

# Hedging with Stock Index Options: A Mean-Extended Gini Approach

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## ABSTRACT

One of the more efficient methods to hedge portfolios of securities whose put options are not traded is to use stock index options. We use the mean-extended Gini (*MEG*) model to derive the optimal hedge ratios for stock index options. We calculate the *MEG* ratios for some main stocks traded on the Tel Aviv Stock Exchange and compare them to the minimum-variance hedge ratios. Computed for specific values of risk aversion, *MEG* hedge ratios combine systematic risk with basis risk. Our results show that increasing the risk aversion used in the computation reduces the size of the hedge ratio, implying that less put options are needed to hedge away each and every security.

**Keywords:** Hedge Ratios; Systematic Risk; Basis Risk; Risk Aversion; Mean-Gini

## 1. Introduction

In this paper we use the mean-extended Gini (*MEG*) model to derive optimal hedge ratios for portfolios with stock index options. Since their introduction in the earlier 1980's, stock index futures and options have allowed investors to manage equity portfolios by hedging against systematic risk. The main practical issue is to determine the proper hedge ratios, *i.e.*, the number of futures contracts or put options to be traded in order to insure the portfolio. Hedge ratios of stock index options are expected to reduce two types of risk: systematic risk of the portfolio and risk of futures hedging, for which reason it has become a major investment instrument.

The standard approach for reducing risk in futures hedging is to use minimum variance to maximize expected utility so as to determine the optimal hedge ratios. Another approach, which has been in practice for the past 15 years, is to use *MEG* hedge ratios. Contrary to minimum variance, *MEG* hedge ratios allow the incorporation of risk aversion intensity into the hedging coefficient. A comprehensive review of futures hedge ratios and, in particular, mean-Gini hedging can be found in Lien and Tse [1], and Chen, Lee and Shrestha [2]. *MEG* has also been used to investigate hedging effectiveness in futures commodities contracts by Shaffer [3], in FTSE contracts by Butterworth and Holmes [4], and in currency hedging by Shaffer and DeMaskey [5]. These papers confirm the superiority of the *MEG* model over the mean-variance model in futures hedging. Indeed, their results show that

*MEG* hedge ratios achieve greater risk reduction for all classes of risk-averse investors.

There are several main reasons why the *MEG* model should be used to insure a portfolio. First, *MEG* allows the derivation of hedge ratios that comply with the necessary and sufficient conditions for stochastic dominance. As such, the *MEG* model ensures that the hedge ratio is included in the second degree stochastic dominance (*SSD*) efficient set (Cheung, Kwan, and Yip [6]). Second, *MEG* ratios remedy the failures incurred by the interdependence of the price index and the error terms. In particular, the Gauss-Markov conditions required by the ordinary-least-squares (*OLS*) regression model may be violated and the results will not be validated as optimal hedge ratios. Thus, *MEG* ratios are consistent estimators for minimum variance ratios (Shalit [7]). Third, if the probability distribution of the stock price index is not normal, as would be expected based on empirical investigations, the *OLS* coefficients will draw most of their statistical significance from the extreme observations whereas with *MEG* all observations contribute more evenly to the power of the estimates (Shalit and Yitzhaki [8]).

In the next section we derive the theoretical hedge ratios using a portfolio hedging model with stock index put options. Then in the third section, we present a primer on mean-Gini theory whose purpose is to show why the *MEG* model has been used in futures hedging. In the fourth section, we use the mean-Gini methodology to derive the *MEG* hedge ratios with stock index put options.

In the fifth section, we apply this methodology to securities traded on the Tel-Aviv Stock Exchange and estimate the hedging ratios.

## 2. The Portfolio Insurance Model with Index Put Options

Consider a standard two-period model of portfolio insurance. An investor who holds a portfolio of  $n$  securities buys stock index put option contracts to limit the portfolio's downside risk. We assume this is the only available strategy because, as it is the case in many financial markets, futures contracts and options on individual stocks are not readily traded or lack liquidity. The initial portfolio value is:

$$w^0 = \sum_{i=1}^n \alpha_i S_i^0 \quad (1)$$

where  $S_i^0$  are the initial stocks prices and  $\alpha_i$  are their shares in the portfolio. To insure the portfolio against downside risk, the investor buys  $x$  index put options that expire at the end of the holding period at which time the hedged portfolio value is:

$$w^1 = \sum_{i=1}^n \alpha_i S_i^1 + x(P^1 - P^0) \quad (2)$$

where  $P^0$  and  $P^1$  are the initial and the final index put option prices and  $S_i^1$  are the final stock prices.

Our goal is to determine the hedge ratio that comprises the number of index contracts needed to insure the portfolio. When investors maximize expected utility of portfolio returns, the optimal hedge ratio can be obtained by using the mean-variance ( $MV$ ) model since, as shown by Levy and Markowitz [9],  $MV$  approximates expected utility, regardless of the utility and the probability distribution. Furthermore, Benninga, Eldor and Zilcha [10,11] showed that the optimal hedge ratio is equal to the minimum-variance hedge ratio which is:

$$x^* = - \sum_{i=1}^n \alpha_i \frac{\text{cov}(S_i^1, P^1)}{\sigma_p^2} = - \sum_{i=1}^n \alpha_i \delta_i \quad (3)$$

where  $\delta_i$  is the regression coefficient of the share price on the index put option price as follows:

$$S_i^1 = \delta_0 + \delta_i P^1 + \varepsilon_i \quad (4)$$

When the index put option is written on a wider market index, the hedge ratio can be decomposed into two elements. The first is the standard systematic risk  $\beta_i$  and the second is the sensitivity of the index to changes in the put option prices, or the inverse of the put option delta. Indeed from Equation (4), the optimal hedge ratios  $\delta_i$  are derived as:

$$\delta_i = \frac{dS_i}{dP} = \frac{dS_i}{dI} \cdot \frac{dI}{dP} = \beta_i \cdot \frac{1}{\Delta} \quad (5)$$

where  $I$  is the market index. The systematic risk  $\beta_i$  is obtained by regressing the share price over the market index  $I$ . The index put option delta,  $\Delta$ , is the rate of change of the put option with respect to the market index. Since the put option delta is identical for all assets in the portfolio, it does not affect the hedge ratio when the shares in the portfolio get changed.

The systematic risk  $\beta_i$  used for the hedge ratio is slightly different from the usual definition of beta because it is obtained by regressing the stock prices on the index underlying the put option, which is done as follows:

$$S_i = \beta_0 + \beta_i I + \varepsilon_i \quad (6)$$

For the hedge ratio to be optimal the regression model must be valid, *i.e.*,  $I$  and  $\varepsilon_i$  must be statistically independent. Since this condition may be violated, we propose to apply the *MEG* model to hedging in portfolio insurance. To understand the rationale of using this model, we begin with a brief review of the mean-Gini theory.

## 3. A Primer on Mean-Gini

Mean-Gini (*MG*) theory was originally developed by Yitzhaki [12,13]. Afterwards it was applied to finance by Shalit and Yitzhaki [14] as an alternative model to *MV* for evaluating systematic risk and constructing optimal portfolios that are consistent with expected utility maximization and stochastic dominance. *MG* presents robust results when *MV* is bound to fail, in particular, when assets are not normally distributed or when the regression used to estimate betas by ordinary least-squares provide biased estimators (Shalit and Yitzhaki [8]). Furthermore, *MEG* allows for the introduction of risk aversion differentiation into the estimation of systematic risk (Gregory-Allen and Shalit [15]). For these reasons, the *MEG* model has been used to estimate optimal hedge ratios in futures markets (see Lien and Tse (2002) [1] and Chen, Lee, and Shrestha, [2]).

The Gini coefficient is a measure of dispersion used mainly in income inequality where the index is related to the Lorenz curve. In finance, it quantifies risk similarly to the role played by the variance as a measure of risk. Gini's mean difference is defined as half the expected value of the distance between all pairs of returns. For portfolio returns  $w$ , it is written as:

$$\Gamma(w) = \frac{1}{2} E|w_1 - w_2|, \quad (7)$$

where  $w_1$  and  $w_2$  are independent realizations of the portfolio returns. This definition of the Gini can be developed into the following more practical representation that is commonly used in financial applications<sup>1</sup>:

<sup>1</sup>See Yitzhaki [16] for the numerous representations of the Gini.

$$\Gamma(w) = 2 \text{cov}[w, G(w)] \tag{8}$$

where  $G$  is the cumulative probability distribution of  $w$ . The Gini is a dispersion statistic that measures risk the same way the standard deviation evaluates risk. Even more advantageous to risk analysis is the extended Gini that allows specifying risk aversion intensity in the dispersion statistic. The extended Gini coefficient of portfolio  $w$  is defined as:

$$\Gamma(\nu) = -\nu \text{cov}\left\{w, [1 - G(w)]^{\nu-1}\right\} \tag{9}$$

where  $\nu$  is the extended Gini parameter associated with risk aversion. This parameter expresses the extent to which the lower realizations relative to the highest returns are weighted in order to evaluate risk. As investors become more averse to risk, they worry significantly more about lower returns, thus giving them comparatively more weight than that given to the higher returns when computing the measure of dispersion. The parameter of risk aversion  $\nu$  ranges from 1 (representing a risk neutral investor) to infinity (for the most risk-averse investor exemplified by the max-min individual)<sup>2</sup>. In particular for  $\nu = 2$ , the standard Gini coefficient is obtained as in Equation (8).

The main advantage of *MEG* theory stems from the necessary and sufficient conditions for stochastic dominance which state that portfolio  $A$  is preferred to portfolio  $B$  for all risk-averse investors if

$$\begin{aligned} \mu_A &\geq \mu_B \\ \mu_A - \Gamma_A(\nu) &\geq \mu_B - \Gamma_B(\nu) \end{aligned} \tag{10}$$

for all  $\nu = 1, 2, 3, \dots, \infty$

where  $\mu_A$ ,  $\mu_B$ ,  $\Gamma_A(\nu)$ , and  $\Gamma_B(\nu)$  are the means and the extended Ginis of portfolio  $A$  and  $B$ , respectively. It follows from Equation (10) that maximizing  $\mu_\alpha - \Gamma_\alpha$  for all portfolios  $\alpha$  provide investors whose risk aversion parameter is  $\nu$  with their *MEG* efficient frontier. As an alternative, financial analysts sometimes minimize the extended Gini of the portfolio  $\Gamma(\nu)$  subject to a given mean return, as done in Shalit and Yitzhaki [17].

#### 4. The Mean-Extended Gini Hedging Methodology

The *MEG* model in futures hedging is rooted in research papers that advocate the use of Gini methods in futures markets (Cheung, Kwan and Yip [6]; Hodgson and Okunev [18]; Kolb and Okunev [19] [20]; Lien and Luo [10]; and Shalit [7]). Some of the more comprehensive reviews of *MEG* in futures markets appear in Lien and Tse [1] and Chen, Lee, and Shrestha [2].

Many methods are used to estimate *MEG* hedging ra-

tios, all of which are based on minimizing the extended Gini of the hedged portfolio subject to the mean return. The problem resides in calculating the extended Gini as the covariance of the portfolio return and its cumulative probability distribution. Kolb and Okunev [19,20] used the rank of the returns as an empirical distribution and derived the minimizing Gini hedge ratios by means of a search method. On the other hand, Lien and Luo [21] improved the estimation of the cumulative probability function using a smoothing kernel method while maintaining the numerical searching procedure. Shalit [7] provided an analytical solution to the *MEG* hedge ratios based on the instrumental variable (*IV*) regression. Later, Lien and Shaffer [22] showed that Shalit [7] had erred when he assumed identical rankings for the hedged portfolios returns and the futures prices in order to estimate the hedge ratio.

However, the portfolio insurance model is different from the futures hedging model because the index put option is written on market index in the same manner that the beta *CAPM* is obtained as the regression of the risky asset on the market portfolio. The portfolio hedging model is developed as follows. Consider investors with a risk-aversion coefficient  $\nu$ . The optimal mean-extended Gini hedge ratio for an index option is obtained by maximizing the mean minus the extended Gini of the hedged portfolio as follows:

$$\max H = E(w) - \Gamma_w(\nu) \tag{11}$$

where  $w = \sum_{i=1}^n \alpha_i S_i + x(P^1 - P^0)$  and

$$\Gamma_w(\nu) = -\nu \text{cov}\left\{w, [1 - G(w)]^{\nu-1}\right\}.$$

We then differentiate Equation (11) with respect to  $\alpha_i$  and  $x$ . Since the extended Gini is homogenous of degree one in the  $\alpha_i$  and  $x$  we now apply Euler's theorem to express the Gini as:

$$\Gamma_w(\nu) = \sum_{i=1}^n \alpha_i \frac{\partial \Gamma_w(\nu)}{\partial \alpha_i} + x \frac{\partial \Gamma_w(\nu)}{\partial x} \tag{12}$$

The result yields:

$$\begin{aligned} \sum_{i=1}^n \alpha_i E(S_i) + \nu \sum_{i=1}^n \alpha_i \text{cov}\left\{S_i, [1 - G(w)]^{\nu-1}\right\} \\ + x E(P^1 - P^0) + \nu x \text{cov}\left\{P^1, [1 - G(w)]^{\nu-1}\right\} = 0 \end{aligned} \tag{13}$$

or

$$E(w) - \Gamma_w(\nu) = 0 \tag{14}$$

As the covariance remains unchanged when subtracting a constant, we obtain the optimal hedge as that which brings the extended Gini of the portfolio to zero:

<sup>2</sup>See Butterworth and Holmes [4] for an illustration of the risk aversion parameter used in the extended Gini.

$$\begin{aligned}
 & -\nu \operatorname{cov}\left\{xP^I, [1-G(w)]^{\nu-1}\right\} \\
 & -\nu \sum_{i=1}^n \alpha_i \operatorname{cov}\left\{S_i, [1-G(w)]^{\nu-1}\right\} = 0
 \end{aligned} \tag{15}$$

or

$$x = -\sum_{i=1}^n \alpha_i \frac{\operatorname{cov}\left\{S_i, [1-G(w)]^{\nu-1}\right\}}{\operatorname{cov}\left\{P^I, [1-G(w)]^{\nu-1}\right\}} = -\sum_{i=1}^n \alpha_i \delta_i(\nu), \tag{16}$$

where  $\delta_i(\nu)$  is the optimal *MEG* hedge ratio that uses index options for an investor with risk aversion coefficient  $\nu$ . The question now is how to evaluate the ratio using financial data. As  $w$  are returns of a well-diversified portfolio of many securities and  $P$  is a put option written on a wider market index, the assumption that  $w$  and  $P$  have the same probability distribution as the market index  $I$  is valid one. Hence, one can write Equation (16) as

$$\begin{aligned}
 x &= -\sum_{i=1}^n \alpha_i \delta_i(\nu) \\
 &= -\sum_{i=1}^n \alpha_i \frac{\operatorname{cov}\left\{S_i, [1-G(I)]^{\nu-1}\right\}}{\operatorname{cov}\left\{I, [1-G(I)]^{\nu-1}\right\}} \frac{\operatorname{cov}\left\{I, [1-G(I)]^{\nu-1}\right\}}{\operatorname{cov}\left\{P, [1-G(I)]^{\nu-1}\right\}} \\
 &= -\sum_{i=1}^n \alpha_i \beta_i^I(\nu) \frac{1}{\Delta(\nu)}
 \end{aligned} \tag{17}$$

where the put option delta  $\Delta(\nu)$  is expressed in terms of *MEG*. We obtain the optimal *MEG* hedge ratio using index options in two steps. First, the  $\beta_i^I(\nu)$  are found as the mean-extended Gini regression coefficients of the stock returns over the market index for a specific  $\nu$ . These are basically *IV* regression coefficients where the instrument is  $[1-G(I)]^{\nu-1}$  for each  $\nu$ . The cumulative probability distribution  $G(I)$  is estimated by using the rank of the market index  $I$ . Second, the  $\Delta(\nu)$  are obtained from the *IV* regressions of the put option price over the market index with each one using the appropriate instrument  $[1-G(I)]^{\nu-1}$  for the different  $\nu$ .

The main issue in using *MEG* hedge ratios is to check whether these ratios differ statistically from *MV* ratios. Indeed, if the ratios are basically the same there is no need to calculate *MEG* ratios and the *MV* hedging ratios will satisfy all risk-averse investors. A natural question that arises is how to assess whether *MEG* ratios differ from *MV* ratios? Two avenues may be pursued: The first is theoretical since, as shown by Shalit [7], *MEG* ratios subside to the *MV* ratio if stock returns are normally distributed. Then, the issue is to test the normality of the financial returns. The second is an econometric approach that consists of applying Hausman's [23] specification error test to examine whether the *MEG* ratios differ from the *MV* ratio. The Hausman [23] test uses the statistic:

$$m(\nu) = \frac{[\beta^{MV} - \beta(\nu)]^2}{V(\beta^{MV})(1-\rho^2)/\rho^2}, \tag{18}$$

where  $V(\beta^{MV})$  is the variance of *MV* beta and  $\rho$  is the correlation between the stock return and the instrumental variable. The  $m(\nu)$  statistic is distributed Chi-square with one degree of freedom.

### 5. Data and Estimation Results

We conducted our research using data from the Tel-Aviv Stock Exchange (TASE) since no stock options on individual securities are traded there. The only way investors can hedge individual stocks is by holding positions in stock index options and futures although some firms whose shares are listed overseas have options traded on their stocks, (for example, Teva Pharmaceuticals, which is listed on the TASE and NASDAQ, has options traded on AMEX).

The sample consists of 1080 daily returns of 57 stocks traded on the TASE from August 1, 1993 until December 31, 1997, together with 14,340 observations of put options written on the TASE 25 stock index for the same time period. The Tel Aviv Stock Exchange began to officially trade stock index options on August 1, 1993, hence the sample period has some historical significance. The TASE 25 stock index is a capitalization-weighted index of the 25 stocks with the highest market values traded on the exchange. Options contracts on the TASE 25 stock index are traded daily from Sunday through Thursday. The contracts are quoted in New Israeli Shekels (NIS) at 100 NIS times the TASE 25 level.

Our goal is to estimate the 57 stocks hedge ratios for the TASE25 options contracts as expressed by Equation (5). First, we calculate the systematic risks for all 57 stocks using both the *MV* and the *MEG* approach for several coefficients or risk aversion  $\nu$  ranging from 2 to 20. This is done by estimating Equation (6), and then regressing securities daily returns on the daily returns of the TASE 25 stock index using *OLS* and *MEG (IV)* regressions. Then, to test whether the *MEG* betas are statistically different from the *MV* beta we compute Hausman's statistic to see whether this result depends on the normality distribution of the stock returns. We test for normality of stock returns by using the standard Jarque-Bera statistic.

The systematic risk coefficients for all the firms are presented in **Table 1**. For the major stocks traded on the TASE, the betas vary around 1 for the *MV* and the *MEG* models. To what extent the *MEG* betas differ from the *MV* beta depends upon the Hausman statistic reported below the coefficient for each *MEG* hedge. If the Hausman statistic is greater than 3.84 the *MEG* beta is statistically different (at 5%) from the *MV* hedge ratio. In ge-

**Table 1. MV and MEG betas on the TASE (Daily returns 1/08/1993-31/12/1997).**

| Firms                | $\beta_{MV}$ | $\beta(v=2)$ | $\beta(v=4)$ | $\beta(v=6)$ | $\beta(v=8)$ | $\beta(v=10)$ | $\beta(v=12)$ | $\beta(v=14)$ | $\beta(v=16)$ | $\beta(v=18)$ | $\beta(v=20)$ | Max Hausman | JarqueBera |
|----------------------|--------------|--------------|--------------|--------------|--------------|---------------|---------------|---------------|---------------|---------------|---------------|-------------|------------|
| Ackerstein           | 1.041        | 1.072        | 1.108        | 1.11         | 1.108        | 1.105         | 1.103         | 1.101         | 1.099         | 1.097         | 1.095         |             |            |
|                      |              | 2.875        | 7.295        | 5.248        | 3.835        | 2.959         | 2.376         | 1.962         | 1.653         | 1.411         | 1.217         | 7.295       | 98.53      |
| Africa               | 1.068        | 1.056        | 1.082        | 1.096        | 1.105        | 1.11          | 1.115         | 1.118         | 1.122         | 1.124         | 1.126         |             |            |
|                      |              | 0.565        | 0.362        | 1.08         | 1.437        | 1.602         | 1.689         | 1.74          | 1.77          | 1.783         | 1.78          | 1.783       | 130.5      |
| Africa 1             | 0.992        | 0.978        | 1.02         | 1.041        | 1.05         | 1.053         | 1.054         | 1.053         | 1.051         | 1.049         | 1.047         |             |            |
|                      |              | 0.71         | 1.682        | 3.42         | 3.725        | 3.462         | 3.046         | 2.626         | 2.247         | 1.917         | 1.633         | 3.725       | 41874      |
| Agan                 | 0.976        | 0.989        | 0.983        | 0.972        | 0.964        | 0.957         | 0.953         | 0.95          | 0.947         | 0.946         | 0.945         |             |            |
|                      |              | 1.37         | 0.237        | 0.052        | 0.428        | 0.795         | 1.046         | 1.195         | 1.269         | 1.293         | 1.284         | 1.37        | 284.4      |
| Agis                 | 1.048        | 1.038        | 1.077        | 1.092        | 1.101        | 1.108         | 1.113         | 1.118         | 1.122         | 1.126         | 1.129         |             |            |
|                      |              | 0.428        | 1.953        | 3.078        | 3.437        | 3.609         | 3.722         | 3.804         | 3.861         | 3.897         | 3.912         | 3.912       | 135.7      |
| Ahsharat Hayeshuv    | 1.114        | 1.114        | 1.163        | 1.18         | 1.186        | 1.188         | 1.187         | 1.186         | 1.184         | 1.182         | 1.179         |             |            |
|                      |              | 1E-05        | 4.735        | 5.734        | 5.328        | 4.657         | 3.994         | 3.405         | 2.898         | 2.469         | 2.106         | 5.734       | 480.8      |
| Azorim               | 0.954        | 0.953        | 0.978        | 0.983        | 0.981        | 0.977         | 0.971         | 0.965         | 0.959         | 0.953         | 0.946         |             |            |
|                      |              | 0.013        | 1.85         | 1.835        | 1.255        | 0.734         | 0.363         | 0.135         | 0.023         | 0.002         | 0.051         | 1.85        | 190.5      |
| BankHapoalim         | 0.918        | 0.91         | 0.899        | 0.9          | 0.902        | 0.906         | 0.909         | 0.912         | 0.915         | 0.918         | 0.921         |             |            |
|                      |              | 0.562        | 1.86         | 1.264        | 0.697        | 0.348         | 0.152         | 0.052         | 0.009         | 3E-04         | 0.013         | 1.86        | 87.33      |
| Benleumi             | 0.895        | 0.864        | 0.877        | 0.891        | 0.902        | 0.911         | 0.918         | 0.924         | 0.93          | 0.934         | 0.938         |             |            |
|                      |              | 7.757        | 1.453        | 0.047        | 0.122        | 0.503         | 0.919         | 1.298         | 1.621         | 1.888         | 2.101         | 7.757       | 281.6      |
| Benleumi 5           | 0.869        | 0.836        | 0.852        | 0.867        | 0.876        | 0.882         | 0.886         | 0.889         | 0.891         | 0.892         | 0.893         |             |            |
|                      |              | 9.607        | 1.291        | 0.014        | 0.12         | 0.343         | 0.513         | 0.621         | 0.678         | 0.697         | 0.688         | 9.607       | 117.1      |
| Bezeq                | 1.011        | 1.004        | 0.987        | 0.983        | 0.983        | 0.985         | 0.988         | 0.99          | 0.991         | 0.992         | 0.993         |             |            |
|                      |              | 0.375        | 2.929        | 2.735        | 2.024        | 1.437         | 1.031         | 0.764         | 0.59          | 0.476         | 0.402         | 9.607       | 731.5      |
| Calcalit Yam         | 0.994        | 1.009        | 1.06         | 1.072        | 1.074        | 1.074         | 1.074         | 1.073         | 1.073         | 1.072         | 1.071         |             |            |
|                      |              | 0.952        | 10.87        | 10.24        | 8.503        | 7.099         | 6.059         | 5.282         | 4.683         | 4.205         | 3.814         | 10.87       | 1839       |
| Clal Insurance       | 0.872        | 0.867        | 0.877        | 0.878        | 0.879        | 0.88          | 0.882         | 0.884         | 0.886         | 0.888         | 0.889         |             |            |
|                      |              | 0.112        | 0.079        | 0.075        | 0.076        | 0.089         | 0.109         | 0.133         | 0.16          | 0.188         | 0.217         | 0.217       | 160.9      |
| Clal Israel          | 1.017        | 1.028        | 1.041        | 1.041        | 1.04         | 1.039         | 1.038         | 1.037         | 1.037         | 1.036         | 1.036         |             |            |
|                      |              | 1.98         | 4.918        | 3.38         | 2.376        | 1.8           | 1.445         | 1.207         | 1.033         | 0.898         | 0.786         | 4.918       | 21382      |
| Clal Sahar           | 0.852        | 0.904        | 0.937        | 0.942        | 0.946        | 0.95          | 0.953         | 0.956         | 0.957         | 0.958         | 0.958         |             |            |
|                      |              | 6.305        | 9.038        | 7.016        | 5.919        | 5.311         | 4.894         | 4.552         | 4.239         | 3.938         | 3.643         | 9.038       | 259.6      |
| Clal Industries      | 1.034        | 1.058        | 1.057        | 1.046        | 1.035        | 1.026         | 1.018         | 1.011         | 1.005         | 0.999         | 0.994         |             |            |
|                      |              | 8.703        | 4.389        | 0.787        | 0.005        | 0.246         | 0.825         | 1.489         | 2.144         | 2.751         | 3.3           | 8.703       | 82.42      |
| Delek                | 0.86         | 0.833        | 0.861        | 0.884        | 0.9          | 0.911         | 0.919         | 0.924         | 0.927         | 0.929         | 0.93          |             |            |
|                      |              | 5.57         | 0.003        | 1.605        | 3.481        | 4.694         | 5.321         | 5.547         | 5.524         | 5.358         | 5.113         | 5.57        | 140.6      |
| Discount Investments | 1.081        | 1.102        | 1.098        | 1.09         | 1.085        | 1.081         | 1.079         | 1.078         | 1.077         | 1.076         | 1.076         |             |            |
|                      |              | 5.449        | 2.04         | 0.395        | 0.056        | 0.001         | 0.005         | 0.019         | 0.031         | 0.04          | 0.044         | 5.449       | 205.5      |

**Continued**

|                |       |       |       |       |       |       |       |       |       |       |       |       |       |  |
|----------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--|
| EIL            | 0.916 | 0.898 | 0.934 | 0.95  | 0.961 | 0.97  | 0.977 | 0.983 | 0.989 | 0.994 | 0.998 |       |       |  |
|                |       | 0.941 | 0.481 | 1.195 | 1.616 | 1.909 | 2.126 | 2.286 | 2.405 | 2.493 | 2.56  | 2.56  | 239.9 |  |
| Elbit          | 1.068 | 1.07  | 1.082 | 1.086 | 1.084 | 1.08  | 1.075 | 1.069 | 1.064 | 1.06  | 1.056 |       |       |  |
|                |       | 0.015 | 0.372 | 0.397 | 0.256 | 0.114 | 0.029 | 5E-04 | 0.01  | 0.041 | 0.08  | 0.397 | 48.15 |  |
| Elco Holdings  | 0.899 | 0.89  | 0.899 | 0.9   | 0.897 | 0.895 | 0.893 | 0.892 | 0.892 | 0.892 | 0.893 |       |       |  |
|                |       | 0.418 | 1E-04 | 0.001 | 0.003 | 0.02  | 0.037 | 0.044 | 0.041 | 0.032 | 0.02  | 0.418 | 2651  |  |
| Elite          | 0.965 | 0.902 | 0.932 | 0.961 | 0.983 | 0.999 | 1.011 | 1.021 | 1.03  | 1.037 | 1.044 |       |       |  |
|                |       | 18.43 | 2.74  | 0.024 | 0.431 | 1.297 | 2.099 | 2.765 | 3.306 | 3.751 | 4.122 | 18.43 | 172.3 |  |
| Elron          | 1.108 | 1.056 | 1.114 | 1.113 | 1.11  | 1.107 | 1.106 | 1.105 | 1.105 | 1.105 | 1.106 |       |       |  |
|                |       | 0.027 | 0.113 | 0.043 | 0.004 | 6E-04 | 0.005 | 0.009 | 0.009 | 0.007 | 0.004 | 0.113 | 295.4 |  |
| FIBI           | 1.081 | 1.079 | 1.093 | 1.097 | 1.095 | 1.092 | 1.089 | 1.086 | 1.082 | 1.08  | 1.077 |       |       |  |
|                |       | 0.056 | 0.734 | 0.902 | 0.595 | 0.308 | 0.128 | 0.036 | 0.003 | 0.004 | 0.025 | 0.902 | 157.3 |  |
| Formula        | 1.322 | 1.288 | 1.353 | 1.381 | 1.397 | 1.409 | 1.417 | 1.423 | 1.428 | 1.432 | 1.435 |       |       |  |
|                |       | 2.693 | 1.255 | 3.091 | 3.934 | 4.328 | 4.49  | 4.523 | 4.484 | 4.407 | 4.312 | 4.523 | 626.2 |  |
| Formula Vision | 1.149 | 1.139 | 1.192 | 1.209 | 1.217 | 1.223 | 1.229 | 1.233 | 1.237 | 1.241 | 1.243 |       |       |  |
|                |       | 0.149 | 1.781 | 2.363 | 2.376 | 2.339 | 2.314 | 2.292 | 2.266 | 2.231 | 2.186 | 2.376 | 457.4 |  |
| Hanal          | 1.015 | 0.945 | 0.99  | 1.043 | 1.079 | 1.103 | 1.119 | 1.13  | 1.138 | 1.143 | 1.147 |       |       |  |
|                |       | 2.609 | 0.18  | 0.147 | 0.608 | 0.959 | 1.164 | 1.264 | 1.299 | 1.297 | 1.274 | 2.609 | 8.649 |  |
| Israel Corp    | 1.05  | 1.02  | 1.052 | 1.071 | 1.087 | 1.101 | 1.113 | 1.125 | 1.135 | 1.144 | 1.152 |       |       |  |
|                |       | 5.616 | 0.006 | 1.002 | 2.351 | 3.709 | 4.996 | 6.169 | 7.207 | 8.111 | 8.887 | 8.887 | 271.4 |  |
| Israel Corp 5  | 0.89  | 0.876 | 0.891 | 0.886 | 0.884 | 0.885 | 0.888 | 0.892 | 0.896 | 0.9   | 0.904 |       |       |  |
|                |       | 0.683 | 0.002 | 0.015 | 0.032 | 0.017 | 0.002 | 0.003 | 0.022 | 0.057 | 0.103 | 0.683 | 193.1 |  |
| IDB Holdings   | 1.024 | 1.035 | 1.035 | 1.03  | 1.026 | 1.023 | 1.021 | 1.019 | 1.017 | 1.016 | 1.015 |       |       |  |
|                |       | 1.355 | 0.787 | 0.136 | 0.008 | 0.005 | 0.031 | 0.061 | 0.091 | 0.117 | 0.137 | 1.355 | 586.8 |  |
| Isramco        | 1.226 | 1.079 | 1.104 | 1.132 | 1.147 | 1.153 | 1.153 | 1.151 | 1.147 | 1.142 | 1.137 |       |       |  |
|                |       | 1.336 | 0.128 | 0.024 | 0.117 | 0.15  | 0.136 | 0.103 | 0.069 | 0.04  | 0.02  | 1.336 | 11148 |  |
| Joel           | 1.139 | 1.107 | 1.19  | 1.248 | 1.284 | 1.307 | 1.32  | 1.327 | 1.329 | 1.327 | 1.324 |       |       |  |
|                |       | 0.987 | 1.407 | 4.354 | 5.993 | 6.62  | 6.643 | 6.325 | 5.83  | 5.258 | 4.669 | 6.643 | 210.4 |  |
| Kardan         | 1.359 | 1.349 | 1.409 | 1.434 | 1.45  | 1.462 | 1.471 | 1.479 | 1.484 | 1.489 | 1.492 |       |       |  |
|                |       | 0.255 | 3.223 | 5.05  | 5.796 | 6.152 | 6.301 | 6.32  | 6.252 | 6.125 | 5.96  | 6.32  | 12    |  |
| Kirur          | 0.933 | 0.913 | 0.96  | 0.979 | 0.988 | 0.993 | 0.997 | 0.999 | 1.001 | 1.002 | 1.003 |       |       |  |
|                |       | 1.824 | 1.679 | 3.405 | 3.823 | 3.814 | 3.675 | 3.499 | 3.316 | 3.137 | 2.967 | 3.823 | 192   |  |
| Kitan          | 0.836 | 0.833 | 0.82  | 0.815 | 0.812 | 0.808 | 0.804 | 0.799 | 0.795 | 0.791 | 0.786 |       |       |  |
|                |       | 0.042 | 0.558 | 0.629 | 0.661 | 0.733 | 0.839 | 0.965 | 1.098 | 1.229 | 1.355 | 1.355 | 174.1 |  |
| Koor           | 1.074 | 1.067 | 1.053 | 1.051 | 1.051 | 1.051 | 1.051 | 1.051 | 1.051 | 1.05  | 1.05  |       |       |  |
|                |       | 0.503 | 2.196 | 1.852 | 1.486 | 1.246 | 1.082 | 0.962 | 0.872 | 0.804 | 0.753 | 2.196 | 468.9 |  |
| Makhteshim     | 1.048 | 1.072 | 1.065 | 1.055 | 1.046 | 1.039 | 1.033 | 1.029 | 1.025 | 1.021 | 1.018 |       |       |  |
|                |       | 4.671 | 1.272 | 0.141 | 0.008 | 0.157 | 0.368 | 0.573 | 0.752 | 0.902 | 1.025 | 4.671 | 104   |  |

## Continued

|                   |       |       |       |       |       |       |       |       |       |       |       |       |       |
|-------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Malibu            | 1.024 | 1.046 | 1.06  | 1.057 | 1.054 | 1.051 | 1.048 | 1.046 | 1.043 | 1.041 | 1.039 |       |       |
|                   |       | 1.137 | 1.619 | 0.962 | 0.609 | 0.405 | 0.279 | 0.198 | 0.142 | 0.104 | 0.076 | 1.619 | 235.2 |
| Mivtach Shamir    | 1.121 | 1.094 | 1.128 | 1.149 | 1.164 | 1.176 | 1.186 | 1.194 | 1.2   | 1.206 | 1.211 |       |       |
|                   |       | 2.213 | 0.078 | 0.853 | 1.572 | 2.133 | 2.558 | 2.87  | 3.095 | 3.252 | 3.356 | 3.356 | 238.3 |
| Multilock         | 0.846 | 0.87  | 0.913 | 0.918 | 0.914 | 0.908 | 0.901 | 0.895 | 0.889 | 0.883 | 0.878 |       |       |
|                   |       | 1.75  | 7.182 | 5.763 | 4.012 | 2.754 | 1.896 | 1.309 | 0.903 | 0.62  | 0.421 | 7.182 | 189   |
| Neto              | 1.472 | 1.478 | 1.544 | 1.579 | 1.6   | 1.614 | 1.623 | 1.629 | 1.633 | 1.635 | 1.636 |       |       |
|                   |       | 0.051 | 3.757 | 5.636 | 6.303 | 6.439 | 6.31  | 6.047 | 5.718 | 5.365 | 5.009 | 6.439 | 168.9 |
| Paper Mills       | 0.92  | 0.907 | 0.938 | 0.951 | 0.956 | 0.958 | 0.958 | 0.958 | 0.958 | 0.959 | 0.959 |       |       |
|                   |       | 1.087 | 1.108 | 2.265 | 2.391 | 2.193 | 1.944 | 1.725 | 1.553 | 1.426 | 1.335 | 2.391 | 200.4 |
| Noga Insurance    | 0.984 | 0.952 | 0.986 | 1.01  | 1.024 | 1.033 | 1.04  | 1.047 | 1.054 | 1.06  | 1.066 |       |       |
|                   |       | 0.72  | 0.001 | 0.187 | 0.327 | 0.405 | 0.465 | 0.521 | 0.574 | 0.623 | 0.666 | 0.72  | 304.6 |
| Ofer Development  | 0.826 | 0.781 | 0.805 | 0.823 | 0.833 | 0.84  | 0.845 | 0.849 | 0.852 | 0.855 | 0.858 |       |       |
|                   |       | 7.859 | 0.89  | 0.013 | 0.06  | 0.185 | 0.29  | 0.374 | 0.444 | 0.506 | 0.563 | 7.859 | 446.6 |
| Ormat             | 1.252 | 1.24  | 1.273 | 1.283 | 1.29  | 1.297 | 1.305 | 1.312 | 1.319 | 1.326 | 1.332 |       |       |
|                   |       | 0.44  | 0.742 | 1.111 | 1.289 | 1.498 | 1.744 | 2.008 | 2.269 | 2.513 | 2.732 | 2.732 | 69.42 |
| Osem              | 0.868 | 0.818 | 0.82  | 0.836 | 0.85  | 0.862 | 0.873 | 0.881 | 0.888 | 0.894 | 0.9   |       |       |
|                   |       | 16.82 | 8.191 | 2.485 | 0.57  | 0.042 | 0.034 | 0.219 | 0.468 | 0.725 | 0.97  | 16.82 | 408.7 |
| Periclass         | 0.944 | 0.919 | 0.93  | 0.935 | 0.939 | 0.942 | 0.945 | 0.949 | 0.952 | 0.955 | 0.958 |       |       |
|                   |       | 3.069 | 0.513 | 0.131 | 0.034 | 0.003 | 0.003 | 0.021 | 0.052 | 0.089 | 0.13  | 3.069 | 340.3 |
| Petrochimia       | 0.936 | 0.917 | 0.942 | 0.961 | 0.976 | 0.988 | 0.997 | 1.005 | 1.012 | 1.017 | 1.021 |       |       |
|                   |       | 1.224 | 0.071 | 0.804 | 1.616 | 2.269 | 2.751 | 3.096 | 3.334 | 3.489 | 3.579 | 3.579 | 25.74 |
| Polar Investments | 1.116 | 1.082 | 1.123 | 1.15  | 1.165 | 1.175 | 1.18  | 1.184 | 1.186 | 1.187 | 1.187 |       |       |
|                   |       | 4.858 | 0.111 | 1.674 | 2.806 | 3.325 | 3.467 | 3.407 | 3.248 | 3.046 | 2.83  | 4.858 | 57.89 |
| Polgat            | 0.921 | 0.894 | 0.88  | 0.873 | 0.869 | 0.869 | 0.871 | 0.874 | 0.877 | 0.881 | 0.884 |       |       |
|                   |       | 1.873 | 2.245 | 2.166 | 1.924 | 1.611 | 1.299 | 1.024 | 0.796 | 0.613 | 0.47  | 2.245 | 312.3 |
| Sapanut           | 1.268 | 1.234 | 1.283 | 1.316 | 1.338 | 1.352 | 1.363 | 1.37  | 1.375 | 1.378 | 1.381 |       |       |
|                   |       | 3.159 | 0.291 | 2.245 | 3.688 | 4.493 | 4.881 | 5.014 | 4.99  | 4.87  | 4.691 | 5.014 | 340.4 |
| Supersol          | 0.931 | 0.886 | 0.89  | 0.9   | 0.906 | 0.909 | 0.911 | 0.912 | 0.913 | 0.914 | 0.916 |       |       |
|                   |       | 21.08 | 9.288 | 3.676 | 1.897 | 1.204 | 0.871 | 0.677 | 0.544 | 0.44  | 0.352 | 21.08 | 249.7 |
| Teva              | 0.885 | 0.889 | 0.879 | 0.868 | 0.859 | 0.852 | 0.847 | 0.844 | 0.842 | 0.841 | 0.841 |       |       |
|                   |       | 0.069 | 0.086 | 0.487 | 0.902 | 1.187 | 1.336 | 1.381 | 1.358 | 1.295 | 1.211 | 1.381 | 411.7 |
| Urdan             | 0.969 | 0.966 | 0.972 | 0.973 | 0.974 | 0.974 | 0.972 | 0.969 | 0.965 | 0.96  | 0.955 |       |       |
|                   |       | 0.038 | 0.007 | 0.015 | 0.017 | 0.012 | 0.004 | 1E-04 | 0.01  | 0.038 | 0.087 | 0.087 | 169.2 |
| Dead Sea Works    | 1.05  | 1.044 | 1.042 | 1.044 | 1.044 | 1.042 | 1.04  | 1.037 | 1.034 | 1.032 | 1.029 |       |       |
|                   |       | 0.263 | 0.28  | 0.115 | 0.093 | 0.118 | 0.165 | 0.226 | 0.293 | 0.363 | 0.43  | 0.43  | 231.3 |
| Yetzu             | 1.056 | 1.058 | 1.09  | 1.104 | 1.114 | 1.122 | 1.128 | 1.133 | 1.137 | 1.14  | 1.142 |       |       |
|                   |       | 0.016 | 2.162 | 2.98  | 3.369 | 3.587 | 3.698 | 3.736 | 3.723 | 3.673 | 3.595 | 3.736 | 107.7 |
| Ytong             | 0.754 | 0.787 | 0.824 | 0.833 | 0.832 | 0.827 | 0.82  | 0.813 | 0.805 | 0.797 | 0.79  |       |       |
|                   |       | 6.217 | 16.36 | 14.32 | 10.9  | 7.938 | 5.638 | 3.921 | 2.662 | 1.752 | 1.103 | 16.36 | 213.1 |

neral, the *MEG* systematic risk coefficients are greater than the *MV* beta and they increase as the risk aversion parameter increases from  $\nu = 2$  to  $\nu = 20$ . This is commonly the case when the Hausman statistic shows that the *MEG* beta is statistically different from the *MV* beta. We can see from the maximum Hausman statistic, only 33 stocks from a total of 57 have at least one *MEG* beta that significantly differs from the *MV* hedge ratio. The Hausman statistic is not as large as one would expect for non-normally distributed stock returns. Indeed, as shown by the Jarque-Bera statistic being greater than 10, the hypothesis that all stock returns follow a normal distribution is rejected. Nevertheless, using *MEG* betas instead of the *MV* beta allows us to account for specific risk aversion.

The next step is to estimate delta  $\Delta$  as the rate of change of the put option price with respect to the stock market index as shown in Equations (5) and (17). To account for changes in the exercise index price and the maturity date, we include these variables in the regression. The regression results are shown in the top three rows (Equation A) of **Table 2**. The index put option delta,  $\Delta$ , estimated for the entire period, is  $-0.425$ . As shown in Equation (5), the hedge ratios are obtained by dividing the systematic risk by delta. In the *MEG* model, the hedge ratios as shown in Equation (17) must account for the differentiated risk aversion,  $\nu$ . Hence, we estimate  $\Delta(\nu)$  as follows. First, we account for the changes in exercise price as well as in the exercise date by running a regression model of the put option price over these variables (see the bottom rows (Equation B) of **Table 2**). Then, we use the regression residuals of Equation B to calculate  $\Delta(\nu)$  as

$$\Delta(\nu) = \frac{\text{cov}\left\{P, [1 - G(I)]^{\nu-1}\right\}}{\text{cov}\left\{I, [1 - G(I)]^{\nu-1}\right\}} \quad (19)$$

The results are shown in **Table 3** for the various values of  $\nu$  used in the research, together with the  $\Delta$  calculated for the *MV* model. We can see that  $\Delta(\nu)$ , the rates of change of the put option with respect to the market index, increase as the risk aversion parameter increases and that they all are greater than the  $\Delta$  implied by *MV*. This is an expected result for the stock market index.

Now we can calculate the hedge coefficients for each security and for each coefficient of risk aversion  $\nu$  by dividing the betas with the appropriate  $\Delta(\nu)$  following Equation (17). The hedge ratios presented in **Table 4** show how investors can evade the two types of risks incurred by holding a stock portfolio, namely the standard systematic risk and the basis risk of hedging the portfolio. By analyzing **Table 4** we see why this approach is different from what we have ever seen in hedge ratios. For most securities, increasing risk aversion as expressed by  $\nu$  reduces the size of the ratio, implying that a smaller number of put options is needed to hedge each and every security. This is an unexpected result that can be attributed to the combination of the two risks factors (systematic risk and basis risk) and taking into account the risk aversion parameter.

## 6. Conclusion

As calculated in our paper, we have shown the advantages of using mean-extended Gini hedge ratios versus the standard mean-variance hedge ratios. Since these ratios combine systematic risk and the basis risk for a wide range of risk aversion coefficients, our results indicate that the hedge coefficients can accurately measure the number of stock index options needed to hedge securities in a diversified portfolio. The standard mean-variance hedge ratios consider only systematic risk and are insensitive to the investor risk aversion differentials. We have presented a procedure to obtain optimal *MEG* hedge

**Table 2. The put option index regression equation.**

|            | Variable       | Constant | TA 25 Index | Strike Price | Days to Strike | R Square |
|------------|----------------|----------|-------------|--------------|----------------|----------|
| Equation A | Coefficient    | 9.202    | -0.425      | 0.4317       | -0.00017       | 0.7656   |
|            | Standard Error | 0.246    | 0.0022      | 0.002        | 0.0013         |          |
|            | t-Statistic    | 37.464   | -196.29     | 215.985      | -0.133         |          |
| Equation B | Coefficient    | -9.122   |             | 0.0866       | 0.0017         | 0.1357   |
|            | Standard Error | 0.4362   |             | 0.0018       | 0.0025         |          |
|            | t-Statistic    | -20.91   |             | 47.43        | 0.681          |          |

Dependent variable: Put price. Number of observations: 14,339.

**Table 3. Estimates of  $\Delta(\nu)$  computed with the residuals of Equation B.**

|          | MV      | $\nu = 2$ | $\nu = 4$ | $\nu = 6$ | $\nu = 8$ | $\nu = 10$ | $\nu = 12$ | $\nu = 14$ | $\nu = 16$ | $\nu = 18$ | $\nu = 20$ |
|----------|---------|-----------|-----------|-----------|-----------|------------|------------|------------|------------|------------|------------|
| $\Delta$ | -0.9626 | -1.056    | -1.211    | -1.284    | -1.3166   | -1.3314    | -1.3384    | -1.3420    | -1.3444    | -1.3469    | -1.3498    |



**Table 4. MEG and MV hedge coefficients  $\delta$  for each stock and for each risk aversion coefficient.**

| Firms                | $\delta(MV)$ | $\delta(v=2)$ | $\delta(v=4)$ | $\delta(v=6)$ | $\delta(v=8)$ | $\delta(v=10)$ | $\delta(v=12)$ | $\delta(v=14)$ | $\delta(v=16)$ | $\delta(v=18)$ | $\delta(v=20)$ |
|----------------------|--------------|---------------|---------------|---------------|---------------|----------------|----------------|----------------|----------------|----------------|----------------|
| Ackerstein           | 1.08169      | 1.01519       | 0.914863      | 0.864229      | 0.841258      | 0.830134       | 0.824096       | 0.820298       | 0.817331       | 0.814381       | 0.811224       |
| Africa               | 1.10975      | 1.00016       | 0.893023      | 0.85359       | 0.838964      | 0.833987       | 0.832935       | 0.83342        | 0.834246       | 0.834657       | 0.834494       |
| Africa 1             | 1.03006      | 0.926191      | 0.842226      | 0.81046       | 0.797258      | 0.790942       | 0.787253       | 0.784516       | 0.781925       | 0.778959       | 0.775596       |
| Agan                 | 1.01435      | 0.936256      | 0.811929      | 0.757391      | 0.731936      | 0.719048       | 0.711946       | 0.707663       | 0.704708       | 0.702203       | 0.699864       |
| Agis                 | 1.08876      | 0.983076      | 0.889456      | 0.850717      | 0.836344      | 0.832026       | 0.831829       | 0.833204       | 0.834885       | 0.836127       | 0.836776       |
| Ahsharat Hayeshuv    | 1.15766      | 1.05542       | 0.960639      | 0.918715      | 0.900608      | 0.892008       | 0.887164       | 0.883756       | 0.880653       | 0.877214       | 0.873381       |
| Azorim               | 0.991167     | 0.902227      | 0.8074        | 0.765329      | 0.745033      | 0.733523       | 0.725603       | 0.719166       | 0.713224       | 0.707216       | 0.701076       |
| BankHapoolim         | 0.953252     | 0.8621        | 0.74267       | 0.700558      | 0.685373      | 0.680325       | 0.679303       | 0.679858       | 0.680838       | 0.681593       | 0.681994       |
| Benleumi             | 0.929769     | 0.818665      | 0.724085      | 0.693979      | 0.685217      | 0.684238       | 0.68609        | 0.688802       | 0.691437       | 0.693449       | 0.694773       |
| Benleumi 5           | 0.902502     | 0.791361      | 0.703628      | 0.674981      | 0.665109      | 0.662168       | 0.661757       | 0.662113       | 0.662403       | 0.662146       | 0.661301       |
| Bezeq                | 1.04985      | 0.95116       | 0.814714      | 0.765332      | 0.746888      | 0.740124       | 0.73791        | 0.73739        | 0.737243       | 0.736747       | 0.735772       |
| Calcalit Yam         | 1.03295      | 0.955204      | 0.875403      | 0.834587      | 0.81592       | 0.80703        | 0.802473       | 0.799851       | 0.79791        | 0.795902       | 0.793658       |
| Clal Insurance       | 0.90547      | 0.820951      | 0.72418       | 0.68381       | 0.667597      | 0.661218       | 0.659002       | 0.658577       | 0.658791       | 0.65897        | 0.658955       |
| Clal Israel          | 1.05624      | 0.973549      | 0.859458      | 0.810701      | 0.789731      | 0.780179       | 0.775516       | 0.772981       | 0.771206       | 0.769396       | 0.767358       |
| Clal Sahar           | 0.885615     | 0.856274      | 0.773581      | 0.733929      | 0.718628      | 0.713441       | 0.712131       | 0.712072       | 0.712031       | 0.711327       | 0.709846       |
| Clal Industries      | 1.07432      | 1.0022        | 0.873157      | 0.814712      | 0.786275      | 0.770482       | 0.760423       | 0.753159       | 0.747233       | 0.74179        | 0.736583       |
| Delek                | 0.89329      | 0.788649      | 0.710732      | 0.68841       | 0.683611      | 0.684304       | 0.686308       | 0.688176       | 0.689348       | 0.689551       | 0.688899       |
| Discount Investments | 1.12262      | 1.04319       | 0.906663      | 0.848832      | 0.823773      | 0.812145       | 0.806314       | 0.803085       | 0.8009         | 0.798894       | 0.796829       |
| EIL                  | 0.951827     | 0.850334      | 0.771317      | 0.74016       | 0.730103      | 0.728528       | 0.730164       | 0.732837       | 0.735525       | 0.737655       | 0.739171       |
| Elbit                | 1.10972      | 1.0136        | 0.893477      | 0.845421      | 0.823318      | 0.811018       | 0.802847       | 0.796669       | 0.791476       | 0.786629       | 0.78199        |
| Elco Holdings        | 0.933763     | 0.842624      | 0.741993      | 0.700648      | 0.681584      | 0.672042       | 0.667093       | 0.664573       | 0.663301       | 0.6625         | 0.661887       |
| Elite                | 1.00218      | 0.854682      | 0.769506      | 0.748424      | 0.746252      | 0.750047       | 0.755492       | 0.761051       | 0.766074       | 0.770161       | 0.773374       |
| Elron                | 1.15087      | 1.            | 0.919924      | 0.86648       | 0.842746      | 0.831576       | 0.826076       | 0.823271       | 0.821668       | 0.820358       | 0.819092       |
| IBI                  | 1.12318      | 1.02172       | 0.902262      | 0.854097      | 0.832029      | 0.820527       | 0.813651       | 0.808942       | 0.805155       | 0.801529       | 0.797889       |
| Formula              | 1.37316      | 1.22023       | 1.11707       | 1.07535       | 1.06126       | 1.05805        | 1.05877        | 1.06065        | 1.0624         | 1.06333        | 1.06342        |
| Formula Vision       | 1.1932       | 1.07905       | 0.984171      | 0.94155       | 0.92454       | 0.918875       | 0.918007       | 0.918987       | 0.920292       | 0.921056       | 0.921099       |
| Hanal                | 1.05493      | 0.895279      | 0.817708      | 0.812243      | 0.819444      | 0.828354       | 0.836133       | 0.842168       | 0.846422       | 0.848927       | 0.850052       |
| Israel Corp          | 1.0913       | 0.96636       | 0.868458      | 0.83447       | 0.825566      | 0.826761       | 0.831799       | 0.838025       | 0.844139       | 0.849425       | 0.853764       |
| Israel Corp 5        | 0.924116     | 0.829618      | 0.735348      | 0.690181      | 0.671483      | 0.664807       | 0.663446       | 0.664393       | 0.666173       | 0.667959       | 0.669515       |
| IDB Holdings         | 1.06392      | 0.979903      | 0.854678      | 0.801908      | 0.778984      | 0.768199       | 0.762567       | 0.759203       | 0.756747       | 0.754414       | 0.75203        |
| Isramco              | 1.27343      | 1.0219        | 0.911717      | 0.881729      | 0.87094       | 0.865638       | 0.861686       | 0.857712       | 0.853236       | 0.847999       | 0.842206       |
| Joel                 | 1.18324      | 1.04883       | 0.982875      | 0.972142      | 0.975535      | 0.981486       | 0.986163       | 0.988472       | 0.988218       | 0.985411       | 0.980545       |
| Kardan               | 1.41165      | 1.27721       | 1.16304       | 1.11687       | 1.10152       | 1.09827        | 1.09942        | 1.10186        | 1.10409        | 1.10531        | 1.10545        |
| Kirur                | 0.96918      | 0.864307      | 0.792275      | 0.762233      | 0.750389      | 0.74604        | 0.744688       | 0.744434       | 0.744332       | 0.743812       | 0.742806       |
| Kitan                | 0.868299     | 0.78852       | 0.676876      | 0.634896      | 0.616624      | 0.606963       | 0.600646       | 0.595722       | 0.591335       | 0.587004       | 0.582654       |
| Koor                 | 1.11538      | 1.01011       | 0.869837      | 0.818715      | 0.79817       | 0.789207       | 0.785027       | 0.782891       | 0.781449       | 0.779932       | 0.778138       |
| Makhteshim           | 1.089        | 1.01538       | 0.879581      | 0.821737      | 0.794774      | 0.780592       | 0.772153       | 0.766483       | 0.762102       | 0.758133       | 0.754312       |
| Malibu               | 1.06409      | 0.990719      | 0.875072      | 0.823505      | 0.800661      | 0.789417       | 0.783166       | 0.77918        | 0.776101       | 0.773131       | 0.770062       |
| Mivtach Shamir       | 1.16454      | 1.03594       | 0.931352      | 0.894688      | 0.883951      | 0.883085       | 0.885774       | 0.889434       | 0.892889       | 0.895464       | 0.897133       |
| Multilock            | 0.879321     | 0.824262      | 0.753464      | 0.714943      | 0.694338      | 0.682015       | 0.673527       | 0.666916       | 0.661191       | 0.655747       | 0.650442       |
| Neto                 | 1.52888      | 1.39963       | 1.27474       | 1.22937       | 1.21513       | 1.21217        | 1.21279        | 1.21406        | 1.21469        | 1.21398        | 1.212          |

## Continued

|                   |          |          |          |          |          |          |          |          |          |          |          |
|-------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| Paper Mills       | 0.95569  | 0.858909 | 0.774413 | 0.740625 | 0.726188 | 0.71951  | 0.716128 | 0.714232 | 0.712928 | 0.711661 | 0.710327 |
| Noga Insurance    | 0.96918  | 0.864307 | 0.792275 | 0.762233 | 0.750389 | 0.74604  | 0.744688 | 0.744434 | 0.744332 | 0.743812 | 0.742806 |
| Ofer Development  | 0.85763  | 0.739219 | 0.664592 | 0.640584 | 0.632647 | 0.630727 | 0.631118 | 0.632365 | 0.633762 | 0.63487  | 0.635631 |
| Ormat             | 1.30032  | 1.17405  | 1.05108  | 0.999338 | 0.97991  | 0.974305 | 0.974709 | 0.977608 | 0.981204 | 0.984416 | 0.986954 |
| Osem              | 0.901281 | 0.774374 | 0.677102 | 0.651033 | 0.645889 | 0.647785 | 0.65191  | 0.656459 | 0.660642 | 0.664033 | 0.666664 |
| Periclass         | 0.98034  | 0.869887 | 0.767594 | 0.72828  | 0.713007 | 0.707594 | 0.706358 | 0.706873 | 0.707939 | 0.708857 | 0.709467 |
| Petrochimia       | 0.971973 | 0.868455 | 0.777605 | 0.748065 | 0.741044 | 0.741845 | 0.745175 | 0.749024 | 0.752477 | 0.755023 | 0.756623 |
| Polar Investments | 1.15963  | 1.02466  | 0.927545 | 0.895249 | 0.884923 | 0.882229 | 0.881934 | 0.882116 | 0.881947 | 0.880964 | 0.879219 |
| Polgat            | 0.956512 | 0.846351 | 0.726846 | 0.679682 | 0.660321 | 0.652809 | 0.650681 | 0.651043 | 0.652392 | 0.653838 | 0.65508  |
| Sapanut           | 1.31765  | 1.16878  | 1.059    | 1.02493  | 1.01599  | 1.01571  | 1.01804  | 1.0207   | 1.02268  | 1.02339  | 1.02291  |
| Supersol          | 0.967501 | 0.839196 | 0.735171 | 0.701072 | 0.688087 | 0.682832 | 0.680659 | 0.679787 | 0.679375 | 0.678912 | 0.678312 |
| Teva              | 0.919899 | 0.842385 | 0.726138 | 0.676047 | 0.652102 | 0.639602 | 0.632658 | 0.628643 | 0.626151 | 0.624303 | 0.622763 |
| Urda              | 1.00717  | 0.914818 | 0.802285 | 0.757956 | 0.739713 | 0.731223 | 0.726168 | 0.722066 | 0.717854 | 0.713015 | 0.70757  |
| Dead Sea Works    | 1.09119  | 0.988967 | 0.860168 | 0.81285  | 0.792602 | 0.78259  | 0.776778 | 0.772757 | 0.769392 | 0.766033 | 0.76255  |
| Yetzu             | 1.09673  | 1.00186  | 0.899835 | 0.85986  | 0.846149 | 0.842557 | 0.842738 | 0.844136 | 0.845552 | 0.846306 | 0.846311 |
| Ytong             | 0.78359  | 0.744925 | 0.680159 | 0.648636 | 0.631969 | 0.621245 | 0.61294  | 0.605686 | 0.598838 | 0.592006 | 0.58516  |

ratios. First, the analyst needs to establish the relevant risk aversion parameter for investors and portfolios managers to be used for the extended Gini. For a mild risk aversion, a parameter of  $\nu$  of about 2 can be used. For higher risk-averse investors, parameters of  $\nu$  greater than 4 is deemed appropriate and for extremely high risk-averse investors a parameter of  $\nu$  that are greater than 16 are necessary. Second, for each risk aversion  $\nu$  and for each stock the MEG systematic risk is to be estimated. Finally, for each risk aversion parameter  $\nu$  the delta option parameter  $\Delta$  expressed as the rate of change of the put option price with respect to the stock market index is estimated. The MEG hedge ratios are thus individually tailored for each stock and for each type of investors. For most analyzed securities of the Tel Aviv Stock Exchange, increasing risk aversion reduces the hedge ratio entailing that less put options are needed to circumvent systematic risk and basis risk for a given the risk aversion.

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