

Development of Rainfall Intensity Duration Frequency Curves for Mumbai City, India

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Abstract

The change in rainfall pattern and intensity is becoming a great concern for hydrologic engineers and planners. Many parts of the world are experiencing extreme rainfall events such as experienced on 26th July 2005 in Mumbai, India. For the appropriate design and planning of urban drainage system in an area, Intensity Duration Frequency (IDF) curves for given rainfall conditions are required. The aim of the present study is to derive the IDF curves for the rainfall in the Mumbai city, Maharashtra, India. Observed rainfall data from 1901 pertaining to Colaba and from 1951 of the Santacruz rain gauge stations in Mumbai are used in the present study to derive the IDF curves. Initially, the proposed IDF curves are derived using an empirical equation (Kothyari and Garde), by using probability distribution for annual maximum rainfall and then IDF curves are derived by modifying the equation. IDF curves developed by the modified equation gives good results in the changing hydrologic conditions and are compatible even with the extreme rainfall of 26th July 2005 in Mumbai.

Keywords

Rainfall, Intensity, Duration, Return Period, Frequency, IDF Curves

1. Introduction

In many parts of the world, flooding is probably the most severe hazard among the natural hazards occurring due to change in rainfall pattern. Development of rainfall Intensity-Duration-Frequency (IDF) relationship is a primary basic input for the design of the storm water drainage system for cities [1]. The rainfall depths derived from the intensity duration frequency relationship is being used by water resource managers for planning, designing and operation of water resource related projects [2]. To ascertain the hydrologic risks, assessment of ex-

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treme precipitation and establishment of IDF curves are important [3] [4]. The relationship between rainfall intensity and duration was demonstrated by Kuichling [5] having maximum discharges of runoff. A generalized IDF formula for any location in the United States was presented using three basic rainfall depths, that is, R_1^{10} (1 h, 10-year rainfall depth), R_{24}^{10} (24 h, 10-year rainfall depth), and R_1^{100} (1 h, 100-year rainfall depth) [6]-[8]. Kothyari and Garde [9] developed a general relationship between the rainfall intensity, duration (P_{24}^2) and frequency with the Indian conditions. They developed the equation for IDF curves using the rainfall data of 78 rain gauge stations from all over India considering the value of mean annual rainfall (R) for 24 hr, and two-year rainfall, R_{24}^2 . IDF is a statistical relationship between the rainfall intensity (*i*), the duration (*d*), and the return period (T) [2]. This approach was further extended by combining high frequency rainfall extremes having long term daily information and derived IDF curves taking into consideration of a short instrumental data set for time less than one day [10]. IDF curves for part of Saudi Arabia were developed by using statistical distribution techniques for different return periods [11].

While designing the new drainage system, proper information having IDF relationship reflecting recent hydrologic changes has to be used as design criteria [12]. Mumbai being the coastal city, surrounded by sea and creek is vulnerable to flooding when the high intensity of rainfall coincides with high tidal conditions. Therefore proper knowledge of rainfall intensity should be available for the proper and efficient design of the storm water drainage system. Earlier, Chawathe *et al.* [1] had presented a detailed rainfall analysis for Mumbai. It was done with the data taken for 24 and 33 years for Colaba and Santacruz rain gauge station respectively. Zope *et al.* [13] carried out the spatio—temporal rainfall variation for Mumbai city. Further it is felt that there is a necessity and need to update the IDF relationship, especially depending on today's changing hydrological conditions [14].

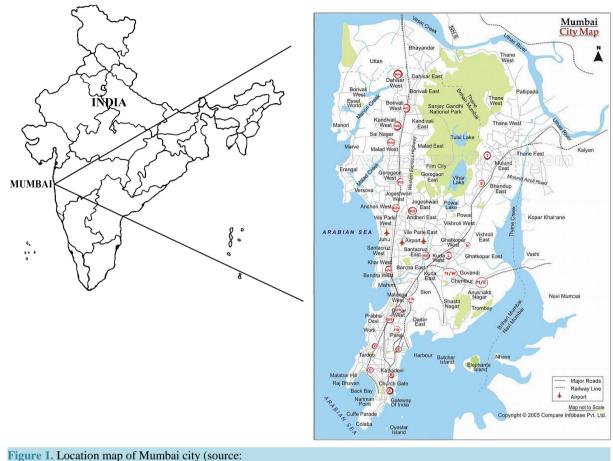
The aim of the present study is to develop the IDF rainfall curves for the Mumbai city using longer length of observed rainfall data. Initially, the proposed IDF curves are modeled using the empirical relationship developed by Kothyari and Garde [9], using the probability distribution method for annual maximum rainfall and then the same equation has been modified to derive the IDF curves by incorporating the varying return period concept. The results obtained were compared with respect to the changing hydrological conditions, especially with the extreme rainfall observed on 26th July 2005 in the Mumbai region.

2. Case Study Area and Hydro Metrological Features

Mumbai (lat. 18.50°N, long. 72.52°E), (Figure 1) being the capital of Maharashtra state and financial trade centre and financial capital of India has great concern about the economic development of the country [15]-[17]. Due to migration of people from all over the country in search of employment and trade, the population of the city is growing very fast. The city is surrounded by sea, hills and creeks and therefore has limitations on horizontal growth as well as to provide required infrastructural facilities due to scarcity of land. The existing drainage system of Mumbai city has a network of roadside surface drains, an underground drainage system in the island city, major and minor nallah discharging storm water, either into four main rivers or directly into the creek and finally to the Arabian sea [13] [18]. Being a coastal city, while designing the drainage system, there are limitations on depth of the storm water drainage system due to the tidal effect and water levels at discharge point. Existing storm water drainage system of Mumbai city have 45 outfalls below mean sea level, 135 outfalls above mean sea level but below high tide level and 6 outfalls above high tide level [19]. On 26th July 2005, Mumbai city experienced extreme rainfall event with highest rainfall intensity of 190.3 mm/hr and total rainfall of 944.2 mm in 24 hours period coinciding with highest tide level. There was severe loss of lives and huge economic losses [15] [16] [19]. After deluge of 26th July 2005, Municipal Corporation of Greater Mumbai (MCGM) has installed total 60 automatic weather stations all over the city which records rainfall as well as other weather data at an interval of 15 minutes. Thus, considering the importance of the city and vulnerability to flooding, for proper designing of the drainage system, knowledge of proper rainfall intensity for different return periods is necessary.

3. Data Used in the Analysis

Before 26th July 2005 floods, there were only two rain gauge stations in Mumbai. The observed daily rainfall data for a period of 108 years (1901 to 2008) from Colaba rain gauge station, and 58 years (1951 to 2008) from the Santacruz rain gauge station were used [13] in deriving the IDF curves using the equation given by Kothyari



http://www.mcgm.gov.in/irj/portal/anonymous?NavigationTarget=navurl://ce7407c74001ac932426502e58da0827)

and Garde [9] as well as from the modified equation. The hourly rainfall data from 1969 to 2008 for both rain gauge stations [13] was used for deriving the IDF curves by the annual maxima method. The rainfall data has been collected from the Indian Meteorological Department (IMD) Pune as well as from the Municipal Corporation of Greater Mumbai (MCGM).

4. Methodology

The statistical analysis of daily as well as hourly rainfall data was carried out using Gumbel distribution [13]. The hourly rainfall at the Colaba rain gauge varies from 28.3 mm/hr to 113 mm/hr, whereas at the Santacruz, it varies from 27 mm/hr to 190 mm/hr [27]. Basic statistical results of an hourly rainfall data series were carried out [27]. On 26th July 2005, IMD at Santacruz rain gauge station recorded 944 mm of total rainfall in 24 hours time (Figure 2).

The maximum intensity of rainfall recorded was 190.3 mm/hr during 14.30 to 15.30. The Colaba rain gauge station which is within 23 km apart recorded only 74 mm of total rainfall on the same day [15] [19]. To ascertain the effects of these changing rainfall pattern, IDF curves for a Santacruz rain gauge station has been developed by including as well as excluding the rainfall on 26th July 2005.

In this study, annual maximum daily method [20] is used in the IDF development. The step by step procedure used is given below.

- Find out year wise annual maximum daily rainfall series.
- Rank (*m*) the rainfall totals.
- Find out return periods (*T*).

$$T = \left(N+1\right)/m \tag{1}$$

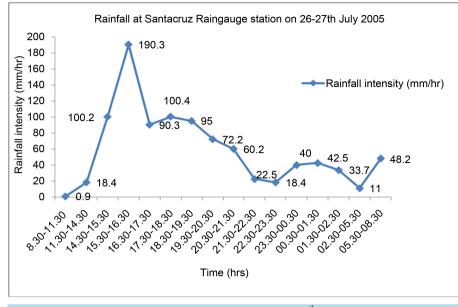


Figure 2. Rainfall at the Santacruz rain gauge station on 26-27th July 2005 (FFC, 2006).

where N is the number of years data.

- Plot the graph of rainfall depth v/s return period on semi log paper.
- Find out the equation of regression line to find out precipitation depth.

$$R_{24}^2 = P_{(mm)} = a \ln(T) + b \tag{2}$$

where, P = maximum daily precipitation.

Find out rainfall intensity for different return periods and different durations by using formulas as described below.

4.1. IDF Curves by Kothyari and Garde's Method

Kothyari and Garde [9] developed a formula to derive IDF relationship for India by analyzing the rainfall data from 78 rain gauge stations across India. The generalized relationship with realistic estimates of rainfall proposed by them for various zones of India is [9]

$$I_t^T = C \frac{T^{0.20}}{t^{0.71}} \left(R_{24}^2 \right)^{0.33} \tag{3}$$

where, I_t^T rainfall intensity in mm/hr; *T* return period in years and *t* duration of rainfall in hr., R_{24}^2 is 24 hr, a two-year rainfall in mm. Here values of constant *C* in different Geographical Regions of India proposed by them are given in the **Table 1**. Mumbai being in western India, the value of *C* can be taken as 8.3 for analysis of rainfall.

In the above equation, the value of *R* (mean annual rainfall) is taken as constant as 24 hr rainfall and 2-year return period to find out the rainfall intensities for the shorter time durations with respect to different return periods (*T*). IDF curves with the above equation have been developed by analyzing the rainfall data of an annual daily maximum series [22] for the Colaba rain gauge station (**Figure 2**). The same equation is used to derive IDF rainfall curve for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station [22]. The developed IDF rainfall curves for the Santacruz rain gauge station are shown in **Figure 3** and **Figure 4** respectively, with and without 26^{th} July 2005 rainfall. The IDF curves derived by using the Equation (3) as given by Kothyari and Garde [9], it has been observed that for 100-year return period [23], the rainfall intensity at Colaba (**Figure 3**) is 112.48 mm/hr and at the Santacruz rain gauge station with and without considering the rainfall on 26^{th} July 2005 (**Figure 4** and **Figure 5** respectively) is 117.65 mm/hr and 117.39 mm/hr respectively.

Thus, IDF curves established by equation given by Kothyari and Garde are not compatible with the rainfall on

26th July 2005 in Mumbai with an intensity of about 190 mm/hr as well as today's changing hydrological conditions and extremities of the rainfall event.

4.2. IDF Curves by Probability Distribution for Annual Maximum Rainfall

In this method, the rainfall frequency analysis of the maximum rainfall depth corresponding to hourly storm

Table 1. Values of constant C in different geographical regions of India (source: Kothyari and Garde; 1992) [9] [21].		
Geographical region	Zone	Value of <i>C</i>
Northern India	1	8.0
Central India	2	7.7
Western India	3	8.3
Eastern India	4	9.1
Southern India	5	7.1

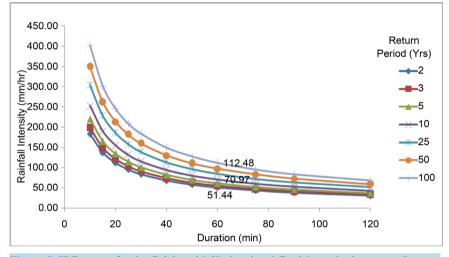


Figure 3. IDF curves for the Colaba with Kothyari and Garde's method-constant *R*.

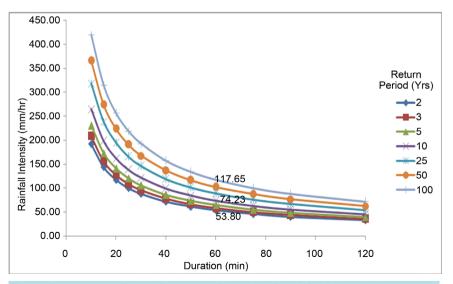


Figure 4. IDF curves for the Santacruz with Kothyari and Garde's method-constant *R* with extreme rainfall of 2005.

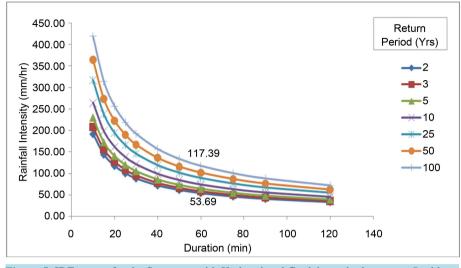


Figure 5. IDF curves for the Santacruz with Kothyari and Garde's method-constant *R* without extreme rainfall of 2005.

durations (1969-2008) were determined for each year of data for both the rain gauge stations, and then the results were ranked in descending order with the highest intensity taking the value of one in the rank. Probability function was used to fit the data. Rainfall frequency analysis for different return periods was done by using the extreme value Gumbel Type I distribution [24]-[27]. Frequency of precipitation X_T (in mm) for each duration having the specified return period *T* (year) is given by Equation (4) [21] as below.

$$X_T = X_t + K\sigma_{n-1} \tag{4}$$

where, \overline{X}_t = mean of annual maximum depth; σ_{n-1} = standard deviation of annual maximum depths; and, K = Frequency factor.

For the Gumbel distribution, the value of *K* is given in the Equation (5) as below [21].

$$K = -\left(\frac{\sqrt{6}}{\pi}\right) \left(0.5772 + \ln\left(\ln\left(\frac{T}{T-1}\right)\right)\right)$$
(5)

For the rain gauge stations, statistical analyses were carried out with mean and standard deviations and value of K of annual maximum depths having various durations were derived. The IDF relationships obtained by an annual maximum method for the Colaba rain gauge station is shown in Figure 6 and for the Santacruz rain gauge station with and without considering 26th July 2005 rainfall are shown in Figure 7 and Figure 8 respectively.

As per the derived IDF rainfall curves, rainfall intensity for the 100-year return period is 124.86 mm/hr for the Colaba rain gauge station and 160.11 mm/hr and 132.72 mm/hr respectively with and without considering 26th July 2005 rainfall for the Santacruz rain gauge station.

5. Results and Discussion

In the present study, it was aimed to develop the IDF curves for the rainfall in the Mumbai city in changing hydrologic conditions. The IDF curves developed by using the Equation (3) as given by Kothyari and Garde [9], it had been observed that for the 100-year return period [23], the rainfall intensity at Colaba (Figure 3) is 112.48 mm/hr and at the Santacruz rain gauge station with considering and excluding the rainfall of 26^{th} July 2005 (Figure 4 and Figure 5 respectively) is 117.65 mm/hr and 117.39 mm/hr respectively. However, as per past rainfall record, Mumbai has experienced 190 mm/hr rainfall intensity in July 2005. Thus the IDF curves developed by using equation given by Kothyari and Garde [9], by keeping value of *R* constant as 2-year return period, does not show the proper results in the recently changing hydrologic conditions for the Mumbai city. In view of this, to obtain better results, the Equation (3) was modified and the new Equation (6) is given as below.

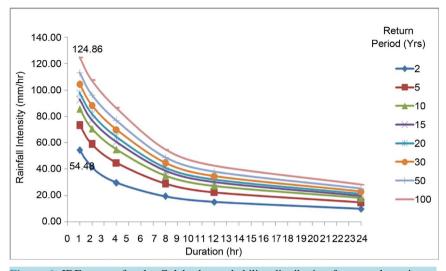


Figure 6. IDF curves for the Colaba by probability distribution for annual maximum rainfall.

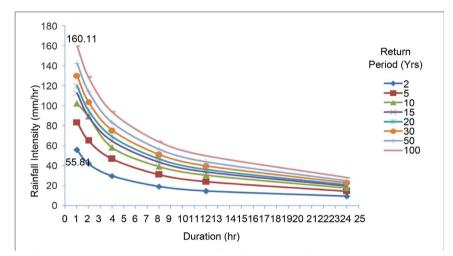


Figure 7. IDF curves for the Santacruz by probability distribution for annual maximum rainfall with 26th July 2005 Rainfall.

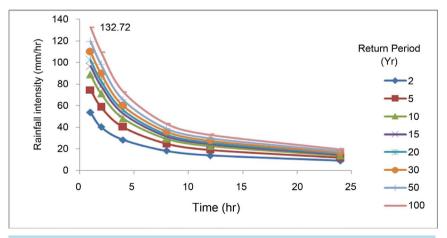


Figure 8. IDF curves for the Santacruz by probability distribution for annual maximum rainfall without 26th July 2005 Rainfall.

Modified Kothyari and Garde's Method

In the changing climatic conditions, to avoid urban flooding and to take appropriate care, proper knowledge of rainfall intensity should be available for the proper and efficient design of the storm water drainage system. As discussed above, to obtain better results, the Equation (3) was modified and the new equation is obtained as:

$$I_t^T = C \frac{T^{0.20}}{t^{0.71}} \Big(R_{24}^T \Big)^{0.33}$$
(6)

In the above equation, the value of an R will vary with the return period (T) to derive the rainfall intensity for smaller durations. The IDF curves developed by using the above Equation (6), for the Colaba rain gauge station (**Figure 9**), and with considering and excluding the rainfall of 26th July 2005 for the Santacruz rain gauge station are shown in **Figure 10** and **Figure 11** respectively.

From the modeled IDF curves by the above new equation, it had been observed that for 100-year return period, the rainfall intensity at the Colaba is 164.56 mm/hr and at the Santacruz rain gauge station with considering and excluding the rainfall of 26th July 2005 is 176.37 mm/hr and 160.35 mm/hr respectively, which shows the better results as compared with the past rainfall records for a Mumbai city. As per IDF curves modeled by the probability distribution for annual maximum rainfall, the rainfall intensity [28] at the Colaba is 124.86 mm/hr and at Santacruz rain gauge station with and without considering 26th July 2005 rainfall is 160.11 mm/hr and 132.72 mm/hr respectively. Thus, comparing the results obtained from the equation given by Kothyari and Garde, the

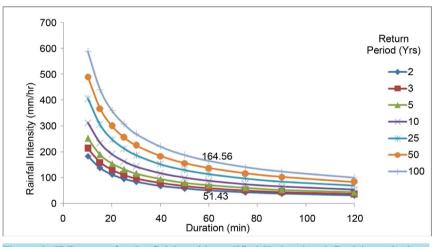


Figure 9. IDF curves for the Colaba with modified Kothyari and Garde's method-varying *R*.

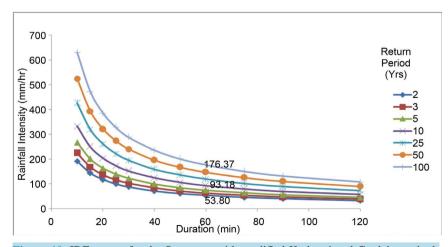
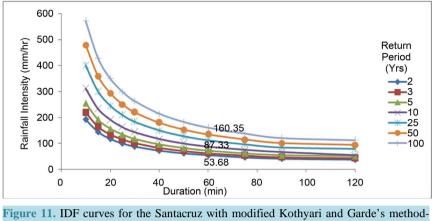


Figure 10. IDF curves for the Santacruz with modified Kothyari and Garde's methodvarying *R* with 2005 rainfall.



varying *R* without 2005 rainfall.

new modified equation and an annual maximum rainfall method, IDF curves established by using the new modified equation shows better results in the changing hydrologic conditions as observed on 26th July 2005 in Mumbai. Also, from the rainfall analysis, it was observed that the intensities for all frequencies and durations of storms are generally lower for Colaba as compared to those at Santacruz.

6. Conclusion

Due to change in global mean temperature and hydrological changes, the higher frequency of rainfall may occur in the future as observed in the last few years in many parts of the world. Mumbai being the coastal city, surrounded by sea and creek, is vulnerable to flooding due to many reasons such as high intensity of rainfall, high tides, loss of drainage capacity due to design faults, development of reclaimed areas and improper knowledge and adoption of intensity of rainfall in designing the drainage system. For the design of appropriate drainage system, IDF curves are to be considered. The IDF relationships developed in the present study can be used effectively in designing the new drainage system and in modifying or replacing the old ones. As observed, the IDF curves derived by modifying the Kothyari and Garde's equation shows good results in the changing hydrologic conditions as reported on 26th July 2005 in Mumbai. Alternatively, the IDF relationship developed for Santacruz rain gauge station may be used for the entire city, since it is located centrally and also being expressing the higher intensities of rainfall, the design would be safer to avoid flooding in the future.

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