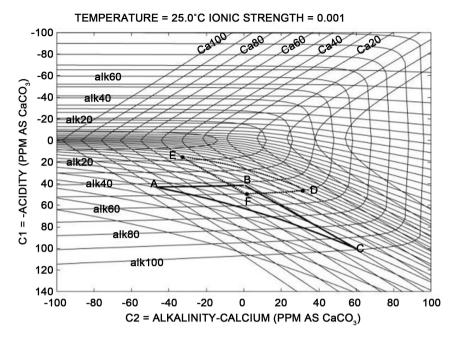


Figure 2. Evaluation process of water quality changes due to addition of water stabilizers.

The saturated calcium concentration $[Ca]_{sat}$ was obtained by reading out the calcium value at intersection *F*, where the extended line of acidity and the vertical line from point *B* were met. A potential quantity of calcium carbonate precipitation (CCPP) was obtained from subtraction of the saturated calcium concentration and the measured calcium concentration, which CCPP was -4, signifying that the water is under-saturated or corrosive.

The corrosion evaluation indexes resulting from steps 4 and 5 expressed that the raw water was corrosive. A chemical product injected to change the noncorrosive water to the corrosive water is called water quality stabilizer, for which calcium hydroxide or sodium hydroxide is widely used. The procedures to evaluate changes of water quality according to an injection of water quality stabilizer are examined in the following sections.

The procedures to change corrosive water into noncorrosive water while increasing the concentration of calcium hydroxide by 5 mg/L and 10 mg/L as a water quality stabilizer are summarized in the following, and the results are listed in Table 1.

In cases where the raw water is under-saturated, it is necessary to change the water to a saturated state by injecting conditioning chemicals. As a result of adding calcium hydroxide 5 mg/L, the calcium concentration becomes 46 mg/L by increasing 5 mg/L. At that time, the hydroxyl ion (OH⁻) concentration is increased by 5 mg/L, so that alkalinity (= $[HCO_3^-]+[CO_3^-]+[OH^-]-[H^+]$) becomes 47 mg/L by increasing 5 mg/L. The increase of hydroxyl ion concentration caused to decrease the acidity (= $[HCO_3^+]+[HCO_3^-]+[H^+]-[OH^-])$ by 5 mg/L, and then the acidity becomes 42 mg/L.

The pHof the interim water is found according to change of injection amounts. In **Figure 2**, after addition of water quality stabilizer, the pH read 9.0 at the intersection where it met with the value of the alkalinity line (47 mg/L) by extending the acidity line (42 mg/L). When the calcium line (45 mg/L), the alkalinity line (47 mg/L), and the pH line (pH = 9.0) were connected, the envelope enclosed by DEF is formed, signifying that the interim water is in an unsaturated state.

As the concentration of the calcium line (15 mg/L) passing through the intersection D between the alkalinity line and the pH line is lower than the calcium concentration of the interim water 45 mg/L, the interim water is over-saturated and precipitation can occur. The saturated pH read as 8.45 at the intersection between the alkalinity line and calcium line of the interim water for the saturated state. LSI of 0.55 was obtained by estimating the index. Since the index is positive, the water is in noncorrosive state. The area enclosed by dotted lines DEF becomes reduced and collected to the point F. The point is the intersection between the (alkalinity-calcium) line (1 mg/L) and the acidity line (42 mg/L), signifying the saturated calcium concentration is 40 mg/L. A possible precipitation amount is obtained by subtracting the saturated calcium concentration and the calcium concentration of the interim water (45 mg/L), so that 5 mg/L of precipitation can occur. Changes of water quality were evaluated by repeating the procedures step 9 through step 13 until the saturation state is slightly oversaturated, which means Langelier index is nearly zero or potential precipitation is about zero.

Sodium hydroxide 5 mg/L was injected as a water quality stabilizer, and increased or decreased amounts of calcium, alkalinity, and acidity of the treated water was estimated due to the injection. As the calcium concentration is not increased, so it comes out at 41 mg/L. The concentration of hydroxyl ion (OH⁻) is increased by 5 mg/L, so that the alkalinity becomes 47 mg/L by increasing 5 mg/L.

The acidity line (42 mg/L) was extended to obtain the pH of processing water corresponding to changes of injection amount, and then the pH of 9.0 was read at intersection between the extended acidity line (42 mg/L) and the alkalinity line (47 mg/L). When the calcium line (45 mg/L), the alkalinity line (47 mg/L), and the pH 9.0 line were connected, an envelope enclosed by three-sided lines was formed, signifying that the treated water is in an under-saturated state.

Because the concentration of the calcium line (15 mg/L) passing through the intersection between the alkalinity line and the pH line in step 11 is lower than the calcium concentration of the interim water (45 mg/L), the interim water is in a supersaturated state, therefore signifying the possibility to be precipitated.

The saturated pH of 8.5 was obtained by reading out the pH value at the intersection between alkalinity line and the calcium line of the interim water for the saturated state. LSI of 0.50 was obtained by estimating the Langlier Index. The index is positive, signifying a corrosive water quality. In step 13, the area surrounded by the dotted lines became reduced and collected to point F, which is the intersection between the alkalinity minus calcium line (1 mg/L) and the acidity line (42 mg/L), signifying a saturated calcium concentration is 36 mg/L. The possible precipitation amount was found by subtracting the saturated calcium concentration (36 mg/L) and the calcium concentration (45 mg/L), and 9 mg/L of precipitation can occur.

5. Conclusions

The model that can generate charts conforming to combinations of temperatures and ionic strengths has been developed to control corrosive waters. The results using the model are summarized as follows:

Water quality of the raw water that collected in sampling station was evaluated, with the results showing that it is in an unsaturated state because LSI was -1.4 and possible precipitation amount of calcium carbonate was -4 mg/L, signifying corrosive water. 5 mg/L of calcium hydroxide as a water conditioning chemical was injected as an effort to convert corrosive waters to non-corrosive waters, and changes of water quality were estimated. As a result, Langelier index of the treated water turns out to be LSI of 0.55 and possible precipitation amount of calcium carbonate is 5 mg/L, which signifies noncorrosive water. When 10 mg/L of calcium hydroxide is injected, it may generate calcium carbonate precipitation; therefore it has been judged by us that the more injection will not be needed.

In case of injection of sodium hydroxide 5 mg/L, the pH was estimated at 9.0 and the saturated pH was 8.5. LSI of 0.50 and possible precipitation amount of calcium carbonate was 9 mg/L, which means non-corrosive. The saturated calcium concentration was 36 mg/L and the calcium concentration of the treated water 46 mg/L, so that it signifies to be precipitated. Therefore the model developed in this study could serve as a useful tool controlling corrosive waters in practice by an operator.

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References

- Lim, J.C., Kim, J.K. and Koo, J.Y. (2012) Coating Formation of Water Supply Pipes by Inhibitor and Water Quality Improvement Effect. *Journal of the Korean Society* of Water and Wastewater, 26, 97-106. <u>https://doi.org/10.11001/jksww.2012.26.1.097</u>
- [2] Woo, D.S. and Hwang, B.G. (2014) Corrosivity Evaluation of SWRO Membrane Desalted Permeate. *Journal of the Korean Society of Civil Engineers*, 18, 53-59. <u>https://doi.org/10.1007/s12205-014-0161-7</u>
- [3] Lee, D.J., Kim, Y.I. and Park, H.A. (2008) Corrosion Control in Water Distribution System Using Lime and Carbon Dioxide. *Journal of the Korean Society of Water* and Wastewater, 22, 379-388.
- [4] Woo, D.S. and Hwang, B.G. (2008) A Study on the Corrosion Characteristics of

Carbon Steel Pipes by Phosphate Corrosion Inhibitor. Journal of the Korea Academia-Industrial Cooperation, 9, 493-499. https://doi.org/10.5762/KAIS.2008.9.2.493

- [5] Hwang, B.G. (2014) Determination of an Optimum Injection Rate Using Calcium Carbon Saturation Indices for Internal Corrosion Control in Distribution Water Pipe. Journal of the Korean Society of Water Treatment, 22, 11-18.
- [6] Caldwell, D.H. and Lawrence, W.B. (1953) Water Softening and Conditioning Problems. Industrial & Engineering Chemistry, 45, 535-548. https://doi.org/10.1021/ie50519a027
- [7] Loewenthal, R.E. and Marais, G.R. (1976) Carbonate Chemistry of Aquatic Systems, Vol. I: Theory and Application. Ann Arbor, Michigan.
- [8] Rossum, J.R. and Merrill, D.T. (1983) An Evaluation of the Calcium Carbonate Saturation Indexes. AWWA, 75, 95-100.
- [9] Murrill, D.T. and Sanks, R.L. (1977) Corrosion Control by Deposition of CaCO₃ Films: Part 1. A Practical Approach for Plant Operators. A WWA, 69, 592-599.
- [10] Murrill, D.T. and Sanks, R.L. (1977) Corrosion Control by Deposition of CaCO₃ Films: Part 2. A Practical Approach for Operators. AWWA, 69, 634-640.
- [11] Murrill, D.T. and Sanks, R.L. (1978) Corrosion Control by Deposition of CaCO₃ Films: Part 3. A Practical Approach for Plant Operators. AWWA, 70, 12-18.
- [12] Chapra, S.C. (2012) Applied Numerical Methods with MATLAB for Engineers and Scientists. McGraw Hill.
- [13] Press, W.H., Teukolsky, S.A., Vetterling, W.T. and Flannery, B.P. (1997) Numerical Recipes in Fortran 77. Cambridge University Press, Cambridge.
- [14] Langelier, W.F. (1936) The Analytical Control of Anti-Corrosion Water Treatment. AWWA, 28, 1500.

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