

A New Version of Special Relativity Absorbed the Uncertainty Principle: Its Content as Well as Application and Experimental Test

Dapeng Qian

Public Security Bureau of Yingkou, Yingkou, China
Email: gdpnew@sina.com

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Abstract

Based on the space spherical symmetry of 3-dimensional and the translational symmetry of time and the uncertainty principle, a 4-dimensional space-time cylinder model of quarks and leptons is established. With this model, equations of the special relativity can be extended more perfectly, thereby achieving a unity of the special relativity and quantum mechanics in deeper level. New equations can not only interpret issues explained by old equations but also solve several important pending problems. For example, a formula to strictly calculate the coefficient ξ of Lorentz invariance violation (LIV) is derived, to above 4×10^{19} eV UHECR protons the calculated $|\xi| < 4.5 \times 10^{-30}$, although there is the LIV effect it is too weak to change the GZK cutoff, which is consistent with observations of HiRes and Auger; Also, a relation formula between the Hubble constant and several basic constants is derived, thus theoretically calculated $H_0 = 70.937 \text{ km}\cdot\text{s}^{-1}\cdot\text{Mpc}^{-1}$, which is well consistent with the final observation result of HST Key Project. In addition, an unusual effect predicted by new equations can be experimentally tested in the electron storage ring; a preliminary experiment result has hinted its signs of existence.

Keywords

Special Relativity, Uncertainty Principle, Cylinder Model with Intrinsic 4-Dimensional Space-Time of Quarks/Leptons, Lorentz Invariance Violation, GZK Cutoff of UHECR, Planck Energy, Hubble Constant, Super-High Energy Electron, Electron Storage Ring

1. Introduction

How to unify the relativity and the quantum mechanics? This is a great problem in physics across the centuries, which has been a concern. Popular view is that, since the establishment of quantum electrodynamics, the unification of special relativity and quantum mechanics has been completed, the remaining work is only to explore the issue of unification of general relativity and quantum mechanics. However, if broadened thinking, it can be found that above view is flawed.

As we all know, from the fundamental sense, the special relativity firstly is a measurement theory about time, space, energy, momentum and so on, *i.e.* it is a physical framework to theory to do principled rules for all measurement acts. On the other hand, we also know that measurements of these physical quantities must be subject to the insurmountable constraint of one natural law, that is, the Heisenberg uncertainty principle that reflected essential feature of quantum mechanics. So in this sense judgment, the special relativity as a clean measurement theory that utterly disregards uncertainty relation, can not be a complete theory. Thus if taking into account the universality constraint of the uncertainty principle, it is necessary to further improve the special relativity; only completing this work can truly achieve unifying relativity and quantum mechanics.

In fact people already realized that any perfect physical theory regarding space-time not only has the rational core of the relativity also must contain the uncertainty principle and treat it as one of fundamentals of the theory. However, what specific method should be taken to make the uncertainty principle naturally implant into the concept system of special relativity and keep that the overall structure of special relativity is not destroyed? For this problem, the physics must make satisfactory answer.

Now this paper presents a way to solve this problem. First, based upon the uncertainty principle, the time translational symmetry and the 3-dimensional space spherical symmetry, for the elementary particles of the level of quarks and leptons there established a cylinder model with 4-dimensional space-time (PSTC model). Then, used this model, we deduced a series of new equations that are compatible with old equations of special relativity and also fit for the uncertainty principle, thus achieve unifying special relativity and quantum mechanics in deeper level via a way different from the quantum electrodynamics.

New equations which reveal the concepts of space, time, mass, energy etc. have richer connotations, so that can help people to re-understand the essence of some physical phenomena and solve several pending important problems, such as: 1) The new mass equation directly shows the inevitable existence of the Lorentz invariance violation (LIV) and derives a strict formula to calculate the LIV coefficient ξ . For energy higher than 4×10^{19} eV UHECR protons, the calculation $|\xi| < 4.5 \times 10^{-30}$, although there is the LIV effect but $|\xi|$ value is too small to change the GZK cutoff, which is consistent with observations of the HiRes [1] and the Auger [2]. 2) It can be proved that the Planck energy is a Lorentz invariant, so for “the observer independence of Planck energy” [3], that has been regarded as basic principle; its theoretical source is finally found. Also, it is proved that the Planck energy is not the common upper limit of energy of all particles. 3) Using the new equation, a relation formula between the Hubble constant and several basic constants is derived, thereby theoretically calculated $H_0 = 70.937 \text{ km}\cdot\text{s}^{-1}\cdot\text{Mpc}^{-1}$, which is well consistent with the final measuring result of the HST Key project [4]. Via this relation formula the mystery of Dirac large numbers can also be clarified.

According to an extraordinary effect prophesied by new equations, it is expected that in the electron storage ring RF cavity downstream direction there is an emission of unusual electrons of much higher than the beam energy. It is possible to test the new equations of special relativity by detecting those small probability unusual events. A preliminary experiment was done and its result hinted the signs of emission of super-high energy electrons. To this end I propose an experimental program and called for experimental physicists to exactly complete the interesting exploratory experiment.

This paper is organized as follows. Section 2 describes the cylinder model of intrinsic 4-dimensional space-time of particles. Section 3 gives new improved equations of special relativity. Section 4 describes that use new equations to solve several important problems. Section 5 proposes an experimental plan to test the prophecy of the new equation. Section 6 gives the conclusion.

2. The Cylinder Model of Intrinsic 4-Dimensional Space-Time of Particles

2.1. Establishment of the Model

Einstein’s idea on space-time was to take the “physical object” as the premise. He said: “Space-time is not nec-

essarily something to which one can ascribe a separate existence, independently of the actual objects of physical reality. Physical objects are not in space, but these objects are spatially extended” [5]. Einstein’s words remind people: the space-time is actually one kind of attributes of physical objects. In order to understand more deeply the space-time, it is necessary to more sufficiently face the object. It has long been known, “the actual objects of physical reality” are in hierarchical structure. In general, between different structural levels the objects could have fundamentally different concept and attributes. On the space-time attributes of the object, if accept the viewpoint of Einstein at his later years, namely the actual space-time must depend on the actual object, we will not be able to rule out such a possibility that the current understanding space-time will only be maintained to certain one very low-level particles. Starting from this assumption, we can further deduce as follows.

- When measuring such a particle, because the uncertain amount of the momentum and the energy can not be infinite, according to the Landau interpretation of the uncertainty principle, then the space uncertain amount and the time interval between twice measuring are impossible to zero. If abandoning the unreasonable infinity of the uncertain amount of momentum and energy, and taking a limited maximum value to replace them respectively, then the uncertain amount of space and the time interval will have the minimum value that are greater than zero. This indicates that in the actual observable sense the particles on this level should have a certain size.
- So-called the particle has “a certain size”, it means that the particle not only has a 3-dimensional space size, also has an intrinsic time size. Thus, according to the space-time unity of the special relativity, such a particle that has the nonzero and finite intrinsic scales of space-time should have an intrinsic 4-dimensional geometric shape.
- Taking into account when the particle is in rest, because there are the 3-dimensional space spherical symmetry and time translation symmetry, then the geometrical shape of particle should be a 4-dimensional cylinder that the timeline is taken as the rotational symmetry axis, and its axial height is the maximum value of the intrinsic time interval of particle.
- According to the above, the space and time of the 4-dimensional cylinder of particles must be the real physical space-time, rather than any formal mathematical space-time, such as the Minkowski space-time etc., so only Euclidean geometry is suitable for it.
- What particles are the final form that maintain the understandable time and space? According to the existing knowledge let us assume that they are particles of the quarks-leptons level. Of course, this is a mandatory assumption, of which correct or not need by testing its derived results later to judge.

Above these can be attributed to a basic postulate:

[Postulate] The particle of quarks-leptons level is not the point particle but Euclid 4-dimensional space-time cylinder with a certain time interval as its axial height.

This [Postulate] gives the particles the cylinder model with intrinsic 4-dimensional space-time (for short PSTC model). In accordance with the requirements of [Postulate], when the particle is rest relative to the observer, its intrinsic time axis t' is parallel with the time axis t of the coordinate system of observer, namely there is a zero deflection from the axis t' to the axis t ; when the particle movement at the light-speed c relative to the observer, there is the maximum deflection angle from the axis t' to the axis t . Because the geometry of 4-dimensional cylinder is of Euclid, so in this case the t' axis is orthogonal with the axis t . Therefore, in general, according to [Postulate] and the particle’s 4-dimensional space-time cylinder on $t-u-t'$ plane projection (Figure 1), the following two corollaries can directly be derived:

[Corollary 1] If a particle is moving at a speed $u \leq c$ relative to an observer, there is a deflect angle Ω between the intrinsic time axis t' of particle and the time axis t of coordinates system of observer on the $t-u-t'$ plane, which

$$\Omega = \arcsin(u/c) \quad (1)$$

[Corollary 2] The shape of particle observed randomly at one moment is a 3-dimensional space cross-section of the 4-dimensional space-time cylinder in the observer’s coordinates-system.

2.2. The Intrinsic Time Height of Particle and the Intrinsic Time-Space Ratio of Particle

Having a nonzero and finite intrinsic time height is the most important feature of the particles 4-dimensional space-time cylinder model. The time height concept comes from the Landau interpretation of the energy-time uncertainty relation [6], Landau believes that the particle energy E at one moment can be arbitrarily accurately

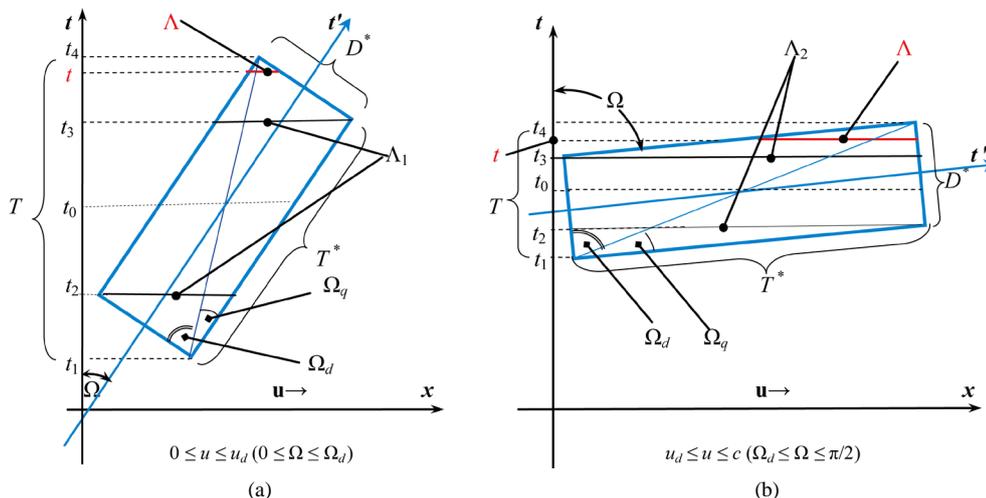


Figure 1. Projection of the particle's intrinsic 4-dimensional space-time cylinder on the t - u - t' plane (The velocity u of particle is along the x -axis direction of the coordinate system of observer).

measure, in the uncertainty relation

$$\Delta E \cdot \Delta t \geq \hbar/2 \tag{2}$$

ΔE is the difference of two accurate measurement values of energy, Δt is the time interval between twice measurements. Therefore, in according to the meaning of particle's intrinsic time height concept defined by the [Postulate], there is obviously:

[Corollary 3] If an observer successively twice measures a particle but their time interval is less than the particle's apparent time height, then such measurements is meaningless.

Here the so-called "apparent time height" (denoted by T) is a projection value of the particle 4-dimensional cylinder on the observer's coordinate system time axis, according to [Corollary 1], T changes with speed u . The axial height of the particle 4-dimensional cylinder defined by the [Postulate] is called the particle's intrinsic time height (denoted by T^*), for the same kind particles T^* is a fixed value, which is a Lorentz invariant. By (1) it can be proved

$$T = T^* \cdot \left(\sqrt{1 - \frac{u^2}{c^2}} + \frac{u}{\Phi c} \right) \tag{3}$$

where

$$\Phi = \frac{cT^*}{D^*} \tag{4}$$

D^* denotes the diameter of particle, the dimensionless constant Φ called as the intrinsic time-space ratio of particle is an important parameter describing the intrinsic geometry feature of particle. The value of Φ need to use the new special relativity to calculate, which will be elaborated in Section 3.4.1, now in advance the results are given:

$$\Phi = 1.037 \times 10^{19} \tag{5}$$

In addition, the calculating formula of the particle's intrinsic time height will in Section 3.4.2 be deduced, now it is also written in advance:

$$T^* = \frac{\hbar}{2m_0 c^2} \tag{6}$$

(6) show that T^* depend on the particle mass m_0 , so different quarks, leptons and so on have different intrinsic time height. For example, the electron's T_e^* or cT_e^* calculation as follows:

$$T_e^* = 6.44 \times 10^{-22} \text{ s} \text{ or } cT_e^* = 1.93 \times 10^{-13} \text{ m} \tag{7}$$

Further use of (4) and (5) to calculate the diameter of electron:

$$D_e^* = 1.86 \times 10^{-32} \text{ m} \quad \text{or} \quad D_e^*/c = 6.20 \times 10^{-41} \text{ s} \quad (7')$$

On high-level composite particles as well as macroscopic objects, because they are the gathering of quarks and leptons in 3-dimensional space, so although their space scales can continue to amplify, their intrinsic time scale remains the intrinsic time height of elementary particles.

The intrinsic time-space ratio of particle is very large value, which shows the serious imbalance between the intrinsic time scale and intrinsic space scale, so saying geometry form of particle is the “4-dimensional cylinder”, rather is a very slender “4-dimensional thorn”.

2.3. The 3-Dimensional Space Cross-Section of the 4-Dimensional Space-Time Cylinder of Particle

The [Corollary 2] points out that the particle’s shape that is randomly observed at one moment is a 3-dimensional space cross-section of the particle’s 4-dimensional space-time cylinder in the coordinates-system of observer. Referring to **Figure 1**, according to the space rotational symmetry with the velocity u direction as axis, it can be seen that the 3-dimensional space cross-section is the rotational ellipsoid or its section, that is, an ellipsoid crown, an ellipsoid zone as well as the sphere or a cylinder in extreme situations. What specific shape is depends on two factors: 1) the angle Ω , which is associated with the speed u according to (1); 2) the randomness that a moment of measurement occurs in the time height T . Referring to **Figure 1**, all types of 3-dimensional space cross-section are listed in **Table 1**:

In **Table 1**, Ω_d denotes the angle between the short side and the diagonal in the rectangle that the particle’s 4-dimensional cylinder is projected on the plane $u-t$ of observer’s coordinate system, the speed corresponding to $\Omega = \Omega_d$ is

$$u_d = \frac{\Phi c}{\sqrt{\Phi^2 + 1}} = (1 - 4.649 \times 10^{-39}) \cdot c \quad (8)$$

When $\Omega \leq \Omega_d$ i.e. $u \leq u_d$ (see **Figure 1(a)**), for any moment t in time intervals $[t_1 t_2]$ and $[t_3 t_4]$ we can define a dimensionless variable ζ :

$$\zeta = \frac{t-t_1}{t_2-t_1} \quad (t_1 \leq t \leq t_2) \quad \text{and} \quad \zeta = \frac{t_4-t}{t_4-t_3} \quad (t_3 \leq t \leq t_4) \quad (9)$$

Similarly, when $\Omega \geq \Omega_d$ i.e. $u \geq u_d$ (see **Figure 1(b)**), for any moment t in time intervals $[t_1 t_0]$ and $[t_0 t_4]$ we can also define the dimensionless variable ζ :

$$\zeta = \frac{t-t_1}{t_0-t_1} \quad (t_1 \leq t \leq t_0) \quad \text{and} \quad \zeta = \frac{t_4-t}{t_4-t_0} \quad (t_0 \leq t \leq t_4) \quad (9')$$

ζ is called the random fluctuation variable, apparently there is

$$0 \leq \zeta \leq 1 \quad (10)$$

According to **Figure 1** and (1) (3) (4) (9) (9') (10), using the elliptic equation to make definite integrals the

Table 1. The 3-dimensional space cross-sections of the 4-dimensional space-time cylinder of particles.

	$u = 0, \Omega = 0$	$0 < u \leq u_d, 0 < \Omega \leq \Omega_d$	$u_d < u < c, \Omega_d < \Omega < \pi/2$	$u = c, \Omega = \pi/2$
(t, t_2)		Ellipsoid crowns with different heights $\Lambda (0 < \Lambda < \Lambda_1)$	Ellipsoid crowns with different heights $\Lambda (0 < \Lambda < \Lambda_2)$	
$[t_2, t_3]$	Sphere with diameter D^*	Complete ellipsoid with major axis Λ_1 and minor axis D^*	Ellipsoid zones with same height ($=\Lambda_2$), different end-plane diameters	Cylinders with same height ($=cT^*$) and different diameters $D (0 \leq D \leq D^*)$
(t_3, t_4)		Same as (t, t_2)	Same as (t, t_2)	

volume V of 3-dimensional space cross-sections can be gotten:

$$V = \begin{cases} \frac{V_0(3\zeta^2 - 2\zeta^3)}{\sqrt{1 - \frac{u^2}{c^2}}} & (0 \leq u \leq u_d, 0 \leq \zeta \leq 1) \end{cases} \quad (11-1)$$

$$V = \begin{cases} V_0 \left[\frac{3\zeta^2}{(2-\eta)^2} - \frac{2\zeta^3}{(2-\eta)^3} \right] / \sqrt{1 - \frac{u^2}{c^2}} & (u_d \leq u \leq c, 0 \leq \zeta \leq \eta) \end{cases} \quad (11-2a)$$

$$V = \begin{cases} V_0 \left[\frac{\eta^2 - 6\eta + 12\zeta - 6\zeta^2}{(2-\eta)^2} \right] / \frac{u}{\Phi c} & (u_d \leq u \leq c, \eta \leq \zeta \leq 1) \end{cases} \quad (11-2b)$$

where

$$\eta = 2\sqrt{1 - \frac{u^2}{c^2}} / \left(\sqrt{1 - \frac{u^2}{c^2}} + \frac{u}{\Phi c} \right) \quad (12)$$

$V_0 = \pi D^{*3} / 6$ is the volume of 3-dimensional space cross-section of rest particle relative to observer, that is the volume of sphere with diameter as D^* .

According to **Figure 1** further getting other features of the 3-dimensional space cross-sections as follows:

1) If $0 \leq u \leq u_d$ and $\zeta = 1$, it is a complete ellipsoid whose minor axis is D^* and long axis is Λ_1 (especially when $u = 0$, $\Lambda_1 = D^*$, it becomes a sphere),

$$\Lambda_1 = \frac{D^*}{\cos\Omega} = D^* / \sqrt{1 - \frac{u^2}{c^2}} \quad (13)$$

2) If $0 \leq u \leq u_d$ but $0 < \zeta < 1$, it is an ellipsoid crown having different height Λ and bottom area S ,

$$\Lambda = \zeta \Lambda_1 \quad (14)$$

$$S = \begin{cases} 4\zeta(1-\zeta)S_0 & (0 < \zeta \leq 0.5) \\ S_0 & (0.5 \leq \zeta \leq 1) \end{cases} \quad (15)$$

where $S_0 = \pi D^{*2} / 4$ is the area of ellipsoid projection in observer $y-z$ coordinate plane.

3) If $u_d < u < c$ and $0 < \zeta < \eta$, it is an ellipsoid crown having different height Λ ,

$$\Lambda = \zeta \Lambda_2 \quad (14')$$

4) If $u_d < u < c$ and $\eta \leq \zeta \leq 1$, it is an ellipsoid zone having different end-plane diameters and a same height Λ_2 ,

$$\Lambda_2 = \Phi c D^* / u \quad (16)$$

5) If $u = c$, it is a 3-dimensional space cylinder having the same height ($= cT^*$) and different diameter D ,

$$D = \sqrt{\zeta(2-\zeta)} \cdot D^* \quad (17)$$

6) If $\zeta = 0$, the particle is no observed at this moment.

2.4. Advantages of the PSTC Model

To sum up, the differences as well as advantages of the PSTC model compared to other non-point particle models as follows:

1) The basis of establishment of PSTC model is realistic and reliable, it is based upon the spherical symmetry of 3-dimensional space, the translational symmetry of time, the space-time unity of relativity, the Heisenberg uncertainty principle, and its applying objects are quarks and leptons, which all are empirical facts and recognized principle, there are no additional imaginary content.

2) The PSTC model is simple, there is only 4-dimensional space-time, with no additional dimension.

3) For space-time, the PSTC model requires real physical space-time, *i.e.* Euclidean space-time, rather than any mathematical space-time, such as the Minkowski space-time etc. We know that the Minkowski geometry is one of expression forms of special relativity but has not the substantive contribution to the special relativity.

4) The PSTC model points out that the particles not only has a size of the space, in the time also has a non-zero and finite intrinsic “height”, the ratio of the time height T^* to the diameter D^* , $\Phi = cT^*/D^* = 1.037 \times 10^{19}$, is a large number, which shows the difference between the particle’s intrinsic time scale and space scale.

5) The PSTC model can be used to develop the basic theory of physics, such as the development and improvement of special relativity.

3. The New Improved Equations of Special Relativity Based upon the PSTC Model

Using the particle’s intrinsic 4-dimensional space-time cylinder model (PSTC model), a series of new more perfect equations corresponding to old equations of the special relativity are derived. The PSTC model is based on the uncertainty principle, so new equations have reflected the constraint of uncertainty principle. Taking into the applicability and the testability, we first focus on the new mass equation.

3.1. More Perfect New Mass Equation

In accordance with [Postulate], “the amount of mass” included inside the particle of quarks and leptons etc. must uniformly be distributed in the intrinsic 4-dimensional space-time cylinder, and further in accordance with [Corollary 2], the particle’s shape observed at one moment is a 3-dimensional space cross-section of the 4-dimensional cylinder, so the mass m of particle is proportional to the volume V of 3-dimensional cross-section, that is

$$\frac{m}{V} = \frac{m_0}{V_0} \tag{18}$$

where, m_0 denotes the rest mass of particle. Then (11) into (18) we obtain the more universal mass equation:

$$m = \begin{cases} \frac{m_0(3\zeta^2 - 2\zeta^3)}{\sqrt{1 - \frac{u^2}{c^2}}} & (0 \leq u \leq u_d, 0 \leq \zeta \leq 1) \end{cases} \tag{19-1}$$

$$m = \begin{cases} m_0 \left[\frac{3\zeta^2}{(2-\eta)^2} - \frac{2\zeta^3}{(2-\eta)^3} \right] / \sqrt{1 - \frac{u^2}{c^2}} & (u_d \leq u \leq c, 0 \leq \zeta \leq \eta) \end{cases} \tag{19-2a}$$

$$m = \begin{cases} m_0 \left[\frac{\eta^2 - 6\eta + 12\zeta - 6\zeta^2}{(2-\eta)^2} \right] / \frac{u}{\Phi c} & (u_d \leq u \leq c, \eta \leq \zeta \leq 1) \end{cases} \tag{19-2b}$$

where on the speed u_d please see (8), on the speed substitution variable η please see (12).

To this equation interpretations and in-depth discussions as follows:

[I] The mass m is not a single variable function of the speed u , it depend on both of the speed u and the random variable ζ . The variable ζ that appears in the derivation process of equation makes the randomness concept automatically enter the relativistic equations.

[II] When $\zeta = 1$, (19) has the maximum value form

$$m_R = \begin{cases} \frac{m_0}{\sqrt{1 - \frac{u^2}{c^2}}} & (0 \leq u \leq u_d) \end{cases} \tag{20-1}$$

$$m_R = \begin{cases} \left(\frac{\Phi m_0}{u/c} \right) \cdot \left(\frac{3 + \Phi^2 - c^2 \Phi^2 / u^2}{2} \right) & (u_d \leq u \leq c) \end{cases} \tag{20-2}$$

It can be seen that m_R depends singly on u . When $u \leq u_d$ (20-1) happens to be the Lorentz-Einstein mass formula (In this case m_R and $E_R = m_R c^2$ are called Lorentz mass and Lorentz energy). However when $u_d \leq u \leq c$, the maximum form is another (20-2), in particular $u = c$, the mass is not the infinity but a finite maximum value.

$$m_{\max} = 1.5\Phi m_0 \tag{21}$$

Because the new equation eliminates the infinity, so the theoretical suppression of the physical particles moving at light speed will be eliminated. When $u = c$ the electron's maximum mass

$$m_{e(\max)} = 7.956 \times 10^{15} \text{ GeV}/c^2 \tag{22}$$

[III] Because generally m is a double variable function on u and ζ , even when the particle's speed is constant, its mass m and its energy $E (= mc^2)$ still at $0 \leq m \leq m_R$ and $0 \leq E \leq E_R$ change with ζ . When $\zeta < 1$, $m < m_R$ and $E < E_R$, which shows in particles movement there is a strange "high speed but low mass (energy)" effect or HSLM effect for short.

[IV] With reference to **Figure 1(a)**, it can be proved that when $u < u_d$ the probability P_S that the particle appears in the HSLM state of $\zeta < 1$ (*i.e.* $E < E_R$) is calculated by the following formula

$$P_S = \frac{2u/c}{\Phi\sqrt{1-u^2/c^2} + u/c} \quad (u < u_d) \tag{23}$$

Since Lorentz energy E_R is singly corresponding to the speed u , so the probability P_S can be calculate by E_R replacing u via (20-1)

$$P_S = \frac{2\sqrt{E_R^2 - E_0^2}}{\Phi E_0 + \sqrt{E_R^2 - E_0^2}} \quad (E_R < E_0) \tag{23'}$$

The formula shows that the higher the particle's speed u (*i.e.* the higher the Lorentz energy E_R), the greater the possibility appearing in HSLM state. Because ΦE_0 is huge and there is always $E_R \ll \Phi E_0$ in the current observation, so the probability of particle in HSLM state is very small. Such as the electron's $\Phi E_0 = 5.3 \times 10^{24} \text{ eV}$, the probability of different energy electron appearing in HSLM state is shown in the following table (**Table 2**):

The probability of particle appearing in a neighborhood of $\zeta < 1$

$$dP = P_S d\zeta \tag{24}$$

However the probability of particle in "normal state" of $\zeta = 1$ *i.e.* $E = E_R$ is

$$P_R = 1 - P_S \tag{25}$$

Because there is always $P_R \approx 1$ in the current observation range, so $\zeta = 1$ *i.e.* $m = m_R$ and $E = E_R$ state is most probable, what described by the Lorentz-Einstein mass formula is just the mass-speed relationship in this state.

[V] It can be seen in **Figure 1(b)**, when $u_d \leq u \leq c$, the probability of particle appearing in each $0 \leq \zeta \leq 1$ state is all equal, so the particle is in the fluctuation state of the mass and energy. Especially when $u = c$, the following $m_c - \zeta$ relation is deduced from (19-2b):

$$m_c = 1.5\Phi m_0 (2\zeta - \zeta^2) \quad (0 \leq \zeta \leq 1) \tag{26}$$

when $u = c$, the projection of the particle's 4-dimensional spacetime cylinder on the $t - y$ plane and $t - z$ plane of coordinate system of observer is a circle, in which there is the relationship of an arbitrary circumferential angle ψ and ζ :

$$\cos \psi = 1 - \zeta \tag{27}$$

(27) into (26) and using (21), to obtain

$$E_c = E_{\max} \sin^2 \psi \tag{28}$$

Table 2. The probability P_S of different E_R value electron appearing in HSLM state.

	In high energy cosmic ray	By artificial accelerated	In nuclear β decay	In hydrogen atom
E_R (eV)	$\sim 10^{16}$	$< 10^{11}$	$\sim 10^6$	$< 5.11 \times 10^5 + 13.6$
P_S	$\sim 10^{-8}$	$< 4 \times 10^{-14}$	$\sim 10^{-19}$	$< 10^{-21}$

which shows that when a particle moving at the light speed, its energy changes proportional to the square of the sinusoidal of phase angle.

[VI] For the mass $m = m(\zeta)$, according to the ζ state probability to weighted average, we get the mean mass

$$\bar{m} = \frac{m_0}{\sqrt{1 - \frac{u^2}{c^2} + \frac{u}{\Phi c}}} \quad (29)$$

The (29) shows:

1) The mean mass \bar{m} has included overall effects of the variable ζ , it is only associated with the speed u and is applicable in the all speed range $0 \leq u \leq c$.

2) In the “lower energy” state of $E_R \ll \Phi E_0$, (29) and the Lorentz-Einstein formula difference is very small.

3) For composite particles and macroscopic objects, as long as the rest mass m_0 have define, then (29) are generally applicable for physical objects of all levels.

4) The mass/energy of satisfying the conservation law are neither the m_R/E_R nor the m/E , but the \bar{m}/\bar{E} .

5) (29) multiplied (3) to obtain

$$\bar{m}T = m_0T^* = \frac{\hbar}{2c^2} = \text{const} \quad (30)$$

That is, the product of the particle’s apparent time height T multiplied by the mean mass is a Lorentz invariant.

6) When $u = c$, \bar{m} has the maximum

$$\bar{m}_{\max} = \Phi m_0 = 1.037 \times 10^{19} m_0 \quad (31)$$

when

$$u = u_q = \frac{c}{\sqrt{\Phi^2 + 1}} = 9.643 \times 10^{-20} \cdot c \quad (32)$$

\bar{m} has the minimum value

$$\bar{m}_{\min} = \frac{\Phi m_0}{\sqrt{\Phi^2 + 1}} = (1 - 4.649 \times 10^{-39}) \cdot m_0 < m_0 \quad (33)$$

It should be noted, according to the PSTC model, only to the particles of level of quarks/leptons the speed u_q is meaningful, but for composite particles such a speed can not be defined. (32), (33) show that the particle in the lowest energy state is not in absolute motionless but in motion at the tiny speed $u_q = 2.89 \times 10^{-11}$ m/s.

7) Putting the total mean energy $\bar{E} = \bar{m}c^2$, the mean momentum $\bar{p} = \bar{m}u^2$ and the rest energy $E_0 = m_0c^2$ into Equation (29), the new energy-momentum relation formula is obtained as follows

$$\bar{E}^2 = E_0^2 + (c\bar{p})^2 + \zeta (c\bar{p})^2 \quad (34)$$

where

$$\zeta = - \left(\frac{2\sqrt{1 - u^2/c^2}}{\Phi u/c} + \frac{1}{\Phi^2} \right) \quad (35)$$

Compared with the old energy-momentum relationship

$$E_R^2 = E_0^2 + (cp_R)^2 \quad (36)$$

(34) than (36) multi-a $\zeta (cp_R)^2$, which indicates that the existence of so-called Lorentz invariance violation (LIV) is an inevitable result of the new special relativity, and the violation coefficient ζ can be directly exactly calculate by (35). Equation (35) shows that the absolute value of LIV coefficient $|\zeta|$ is dependent on the speed u of particle, that is the higher the u the smaller (not the larger!) the $|\zeta|$, when $u = c|\zeta|$ attains the minimum value $|\zeta|_{\min} = \Phi^{-2} \approx 10^{-38}$. **Table 3** lists LIV coefficients corresponding to different speeds. Of particular note is that if the particle speed is low to $u = u_q \approx c/\Phi = 2.89 \times 10^{-11}$ (m/s) = 0.289 (Å/s) then $\zeta = -2$, (34) becomes the strange form

Table 3. LIV coefficients ζ corresponding to different speeds u .

	(Unknown)	Ultra-high energy cosmic ray protons	LHC accelerator protons	Slow neutrons in the reactor	Laser frozen atoms	(Unknown)
u	c	$\sim (1 - 10^{-22})c$	$\sim (1 - 10^{-8})c$	$\sim 10^{-5}c$	$\sim 10^{-11}c$	$c/\Phi = 0.289$ (Å/s)
ζ	$\sim 10^{-38}$	$\sim 10^{-30}$	$\sim 10^{-23}$	$\sim 10^{-15}$	$\sim 10^{-8}$	-2

$$\bar{E}^2 = E_0^2 - (cp)^2 \tag{37}$$

(37) suggests that people should re-understanding of the “stationary” concept, because such an extreme tiny speed ~ 0.289 (Å/s) has never been actually observed. About (29) and (34) we will do for a more in-depth discussion in Section 4.

3.2. Improved Lorentz Transformations and Kinematic Formulas

By the ζ state probability to weighted average Λ , the maximum average length $\bar{\Lambda}$ of the 3-dimensional space cross-sectional in the particle movement direction is got (see **Figure 1**, **Table 1**, (13) (14) (14') (16)). According to the [Postulate], Λ is the final standard ruler in the length measurement in the particle movement direction. Using Λ , the improved Lorentz transformations can be derived:

$$x' = \frac{x - vt}{\sqrt{1 - \beta^2} + \beta/\Phi} \tag{38-1}$$

$$y' = y \tag{38-2}$$

$$z' = z \tag{38-3}$$

$$t' = \frac{t - \beta x/c}{\sqrt{1 - \beta^2} + \beta/\Phi} \tag{38-4}$$

and inverse transforms

$$x = \frac{x' + vt'}{\sqrt{1 - \beta^2} + \beta/\Phi} \tag{39-1}$$

$$y' = y \tag{39-2}$$

$$z' = z \tag{39-3}$$

$$t = \frac{t' + \beta x'/c}{\sqrt{1 - \beta^2} + \beta/\Phi} \tag{39-4}$$

where v is the movement velocity of an inertial Σ' relative to another inertial Σ along the x -axis, and $\beta = v/c$. According to the reasoning mode of the classical theory of special relativity, from the above coordinate transformations it can be further derived that

the time dilation
$$\Delta t = \frac{\Delta t'}{\sqrt{1 - \beta^2} + \beta/\Phi} \tag{40}$$

the “length contraction”
$$L = L_0 \left(\sqrt{1 - \beta^2} + \beta/\Phi \right) \tag{41}$$

the velocity addition law
$$u'_x = \frac{u_x - v}{1 - \beta u_x/c} \tag{42}$$

$$u'_{y,z} = \frac{\sqrt{1 - \beta^2} + \beta/\Phi}{1 - \beta u_x/c} u_{y,z} \tag{43}$$

and

$$u_x = \frac{u'_x + v}{1 + \beta u'_x/c} \quad (42')$$

$$u_{y,z} = \frac{\sqrt{1-\beta^2} + \beta/\Phi}{1 + \beta u_x/c} u'_{y,z} \quad (43')$$

3.3. The Transformation of Physical Quantities and the Covariance of Physics Laws

3.3.1. The Energy and Momentum Transformations between Two Inertial Frames

Defining $\bar{E} = \bar{m}c^2$, $\bar{p}_x = \bar{m}u_x$, and then using (29) and (42) (43) it can be proved that

$$\bar{E}' = \frac{\bar{E} - \beta c \bar{p}_x}{\sqrt{1-\beta^2} + \frac{c \bar{p}_x (1 - \sqrt{1-\beta^2}) - \beta \bar{E}}{\Phi m_0 c^2}} \quad (44)$$

$$\bar{p}'_x = \frac{\bar{p}_x - \beta \bar{E}/c}{\sqrt{1-\beta^2} + \frac{c \bar{p}_x (1 - \sqrt{1-\beta^2}) - \beta \bar{E}}{\Phi m_0 c^2}} \quad (45)$$

3.3.2. Transformation of Electromagnetic Fields and the Covariance of Maxwell Equations

If time and space coordinates are transformed by (38) (39) (38') (39'), the electromagnetic field are transformed by following (48), then in all inertial reference frames Maxwell's equations still has the same form,

$$\left. \begin{aligned} \mathbf{E}'_{//} &= \mathbf{E}_{//}, & \mathbf{E}'_{\perp} &= \gamma(\mathbf{E}_{\perp} + \boldsymbol{\beta} \times \mathbf{B}_{\perp}) \\ \mathbf{B}'_{//} &= \mathbf{B}_{//}, & \mathbf{B}'_{\perp} &= \gamma(\mathbf{B}_{\perp} - \boldsymbol{\beta} \times \mathbf{E}_{\perp}) \\ \mathbf{D}'_{//} &= \mathbf{D}_{//}, & \mathbf{D}'_{\perp} &= \gamma(\mathbf{D}_{\perp} + \boldsymbol{\beta} \times \mathbf{H}_{\perp}) \\ \mathbf{H}'_{//} &= \mathbf{H}_{//}, & \mathbf{H}'_{\perp} &= \gamma(\mathbf{H}_{\perp} - \boldsymbol{\beta} \times \mathbf{D}_{\perp}) \\ \mathbf{J}'_{//} &= \gamma(\mathbf{J}_{//} - \boldsymbol{\beta} \rho), & \mathbf{J}'_{\perp} &= \mathbf{J}_{\perp} \\ \rho' &= \gamma(\rho - \boldsymbol{\beta} \cdot \mathbf{J}_{//}) \end{aligned} \right\} \quad (46)$$

where

$$\gamma = \left(\sqrt{1-\beta^2} + \beta/\Phi \right)^{-1} \quad (47)$$

It can be seen that the new transform still kept the beautiful symmetry.

3.3.3. The Doppler Effect and the Invariance of Phase Angle

For the monochromatic plane wave $e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)}$, if the space coordinate and time are transformed by (38) (39) respectively, the frequency ω and wave vector \mathbf{k} of are transformed by the following equations

$$\left. \begin{aligned} k'_x &= \gamma(k_x - b\omega/c) \\ k'_y &= k_y \\ k'_z &= k_z \\ \omega' &= \gamma(\omega - \beta c k_x) \end{aligned} \right\} \quad (48)$$

$$\omega' = \omega \left[1 - \beta \cos(x^k) \right] \gamma \quad (49)$$

where k is in the $x-y$ coordinate plane. Then it could be prove that the phase angle transformation between two inertial frames is

$$\psi' = k'r' - \omega't' = kr - \omega t = \psi \quad (50)$$

so in the new special relativity the phase angle of monochromatic plane wave is still a Lorentz invariant.

3.4. Evaluation of the Particle's Intrinsic Time-Space Ratio and the Intrinsic Time Height

Using above those results we can design two ideal experiments respectively to evaluate the particle's intrinsic time-space ratio Φ and the particle's intrinsic time height T^* .

3.4.1. Evaluation of the Particle's Intrinsic Time-Space Ratio

The new mass equation indicates that when $u = c$ there is no the infinity but the finite maximum value of the mass, then let us imagine as follows: In the earliest period of the universe big bang, an "observer" saw that there were newly generated two neutrons to each other separation at the light speed in a same straight line that he was as center, thus the "observer" did first measurement to the two neutrons system. According to (40), the life of neutron moving at light speed is $\sim 10^{19}$ times of the rest neutron, which equals $\sim 3 \times 10^{14}$ years and greatly exceeds the universe age $\sim 1.38 \times 10^{10}$ years, so the "observer" can still do the second measurement of the two neutrons system. Clearly, the time interval Δt between twice measurements is the maximum of all time intervals, that about equals the universe's age τ_0 . Substituting $\Delta t = \Delta t_{\max} = \tau_0$ into the uncertainty relation formula

$$\Delta E \geq \frac{\hbar}{2\Delta t} \quad (51)$$

to get in twice measurements the minimum value of the uncertain energy

$$\Delta E_{\min} = \frac{\hbar}{2\Delta t_{\max}} = \frac{\hbar}{2\tau_0} \quad (52)$$

However, what is the specific form of energy corresponding ΔE_{\min} ? In general, the specific form of energy must satisfy two conditions: First, it is physically real; Second, it has the lowest strength. The observer saw that these two neutrons are in the movement at the speed of light, then the average kinetic energy of particle is a very large value, so ΔE_{\min} is not about the kinetic energy but a certain kind of potential energy. For two each other distant neutrons, there is only a gravitational potential energy in all kinds of potential energies, and when two neutrons are in the most distant the strength of gravitational potential energy has the minimum value. Therefore, the real ΔE_{\min} is only the gravitational potential energy when the distance of two neutrons is maximum. Today's observer sees, the distance between two neutrons is so large that the gravitational field certainly is the weak field, and because their velocity vectors are in a same straight line, so the Newton's gravity equation can be used to calculate the minimum of gravitational potential energy U_{\min} of this two-neutrons system, but the mass substituted into the equation is not the rest mass $m_{0(n)}$ but $\bar{m}_c = \Phi m_{0(n)}$ given by (31), so

$$\Delta E_{\min} = U_{\min} = \frac{G(\Phi m_{0(n)})^2}{2R_0} \quad (53)$$

In addition, for the expression of the universe age, we require an in-depth analysis. Two neutrons predecessors, *i.e.* quarks and so on primordial particles, were from a same cosmic singularity starting, the big bang caused they fly at the light speed at that time. If the subsequent expansion of the universe is roughly uniform and isotropic, today's "observer" and the two neutrons must be on those locations of the great circle shown in **Figure 2**.

As is known, at different periods the universe expansion speed is variable, so the universe age τ_0 is not equal to the great circle radius R_0 divided by the today's light speed c , namely $\tau_0 \neq R_0/c$. However, taking into there is always a same light speed at a same period, *i.e.* on a same great circle, so the universe age should be expressed as the ratio of the quarter of great circle perimeter to the light speed, that is

$$\tau_0 = \frac{\pi R_0}{2c} \quad (54)$$

(53) (54) into (52), to ultimately get

$$\Phi = \sqrt{\frac{2\hbar c}{\pi G m_n^2}} \quad (55)$$

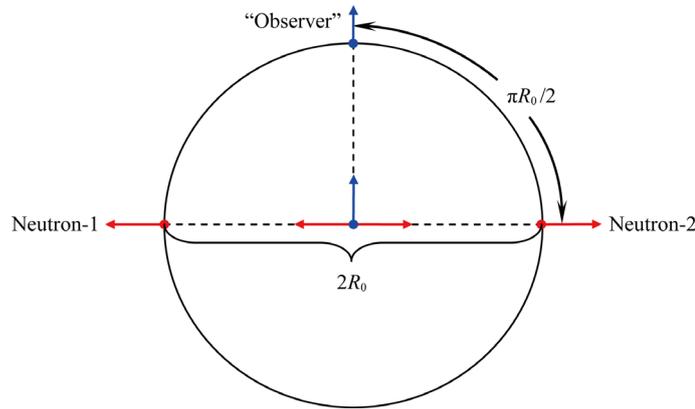


Figure 2. Schematic diagram of the ideal experiment of “two-neutrons”.

All factors of the (55) right side have the known exact value, so $\Phi = 1.037 \times 10^{19}$ is directly calculated, which has previously been given in (5).

It can be seen that Φ is an important constant that reflects the feature of PSTC model as well as the differences between new equations and old equations of the special relativity. Φ value is very large but after all is limited, if it is seen as infinite, new equations will immediately degenerate into old equations. When the speed is not extremely close to the light speed or not extremely close to zero, the difference of the new with the old equations are very small.

Finally it must be noted that the particle that fits this ideal experiment only is the neutron and not any other particles, for the following reasons: So far all astronomical observations and experimental facts show that the weak gravitational source substances satisfying Newton’s gravitation law have all the structural unit with the nucleons as main component, so the real and stable “basic gravitational charge” must be nucleons. In addition, in order to avoid electromagnetic interaction so only the neutron is chosen.

3.4.2. Evaluation of the Particle’s Intrinsic Time Height

We can design another ideal experiment to deduce the formula (6) calculating the particle intrinsic time height. Let us imagine that an observer is measuring the energy of a slow-moving free-particle, such as an electron. He can choose an appropriate way to satisfy always the particle speed $u \ll u_d$ after each measurement, so in twice successive measurements the attainable maximum of uncertainty energy is certainly

$$\Delta E_{\max} = m_R c^2 \tag{56}$$

which correspond to once occur in $\zeta = 0$ state, another occurs at $\zeta = 1$ state. (56) into the uncertainty relationship (2), to obtain $\Delta t \geq \hbar / 2m_R c^2$. According to [Corollary 3], the time interval Δt between twice measurements can be sufficiently large but can not be arbitrarily small, so if Δt takes the minimum value i.e. the particle’s apparent time height T , then the inequality $\Delta t \geq \hbar / (2m_R c^2)$ becomes the equality $T = \hbar / (2m_R c^2)$, further (3) (20-1) into which and taking $u \rightarrow 0$, (6) is got.

4. Applying New Special Relativity to Solve Several Problems

4.1. On the Lorentz Invariance Violation and the GZK Suppression of UHECR

About this issue, the new special relativity gives three levels theoretical results which consistent with observations of HiRes and Auger: First, pointed up the existence of Lorentz invariance violation is inevitable and the LIV coefficient ξ can also be strictly calculated by (35); Second, although existed the LIV effect, for above 4×10^{19} eV UHECR protons the calculated $|\xi| < 4.5 \times 10^{-30}$, which indicates that LIV effect too weak to change the GZK cutoff; Third, although existed the GZK suppression not rule out possible appearing a very few random events beyond GZK energy. Now, detailed as follows.

The people have known that the higher than 10^{18} eV UHECRs, in propagating from the extragalactic sources to the Earth, interact with CMB photons to result in a decline of their energy and flux and finally cause the spectrum suppression at $(3 - 6) \times 10^{19}$ eV, that is the GZK cutoff predicted by Greisen, Zatsepin and Kuzmin in

1960s [7] [8]. However by the 1990s, the AGASA [9] experiment results show an extension of the spectrum beyond the GZK cutoff, so the GZK mechanism based on the special relativity is challenged. For this reason, S. R. Coleman and S. L. Glashow [10] introduced a theory of Lorentz invariance violation (LIV), a tiny correction term $\xi(cp)^2$ is added into the energy-momentum relationship, namely

$$E^2 = E_0^2 + (cp)^2 + \xi(cp)^2 \tag{57}$$

Thus, if the coefficient absolute value $|\xi|$ is just as small as $\sim 10^{-23}$ enough to eliminate the GZK cutoff. However, in 2008, the HiRes Collaboration announced to confirm the GZK cutoff with a 5σ standard deviation [1] and then the Auger collaboration gives the result consistent with HiRes and rejects a single power law spectrum above 4×10^{19} eV with a 6σ standard deviations [2]. Therefore the data of HiRes and Auger can set constraints on the LIV. The current common research way on this problem is from different ξ values to calculate the energy spectrum, then comparison with the data of Auger and HiRes thereby find the most fitting ξ value as the constraint on LIV, obviously this phenomenological study cannot reveal the nature of problem.

Here let us use the new Equation (34) of the special relativity to solve this problem. Although (34) and the Coleman-Glashow formula (57) both have the same form (I even deliberately use the same symbol ξ), their origins and meanings are completely different. A detailed account of (34) characteristics and significance is as follows:

1) (34) is derived out from a basic Equation (29) of the new special relativity, so the occurring of $\xi(cp)^2$ is inevitable, which does not require reluctantly to add. In fact, the existence of so-called Lorentz invariance violation effect is one of inherent features of the new special relativity.

2) The LIV coefficient ξ is a function of the speed and has the strict expression *i.e.* (35), so ξ is a theoretical value independently calculated before the experimental observation, not by fitting observation data to adjust.

3) (29) points out, for all kinds of particle the physical quantity with common upper limit is just the speed *i.e.* the light speed c (not other physical quantities, e.g., energy). When $u = c$, the particle energy is not the infinity but a limited maximum (see (31)), so for different particles according to their different rest energy E_0 there are different maximal attainable energies (and not different maximal attainable speeds).

4) (35) shows, the higher the speed u , the smaller (and not the larger!) the coefficient absolute $|\xi|$, when $u = c$ it attains the minimum value $|\xi|_{\min} = \Phi^{-2} \approx 10^{-38}$.

5) When $u < u_i$ Lorentz energy E_R and speed u is one to one, so via (20-1) E_R can replace u then (35) is rewritten as

$$\xi = -\frac{1}{\Phi} \left(\frac{2}{\sqrt{(E_R/E_0)^2 - 1}} + \frac{1}{\Phi} \right) \tag{58}$$

In the energy region $E_0 \ll E_R \ll \Phi E_0$, (58) can be simplified to

$$\xi \approx -\frac{2E_0}{\Phi E_R} \tag{58'}$$

For the UHECR spectrum ankle region protons and ^{56}Fe , we use (58') to specifically calculate the LIV coefficient values and list to **Table 4**.

To above 4×10^{19} eV protons, the calculated $|\xi| < 4.5 \times 10^{-30}$. By comparison with some fitting calculations [11] [12], it can be seen, although (34) has expected that there is the Lorentz invariance violation effect, the violation coefficient $|\xi|$ is too small to change the GZK suppression of UHECR spectrum, which is consistent with experimental results that the HiRes collaboration and the Auger collaboration confirm the GZK suppression with a 5σ standard deviation [1] [2].

Table 4. Values of LIV coefficient of different energy UHECR protons and ^{56}Fe .

Energy E_R ($\times 10^{19}$ eV)		0.5	1	3	4	6	8	10	20
LIV coefficient	Proton ($\times 10^{-30}$)	36.2	18.1	6.0	4.5	3.0	2.3	1.8	0.9
absolute value $ \xi $	^{56}Fe ($\times 10^{-28}$)	20.3	10.1	3.4	2.5	1.7	1.3	1.0	0.5

On the other hand, we know that events beyond GZK energy were also really recorded in cosmic ray observation, in order to explain this phenomenon, it is necessary to use the basic Equation (19-1). As described above, (34) is derived from (29), and (29) is derived from (19). The mass of composite particles is usually embodied as the mean mass \bar{m} described by (29) that has contained the all influence of the random variables ζ , however, for the proton as most simple composite particle, when its energy is very high the random variable ζ still has some influence, and therefore the high-speed low-energy (HSLM) effect has still a certain degree of performance.

Now let us imagine that a group of beyond the GZK energy protons from an extragalactic source which is more distant than the mean free path fly to the Earth. In this process, a very few of protons could appear in certain HSLM state in some time. Because at the HSLM state the energy and the relative cross-section are both smaller than the normal values, therefore the possibility that the HSLM protons interact with the CMB photons will be smaller than of the normal protons, thereby they can propagate farther than the normal mean free path. If arriving Earth before restored to the normal $\zeta = 1$ state, then the Earth will receive the over GZK energy event. Of course, such event is very rare. To summarize, although the tiny LIV coefficients $|\xi|$ will not change the GZK cutoff, yet not rule out the possibility that a very few of beyond GZK energy protons reach the Earth, moreover, occurring such small probability events beyond GZK energy is random and do not constitute a single power-law spectrum, which are all consistent with Auger observation [2].

4.2. On the Observer Independence of the Planck Energy and the Doubly Special Relativity

2002, J. Magueijo and L. Smolin modified Einstein's special relativity and proposed the "doubly special relativity (DSR)", of which one of four basic principles is the observer independence of the Planck energy [3]. Below we prove that this "basic principle" can be derived by the new special relativity.

Considering a particle at a velocity u moves along the x axis of an inertial frame Σ , its energy and momentum are $\bar{E} = \bar{m}c^2$ and $\bar{p}_x = \bar{m}u$ relative to the observer in inertial frame Σ . In another inertial frame Σ' at speed $v = c\beta$ moving along the x axis relative the Σ , the particle's energy \bar{E}' and momentum \bar{p}'_x are transformed by (44) (45) respectively. When the particle speed $u = c$ relative to the observer of the inertial frame Σ , its mass attains the maximum $\bar{m}_{\max} = \Phi m_0$ (see (31)), thus its energy and momentum attain also the maximum $\bar{E}_{\max} = \Phi m_0 c^2$ and $\bar{p}_{\max} = \Phi m_0 c$. Putting \bar{E}_{\max} and \bar{p}_{\max} into (44) and (45), the calculations are $\bar{E}'_{\max} = \Phi m_0 c^2$ and $\bar{p}'_{\max} = \Phi m_0 c$ respectively, so whether in the Σ or Σ' this particle's energy all attain the maximum value of the same, however, the relative velocity v between two inertial systems has no any impact. The above calculation has proved an important result, that is, when moving at the strict light speed c , each particle can attain its own maximal mean mass Φm_0 (or energy $\Phi m_0 c^2$), which is the invariant independent of the observers.

As a special case, we use (31) and (55) to calculate the maximum value of the mean mass of neutron

$$\bar{m}_{\max(n)} = \Phi m_{0(n)} = \sqrt{\frac{2\hbar c}{\pi G m_{0(n)}^2}} \cdot m_{0(n)} = \sqrt{\frac{2\hbar c}{\pi G}} = M_P \sqrt{\frac{2}{\pi}} \quad (59)$$

where, $m_{0(n)}$ denotes the rest mass of neutron, $M_P = \sqrt{\hbar c/G}$ is the Planck mass. (59) shows, the Planck mass (or energy) and the maximum value of the neutron average mass (or energy) both are in the same order of magnitude, their distinguish is only a constant factor $\sqrt{2/\pi}$. Because the maximum of neutron mean mass (or energy) is the invariant independent of the observers, so the Planck mass (or energy) also is necessarily the invariant independent of the observers, that is, there is the observer independence of the Planck energy.

In addition, we prove that an important formula of DSR can be derived by (29). According to (20-1), letting the Lorentz mass m_R and the rest mass m_0 replace the speed ratio u/c , then (29) is written in the following form

$$\bar{E} = \frac{m_R c^2}{1 + \frac{m_R \sqrt{1 - (m_0/m_R)^2}}{\Phi m_0}} \quad (60)$$

When $m_R \gg m_0$, it can be simplified to

$$\bar{E} = \frac{m_R c^2}{1 + \frac{m_R}{\Phi m_0}} \quad (61)$$

At the same speed the mass ratio m_R/m_0 of any kind of particles can be replaced with the neutron's mass ratio $m_{R(n)}/m_{0(n)}$, so

$$\bar{E} = \frac{m_R c^2}{1 + \frac{m_{R(n)}}{\Phi m_{0(n)}}} \quad (62)$$

According to (59), the Planck mass M_p and the neutron's mean mass maximum $\Phi m_{0(n)}$ are in the same order of magnitude, their difference is just on a constant factor $(2/\pi)^{1/2} \approx 0.8$, so $\Phi m_{0(n)}$ can be substituted by M_p to write (29) as

$$\bar{E} \approx \frac{m_R c^2}{1 + \frac{m_{R(n)}}{M_p}} \quad (63)$$

It is interesting, the DSR also has such a similar formula [3], which even is as the highlight [13].

Now it has been seen that the DSR's one basic principle and a similar to (63) result all can be proved by the new special relativity. However, this does not mean that my new special relativity and the DSR are the same thing, in essence they are different in not only the theoretical fundamentals but also some typical results. For example, the new special relativity has proved that the Planck energy cannot serve as the common upper limit of the energy of all kinds of particles, and indicate that of importance is not the Planck energy but the parameter Φ describing the particle's intrinsic space-time feature. Another example, as described in Section 4.1, the formula (35) calculating LIV coefficient ξ point out, the higher the speed, the weaker the LIV effect, thus to prophesy that the GZK cutoff of UHECR will not change. However, in theories of the DSR as well as superstrings, loop quantum gravity and so on there are no such contents.

4.3. On the Hubble Constant and the Dirac Large Numbers

4.3.1. A Relation Formula between the Hubble Constant and Several Basic Constants Is Derived, Thus Theoretically Calculated the Hubble Constant $H_0 = 70.937 \text{ km}\cdot\text{s}^{-1}\cdot\text{Mpc}^{-1}$

(32) (33) show that there is a specific speed u_q being extremely nearing 0, when $u = u_q$, the particle's mean mass has a minimum value. Let us conceive that in an inertial frame without existence of any force field, there is a free electron moving at the speed u_q from the coordinate origin starting. According to Hubble law, the coordinate origin as center and a_q as radius spherical surface is expanding by the speed u_q along with the universe expansion, where

$$a_q = \frac{u_q}{H_0} \quad (64)$$

Because in the real universe this expansion is inevitable, so even though there is no any external forces, but the electron moving at u_q can only be confined within the sphere of radius as a_q , that is, the electron is equivalently at the lowest energy E_{10} of the infinite deep ball square potential well of radius as a_q [14],

$$E_{10} = \frac{\pi^2 \hbar^2}{2m_e a_q^2} \quad (65)$$

where, m_e denotes the rest mass of electron. On the other hand, because u_q value is very small, so in accordance with the classical mechanics this electron's kinetic energy is expressed as

$$K_q = \frac{m_e u_q^2}{2} \quad (66)$$

Noting (65) is a derived result of the Schrodinger equation, and the energy operator in Schrodinger equation is

of corresponding the classical mechanics, so there must be

$$K_q = E_{10} \quad (67)$$

By (32) and (64)-(67) thus obtaining another Φ expression:

$$\Phi = \sqrt{\frac{m_e c^2}{\pi \hbar H_0}} - 1 \quad (68)$$

According to the magnitude of the “today” H_0 value it can be seen $\frac{m_e c^2}{\pi \hbar H_0} \gg 1$, so (68) is written as

$$\Phi = \sqrt{\frac{m_e c^2}{\pi \hbar H_0}} \quad (69)$$

Here it must be noted that the particle that fits above ideal experiment only is the electron and not any other particles, for the following reasons: 1) According to the PSTC model, only to the particles of quarks/leptons level the speed uq can be defined, so composite particles are rejected; 2) Particles must be in the free state, so only the leptons can be selected; 3) Because neutrinos are always in the oscillation so also are rejected; 4) The life of μ lepton and τ lepton are too short to meet the requirement of a long time and stable movement, so only the electron is qualified.

Combining (69) with (55), a relationship between the Hubble constant and several basic constants is obtained:

$$H_0 = \frac{c G m_e m_n^2}{2 \hbar^2} \quad (70)$$

All factors of (70) right side have known accurate values, so we can use this formula to exactly calculated

$$H_0 = 2.299 \times 10^{-18} \text{ s}^{-1} = 70.937 \text{ km} \cdot \text{s}^{-1} \cdot \text{Mpc}^{-1} \quad (71)$$

(32) (70) into (64) calculated $a_q = 1.26 \times 10^4 \text{ km}$, so our theoretical value is the “near-place” Hubble constant.

Generally believed that the Hubble law is an empirical law and the Hubble constant is obtained by astronomical observations. However, the theoretical result (70) is derived from a non-point model of microscopic particles, in its deductive process the Hubble law is used but does not involve any astronomically observed quantity (such as the redshift, the luminosity), which indicates that the theoretical value (71) is completely independent to astronomical observation, so its comparison with the measuring value of Hubble constant is a persuasive way to test the new special relativity. It is noted that after long efforts the enough credible observed values of the Hubble constant have been obtained, such as the final measurement result of Hubble space telescope key project [4] for $H_0 = 72(71) \pm 4 \pm 7 \text{ km} \cdot \text{s}^{-1} \cdot \text{Mpc}^{-1}$, the exciting is my theoretically calculated value is well consistent with this observed value.

4.3.2. Exposing the Mystery of Dirac Large Numbers

Dirac long noted, there are two approximately equal non-dimensional large numbers,

$$N_1 \approx N_2 \approx 10^{40} \quad (72)$$

N_1 is the ratio of the universe Hubble radius to the electron classical radius, N_2 is the ratio of the static electricity force to the gravitation between proton and electron. In addition there are a series of large pure numbers, which are roughly equal with integer powers of $N_1^{0.5} \approx 10^{20}$ respectively, and can all be attributed to a “mysterious numbers relation” pieced together by the dimension and order of magnitude [15]

$$\sqrt[3]{\frac{\hbar^2 H_0}{cG}} \approx m_\pi \quad (73)$$

or

$$H_0 \approx \frac{c G m_\pi^3}{\hbar^2} \quad (73')$$

where m_π denotes the π meson mass. Dirac considered that the correlation between large numbers, in par-

ticular the numbers relationship given by (73) is not a meaningless coincidence, but implies there should be a fundamental fact that has not yet been elucidated. In view of this, he proposed the famous large numbers assume that: Any two dimensionless large numbers that appear in nature are related to each other, they are linked by a simple mathematical relationship [16].

The Dirac large numbers problem as a mystery to the people left a deep impression, however, so far on this problem did not achieve breakthroughs. Why exists such a mysterious numbers relation (73)? What is the elusive basic fact hiding at behind those large numbers? Dirac had reward to seek answers the questions has not been deciphered.

It is interesting that in our new special relativity there is also a dimensionless large number of approximately $N_1^{0.5}$, that is the parameter $\Phi = 1.038 \times 10^{19}$ describing the geometry characteristic of intrinsic spacetime of particle. In particular, we use the new mass equation to logically derive out the strict and exact relationship (70) between the Hubble constant and a number of fundamental constants. Comparing (70) with (73'), it can be seen that (70) as a rigorous theoretical results has done a thorough clarification for the Dirac's pieced "mystery numbers relation". Now via (55) (69) (70), we can use Φ as the element to one by one analysis for those bewildering large numbers, for example as follows:

The ratio of the Hubble radius to the electron classical radius

$$N_1 = (\pi/\alpha)\Phi^2 = 4.64 \times 10^{40} \approx (10^{20})^2$$

The ratio of the static electricity force to the gravitation between proton and electron

$$N_2 = (\pi\alpha/2\varepsilon)\Phi^2 = 2.27 \times 10^{39} \approx (10^{20})^2$$

The ratio of the electron classical radius to the Planck length

$$N_3 = (\pi/2)^{0.5} (\alpha/\varepsilon)\Phi = 1.74 \times 10^{20} \approx 10^{20}$$

The ratio of the Planck length to the Schwartzchild radius of proton

$$N_4 = (\pi/8)^{0.5} \Phi = 6.50 \times 10^{18} \approx 10^{20}$$

The ratio of the Hubble radius to the Schwartzchild radius of proton

$$N_5 = (\pi^2/4\varepsilon)\Phi^4 = 5.26 \times 10^{79} \approx (10^{20})^4$$

where α denotes the fine structure constant, ε denotes the ratio of mass of electron to proton. Above formulas show: 1) Every one of large numbers all contain the factor Φ ; 2) The integer powers of Φ determines the order of magnitude of large numbers; 3) These large numbers are not vague, they have the exact number, their details are determined by dimensionless small numbers α, π, ε .

Based on the above analysis it can be considered that the Dirac large numbers principle is a secondary effect, the important thing that hides at behind the relevance of large numbers is the particle's intrinsic space-time feature described by parameter Φ , this should be that Dirac had been looking for but never found the "basic fact".

5. Experimental Test of the New Mass Equation

In Section 3.1 [III], it has been pointed out, the new mass equation predicts that there is a unusual "high speed-low mass (HSLM) effect" in motion of particles. The HSLM effect is very weak, however, in the electron storage rings with high current and long time running we could still observe abnormal phenomenon caused by it, that is, an emission of super-high energy electrons much higher than the beam energy in the RF cavity downstream direction. By detecting such small probability abnormal events we can test the new mass equation. In the NSRL800MeV electron storage ring, I used the lead plates-X films detector to cumulatively detect for a long time, preliminary experiment results hinted the signs of existence of super-high energy electrons [17]. To this end I propose an experimental plan and I hope physicists in large electronic accelerator laboratories to complete this interesting exploratory experiment.

5.1. Experimental Principle

According to (19.1), at a same speed, the mass m of HSLM electron in $\zeta < 1$ state is smaller than the mass

m_R of normal electrons in $\zeta = 1$ state, *i.e.* $m = m_R(3\zeta^2 - 2\zeta^3) < m_R$. In the electron storage ring, so when the beam passes through the accelerating electric field, HSLM electrons in the beam will be accelerated more quickly than normal electrons. If these abnormal electrons return to the most probable $\zeta = 1$ state before reaching the deflection magnetic field, their energy E_R^* will certainly be higher than the normal electrons energy E_R , thereby an abnormal emission of electrons much higher than the beam energy will appear in the RF cavity downstream direction (see **Figure 3**).

5.2. Characteristics of Super-High Energy Electrons

1) Strength: Using (19-1) (23') (24) (15) it can be proved that numbers of super-high energy electrons may appear per hour

$$n = \frac{25.6E_R IU^2}{e\Phi E_0 (E_R^* - E_R)^2} \approx \frac{30E_R IU^2}{(E_R^* - E_R)^2} \tag{74}$$

where, E_R^* (MeV) denotes the energy of super-high electron; E_R (MeV) denotes the energy of beam; U (MV) denotes the accelerating voltage; I (mA) denotes the average current intensity; E_0 (MeV) is the rest energy of electron; e (C) is the electron charge. So in $E_{R2}^* \geq E_R^* \geq E_{R1}^*$ the numbers of super-high energy electrons may appear per hour

$$N_{21} \approx 30IU^2 \left(\frac{1}{E_{R1}^* - E_R} - \frac{1}{E_{R2}^* - E_R} \right) \tag{75}$$

In existing electron storage rings, calculated N_{21} values are all very small, such as, if $E_R = 2000$ MeV, $U = 1.5$ MV, $I = 500$ mA, about average 1 hour appearing 1 event of super-high energy electrons of $E_R^* \geq 34,000$ MeV.

2) Energy-positional distribution: Shown in **Figure 3**, the extension line of beam in straight section (*i.e.* the tangent line of beam in deflection section) as the y axis and the bending magnet starting point as the origin point to establish a coordinate system. For different electron storage rings, according to the beam energy, the magnetic field strength and the machine structure parameters, a relation between the energy E_R^* of super-high energy electron and the injection point coordinate x at the absorber can be deduced. For example, the electron storage ring in **Figure 3**, if $E_R^* \gg E_R$, there is

$$E_R^* \approx \frac{a(a+2b)E_R}{2rx} \tag{76}$$

where r is the normal bending radius of beam in the bending magnetic field; a is the length of first bending magnetic field; b is the distance between the exit end of first magnetic field and the absorber.

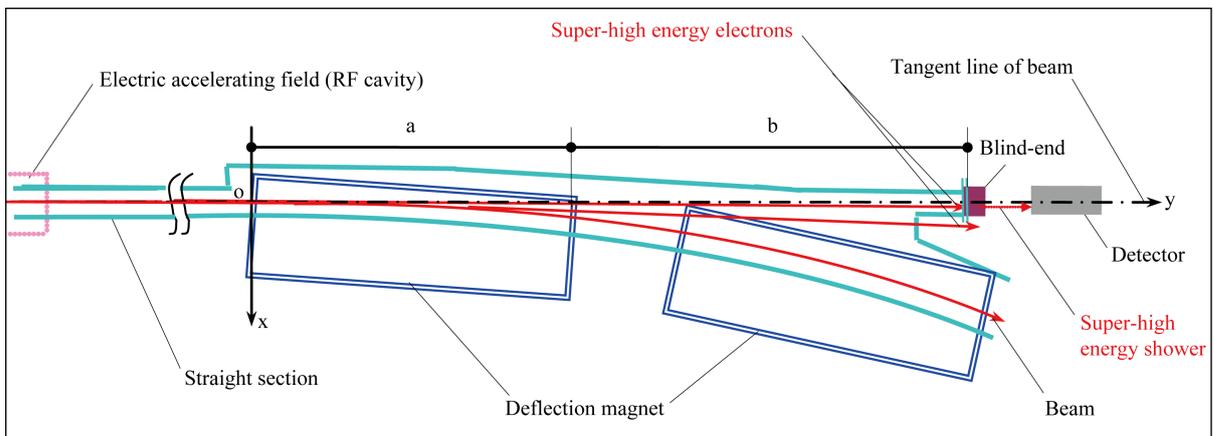


Figure 3. New equations expect that in the electron storage ring RF cavity downstream direction there are small probability events of emission of unusual electrons whose energies are much higher than the beam energy.

5.3. Feasibility of Experiment

The super-high electrons occurring in electron storage rings are very rare, but it is still feasible to detect such small probability events by existing experimental techniques, which because:

1) Electron storage rings have higher current and can run continuously for a long time, so to facilitate the long-term search and cumulative record. And, to many electron storage rings, in the RF cavity downstream direction occurring super-high energy electrons, the beam pipeline of synchrotron radiation are not installed and the vacuum chamber is only closed by the blind end, which facilitate the placement of detector.

2) The sampling electromagnetic calorimeter can be used as a detector, and such detectors are mature technologies. Because the copper blind-end is very thick, the super-high energy electron injects in which will occur electromagnetic cascade shower, so the detector will in fact accept such the secondary particles shower. To the sampling electromagnetic calorimeter, the copper blind-end is equivalent to its front-side absorber. Of course, it is best to place the detector to inside of the vacuum chamber of storage ring. In addition, taking into the residual gas bremsstrahlung along the straight section axis is a main interference, so in order to reduce its impact, the detector should be appropriately off-axis placed.

6. Conclusions

Could the special relativity and the quantum mechanics unify at deeper level via a way different from the quantum electrodynamics? This is a potential big problem which should not be overlooked; In recent years, about whether existing the Lorentz invariance violation has become a hot topic of extensive discussions; Since the superstring theory driven, the way using a non-point particle model to replace the concept of mass point to seek developments of theory has been widely accepted. Under this context, therefore, it is imperative to try to use the basic principles of quantum mechanics, especially the uncertainty principle to further improve the special relativity. This paper is in this direction an independent research and useful contribution.

This work is first based upon the space spherical symmetry of 3-dimensional and the translational symmetry of time, and the uncertainty principle, to establish a 4-dimensional space-time cylinder model of the quarks and leptons. Then, we use this model to deduce a series of new equations that are compatible with old equations of special relativity and also satisfy the uncertainty principle, thereby achieve unifying special relativity and quantum mechanics in basic concepts. New equations which reveal the concepts of space, time, mass, energy etc. have richer connotations, so that can help people to re-understand the essence of some physical phenomena and solve several pending important problems. The results derived by new equations show:

1) The mass is a binary function of speed u and another dimensionless variable ζ ($0 \leq \zeta \leq 1$). The random variable ζ that appears in the derivation process of equation makes the concepts of randomness and probability automatically enters the relativistic equations.

2) When $u = c$ the energy is not the infinity but a finite maximum value $E_{\max} = 1.555 \times 10^{19} m_0 c^2$. This result will eliminate the divergence difficult, and lay a foundation for building a new quantum field theory without re-normalization.

3) The violation of Lorentz invariance is inevitable and the LIV coefficient ξ can be strictly calculated. To above 4×10^{19} eV UHECR protons, the calculated $|\xi| < 4.5 \times 10^{-30}$, so although there is the LIV effect $|\xi|$ is too small to change the GZK cutoff, which is consistent with observations of HiRes and Auger.

4) It is proved that the Planck energy is a Lorentz invariant, so there is certainly “the observer independence of Planck energy”. However it is also proved that the Planck energy isn’t the common upper limit of energy of all kinds of particles.

5) A relation formula between the Hubble constant and several basic constants is derived, thus the theoretical value $H_0 = 70.937 \text{ km} \cdot \text{s}^{-1} \cdot \text{Mpc}^{-1}$ is obtained, which is well consistent with the final result of observation of HST key project. The mystery of Dirac large numbers can be clarified too by this relation formula.

6) An unusual effect is predicted, and accordingly expected that in the electron storage ring RF cavity downstream direction there is an emission of rare unusual electrons of much higher than the beam energy. New equations can be tested by searching for such small probability events.

References

- [1] HiRes Collaboration (2008) *Physical Review Letters*, **100**, Article ID: 101101. [arXiv:astro-ph/0703099]

- <http://dx.doi.org/10.1103/PhysRevLett.100.101101>
- [2] Auger Collaboration (2008) *Physical Review Letters*, **101**, Article ID: 061101. [arXiv:0806.4302]
<http://dx.doi.org/10.1103/PhysRevLett.101.061101>
- [3] Magueijo, J. and Smolin, L. (2002) *Physical Review Letters*, **88**, Article ID: 190403. [arXiv:hep-th/0112090v2]
<http://dx.doi.org/10.1103/PhysRevLett.88.190403>
- [4] Freedman, W.L., Madore, B.F., Gibson, B.K., Ferrarese, L., Kelson, D.D., Sakai, S., *et al.* (2001) *Astrophysical Journal*, **553**, 47-72. [arXiv:astro-ph/0012376v1]
- [5] Einstein, A. (1955) *Relativity: The Special and the General Theory*. Note to the Fifteenth Edition, Methuen & Co. Ltd., London.
- [6] Landau, L.D. and Lifschitz, E.M. (1977) *The Quantum Mechanics*. English Translation, Pergamon.
- [7] Greisen, K. (1966) *Physical Review Letters*, **16**, 748. <http://dx.doi.org/10.1103/PhysRevLett.16.748>
- [8] Zatsepin, G.T. and Kuzmin, V.A. (1966) *Pisma Zh. Eksp. Teor. Fiz.*, **4**, 114-117.
- [9] Takeda, M., Hayashida, N., Honda, K., Inoue, N., Kadota, K., Kakimoto, F., *et al.* (1998) *Physical Review Letters*, **81**, 1163-1166. [arXiv:astro-ph/9807193] <http://dx.doi.org/10.1103/PhysRevLett.81.1163>
- [10] Coleman, S. and Glashow, S.L. (1999) *Physical Review D*, **59**, Article ID: 116008. [arXiv:hep-ph/9812418v3]
<http://dx.doi.org/10.1103/PhysRevD.59.116008>
- [11] Scully, S.T. and Stecker, F.W. (2009) *Astroparticle Physics*, **31**, 220-225. [arXiv:0811.2230v4]
- [12] Bi, X.J., Cao, Z., Li, Y. and Yuan, Q. (2009) *Physical Review D*, **79**, Article ID: 083015. [arXiv:astro-ph/0812.0121]
<http://dx.doi.org/10.1103/PhysRevD.79.083015>
- [13] Magueijo, J. (2003) *Faster than the Speed of Light*. Perseus Publishing, New York.
- [14] Zeng, J.Y. (1981) *Quantum Mechanics*. Science Press, 209-212.
- [15] Dirac, P.A.M. (1937) *Nature*, **139**, 323. <http://dx.doi.org/10.1038/139323a0>
- [16] Weinberg, S. (1980) *Gravitation and Cosmology: Principles and Applications of the General Theory of Relativity* (1972). Chinese Translations, Science Press, 724-726.
- [17] Qian, D.P. (2010) *Journal of Liaoning University, Natural Sciences Edition*, **37**, 236-240.

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