

Numerical Investigation of a UCN Source Based on Solid Deuterium by Combining a Simulation Code with an Analytical Approach

Habib Mohammadi¹, Mohammad Mehdi Firoozabadi¹, Rouhollah Gheisari²

¹Department of Physics, University of Birjand, Birjand, Iran ²Physics Department, Persian Gulf University, Bushehr, Iran Email: mohammadi@birjand.ac.ir

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Abstract

At thermal ultra-cold neutron (UCN) sources (neutrons in thermal equilibrium with the moderator) only a very small fraction of neutrons have velocities ~6 m/s. Therefore, the UCN production rate cannot be substantially increased by simply lowering the temperature of the moderator. The new approach is to use the super-thermal principle, *i.e.*, neutrons not in thermal equilibrium with the converter. We want to investigate scattering kernels for a super-thermal UCN source based on a two-layer arrangement of D_2O and solid D_2 . The solid D_2 (s D_2) at temperature 8 K is kept in close contact with D_2O moderator at room temperature. Using the MCNP code, the fast neutron flux on the spallation target, the thermal flux in the D_2O near the s D_2 , and the cold flux in the s D_2 are simulated. For a given cold flux, neutron transport equations are calculated. In order to obtain precise neutron scattering kernels, and consequently UCN flux and density, 330 neutron energy groups have been taken. The coupled energy dependent transport equations have been solved by combining MCNPX code with an analytical approach and using implicit method in MATLAB. We have obtained an optimal dimension for the UCN source. A suitable space step has been taken for the numerical stability.

Keywords

Two-Layer UCN Source Based on D₂O/sD₂, Scattering Kernel, Monte Carlo Method, Implicit Method, Super-Thermal Principle

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1. Introduction

Ultra-cold neutron (UCN) can be used in fundamental physics experiments, such as neutron electric dipole moment and life-time measurements, which require low velocities and long interaction and observation times [1] [2]. The accuracy of such measurements is limited mainly by statistics [3], and significantly higher UCN densities will allow more tests of the standard model. Several projects have the goal to build new UCN sources in order to provide the required increase in UCN density and flux. Two main source types having the potential to produce substantially higher UCN densities, are based on using either super-fluid helium [4]-[7] or solid deuterium (sD₂) to down scatter cold neutrons [8] [9]. Basic research to produce experimental UCN converters was done by using D₂, O₂, and CD₄ [10] [11]. These converters reduce the speed of the cold neutron (CN) to that of UCN. The research works have shown that deuterium can be used in different states of gas, liquid, and solid. The sD₂ has more applicants [12] [13]. In UCN sources, CN neutrons have a mean energy of ~meV. Considerable fractions of these neutrons slow down to ~neV. We have the goal to study UCN density and flux of a UCN source based on a two-layer arrangement of D₂O and sD₂ by combining MCNPX2.4.0 code with an analytical approach. In Section 2, mathematical tools are presented. The CN flux in the sD₂ is simulated with MCNPX code. This result for the CN flux is then used as boundary condition to calculate the UCN flux and density. The results and discussion are presented in Section 3. Finally, the summary and conclusions are given in Section 4.

2. Material and Methods

A scheme of the UCN source under consideration is shown in **Figure 1**. Fast neutrons are produced by a proton beam hitting spallation target. In the heavy water (D₂O) moderator at room temperature, the mean kinetic energy of fast neutrons (spallation neutrons) is reduced, and consequently thermal neutrons are produced. Some of the thermal neutrons are cooled and eventually converted to UCN (inside the sD₂). In **Table 1**, the proton beam and spallation target parameters have been given as well as UCN source geometry factors, and materials. The sD₂ must be almost pure, to reduce up-scattering on para-D₂. Here the sD₂ layer, with a number density of $N_0 = 3 \times 10^{22}$ cm⁻³ and a high ortho-concentration ($c_0 = 98.5\%$), is considered at temperature of T = 8 K to prevent the dispersion of each UCN. Using the MCNPX code, the fast neutron flux on the target, the thermal



Figure 1. (a) Schematic drawing of a UCN two-layer arrangement of D_2O/sD_2 . The incoming fast neutrons (spallation neutrons) are thermalized in the D_2O moderator. The thermal neutrons are being transported throughout the sD_2 layer, until large fractions of these neutrons are cooled at d = 4 cm. The cold neutrons (CN) are converted to UCN everywhere in the sD_2 . *x* denotes one-dimensional position; (b) Geometric description of the UCN setup used in the MC calculations.

Spallation target composition	Percent (%)	Temperature (K)	Density (g/cm ³)	Diameter (cm)	Length (cm)	Neutron source power, $S_n (n/s)$		
Pb	47.8		11.3					
Zr	16.7	300	6.57	17	25	4.59×10^{16}		
D_2O	35.5		1.1					
Moderator	Volume (liters)	Temperature (K)	Density (g/cm ³)	Diameter (cm)	Length (cm)	Shield material ^b Thickness shield (cm)		
sD_2	≈10 ^a	8	0.199	50	≈5ª	Zr + Steel	Side wall ^c 0.35	Surface area 0.05
D_2O	3570	300	1.1	160	190	Al	2	
Beam	Beam diameter (cm)	E (MeV)		Pulse wi	Pulse width (s) Shield Thickness shield (cm)		ess shield cm)	
Proton	20	590		4		Al	1	

Table 1. Main descript	tion of proton beam,	spallation target, UCN s	ource geometry, and material.
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^aThe optimized length and the corresponding volume (see **Table 3**); ^bThe inner and outer side walls have been made from Zr and Steel, respectively. Here Steel material contains 72% ⁵⁶Fe, 18% ⁵²Cr, 8% ⁵⁸Ni, and 2% ⁵⁵Mn; ^cThe thicknesses of the inner side outer side walls equal 0.05 and 0.3 mm, respectively.

flux in the heavy water near the sD_2 , and the CN flux in the sD_2 are simulated. Cold and thermal neutrons are being transported throughout sD₂ and UCN are being produced everywhere in the sD₂. The CN flux increases (versus position x) and reaches a maximum value at $x = d \cong 4$ cm. We assume that these processes can be treated as one-dimension. The CN flux values at $x' \le d$ are used as boundary conditions. We may write the neutron transport equation as follow.

$$\int_{E_{\min}}^{E_{\max}} \Sigma_{s} \left(E' \to E \right) n\left(E', x \right) \upsilon' dE' = \left[\Sigma_{s} \left(E \right) + \Sigma_{a} \left(E \right) \right] n\left(E, x \right) \upsilon + \left\langle \cos \theta \right\rangle \upsilon \frac{\partial n\left(E, x \right)}{\partial x}$$
(1)

The scattering kernel

$$\Sigma_s \left(E' \to E \right) = N_0 \sigma_s^{\text{UCN}} \left(E' \right), \quad 0.3 \le E' \le 24.1 \text{ meV}, \quad E = E_{\text{UCN}}$$
(2)

Is considered for CN neutrons which are directly converted to UCN. We use

$$\Sigma_{s}\left(E' \to E\right) = N_{0} \frac{\sigma_{s}\left(E'\right)}{E'(1-\alpha)}, \quad E \le E' \le E/\alpha, \quad E = E_{\rm CN}$$
(3)

For description of CN neutrons which slow down and don't fall below about 0.1 meV. The definitions of the symbols used in Equations (1)-(3) are:

 $x = \text{position of CN or UCN in sD}_2$ $N_0 \sigma_s^{\text{UCN}} = \text{UCN}$ scattering kernel

- $\sigma_{s}^{UCN} = UCN$ production cross-section
- $\Sigma_s = N_0 \sigma_s$ = macroscopic scattering cross-section
- $\Sigma_a = N_0 \sigma_a$ = macroscopic absorption cross-section
- σ_{s} = microscopic scattering cross-section
- σ_a = microscopic absorption cross-section
- E' = initial kinetic energy of neutron
- E = final kinetic energy of neutron
- $E_{\rm CN}$ = kinetic energy of each CN
- $E_{\rm UCN}$ = kinetic energy of each UCN
- $E_{\rm max} =$ maximum energy value
- E_{\min} = minimum energy value

- v' = initial neutron speed
- v = final neutron speed

n(E, x) = number density of neutrons with a kinetic energy of E at x

 $\langle \cos \theta \rangle$ = average cosine of the neutron scattering angle in the laboratory system

 N_0 = number density of sD₂

 $\alpha = (A-1)^2 / (A+1)^2$ = collision parameter

A = deuteron mass number

When a neutron has low energy, scattering occurs by means of S waves, and hence is only elastic scattering and angular distribution is isotropic with respect to the center of mass system [14]. In the laboratory system, $\langle \cos \theta \rangle$ equals 2/3A over the angular region $\theta = 0 - \pi$. At temperature of T = 8 K, the thermal and para-up scattering contributions are maximal at the lowest neutron energies and there amount to an increase in cross section by 2.5% [15]. These mean that at such a low temperature CNs lose energy upon elastic scattering and the effects of chemical binding and thermal motion of the scattering nuclei can be ignored. In this way the CN neutron is slowed down until it reaches thermal equilibrium with the sD₂ material. On this basis, the scattering kernel given in Equation (3) would be applicable for T = 8 K. This scattering kernel for a neutron scattering from a completely free nucleus was first shown by Fermi. To numerically solve Equation (1) using algebraic equations, the spatial and energy variables must be discretized. We replace the space derivative by a first order backward difference approximant at position x_i . Substituting Equation (3) into Equation (1) and after the spatial and energy discretization of Equation (1), we obtain the following recurrence equations.

$$\frac{a_g}{h} n^{i+1,g} \left(E_g \right) + \left(b_g - \frac{f_g}{h} \right) n^{i,g} \left(E_g \right) - \sum_{g'=g}^{g_{\text{max}}} c_{g',g'+1} n^{i,g'} \left(E_{g'} \right) = 0,$$

$$g = 1, 2, \dots, 120, \quad g'_{\text{max}} = 10g - 1 \quad (g \le 12),$$

$$g'_{\text{max}} = 120 \quad (g > 12).$$
(4)

Substituting Equation (2) into Equation (1) and after discretization we obtain the following algebraic equations.

$$\frac{e_k}{h} n^{i+1,k} \left(E_k \right) + \left(p_k - \frac{q_k}{h} \right) n^{i,k} \left(E_k \right) - \sum_{g=1}^{120} A_g n^{i,g} \left(E_g \right) = 0, \quad k = 1, 2, \cdots, 210$$
(5)

 $n^{i,g}(E_g)$ and $n^{i+1,k}(E_k)$ represent the numerical densities of CN and UCN with kinetic energies E_g and E_k (g and k energy groups) at x_i , respectively. h represents a space step. Energy variables have typically been discretized by the multi-group model [14], where each energy group represents one constant energy. In our calculations, the parameters a_g , b_g , c_g , f_g , e_k , p_k , q_k , and A_g are defined and are the constants for a given energy group:

$$a_g = f_g = \frac{\upsilon_g}{3}, \quad \upsilon_g = 1.383 \times 10^6 \sqrt{E_g (\text{eV})} \text{ cm/s.}$$
 (6)

$$b_{g} = \left[\Sigma_{a} \left(E_{g} \right) + \Sigma_{s} \left(E_{g} \right) \right] \upsilon_{g}.$$
⁽⁷⁾

$$c_{g',g'+1} = \overline{\Sigma}_{s} \int_{E_{g'}}^{E_{g'+1}} \frac{\upsilon'(E')}{E'(1-\alpha)} dE', \quad \overline{\Sigma}_{s} = \Sigma_{s} \left(\frac{E_{g'} + E_{g'+1}}{2}\right).$$
(8)

$$e_k = q_k = \frac{v_k}{3}, \quad v_k = 1.383 \times 10^6 \sqrt{E_k (\text{eV})} \text{ cm/s.}$$
 (9)

$$p_{k} = \left[\Sigma_{a} \left(E_{k} \right) + \Sigma_{s} \left(E_{k} \right) \right] \upsilon_{k}.$$

$$\tag{10}$$

$$A_{g} = 0.2N_{0}\sigma_{s}^{\mathrm{UCN}}(E_{g})\overline{\nu}_{g,g+1}, \quad \overline{\nu}_{g,g+1} = \frac{\nu_{g} + \nu_{g+1}}{2}.$$
 (11)

For solving Equations (4) and (5) we take the energy difference between each two neighboring energy groups as

$$E_{g+1} - E_g = 0.2 \text{ meV}, \quad E_{k+1} - E_k = 1 \text{ neV}$$
 (12)

The boundary condition is as follow:

$$n(E_{\rm CN}, x') = S_n \frac{f(x', E_{\rm CN})}{\nu_{\rm CN}}, \quad S_n \int f(x', E_{\rm CN}) dE_{\rm CN} = \phi_{\rm CN}(x')$$
(13)

The $f(E_{CN}, x')$ is CN energy spectrum at x', and S_n , in units of s⁻¹, is the neutron source power. The notation ϕ_{CN} , in units of cm⁻²·s⁻¹, represents the CN flux (integrated over $E_{CN} = 0.3 - 24.1 \text{ meV}$) which strongly depends on the proton beam current. Using the MCNPX code, the fast flux on the target, the thermal flux in the D₂O near the sD₂, and the CN flux in the sD₂ are simulated. The Monte Carlo (MC) calculations are based on the neutron cross sections of Pb, Zr, Al, D₂O, Steel at 300 K, sD₂ at 8 K. These cross-sections have been calculated using the nuclear data processing program NJOY [16]. The algebraic Equations (4) and (5) are solved by a backward implicit method in MATLAB. These cross-section values have been extracted from literature data [12] [15] [17]-[19].

3. Results and Discussion

We have considered a UCN two-layer source of D₂O/sD₂ and calculated its UCN yield. In the D₂O moderator the incoming fast neutrons (spallation neutrons) slow down to thermal region at room temperature. They decelerate in the sD₂ fairly and have a velocity distribution in the energy range of $E_{CN} = 0.3 - 24.1 \text{ meV}$. Using the MCNPX code, the average fast flux on the target, the thermal flux in the D_2O near the sD_2 layer, and the CN flux in the sD_2 have been calculated, as given in Table 2. The spallation target produces the fast neutron flux $\phi_{\text{fast}} = 5 \times 10^{14} \text{ cm}^{-2} \cdot \text{s}^{-1}$. The produced thermal neutrons penetrate the sD₂ with the flux $\phi_{\text{th}} = 3.69 \times 10^{13} \text{ cm}^{-2} \cdot \text{s}^{-1}$, until large fractions of them are cooled at x = d = 4 cm. Substituting $f(E_{CN}, x')$ into Equation (13) and taking it as the boundary condition, the evolution in space (x > 0) of UCN and CN has been calculated with solving the coupled transport equations in MATLAB. In order to calculate UCN density and flux, 330 neutron energy groups have been considered. UCNs emerge from a layer (with a thickness about d = 4 cm) near the sD_2 surface area so it is only this layer that needs to be integrated over. By this integration, the UCN flux versus x is shown in Figure 2. The UCN production rate versus x is shown in Figure 3. In Figure 2 and Figure 3 the data points are for UCNs in the energy range of 40 - 250 neV. In the present multi-group calculations, a converge result has been achieved with a suitable space step. The space step h has been determined to be about 0.1 cm. In Table 3, the numerical results of UCN production have been presented for different sizes of the sD₂. In the same table, our results of the average UCN production rate and density have been compared with those of the PSI UCN source [20] [21].

Table 2. The simulation results of the neutron flux $(cm^{-2} \cdot s^{-1})$.			
Depth (cm) ^a	Cold flux in the sD ₂		
1.0	2.94×10^{13}		
2.0	3.31×10^{13}		
3.0	$3.51 imes 10^{13}$		
4.0	3.61×10^{13}		
5.0	$3.60 imes 10^{13}$		
6.0	3.54×10^{13}		
7.0	3.41×10^{13}		
8.0	3.15×10^{13}		

^aThe fast flux on the spallation target is $5 \times 10^{14} \text{ cm}^{-2} \cdot \text{s}^{-1}$. The fast flux, the thermal flux, and the cold flux in the D₂O near the sD₂ approximately equal to 2.12×10^{11} , 3.69×10^{13} and $1.73 \times 10^{13} \text{ cm}^{-2} \cdot \text{s}^{-1}$, respectively.



Figure 2. UCN flux versus thickness *x* of the sD_2 (see **Figure 1(a)**). The curve reaches to a maximum at x = 4.3 cm. Data points represent UCNs in the energy range of 40 - 250 neV.



Figure 3. UCN production rate versus thickness *x* of the sD₂ (see **Figure 1(a)**). The curve reaches to a maximum at $x \approx 4$ cm. Data points represent UCNs in the energy range of 40 - 250 neV.

4. Summary and Conclusions

In the present work, a UCN source based on D_2O/sD_2 has been studied. The sD_2 at 8 K is kept in close contact with the D_2O moderator at room temperature. The sD_2 layer, with a number density of $N_0 = 3 \times 10^{22}$ cm⁻³ and a high ortho-concentration ($c_0 = 98.5\%$), has been considered at temperature of T = 8 K. Using the MCNPX code, the fast flux on the spallation target, the thermal flux in the D_2O near the sD_2 , and the CN flux in the sD_2 have been simulated. Geometric description of the UCN setup has been shown in Figure 1. The simulation results of the neutron flux have been given in Table 2. The penetration depth *d*, where thermal neutrons are transformed fairly into CN neutrons, approximately equals 4 cm. This distance may correspond to the scattering mean-free path of thermal neutrons. By the reason of no ultra-cold scattering cross-sections in input files of MCNP code, it cannot be used to continually model scattering down to neV energies. By considering simulated CN spectrums as boundary conditions, the UCN flux and the corresponding production rate in the sD_2 have been investigated by multi-group model (330 neutron energy groups) and using a backward implicit method. Once CN kinetic energy changes from 9 meV to ≈ 9.7 meV, σ_s^{UCN} falls rapidly. On this basis, we have selected the energy interval $E_{g+1} - E_g = 0.2$ meV. The space step 0.1 cm has been taken in our calculations. It may be worth men-

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Length (cm)	Volume (liters)	Average UCN flux $(cm^{-2} \cdot s^{-1})$	Average UCN production rate $(cm^{-3} \cdot s^{-1})$	Average UCN density (cm^{-3})
1.0	1.963	4.44e+6	1.28e+5	2777
2.0	3.926	7.66e+6	1.48e+5	3211
3.0	5.889	1.04e+7	1.62e+5	3515
4.0	7.852	1.23e+7	1.71e+5	3710
5.0	9.815	1.69e+7	1.89e+5	4101
6.0	11.616	1.61e+7	1.88e+5	4079
7.0	13.741	1.52e+7	1.87e+5	4057
8.0	15.704	1.43e+7	1.86e+5	4036
9.0	17.667	1.36e+7	1.85e+5	4014
10.0	19.630	1.29e+7	1.84e+5	3993
11.0	21.593	1.24e+7	1.82e+5	3949
12.0	23.556	1.18e+7	1.80e+5	3906
13.0	25.519	1.14e+7	1.78e+5	3862
14.0	27.482	1.10e+7	1.76e+5 ^b	3819
15.0	29.445	1.06e+7	1.73e+5	3754

Table 3. The numerical results of average UCN flux, density and production in the sD₂^a

^aThe calculations have been performed without taking temperature increase; ^bAt PSI, the UCN production rate is expected to be 2.9×10^5 cm⁻³·s⁻¹. The volume of sD₂ is disk shaped (with 27 liters in volume and 50 cm in diameter) [20] [21].

tioning that this value is smaller than $\lambda_s/10$. Here λ_s denotes the CN scattering mean-free path in the sD₂. The UCN flux and the corresponding production rate (versus position x) have been given in **Figure 2** and **Figure 3**, respectively. The numerical results of average UCN flux, UCN production rate and density have been shown in **Table 3**. The results have been presented without taking temperature increase. In fact, the limiting UCN density is strongly dependent on the heat load on the moderator and UCN life-time (τ_{ucn}) in the sD₂. For instance, consider ≈ 27 liters of sD₂ and assume a heat load of 0.4 WµA⁻¹. The power density will be ≈ 76 mWg⁻¹·mA⁻¹ [22]. During a 4 s long proton beam pulse, the temperature rises from 8 to 9.7 K, and consequently the UCN density reaches about 63.1% of the maximum value. τ_{ucn} may be determined by

$$\tau_{\rm ucn}^{-1} = \tau_a^{-1} + \tau_{\rm para}^{-1} + \tau_{\rm phonon}^{-1}.$$
 (14)

Here, $\tau_a = \frac{1}{N_0 \sigma_a \upsilon_{\text{UCN}}} = 150 \text{ ms}$ is the nuclear absorption time; $\tau_{\text{para}} = \frac{1}{N_0 (1 - c_0) \sigma_{\text{para}} \upsilon_{\text{UCN}}} = 100 \text{ ms}$ is the

para up-scattering time; and $\tau_{\rm phonon} = \frac{1}{N_0 \sigma_{\rm up}(T) \upsilon_{\rm UCN}} \cong 34 \, {\rm ms}$ is the thermal up-scattering time. Here $\sigma_{\rm para}$

and σ_{up} denote para and thermal up-scattering cross-sections, respectively [17] [19]. Taking such a long pulse and τ_{ucn} about 21.7 ms, the UCN density approximately equals 2406 cm⁻³. However, owing to the good thermal conductivity of sD₂, its temperature may be kept at the level of 8 K by liquid helium cooling [8]. As shown in **Table 3**, we have obtained an optimal length for the UCN source. The optimal thickness of the sD₂ is about 5 cm, where average UCN density reaches to a maximum value. UCNs with speeds of 2.39 and 6.91 m/s, which correspond to UCN minimum and maximum energies, travel 5.18 and 15 cm in 21.7 ms, respectively. These distances are greater than the optimal length of the sD₂. The CN flux values have been provided with acceptable accuracy, mostly below 2.6%, by MCNPX code. In this work, the errors are mainly due to the assumptions made in the calculations of η and $c_{g',g'+1}$. We expect the effects that 1) slowing down of thermal neutrons at larger depths (x > 4 cm) gives an enhancement; 2) variations of neutron scattering angle and effect of thermal motion of the scattering nuclei give a reduction in the values from our model. We recommend to consider these effects for calculations of precise values of η and $c_{g',g'+1}$. The problem was treated as one-dimension by the two reasons: 1) the mean square root of the sD₂ surface area is larger than average distance a CN neutron travels along its path before being converted; 2) UCNs emerge from a layer (with a thickness about d = 4 cm) near the sD₂ surface area. The accuracy of the results can increase when the geometry of the sD₂ is considered using three-dimensional transport equation. The third author is planning to produce a unified code which can combine the CN flux modeling with UCN production and loss.

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