

The Cross-Sectional Risk Premium of Decomposed Market Volatility in UK Stock Market

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Abstract

We decompose UK market volatility into short- and long-run components using EGARCH component model and examine the cross-sectional prices of the two components. Our empirical results suggest that these two components are significantly priced in the cross-section and the negative risk premia are consistent with the existing literature. The Fama-French three-factor model is improved by the inclusion of the two volatility components. However, our ICAPM model using market excess return and the decomposed volatility components as state variables compares inferiorly to the traditional three-factor model.

Keywords

ICAPM, Decomposition of Stock Volatility

1. Introduction

The most fundamental and best known model in asset-pricing theory is the Capital Asset Pricing Model (CAPM) which is essentially a "single factor" model of portfolio returns. However, the assumption of a single risk factor (market beta) limits the validity of this model and the effects of other risk factors have put this model under criticism. Specially, in the late 1970s, a research begins to uncover variables like size, various price ratios, and momentum that add to the explanation of average returns associated with β .

[1] present evidence that beta almost has no explanatory. Their study demonstrates that size and book-to-market equity (BE/ME), combined to capture the cross-sectional variation in average stock returns together with the market β , leverage, and earnings-price (E/P) ratios. [2] further suggest that the traditional CAPM does not account for returns of size and book-to-market sorted portfolios. They show that there are common return factors related to size and BE/ME that help capture the cross-section of average stock returns in a way that is consistent with multifactor asset-pricing models.

[3] report the momentum effect that is left unexplained by the three-factor model. [4] constructs a 4-factor model by including a momentum factor to three-factor model to capture the one-year momentum anomaly. FF

three-factor model and Carhart's four-factor model have been widely accepted and employed in empirical analyses.

In contrast to the lack of theoretical support of three (or four)-factor model, alternative responses to the poor performance of CAPM are to make modifications to the standard CAPM. Among all the developments, intertemporal CAPM and conditional CAPM are most widely applied and various further extensions are proposed to better interpret the risk-return relation and portfolio structure.

The advocates of conditional CAPM argue that the poor empirical performance of CAPM might be due to the failure to account for time-variation in conditional moments. Conditional CAPM tries to preserve the single factor structure of the standard CAPM and assumes that all investors have the same conditional expectations for their asset returns.

The ICAPM of [5] suggests that when there is stochastic variation in investment opportunities, asset risk premia are not only determined by covariation of returns with the market return, but also associated with innovations in the state variables that describe the investment opportunities. [6] & [7] points out, in cross-sectional asset pricing studies, the factors in the model should be related to innovations in state variables that forecast future investment opportunities.

There is no doubt that stock market volatility changes over time, but whether or not volatility represents a priced risk factor remains less certain. [6] & [7] tests the ICAPM and shows that investors care about risks both from the market return and from changes in forecasts of future market returns. Time-varying market volatility induces changes in the investment opportunity set by changing the expectation of future market returns, or by changing the risk-return trade off. [8] develops the ICAPM in a framework in which the conditional means and variances of state variables are time varying and reflect changes in the investment opportunity set. Risk-averse investors tend to hedge against exposures to future market volatility. [9] set up a standard two-factor pricing kernel with the market return and stochastic volatility as factors. They show that market volatility is a significant cross-sectional asset pricing factor.

[10] develop a new specification to model volatility process based on GARCH. They decompose volatility into permanent and transitory components. Following [10], the component GARCH model is applied to numerous economic areas and different countries¹.

[11] incorporate the component GARCH model of [10] and the EGARCH model of [12] to build up a new specification of volatility dynamics, the EGARCH component model. They present that the short- and long-run volatility components have negative, highly significant prices of risk which is robust across sets of portfolios, sub-periods, and volatility model specifications.

The motivation for this paper stems from the fact that there are a growing number of papers dealing with the decomposition of the market volatility into components using Engle and Lee's component GARCH Model. However, to my best knowledge, no studies examine the cross-sectional effect of the two decomposed components of market volatility, especially on UK stock market. Contrary to the existing empirical studies that simply employ Engle and Lee's component GARCH model to explore the time-series effect of volatility, this thesis attempts to understand the cross-sectional effects of the transitory and permanent components of volatility. Furthermore, the EGARCH component framework is implemented together with the simple GARCH component model. Although Adrian and Rosenberg demonstrate that the short- and long-run volatility components are significantly priced in US stock market and their volatility components model compares favorably to the traditional CAPM, Fama-French model and several other model specifications, we are less confident that their volatility components are well priced in UK stock market and the superiority of their model.

To test these, we apply the [11] decomposition of market risk to UK stock market and investigate the pricing of short- and long-run volatility risk in the cross-section of stock returns. The object of this chapter is threefold. First, we attempt to both determine whether the two components of market volatility are priced risk factors and estimate the prices of these components. Second, we try to examine whether the short- and long-run component model remains superior in UK stock markets. Third, we examine the robustness of the volatility component model across sets of portfolios, sub-periods, and model specifications.

The reminder of this article is organized as follows. Methodology and data description are presented in part II and part III. Empirical results are reported in part IV. The final section offers concluding remarks.

¹Research include [13] on futures market; [14] on bond market; [15] exploring US stock market; [16] exploring middle-east stock market; [17] exploring Malaysia stock market.

2. Methodology

2.1. Theoretical Motivation of the Pricing of Volatility Risk

The most parsimonious pricing ICAPM framework in which to study the relationship between innovations of state variables and expected return is given as:

$$E(R) \approx rra \ cov(R, R^{M}) + \lambda_{2} cov(R, \Delta z)$$
(1)

R denotes return in excess of the risk-free rate and R^M is stock market excess return. The state variables z are the variables that determine how well the investor can do in his maximization. *rra* is the elasticity of marginal value with respect to wealth and is often referred as the *coefficient of relative risk aversion*.

When investment opportunities vary over time, the multifactor models of [5] and [18] show that risk premia are associated with the conditional covariance between asset returns and innovations in state variables that describe the time-variation of the investment opportunities. And hence, covariance with these innovations will therefore be priced. In the [6] & [7] ICAPM framework, investors care about risks both from the market return and from changes in forecasts of future market returns.

[8] extends Campbell's model and shows that risk-averse investors tend to directly hedge against changes in future market volatility. Motivated by these multifactor models, [9] express market volatility risk explicitly in Equation (1),

$$E_{t}\left(R_{t+1}\right) \approx rra \operatorname{cov}\left(R_{t+1}, R_{t+1}^{M}\right) + \lambda_{2} \operatorname{cov}\left(R_{t+1}, \Delta v_{t+1}\right) + \sum_{k=1}^{K} \lambda_{k} \operatorname{cov}\left(R_{t+1}, f_{k,t+1}\right)$$

$$\tag{2}$$

where f_k represent other factors other than aggregate volatility that induce changes in the investment opportunity set.

For the convenience of empirical application, the above model can be written in terms of factor innovations. $R_{t+1}^m - \gamma_{m,t}$, $v_{t+1} - \gamma_{v,t}$ and $f_{k,t+1} - \gamma_{k,t}$ represent innovation in the market return, in aggregate volatility risk, and innovations to the other factors respectively. A true conditional multifactor representation of expected returns in the cross-section would take the following form:

$$R_{t+1}^{i} = a_{t}^{i} + \beta_{m,t}^{i}(R_{t+1}^{M} - \gamma_{m,t}) + \beta_{v,t}^{i}(v_{t+1} - \gamma_{v,t}) + \sum_{k=1}^{K} \beta_{k,t}^{i}(f_{k,t+1} - \gamma_{k,t})$$
(3)

where R_{t+1}^{i} is the excess return on stock *i*. $\beta_{m,t}^{i}$, $\beta_{v,t}^{i}$ and $\beta_{k,t}^{i}$ are the loadings on the excess market return, on market volatility risk, and on other risk factors, respectively. The conditional mean of the market return, aggregate volatility and other factors are denoted by $\gamma_{m,t}$, $\gamma_{v,t}$ and $\gamma_{k,t}$, respectively. In equilibrium, the conditional mean of stock *i* is given by

$$a^{i} = E(R^{i}) = \beta^{i}_{m}\lambda_{m} + \beta^{i}_{\nu}\lambda_{\nu} + \sum_{K=1}^{K}\beta^{i}_{k}\lambda_{k}$$

$$\tag{4}$$

where $\lambda_{m,t}$, $\lambda_{v,t}$ and $\lambda_{k,t}$ are the price of risk of the market factor, the price of aggregate volatility risk, and the prices of risk of the other factors, respectively.

2.2. Econometric Methodology—EGARCH Component Model

As an extension of GARCH model, [10] introduce a component GARCH model where the conditional variance is decomposed into transitory and permanent components. In this two-component model, transitory and permanent components are used to capture short- and long-term effects of shock, respectively.

Many studies find that two-component volatility model is superior to one-component specification in explaining equity market volatility and the log-normal model of EGARCH performs better than square-root or affine volatility specifications. Appealed to the merits of the component GARCH and the EGARCH models, [11] incorporate the features of these two models and specify the dynamics of the market return in excess of risk-free rate R_i^M and the conditional volatility $\sqrt{h_i}$ as:

Market return:
$$R_{t+1}^M = \mu_t^M + \sqrt{h_t z_{t+1}}$$
 (1a)

Market volatility:
$$\ln \sqrt{h_t} = l_t + s_t$$
 (1b)

Short-run component:
$$s_{t+1} = \theta_4 s_t + \theta_5 z_{t+1} + \theta_6 \left(|z_{t+1}| - \sqrt{2/\pi} \right)$$
 (1c)

Long-run component:
$$l_{t+1} = \theta_7 + \theta_8 s_t + \theta_9 z_{t+1} + \theta_{10} (|z_{t+1}| - \sqrt{2/\pi})$$
 (1d)

 $z_t \sim i.i.d. N(0,1)$ and μ_t^M is the one-period expected excess return. The log-volatility is the sum of two components l_t and s_t . Each component is an AR(1) processes with its own rate of mean reversion. Without loss of generality, let l_t be the slowly mean-reverting, long-run component and s_t be the quickly mean-reverting, short-run component ($\theta_4 < \theta_8$). The unconditional mean of s_t is normalized to zero.

The terms $|z_{i+1}| - \sqrt{2/\pi}$ in Equations (1c) and (1d) are the shocks to the volatility components. Their expected values are equal to zero, given the normality of z_i . For these error terms, equal-sized positive or negative innovations results in the same volatility change, although the magnitude can be different for the short- and long-run components (θ_6 and θ_{10}). The asymmetric effect of returns on volatility is allowed by including the market innovation in Equations (1c) and (1d) with corresponding coefficients θ_5 and θ_9 .

The market model defined by Equations (1a)-(1d) converges to a continuous-time, two-factor stochastic volatility process. An advantage of this specification is that it can be estimated in discrete time via maximum likelihood. The daily log-likelihood function is:

$$f_t(\theta; s_t, l_t | R_t^M) = -\frac{1}{2} \ln(2\pi) - (s_{t-1} + l_{t-1}) - \frac{(R_t^M - \theta_1 - \theta_2 s_{t-1} - \theta_3 l_{t-1})^2}{2h_{t-1}}$$

where t = 1, ..., T is the daily time index, T is the total number of daily observations, and R_t^M is the daily market excess return.

3. Data

We estimate the EGARCH-component volatility model using daily excess returns. The daily data are used in order to improve the estimation precision and then aggregated to a monthly frequency for the cross-sectional analysis. FTSE All Share Index with its dividend yield is used as the proxy for the market return, r^{M} , and one month return on Treasury Bills for the risk free rate, r^{f} . The daily data range from 01/09/1980 to 31/12/2012 and are collected from LSPD (London Stock Price Database) and data stream.

For the cross-sectional price test of the ICAPM, we apply the Fama and French 25 size and BE/ME portfolios and the portfolio returns and monthly factors are taken directly from [19] website. In the spirit of French's provision of the data to the international academic community, [19] construct the Fama and French size and B/M portfolio and the SMB (size factor), HML (value factor) and UMD (the momentum factor) of UK stock market and make all portfolios and factors downloadable from their website.

4. Empirical Results

4.1. Results of the Time Series Regression

If the short- and long-run volatility components are also asset pricing factor, in the spirit of the ICAPM, the equilibrium pricing kernel thus depends on both short- and long-run volatility components as well as the excess market returns. Denote returns on asset *i* in excess of the risk free rate by R_i^i . The equilibrium expected return for asset *i* is:

$$E_{t}\left(R_{t+1}^{i}\right) = \lambda_{1}cov\left(R_{t+1}^{i}, R_{t+1}^{M}\right) + \lambda_{s}cov\left(R_{t+1}^{i}, s_{t+1}\right) + \lambda_{l}cov\left(R_{t+1}^{i}, l_{t+1}\right)$$
(5)

where λ_1 is the coefficient of relative risk aversion, and λ_s and λ_l are proportional to changes in the marginal utility of wealth due to changes in the state variable s_l and l_l .

Equation (5) shows that expected returns depend on three risk premia. The first risk premium arises from the covariance of the asset return with the excess market return, multiplied by relative risk a version λ_1 . This is the risk-return tradeoff in a static CAPM. The second and third risk premia depend on the covariance of the asset return with the innovations in the short- and long-run factors.

Market expected return μ_t^M is defined as

$$\mu_t^M = \theta_1 + \theta_2 s_t + \theta_3 l_t \tag{6}$$

Examination of the risk-return relation is of fundamental importance to the asset pricing literature. Many authors either fail to detect a statistically significant intertemporal relation between risk and return of the market portfolio or find a negative relation².

The estimation results for the volatility model are shown in **Table 1**. In the expected return equation, short-run volatility has a significant positive coefficient θ_2 , while θ_3 , the coefficient of long-run volatility is significantly negative. The market excess return thus depends positively on short-run volatility but negatively on long-run volatility. [11] identify a negative relationship between short-run volatility and market excess return but a positive relationship between long-run volatility and market excess return. Hence, short-run and long-run volatilities seem to have opposite effects on market excess return. This result might explain why previous research often have difficulty identifying a time-series relationship or mixed results of risk and return relation.

We identify the short- and long-run components by their relative degrees of autocorrelation: the short-run volatility has an autoregressive coefficient of 0.807, and the long-run component has an autoregressive coefficient of 0.994. The long-run component is highly persistent. However, it's not permanent, the hypothesis that $\theta_8 = 1$ is rejected at the 1% significant level. The estimate of θ_4 is smaller than that of θ_8 , which indicates the short-run volatility is less persistent compared to long-run component. Because the short- and long-run components determine log-volatility additively, it's impossible to identify the means of the two components separately, and only the mean the long-run component is estimated. θ_5 and θ_9 detect the asymmetric effect on volatility. Both the estimates of θ_5 and θ_9 are significantly negative and large than minus one. This suggests that a positive surprise (z_r) increases both the short- and long-run volatility less than a negative surprise.

Ljung-box Q statistic suggests that there isn't remaining serial correlation in the mean equation of the market excess return, while the ARCH-LM test reveals that there's no additional ARCH effect exhibiting in the standardized residuals.

4.2. Results of the Cross-Sectional Tests

Monthly data are employed to carry out the cross-sectional tests. The daily short- and long-run volatility components are obtained from the time-series regression. The 21-step out-of-sample forecasts of the short- and long-run components are made respectively. Daily innovations of the volatility components are calculated by subtracting the short- and long-run component from the forecasted values. The daily innovations in each month are then aggregated to a monthly frequency, and providing us with the monthly innovations of the short- and long-run component.

Market excess return: $R_{t+1}^{M} = \theta_1 + \theta_2 s_t + \theta_3 l_t + \sqrt{h_t} z_{t+1}$									
	$ heta_{_{ m I}}$	$\theta_{_2}$	$ heta_{_3}$						
Coef.	-0.007	0.267	-0.499						
Std.err.	0.010	0.106	0.031						
<i>p</i> -value	0.475	0.012	0.000						
Short-run component: $s_{t+1} = \theta_4 s_t + \theta_5 z_{t+1} + \theta_6 (z_{t+1} - \sqrt{2/\pi})$									
	$ heta_{\scriptscriptstyle 4}$	$ heta_{\scriptscriptstyle 5}$	$ heta_{_6}$						
Coef.	0.807	-0.046	-0.009						
Std.err.	0.030	0.004	0.042						
<i>p</i> -value	0.000	0.000	0.829						
	Long-run component: $l_{t+1} = \theta_{\tau} + \theta_{\theta} l_{t} + \theta_{\theta} z_{t+1} + \theta_{10} (z_{t+1} - \sqrt{2/\pi})$								
	$ heta_{_7}$	$ heta_{_8}$	$ heta_{9}$	$\theta_{_{10}}$					
Coef.	0.002	0.994	-0.032	0.028					
Std.err.	0.000	0.001	0.001	0.002					
<i>p</i> -value	0.000	0.000	0.000	0.000					

Table 1. Time series estimation of the volatility components, daily, 01/09/1980 to 31/12/2012.

²Examples include, [20], [21], and [22].

$$sres_m = \sum_{t=1}^{N} (s_t - E_{t-21}[s_t]), \tag{7}$$

$$lres_{m} = \sum_{t=1}^{N} (l_{t} - E_{t-21}[l_{t}]),$$
(8)

where *sres* and *lres* denote innovations of short- and long-run volatility respectively. N is the trading days in month m. The market variance v is aggregated to a monthly frequency, and the time series follows an AR(2) process. Hence, variance innovations (*vres*) are estimated as residuals of a monthly autoregressive process with two lags. The statistics of the innovations and the other pricing factors are summarized in **Table 2**.

Under the ICAPM described in Section 2.1, the pricing kernel is a linear function of the excess return on the market portfolio and the innovations in the state variables, so that the unconditional risk premium on asset *i* may be written as:

$$a^{i} = E(R^{i}) = \beta_{m}^{i}\lambda_{m} + \beta_{s}^{i}\lambda_{s} + \beta_{l}^{i}\lambda_{l}$$
⁽⁹⁾

where $\lambda_{m,t}$ is the price of risk of the market factor, $\lambda_{s,t}$ is the price of the short-run volatility risk, and the $\lambda_{t,t}$ is the price of risk of the long-run volatility.

The implication of the ICAPM for stock returns can be tested directly by implementing the two-stage Fama-MacBeth procedure. We use the correction procedure proposed by [23] to account for the errors-in-variables problem.

In the first stage, the 25 size and BE/ME portfolio returns are regressed on market excess returns, *sres* and *lres*. In the second stage, the portfolio returns are regressed on the estimated betas from the first stage to obtain the prices of market risk, short-run volatility risk and long-run volatility risk.

Table 3 reports the pricing of volatility risk in the cross-section. The regressions of CAPM (column i), the FF three factor model (column ii), Carhart's momentum model (column iii), and a model analogous to [9] with innovations to market variance as risk factor (column iv) are also presented in **Table 3**.

In column (v), we can see that the short- and long-run volatility components are significant pricing factors at the 5% level. The prices of short- and long-run components are -0.334 and -0.842 respectively. This implies that an asset with a short-run volatility beta of unity requires a 0.334% lower returns than an asset with zero exposure to the short-run component. These results are consistent with hypothesis that the cross-section of stock returns reflects exposure to volatility risk. In column (vi) and (vii), the prices of risk when the short- and long-run volatility enters as separate factors are reported. Each of the components has a negative price of risk at 10% significant level. [6]-[8] show that investors intend to hedge against market volatility and they are willing to pay a premium for market downside risk. The hedge motive is indicative of a negative price of market volatility. The negative prices of the decomposed components of market volatility would suggest that risk-averse investors tempt to hedge the overall exposures to market risk, no matter whether the exposures are transitory or persistent.

However, the short- and long-run volatility factor compares inferiorly to the FF three-factor model and Carhart momentum model, in terms of pricing performance. The RMSPE (root-mean-squared pricing error) are reported to evaluate the pricing performance of the different models. The models with FF factors (column ii and viii) achieve the lowest pricing errors.

It's worth noting that adding the two volatility components to FF three-factor model and momentum model reduces the pricing errors. This suggests that the volatility components and the Fama and French factors (or

Pricing factors	Mean	Std. Dev.	Skewness	Kurtosis
Short-run volatility(sres)	0.000	1.064	-0.309	3.192
Long-run volatility(<i>lres</i>)	0.000	2.989	1.697	11.083
Market variance (vres)	0.000	14.520	4.429	47.87
Value factor (HML)	0.004	0.037	0.270	11.092
Size factor (SMB)	0.001	0.034	0.712	7.200
Momentum factor (UMD)	0.008	0.042	-1.258	10.844

Table 2. Summary statistics of the monthly pricing factors.

		(i)	(ii)	(iii)	(iv)	(v)	(vi)	(vii)	(viii)	(ix)
Excess market	Coef.	0.596	0.454	0.498	0.439	0.453	0.608	0.465	0.443	0.438
return	p-value	0.033	0.073	0.073	0.083	0.073	0.026	0.066	0.080	0.084
Short-run volatility	Coef.					-0.334	-0.265		-0.232	-0.287
(sres)	p-value					0.047	0.097		0.091	0.062
Long-run volatility	Coef.					-0.842		-0.602	-0.623	-0.689
(lres)	p-value					0.034		0.071	0.074	0.057
Market variance	Coef.				-3.251					
(vres)	p-value				0.049					
Value factor	Coef.		0.518						0.518	
(HML)	p-value		0.025						0.024	
Size factor	Coef.		0.165						0.156	
(SMB)	Datility Coef. -0.842 p-value 0.034 riance Coef. -3.251 p-value 0.049 ctor Coef. 0.518 .) p-value 0.025 ctor Coef. 0.165 .) p-value 0.386 .) p-value 0.386 .) p-value 0.386 .) p-value 0.029 PE 0.210 0.120 0.142 0.245 0.188			0.212						
Momentum factor	Coef.			0.890						0.801
(UMD)	p-value			0.029						0.076
RMSPE		0.210	0.120	0.142	0.245	0.188	0.210	0.197	0.113	0.138

Table 3. Pricing the cross section of the 25 size and B/M sorted portfolios.

This table reports the two-stage cross-sectional regression results for the 25 size and B/M sorted portfolios under various model specifications, including ICAPM, FF three-factor model, and the CAPM. The *t*-ratios are calculated using Jagannathan and Wang (1998) and Newey and West (1987) procedures to account for the estimation errors in first-stage estimation and correct for the possible heteroskedasticity and autocorrelation. The corresponding *p*-values are reported according to the adjusted *t*-ratios. Root mean square pricing errors (RMPSE) are reported.

momentum factors) capture some orthogonal source of priced risk.

The first-stage FM regression shows that the factor loadings have significant variation across the size dimension, however but less significant variation across the B/M dimension³.

Table 4 shows the risk premium on the 25 size and BE/ME portfolios. The price spread of market risk between small firms and large firms is -0.107, which translate into an annualized premium spread due to market risk of -1.3% per year. Similarly, the annualized premium spreads between small and large firms due to short-run volatility and long-run volatility are -1.76% and 4.14% respectively. Only the risk premium of the long-run volatility is positive, but with much bigger magnitude. Hence, combining the three risk-premium differences yields an average excess risk premium for small firm relative to large firms of 1.08%. The analysis suggests that the size effect of small cap firms earning higher risk adjusted returns may be attributed to the long-run volatility component.

The difference of annualized risk premium between the high B/M firms and low B/M firms due to the risk of short-run volatility component is 0.50% per year, while the difference due to the long-run component is 0.33% per year. Hence, the short- and long-run volatility components have the same effect on the B/M firm portfolio. Combining the value spread due to market risk, the total effect that the high B/M firm portfolio earns 1.32% higher risk premium per year relative to low B/M firm portfolio. The analysis suggests that the B/M effect that high B/M firms earn higher returns may be explained by both the short- and long-run volatility components.

4.3. Robustness Tests⁴

In order to test the robustness of the results we find above, we proceed the following tests:

- 1) Estimate the models using three sub-periods of the whole sample periods.
- 2) The cross-sectional procedure is regressed on returns of different portfolios sorted by other criteria.
- 3) Different mean equations are specified to test the EGARCH component model.
- 4) We compare EGARCH component model with GARCH and GARCH component model by evaluate their

³For reasons of space, the results are available upon a request from the author.

⁴The test procedures and results are available upon a request.

Market risk premium								
	Small	Size 2	Size 3	Size 4	Big	Average		
Growth	0.392	0.421	0.4489	0.443	0.427	0.427		
B/M 2	0.332	0.380	0.423	0.417	0.435	0.398		
B/M 3	0.305	0.368	0.403	0.396	0.480	0.390		
B/M 4	0.327	0.357	0.404	0.480	0.431	0.400		
Value	0.313	0.378	0.403	0.462	0.429	0.397		
Average	0.334	0.381	0.416	0.439	0.441	0.402		
Short-run volatility risk premium								
	Small	Size 2	Size 3	Size 4	Big	Average		
Growth	-0.213	-0.102	-0.124	-0.072	-0.069	-0.106		
B/M 2	-0.247	-0.184	-0.059	0.042	-0.037	-0.092		
B/M 3	-0.139	-0.186	-0.109	0.079	-0.080	-0.056		
B/M 4	-0.152	0.045	0.011	-0.084	0.054	-0.039		
Value	-0.125	-0.050	0.022	-0.113	0.000	-0.065		
Average	-0.175	-0.096	-0.052	-0.029	-0.027	-0.076		
		Long	run volatility risk j	premium				
	Small	Size 2	Size 3	Size 4	Big	Average		
Growth	0.357	0.212	0.104	0.249	-0.035	0.177		
B/M 2	0.393	0.341	0.074	0.184	0.032	0.205		
B/M 3	0.339	0.286	0.105	0.225	0.045	0.200		
B/M 4	0.332	0.286	0.069	0.215	0.109	0.202		
Value	0.361	0.341	0.116	0.287	-0.079	0.205		
Average	0.357	0.293	0.094	0.232	0.014	0.198		

Table 4. Factor risk premia of the 25 size and B/M sorted portfolios.

This table reports the risk premia of portfolio returns on the market excess return, short-run volatility innovations and long-run volatility innovations. The risk premia are computed by multiplying factor loadings from Fama-Macbeth first-stage regression and prices of risk of **Table 3**, column V, second stage Fama-Mac Bethregression.

performance in the cross-sectional pricing.

The magnitudes of the prices of risk for the volatility components are fairly similar across different sets of assets and sample periods. The benchmark specification is superior to the alternatives with lowest root-mean-squared error.

5. Conclusions

ICAPM predicts that financial asset risk premia are not only due to covariation of returns with the market excess return, but also associated with innovations in the state variables that describe the investment opportunities. Multifactor models of risk already predict that aggregate volatility should be a cross-sectional risk factor. [11] further decompose the aggregate volatility into a transitory and a permanent component. They conclude that the short- and long-run volatility components have negative, highly significant prices of risk using American stock market data.

Applying decomposition of market risk to UK stock market, we find that the short- and long-run volatility components also have significantly negative prices of risk. The results are robust across sets of portfolios, sample periods and model specifications. The short- and long-run volatility might provide an explanation of the size and value anomaly of financial market. Specifically, the size effect of small cap firms earning higher risk ad-

justed returns may be attributed to the long-run volatility component. Whereas, the value effect that high B/M firms earn higher returns may be explained by both the short- and long-run volatility components. However, the performance of the decomposition model is superior to the Fama-French three factor model, and [9] market variance model. This might suggest further investigation and improvement on Adrian and Rosenberg's volatility decomposition model.

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