

Risk Evaluation of Dynamic Alliance Based on Fuzzy Analytic Network Process and Fuzzy TOPSIS

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ABSTRACT

Dynamic alliance formations have increased dramatically over the past decade for its adaptation to environmental change and market competition. However, many fail, while an even greater proportion perform poorly. The risk analysis of dynamic alliance will help enterprises to choose a coalition partner and make a reasonable benefit allocation plan. It's also good for reducing the risk and keeping the stability of the alliance. Based on the interaction and feedback relationships between criteria and/or indices, an index system for evaluating the risk of dynamic alliance is developed. With the information uncertainty and inaccuracy being considered, a new hybrid model based on fuzzy analytic network process (FANP) and fuzzy technique for order performance by similarity to ideal solution (TOPSIS) is proposed. The local weights of criteria and indices are obtained by fuzzy preference programming (FPP), and the comprehensive weights are derived by FANP. According to fuzzy TOPSIS, an optimal alternative is chosen by the closeness coefficient based on the shortest distance from the positive and the farthest distance from the negative ideal solutions. Finally, a numerical case is given by the proposed method.

Keywords: Fuzzy Analytic Network Process; TOPSIS; Dynamic Alliance; Risk Evaluation

1. Introduction

With the rapidly increasing competitiveness in global, enterprise cooperation is necessary in order to meet the market's requirements for quality, responsiveness, and customer satisfaction. As a result, dynamic alliance, defined as voluntary interfirm cooperative arrangements, has become a noteworthy trend in recent years. However, despite the growing numbers and increasing significance of dynamic alliance, many fail, while an even greater proportion perform poorly. Recent estimates put the failure rate of alliances between 60% and 70%, suggesting firms that pursue alliances are more likely than not to fail [1]. Although such failures may be for many interrelated reasons—and may be defined in various ways—two common causes are poor partner selection and poor alliance management [2]. Li and Liao [3] pointed out that despite many problems on dynamic alliance, such as partner selection, operation management, information exchanges and their standards, etc. have been investigated, and the risk management of dynamic alliance has not received deserved attention until now. This article focuses on risk evaluation, which is the most important phase of risk management for dynamic alliance.

Venkatesh *et al.* [4] investigated the dynamic aspects

of a co-marketing alliance and offered guidelines to establish profitable and self-sustaining alliances. They examined two questions. First, under what market-driven characteristics should either brand manufacturer forge or sustain the alliance. Second, what product market characteristics should the alliance promoter seek or alter to increase its payoffs from the alliance. Das and Teng [5] proposed a model of dynamic alliance that has managerial risk perception as its core. The model consists of the following parts: the antecedents of risk perception, relational risk and performance risk, risk perception and structural preference, and the resolution of preferences. Rosenkranz and Schmitz [6] explored the dynamic evolution of property rights regimes in R&D alliances using the incomplete contract approach, and characterized different scenarios in which the optimal ownership structure may change over time due to a trade-off between inducing know-how disclosure and ensuring maximum effort. Ip *et al.* [7] pointed out that minimizing risk in partner selection and ensuring the due date of a project were the key problems to overcome in dynamic alliance. They developed a risk-based partner selection method and a rule-based genetic algorithm with embedded project scheduling to solve the problem. Das and Kumar [8]

discussed three kinds of learning in alliances—namely, content, partner-specific, and alliance management—and the saliencies and implications of particular types of learning in different alliance stages. Huang *et al.* [9] proposed a fuzzy synthetic evaluation embedded nonlinear integer programming model of risk programming for dynamic alliance and presented a tabu search algorithm for the model. Delerue and Simon [10] pointed out that cross-cultural interactions were growing at an exponential pace. Consequently, it was becoming important to be aware of the existence and precise nature of cultural differences in risk perceptions. Huang *et al.* [11] introduced a Distributed Decision Making (DDM) model for the risk management of dynamic alliance. The model has two levels, which describe the decision processes of the owner and the partners of the dynamic alliance, respectively. It can be regarded as a combination of both the top-down and bottom-up approaches for risk management of the dynamic alliance. Lee *et al.* [12] demonstrated the locus of dynamic knowledge articulation and dynamic capabilities development by investigating drivers of dynamic learning in service alliance firms, etc.

However, the interaction and feedback relationships between criteria and/or indices are not completely considered in the existing research literatures. What's more, during the risk evaluation process of dynamic alliance, there are lots of uncertainty and fuzzy information, the crisp pairwise comparison seems to be insufficient and imprecise to capture the right judgments of decision-makers. Therefore, Zhou and Song proposed a FANP-based method to make up for the deficiency in the conventional risk assessment process [13].

The objective of this paper is to present a new hybrid model based on FANP and fuzzy TOPSIS for risk evaluation of dynamic alliance. According to FANP, the weights of criteria/indices are derived. The candidates can be ranked based on their relative closeness according to fuzzy TOPSIS. TOPSIS compromise solution is quite similar to what happens during the decision making process in risk evaluation: most of the time, the best solution is not reached since the criteria are not in agreement, some must be maximized and others minimized. Such an ANP/AHP-based TOPSIS driven by a set of weighting factors associated with the selected criteria has been proven effective for final ranking via an iterative procedure [14].

2. Preliminary Knowledge

2.1. Triangular Fuzzy Number

A fuzzy set is a class of objects with a continuum of grades of membership. Such a set is characterized by a membership function, which assigns to each object a grade of membership ranging between zero and one. A

triangular fuzzy number (TFN) is denoted simply as (l, m, u) . The parameters l , m and u , respectively, denote the smallest possible value, the most promising value, and the largest possible value that describe a fuzzy event. Each TFN has linear representations on its left and right side such that its membership function can be defined as

$$u_M(x) = \begin{cases} (x-l)/(m-l), & l \leq x \leq m, \\ (u-x)/(u-m), & m \leq x \leq u, \\ 0, & \text{otherwise.} \end{cases} \quad (1)$$

2.2. Fuzzy Analytic Network Process

The Analytic Network Process (ANP), introduced by Saaty [15], is a generalization of the Analytic Hierarchy Process (AHP). The basic assumption of the AHP is that the decision-making problem can be decomposed in a linear top-to-bottom form as a hierarchy, where the upper levels are functionally independent from all lower levels, and the elements in each level are also independent. However, many decision-making problems cannot be structured hierarchically, or there would have strong interactions and dependencies between criteria and/or indices. The resulting analytic network process provides a framework for dealing with decision-making problems within which assumptions about dependencies between criteria and alternatives are unnecessary.

AHP/ANP has been proposed as a suitable multi-criteria decision analysis tool [16,17]. However, the AHP/ANP-based decision model seems to be ineffective in dealing with the inherent fuzziness or uncertainty for judgment during the pairwise comparison process. Although the use of the discrete scale of 1 - 9 to represent the verbal judgment in pairwise comparisons has the advantage of simplicity, it does not take into account the uncertainty associated with the mapping of one's perception or judgment to a number. In real-life decision-making situation, the decision makers or stakeholders could be uncertain about their own level of preference, due to incomplete information or knowledge, complexity and uncertainty within the decision environment. Such conditions will occur when evaluating the risk of dynamic alliance. Therefore, it's more appropriate to make risk management plan under fuzzy condition.

A number of methods have been developed to handle fuzzy comparison matrices. For example, Laarhoven and Pedrycz [18] suggested a fuzzy logarithmic least squares method (LLSM) to obtain triangular fuzzy weights from a triangular fuzzy comparison matrix. Buckley [19] utilized the geometric mean method to calculate fuzzy weights. Chang [20] proposed an extent analysis method, which derives crisp weights for fuzzy comparison matrices. Xu [21] brought forward a fuzzy least squares priority method (LSM). Csutora and Buckley [22] came up

with a Lambda-Max method, which is the direct fuzzification of the well-known k_{max} method. Mikhailov [23] developed a fuzzy preference programming method, which also derives crisp weights from fuzzy comparison matrices. Srdjevic [24] proposed a multi-criteria approach for combining prioritization methods within the AHP, including additive normalization, eigenvector, weighted least-squares, logarithmic least-squares, logarithmic goal programming and fuzzy preference programming. Wang *et al.* [25] presented a modified fuzzy logarithmic least square method. Yu and Cheng [26] developed a multiple objective programming approach for the ANP to obtain all local priorities for crisp or interval judgments at one time. Huo *et al.* [27] proposed new parametric prioritization methods (PPMs) to determine a family of priority vectors in AHP, etc.

2.3. Fuzzy Preference Programming Method

FPP method, as a reasonable and effective means, is adopted in this study. This method can acquire the consistency ratios of fuzzy pairwise comparison matrices without conducting an additional study, and the local weights can be easily solved with the help of a Matlab program. The stages of Mikhailov’s fuzzy prioritization approach are as follows [23].

Consider a prioritization problem with n elements, where the pairwise comparison judgments are represented by normal fuzzy sets or fuzzy numbers. Suppose the decision-maker can provide a set $F = \{\tilde{a}_{ij}\}$ of $m \leq n(n-1)/2$ fuzzy comparison judgments, $i = 1, 2, \dots, n-1; j = 2, 3, \dots, n; j > i$, represented as triangular fuzzy numbers $\tilde{a}_{ij} = (l_{ij}, m_{ij}, u_{ij})$. The problem is to derive a crisp priority vector $w = (w_1, w_2, \dots, w_n)^T$, such that the priority ratios w_i/w_j are approximately within the scopes of the initial fuzzy judgments, or

$$l_{ij} \lesssim \frac{w_i}{w_j} \lesssim u_{ij}, \tag{2}$$

where the symbol “ \lesssim ” denotes the statement “fuzzy less or equal to”.

Each crisp priority vector w satisfies the double-side inequality (2) with some degree, which can be measured by a membership function, linear with respect to the unknown ratio w_i/w_j ,

$$u_{ij} \left(\frac{w_i}{w_j} \right) = \begin{cases} \frac{(w_i/w_j) - l_{ij}}{m_{ij} - l_{ij}}, & \frac{w_i}{w_j} \leq m_{ij}, \\ \frac{u_{ij} - (w_i/w_j)}{u_{ij} - m_{ij}}, & \frac{w_i}{w_j} \geq m_{ij}. \end{cases} \tag{3}$$

Taking into consideration the specific form of the membership functions (3), the prioritization problem can be further transformed into a bilinear program of the type

$$\begin{aligned} &\max \lambda \\ &(m_{ij} - l_{ij})\lambda w_j - w_i + l_{ij}w_j \leq 0, \\ &(u_{ij} - m_{ij})\lambda w_j + w_i - u_{ij}w_j \leq 0, \\ &\sum_{k=1}^n w_k = 1, w_k > 0, k = 1, 2, \dots, n. \\ &i = 1, 2, \dots, n-1; j = 2, 3, \dots, n; j > i. \end{aligned} \tag{4}$$

The optimal solution to the non-linear problem (w^*, λ^*) might be obtained by employing some appropriate numerical method for non-linear optimization. The optimal value λ^* , if it is positive, indicates that all solution ratios completely satisfy the fuzzy judgment, which means that the initial set of fuzzy judgments is rather consistent. A negative value of λ^* shows that the solutions ratios approximately satisfy all double-side inequalities (2). Therefore, the optimal value λ^* can be used for measuring the consistency of the initial set of fuzzy judgments.

3. Proposed Risk Evaluation of Dynamic Alliance Framework

This study proposes a novel hybrid analytic approach based on the FANP and fuzzy TOPSIS methodologies to assist in risk evaluation of dynamic alliance. We first identify the evaluation criteria, and present the evaluation model in the following subsections.

3.1. Index system of Risk Evaluation

With the risk sources of dynamic alliance being considered, an index system of risk evaluation for dynamic alliance is presented. The index system is made up of five parts: technique risk, market risk, cooperation risk, risk of natural environmental and risk of social environmental, as shown in **Figure 1**.

Technique risk and cooperation risk belong to inner risk. On the contrary, market risk, risk of natural environment and social environment belong to outer risk. Technique risk is caused by the technique of partners, including complication of technique, maturity of technique and relationships of technique. Cooperation risk is due to the differences in management, communication and partner’s business reputation in an alliance. Market risk is caused by the situation of market competition, new product development or the appearance of substitute and environmental change of target market. The risk of natural environment is due to the earthquakes, droughts, and other natural risk, including frequency of disasters, disaster losses per year and harm degree of single disaster. The risk of social environment is caused by war, policy and legal system, and so on, including domestic political environment, foreign political environment, policy and legal system and capacity of solving emergency.

In **Figure 1**, the interaction and feedback relationships

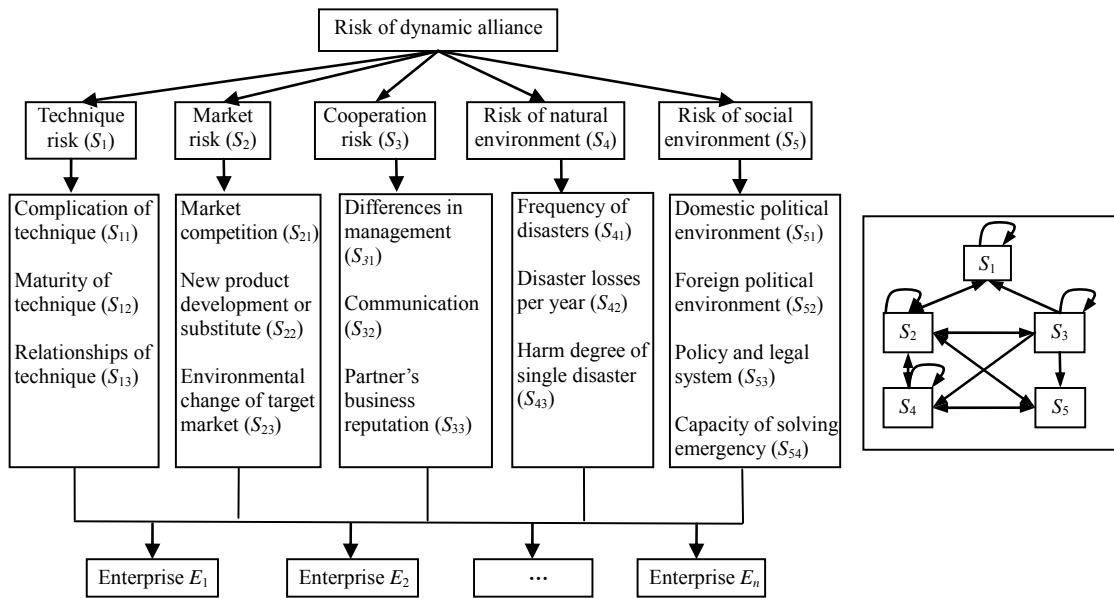


Figure 1. Index system of risk evaluation of dynamic alliance.

between criteria and/or indices are being considered. Generally, if market risk (S_2) has an effect on technique risk (S_1), then a line with arrow from S_1 to S_2 is added. If the sub-criteria of market risk (S_2) have interaction itself, then S_2 is inner dependence, and an arc with arrow is added to S_2 .

3.2. Fuzzy Linguistic Variables

During the process of risk evaluation, experts tend to specify their preferences in the form of natural language expressions. The fuzzy linguistic variables are variables reflect different aspects of human language. Their values represent the range from natural to artificial language.

When the values of a linguistic factor are being reflected, the resulting variable must also reflect appropriate modes of change. Moreover, variables describing a human word or sentence can be divided into numerous linguistic criteria, such as equally important, moderately important, important, very important and absolutely important. For the purposes of the present study, two 9-point scales are proposed for relative importance of pairwise comparison and rating the candidates, as shown in **Tables 1** and **2**.

3.3. FANP-Based Approach

The weights of criteria and sub-criteria are obtained based on FANP. The FANP-based approach is proposed step-by-step as follows.

Step 1. Build a network structure and list the interaction and feedback relationships among the components, as shown in **Figure 1**. A four-level evaluation index system is presented: the first level is the comprehensive risk

Table 1. Linguistic scales for relative importance of pairwise comparison.

Linguistic scales for importance	Triangular fuzzy numbers	Triangular fuzzy reciprocal numbers
Equally important (EI)	(1, 1, 1)	(1, 1, 1)
Intermediate 1 (IM ₁)	(1, 2, 3)	(1/3, 1/2, 1)
Moderately important (MI)	(2, 3, 4)	(1/4, 1/3, 1/2)
Intermediate 2 (IM ₂)	(3, 4, 5)	(1/5, 1/4, 1/3)
Important (I)	(4, 5, 6)	(1/6, 1/5, 1/4)
Intermediate 3 (IM ₃)	(5, 6, 7)	(1/7, 1/6, 1/5)
Very important (VI)	(6, 7, 8)	(1/8, 1/7, 1/6)
Intermediate 4 (IM ₄)	(7, 8, 9)	(1/9, 1/8, 1/7)
Absolutely important (AI)	(9, 9, 9)	(1/9, 1/9, 1/9)

Table 2. Linguistic scales for rating the candidates.

Linguistic scales for positive sub-factors	Triangular fuzzy numbers
Absolutely high (AH)	(0.8, 0.9, 1)
Very high (VH)	(0.7, 0.8, 0.9)
High (H)	(0.6, 0.7, 0.8)
Medium high (MH)	(0.5, 0.6, 0.7)
Fair (F)	(0.4, 0.5, 0.6)
Medium low (ML)	(0.3, 0.4, 0.5)
Low (L)	(0.2, 0.3, 0.4)
Very low (VL)	(0.1, 0.2, 0.3)
Absolutely low (AL)	(0, 0.1, 0.2)

of dynamic alliance; the second level is criteria, including technique risk, market risk, cooperation risk, risk of natural environment and risk of social environment; the third level is sub-criteria, including 16 indicators; the lowest one is candidates.

Step 2. Establish pairwise comparison matrices by the decision committee using the linguistic scales given in **Table 1**. The decision makers are asked to respond to a series of pairwise comparison with respect to the dimensions/attributes-enablers levels in **Figure 1**. For example, the market competition (S_{21}) and the new product development or substitute (S_{22}) are compared using the question “How important is the market competition when it is compared with the new product development or substitute at the dimension of market risk?” and the answer is “intermediate important (IM_1)”, so this linguistic scale is placed in the relevant cell against the triangular fuzzy numbers (1, 2, 3). All the fuzzy evaluation matrices are produced in the same way.

Step 3. Calculate the local weights and consistency ratios. According to formulation (4), local weights and consistency ratios of the criteria and sub-criteria are calculated by FPP method with the help of Matlab.

Step 4. Construct an unweighted supermatrix on the basis of the interdependencies in the network. The supermatrix is a partitioned matrix, where each submatrix is composed of a set of relationships between criteria and indices. Three types of relationships may be encountered in this model: independence from succeeding components, interdependence among components and interdependence between levels of components.

Step 5. Derive a weighted supermatrix. Because in each column it consists of several eigenvectors each of them sums to one and hence the entire column of the matrix may sum to an integer greater than one, the unweighted supermatrix needs to be stochastic to derive the weighted supermatrix.

Step 6. Generate a limit supermatrix by raising the weighted supermatrix to powers until it converges.

$$\bar{W} = \lim_{t \rightarrow \infty} W^t. \tag{5}$$

Step 7. Obtain the global weight. A global weight of each index can be computed by multiplying the local weight of the criterion level indicator, the weight of independent sub-criterion and the weight of interdependent sub-criterion.

$$w_{ij} = P_i * A_{ij}^D * A_{ij}^I, \tag{6}$$

where w_{ij} is the comprehensive weight, P_i is relative importance weight of dimension i on final goal; A_{ij}^D , relative importance weight for attribute-enabler j of dimension i , and for the dependency (D) relationships within attribute-enabler's component level; A_{ij}^I , stabilized relative importance weight for attribute-enabler j of dimen-

sion i , and for the independency (I) relationships within attribute-enabler's component level.

3.4. Fuzzy TOPSIS Approach

TOPSIS method is a classical approach to multi-attribute or multi-criteria decision making problems, which was first proposed by Hwang and Yoon [28] and expanded by Chen and his cooperators [29]. It is a practical and useful technique for ranking and selection of a number of externally determined alternatives through distance measures. The foundational principle is that the chosen alternative should have the shortest distance from the positive ideal solution and the farthest distance from the negative ideal solution.

In the traditional TOPSIS, the performance ratings and the weights of the criteria are given as crisp values. Under many conditions, crisp values are inadequate to model real world situations because human judgment and preference are often ambiguous and cannot be estimated with exact numerical values. To resolve the ambiguity frequently existing in the process of judgment and evaluation, fuzzy sets were applied to establish a prototype fuzzy TOPSIS [30,31].

According to fuzzy TOPSIS, the candidates can be ranked based on their relative closeness. The process is proposed step-by-step as follows.

Step 8. Evaluate the ratings of candidates by the decision committee using the linguistic variables given in **Table 2**. Assume that a decision group has K persons, and then the ratings of candidates with respect to each criterion can be calculated as

$$x_{ij} = \frac{1}{k} [x_{ij}^1 + x_{ij}^2 + \dots + x_{ij}^k], \tag{7}$$

where x_{ij}^k is the rating of the k th decision maker, and x_{ij} can be described by triangular fuzzy numbers, such as $x_{ij} = (a_{ij}, b_{ij}, c_{ij})$.

Step 9. Construct a fuzzy decision matrix by converting the linguistic scales into triangular fuzzy numbers according to **Table 2**.

Step 10. Normalize the fuzzy decision matrix. As there are benefit criteria and cost criteria, the fuzzy decision matrices need to be normalized. Given a TFN

$\tilde{x} = (a_{ij}, b_{ij}, c_{ij})$, in reference to the fuzzy TOPSIS method developed by Chen [28], the normalized performance rating can be calculated by

$$\tilde{r}_{ij} = \left(\frac{a_{ij}}{c_j^+}, \frac{b_{ij}}{c_j^+}, \frac{c_{ij}}{c_j^+} \right), i = 1, 2, \dots, n, j \in W_B, \tag{8}$$

and

$$\tilde{r}_{ij} = \left(\frac{a_j^-}{c_{ij}}, \frac{a_j^-}{b_{ij}}, \frac{a_j^-}{a_{ij}} \right), i = 1, 2, \dots, n, j \in W_C, \tag{9}$$

where

$$c_j^+ = \max c_{ij}, j \in \Omega_b,$$

$$a_j^- = \min a_{ij}, j \in \Omega_c,$$

with B being the benefit criteria set (the larger \tilde{r}_{ij} , the greater preference), and C being the cost criteria set (the smaller \tilde{r}_{ij} , the greater preference).

Hence, the normalized matrix $\tilde{R} = [\tilde{r}_{ij}]_{n \times m}$ can be obtained.

Step 11. Obtain the deal and negative ideal solutions. The ideal solutions can be defined as:

$$A^+ = (1, 1, 1), j \in W_b; A^- = (0, 0, 0), j \in W_c.$$

Step 12. Determine the distances between each candidate and the positive or negative ideal candidate.

By considering the different importance of each criterion obtained from FANP method, the weighted distance can be calculated as:

$$d^-(\tilde{N}, \tilde{M}) = w_{ij} \sqrt{\frac{1}{3} \sum_{i=1}^3 \left[(N_{x_i}^-, M_{y_i}^-)^2 \right]}, \quad (10)$$

$$D^+(\tilde{N}, \tilde{M}) = w_{ij} \sqrt{\frac{1}{3} \sum_{i=1}^3 \left[(N_{x_i}^+, M_{y_i}^+)^2 \right]}, \quad (11)$$

where $D^-(\tilde{N}, \tilde{M})$ and $D^+(\tilde{N}, \tilde{M})$ are the primary and secondary distant measure, respectively. The distance of each candidate from the ideal alternative can be thereby calculated by

$$d_i^+ = \sum_{j=1}^m w_{ij} \sqrt{\frac{1}{3} \left[(g_{ij} - 1)^2 + (h_{ij} - 1)^2 + (l'_{ij} - 1)^2 \right]}. \quad (12)$$

Similarly, the separation from the negative ideal solution is given by

$$d_i^- = \sum_{j=1}^m w_{ij} \sqrt{\frac{1}{3} \left[(g_{ij} - 0)^2 + (h_{ij} - 0)^2 + (l'_{ij} - 0)^2 \right]}. \quad (13)$$

Step 13. Calculate the relative closeness RC_i^* .

$$RC_i^* = \frac{d_i^-}{d_i^+ + d_i^-}. \quad (14)$$

According to the values of RC_i^* , the candidates can be ranked.

4. Case Study

Suppose four spinning mills will form a dynamic alliance through pre-test. The four candidates are recorded as E_1, E_2, E_3 and E_4 . In order to make a reasonable benefit allocation plan and attain a stability of the alliance, a cross-functional decision committee consisting of various departments works to evaluate the risk of the four enterprises, named as D_1, D_2 and D_3 . The results will assist in

making benefit allocation plan and risk management as well. The risk evaluating process based on FANP and fuzzy TOPSIS is as follows.

Step 1. With the interaction and feedback relationships between dimensions and/or attribute-enablers being considered, a four-level evaluation index system is presented, as shown in **Figure 1**.

Step 2. Pairwise comparison matrices among dimensions and/or attributes are formed by the decision committee using the linguistic scales given in **Table 1**. For example, **Table 3** is the pairwise comparison matrix for market competition (S_{21}), new product development or substitute (S_{22}) and environmental change of target market (S_{23}) at the dimension of market risk.

Expert opinions will be converted into the corresponding triangular fuzzy numbers, as shown in **Table 4**. All the fuzzy evaluation matrices are produced in the same manner.

Step 3. Local weights of the factors and sub-factors which take part in the second and third levels of the ANP model, provided in **Figure 1**, are calculated by FPP method. For instance, according to equation (4), the local weights of **Table 4** can be obtained by solving the following non-linear programming.

$$\begin{aligned} & \max \lambda \\ & \lambda w_2 - w_1 + w_2 \leq 0; \\ & \lambda w_2 + w_1 - 3w_2 \leq 0; \\ & \lambda w_3 - w_1 + w_3 \leq 0; \\ & \lambda w_3 + w_1 - 3w_3 \leq 0; \\ & \lambda w_3 - w_2 + w_3 \leq 0; \\ & \lambda w_3 + w_2 - 3w_3 \leq 0; \\ & w_1 + w_2 + w_3 = 1; \\ & w_1, w_2, w_3 \geq 0. \end{aligned}$$

Table 3. The comparison matrix at the dimension of market risk using linguistic variables.

S_2	S_{21}	S_{22}	S_{23}
S_{21}	EI	IM ₁	IM ₁
S_{22}		EI	IM ₁
S_{23}			EI

Table 4. The comparison matrix at the dimension of market risk using TFNs.

S_2	S_{21}	S_{22}	S_{23}	w
S_{21}	(1, 1, 1)	(1, 2, 3)	(1, 2, 3)	0.4877
S_{22}		(1, 1, 1)	(1, 2, 3)	0.3123
S_{23}			(1, 1, 1)	0.2000
$CR = 0.5616$				

It can be solved by Matlab, and the optimal solutions are $w_1 = 0.4877$, $w_2 = 0.3123$, $w_3 = 0.2000$, as shown in **Table 4**. Consistency index CR is 0.5616, which shows that the experts' opinions have a good consistency, and the local weights are acceptable. All the local weights of comparison matrices are calculated in the same way.

Step 4. According to the interdependencies among dimensions and attribute-enablers of the ANP model, an unweighted supermatrix is built, as shown in **Table 5**.

Step 5. The unweighted supermatrix is being randomized to derive the weighted supermatrix.

Step 6. According to Equation (5), multiplying the weighted supermatrix by itself until the supermatrix's row values converge to the same value for each column of the matrix, then we choose any column from the steady limit supermatrix as the local weights of the interdependency indicators, as shown in **Table 6**.

Step 7. According to Equation (6), the comprehensive weight w_{ij} of each index can be calculated, as shown in **Table 7**, and w'_{ij} is the normalized weight of w_{ij} .

Step 8. The ratings of the enterprises with respect to each indicator are determined by **Table 2**.

Step 9. To construct fuzzy decision matrix, the linguistic scales are converted into triangular fuzzy numbers. According to the formulation (7), the ratings of the candidates with respect to each criterion can be calculated

Step 10. According to Equations (8) and (9), the normalized fuzzy decision matrix can be acquired, as shown

in **Table 8**.

Step 11. Positive and negative ideal solutions are defined as

$$A^+ = (1, 1, 1), j \in W_b; A^- = (0, 0, 0), j \in W_c.$$

Step 12. According to Equations (12) and (13), the weighted distances of each candidate from FPIS and FNIS can be calculated, as shown in **Table 9**.

Step 13. According to Equation (14), the relative closeness of the four enterprises can be calculated by $RC_1 = 0.8199$, $RC_2 = 0.8221$, $RC_3 = 0.830$ and $RC_4 = 0.7861$, as shown in **Table 9**. Therefore, the risk profile of the four enterprises can be ranked as $E_3 > E_2 > E_1 > E_4$, and enterprise E_3 is the best one.

The same ranking of the alternatives is drawn as reference [13], but this time the weights are obtained by FANP, and the ranking is determined by the closeness coefficient based on the distances to the positive and negative ideal solutions. It provides a new approach for evaluating the risk of dynamic alliance. As mentioned before, it is more adaptive to the final ranking of the alternatives as well.

5. Conclusion

With the interaction and feedback relationships between criteria and/or indicators being considered, an index system for evaluating the risk of dynamic alliance is

Table 5. The unweighted supermatrix.

	S_{11}	S_{12}	S_{13}	S_{21}	S_{22}	S_{23}	S_{31}	S_{32}	S_{33}	S_{41}	S_{42}	S_{43}	S_{51}	S_{52}	S_{53}	S_{54}
S_{11}	0.0000	0.6667	0.7500	0.5375	0.3070	0.2500	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
S_{12}	0.3333	0.0000	0.2500	0.1700	0.1677	0.5000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
S_{13}	0.6667	0.3333	0.0000	0.2925	0.5253	0.2500	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
S_{21}	0.3063	0.3063	0.2500	0.0000	0.8000	0.6667	0.5714	0.4000	0.2000	0.2500	0.2500	0.4000	0.5714	0.5714	0.4000	0.1704
S_{22}	0.5270	0.5270	0.5000	0.6667	0.0000	0.3333	0.2857	0.2000	0.4000	0.2500	0.2500	0.2000	0.2857	0.2857	0.2000	0.3003
S_{23}	0.1667	0.1667	0.2500	0.3333	0.2000	0.0000	0.1429	0.4000	0.4000	0.5000	0.5000	0.4000	0.1429	0.1429	0.4000	0.5292
S_{31}	0.5714	0.5000	0.4286	0.5375	0.2500	0.2857	0.0000	0.6667	0.8000	0.2000	0.4000	0.4000	0.5375	0.5375	0.2500	0.1711
S_{32}	0.1429	0.2500	0.1429	0.1700	0.2500	0.1429	0.3333	0.0000	0.2000	0.4000	0.2000	0.2000	0.1700	0.1700	0.2500	0.5361
S_{33}	0.2857	0.2500	0.4286	0.2925	0.5000	0.5714	0.6667	0.3333	0.0000	0.4000	0.4000	0.4000	0.2925	0.2925	0.5000	0.2928
S_{41}	0.0000	0.0000	0.0000	0.5746	0.4000	0.5000	0.0000	0.0000	0.0000	0.0000	0.8333	0.6667	0.2857	0.2857	0.2500	0.5746
S_{42}	0.0000	0.0000	0.0000	0.3143	0.2000	0.2500	0.0000	0.0000	0.0000	0.7500	0.0000	0.3333	0.5714	0.5714	0.5000	0.3143
S_{43}	0.0000	0.0000	0.0000	0.1111	0.4000	0.2500	0.0000	0.0000	0.0000	0.2500	0.1667	0.0000	0.1429	0.1429	0.2500	0.1111
S_{51}	0.0000	0.0000	0.0000	0.2672	0.2222	0.4159	0.0000	0.0000	0.0000	0.2222	0.4159	0.2672	0.0000	0.0000	0.0000	0.0000
S_{52}	0.0000	0.0000	0.0000	0.1399	0.1111	0.1315	0.0000	0.0000	0.0000	0.1111	0.1315	0.1399	0.0000	0.0000	0.0000	0.0000
S_{53}	0.0000	0.0000	0.0000	0.5115	0.2222	0.2263	0.0000	0.0000	0.0000	0.2222	0.2263	0.5115	0.0000	0.0000	0.0000	0.0000
S_{54}	0.0000	0.0000	0.0000	0.0814	0.4444	0.2263	0.0000	0.0000	0.0000	0.4444	0.2263	0.0814	0.0000	0.0000	0.0000	0.0000

Table 6. The limit supermatrix.

	S_{11}	S_{12}	S_{13}	S_{21}	S_{22}	S_{23}	S_{31}	S_{32}	S_{33}	S_{41}	S_{42}	S_{43}	S_{51}	S_{52}	S_{53}	S_{54}
S_{11}	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397	0.0397
S_{12}	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249	0.0249
S_{13}	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354	0.0354
S_{21}	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289	0.1289
S_{22}	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091	0.1091
S_{23}	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953	0.0953
S_{31}	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372	0.1372
S_{32}	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727	0.0727
S_{33}	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234	0.1234
S_{41}	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059	0.059
S_{42}	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467	0.0467
S_{43}	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276	0.0276
S_{51}	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296	0.0296
S_{52}	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127	0.0127
S_{53}	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318	0.0318
S_{54}	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259	0.0259

Table 7. Comprehensive weights of the indicators.

Index	P_i	A_j^p	A_j^t	w_{ij}	w_{ij}'
S_{11}	0.2105	0.5375	0.0397	0.0045	0.0512
S_{12}	0.2105	0.1700	0.0249	0.0009	0.0101
S_{13}	0.2105	0.2925	0.0354	0.0022	0.0248
S_{21}	0.4211	0.4877	0.1289	0.0265	0.3015
S_{22}	0.4211	0.3123	0.1091	0.0143	0.1634
S_{23}	0.4211	0.2000	0.0953	0.008	0.0914
S_{31}	0.2105	0.5375	0.1372	0.0155	0.1768
S_{32}	0.2105	0.1700	0.0727	0.0026	0.0296
S_{33}	0.2105	0.2925	0.1234	0.0076	0.0865
S_{41}	0.0526	0.5746	0.059	0.0018	0.0203
S_{42}	0.0526	0.3143	0.0467	0.0008	0.0088
S_{43}	0.0526	0.1111	0.0276	0.0002	0.0018
S_{51}	0.1053	0.2672	0.0296	0.0008	0.0095
S_{52}	0.1053	0.1399	0.0127	0.0002	0.0021
S_{53}	0.1053	0.5115	0.0318	0.0017	0.0195
S_{54}	0.1053	0.0814	0.0259	0.0002	0.0025

Table 8. The fuzzy normalized decision matrix.

	E_1			E_2			E_3			E_4			w'_j
	D_1	D_2	D_3	D_1	D_2	D_3	D_1	D_2	D_3	D_1	D_2	D_3	
S_{11}	0.6785	0.7856	0.8928	0.7149	0.8221	0.9293	0.6785	0.7856	0.8928	0.7856	0.8928	1.0000	0.0512
S_{12}	0.7033	0.8144	0.9256	0.7778	0.8889	1.0000	0.7411	0.8522	0.9633	0.6667	0.7778	0.8889	0.0101
S_{13}	0.6898	0.7932	0.8966	0.7932	0.8966	1.0000	0.6546	0.7580	0.8614	0.7239	0.8273	0.9307	0.0248
S_{21}	0.7239	0.8273	0.9307	0.7580	0.8614	0.9648	0.7932	0.8966	1.0000	0.6546	0.7580	0.8614	0.3015
S_{22}	0.7778	0.8889	1.0000	0.7411	0.8522	0.9633	0.7411	0.8522	0.9633	0.7033	0.8144	0.9256	0.1634
S_{23}	0.7203	0.8403	0.9604	0.7599	0.8800	1.0000	0.7599	0.8800	1.0000	0.6807	0.8007	0.9208	0.0914
S_{31}	0.7778	0.8889	1.0000	0.6667	0.7778	0.8889	0.7033	0.8144	0.9256	0.6667	0.7778	0.8889	0.1768
S_{32}	0.7239	0.8273	0.9307	0.7932	0.8966	1.0000	0.6546	0.7580	0.8614	0.7580	0.8614	0.9648	0.0296
S_{33}	0.6898	0.7932	0.8966	0.7580	0.8614	0.9648	0.7932	0.8966	1.0000	0.7239	0.8273	0.9307	0.0865
S_{41}	0.6898	0.7932	0.8966	0.6546	0.7580	0.8614	0.5512	0.6546	0.7580	0.7932	0.8966	1.0000	0.0203
S_{42}	0.5359	0.6431	0.7503	0.7503	0.8574	0.9646	0.6431	0.7503	0.8574	0.7856	0.8928	1.0000	0.0088
S_{43}	0.4802	0.6002	0.7203	0.6807	0.8007	0.9208	0.6002	0.7203	0.8403	0.7599	0.8800	1.0000	0.0018
S_{51}	0.7147	0.8218	0.9290	0.5711	0.6782	0.7854	0.7854	0.8925	0.9997	0.7147	0.8218	0.9290	0.0095
S_{52}	0.7932	0.8966	1.0000	0.6205	0.7239	0.8273	0.6898	0.7932	0.8966	0.6205	0.7239	0.8273	0.0021
S_{53}	0.6330	0.7330	0.8330	0.6670	0.7670	0.8670	0.7000	0.8000	0.9000	0.8000	0.9000	1.0000	0.0195
S_{54}	0.6205	0.7239	0.8273	0.7239	0.8273	0.9307	0.6898	0.7932	0.8966	0.7932	0.8966	1.0000	0.0025

Table 9. Distances to FPIS and FNIS.

	E_1		E_2		E_3		E_4	
	VPIS	VNIS	VPIS	VNIS	VPIS	VNIS	VPIS	VNIS
S_{11}	0.0119	0.0405	0.0102	0.0423	0.0119	0.0405	0.0071	0.0459
S_{12}	0.0021	0.0083	0.0014	0.0090	0.0018	0.0087	0.0024	0.0079
S_{13}	0.0055	0.0198	0.0033	0.0223	0.0064	0.0189	0.0048	0.0206
S_{21}	0.0580	0.2507	0.0489	0.2610	0.0403	0.2715	0.0773	0.2300
S_{22}	0.0234	0.1460	0.0283	0.1400	0.0283	0.1400	0.0337	0.1339
S_{23}	0.0171	0.0773	0.0142	0.0809	0.0142	0.0809	0.0203	0.0737
S_{31}	0.0254	0.1580	0.0424	0.1384	0.0365	0.1449	0.0424	0.1384
S_{32}	0.0057	0.0246	0.0040	0.0267	0.0076	0.0226	0.0048	0.0256
S_{33}	0.0193	0.0690	0.0140	0.0749	0.0115	0.0779	0.0166	0.0719
S_{41}	0.0045	0.0162	0.0052	0.0155	0.0072	0.0134	0.0027	0.0183
S_{42}	0.0032	0.0057	0.0015	0.0076	0.0023	0.0066	0.0012	0.0079
S_{43}	0.0007	0.0011	0.0004	0.0015	0.0005	0.0013	0.0003	0.0016
S_{51}	0.0019	0.0079	0.0032	0.0065	0.0013	0.0085	0.0019	0.0079
S_{52}	0.0003	0.0019	0.0006	0.0015	0.0005	0.0017	0.0006	0.0015
S_{53}	0.0054	0.0144	0.0048	0.0150	0.0042	0.0157	0.0025	0.0176
S_{54}	0.0007	0.0018	0.0005	0.0021	0.0006	0.0020	0.0003	0.0023
$\sum S_{ij}$	0.1852	0.8431	0.1829	0.8453	0.1750	0.8551	0.2190	0.8051
RC_i	0.8199		0.8221		0.8301		0.7861	

presented. With the uncertainty and the inaccuracy information during the evaluation process being considered, a model combining FANP and fuzzy TOPSIS is proposed. The local weights of criteria and indices are calculated by FPP, and the global weights are determined by FANP method. The distances between the candidates and positive ideal solutions or negative ones can be calculated by fuzzy TOPSIS. The rank of the candidates is derived by their relative closeness. A numerical case is given by the proposed method. The risk analysis of dynamic alliance will help enterprises to choose a coalition partner and make a reasonable benefit allocation plan, and it is advantageous in acquiring the stability of the union as well.

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