

Energy-Saving Scheduling in a Flexible Flow Shop Using a Hybrid Genetic Algorithm

Rong-Hwa Huang¹, Shun-Chi Yu², Po-Han Chen¹

¹Department of Business Administration, Fu Jen Catholic University, Taiwan

²Department of Tourism and Hospitality, China University of Science and Technology, Taiwan

Email: 026299@mail.fju.edu.tw

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Abstract

Many researches discussing reduced energy consumption for environmental protection focus on machine efficiency or process redesign. To optimize the machine operation time can also save the energy, and these researches have received great interests in recent years. This study considers three different states of machines, among processing there are two different speeds, to solve the problem of minimizing energy costs under time-of-use tariff with no tardy jobs in flexible flow shop. This problem is basically NP-hard, we proposed a hybrid genetic algorithm (GA) to solve problems in reasonable timeliness. The result shows that to optimize different states of machines under time-of use tariff can reduce energy costs significantly in on-time delivery.

Keywords

Flexible Flow Shops, Energy-Saving Genetic Algorithm, Energy Consumption Cost, Non-Tardy, Genetic Algorithms

1. Introduction

Goldratt and Cox [1] posit that goal achievement by a goal-oriented system is limited by at least one constraint. The limitation of electricity affects the energy in Taiwan. Good energy-saving production systems have become important issue during peak time. In practical production, energy saving is essential for enhancing production activity and maximizing the effectiveness of processes on machines. The electricity consumption of industries exceeds half of global consumption and affects the operating efficiency in practical situations.

A flexible flow shop (FFS) scheduling problem provides multiple identical parallel machines at each station for increasing capacity and reducing costs.

Flow shop processing involves constant sequences of initial, standard, steady, and nonpermutable production, such as that of steel, optoelectronics, and metal, which are common in real-world situations [2] [3]. To offer widely application, Linn and Zhang [4] indicated that FFS scheduling applies to traditional flow shop situations. The attempted problem is excellently solved. However, the energy consumption of machines affects the efficiency and quality of production; for instance, increased on-peak electricity consumption of machines causes an increase in temperature, wearing of parts, and improper manual operation. The time-of-use (TOU) tariff is a common used for adjusting peak power consumption worldwide. Generally, the billing period is divided into on-peak hours, mid-peak hours, and off-peak hours. The electricity costs during the on-peak period are the highest, whereas those during the off-peak period are the lowest. Moreover, machines can be switched to operation, standby, and shutdown modes for preventing unnecessary energy wastage.

As for trade-off of energy saving method, Ribas *et al.* [5] demonstrated that enterprises added machines to certain stages, thus enhanced production efficiency and customer satisfaction. An energy-efficient mathematical model for solving FFS scheduling problems and multiobjective optimization to minimize the makespan and total energy consumption [6]. The experimental results showed that the relationship between the makespan and energy consumption may be conflicting. A proposed energy-saving decision is useful for minimizing energy consumption. To minimize trade-off of earliness and tardiness in a practical production environment, Huang *et al.* [7] developed a farness particle swarm optimization (FPSO) algorithm for solving reentrant two-stage multi-processor flow shop scheduling problems.

As for energy-saving issues, because of scarce resources, increasing attention has been focused on developing practical production techniques for clean technologies and protecting the environment [8]. Decreasing emission of CO₂ attracts more attentions. Zhang *et al.* [9] developed a time-indexed integer programming formulation for solving manufacturing schedules that minimize electricity cost and the carbon footprint under TOU tariffs without compromising production throughput. The proposed method used a flow shop with eight process steps that were operated on a typical summer day for an energy-saving test. Results indicated that shifting electricity usage from on-peak hours to mid-peak hours or off-peak hours reduces electricity costs; however, it may increase CO₂ emissions in regions where the grid base load is met with electricity from coal-fired power plants. The tradeoff between minimizing electricity cost and reducing CO₂ emissions was shown using a Pareto frontier. Setlhaolo [10] demonstrated that using residential demand response along with a mixed integer nonlinear optimization model under a TOU electricity tariff can solve the scheduling problem of typical home appliances as well as minimize electricity costs and facilitate earning relevant incentives [11]. An analysis revealed that house-

holds can alter their electricity consumption in response to varying prices and incentives; thus, a consumer may reduce electricity costs by more than 25%. Different values of the weighting factor (α) provide varying costs. According to the α values and their preferences, consumers can choose their electricity costs. FFS scheduling can save energy and lower manufacturing costs by clean technologies, environmental policy, reducing the completion time and inventory in industrial environments.

Energy-saving models are created for important issues, Mouzon and Yildirim [12] developed operational methods for minimizing the energy consumption of manufacturing equipment and total completion time. The energy used in processes can be saved by turning off nonbottleneck (*i.e.*, underutilized) machines or equipment when they are idle for a certain period of time. In particular, an analysis indicated that the proposed dispatching methods are effective in reducing the energy consumption of underutilized manufacturing equipment. Therefore, a production manager has a set of nondominated solutions (*i.e.*, a set of efficient solutions) that he or she can use for determining the most efficient production sequence; moreover, they minimize the total energy consumption while optimizing the total completion time. Fang *et al.* [13] developed a new mathematical programming model for flow shop scheduling problems to minimize the peak power load, energy consumption, and associated carbon footprint along with the cycle time. In a flow shop with two machines producing various parts, the operation speed was considered an independent variable, which can be changed to affect the peak load and energy consumption. The results demonstrated that the proposed approach enables determining near-optimal schedules for achieving energy-saving goals. Tibi and Arman [14] developed a mathematical linear programming model to optimize the decision-making for managing a cogeneration facility as a potential clean-development mechanism project in a hospital in Palestine. The model optimized the cost of energy and the cost of installation of a small cogeneration plant under constraints on electricity-and-heat supply and demand balances. The results proved the efficiency of the proposed method. He *et al.* [15] demonstrated that the environmental load resulting from the energy consumption of machine tool systems is broadly recognized. Improving scheduling saves energy, facilitates efficient use of machine tools, and reduces energy consumption by idle equipment. One proposed energy-saving optimization method involves machine tool selection and a series of machine operations for flexible job shops. The method was designed to reduce the energy consumption of machine operations, and the scheduling was aimed at reducing the unused power consumption of machine tools. The current study investigated how to develop and use clean technologies like non-tardy procedures for scheduling the use of parallel machines to maintain practical production for environmental protection.

To prevent tardiness and ensure effective operation of production equipment, companies create effective and efficient production environments that maximize corporate benefits from production activities. Bruzzone *et al.* [16] developed

energy-aware scheduling of manufacturing processes by using advanced planning and scheduling, a mathematical model for optimally planning energy saving for a given schedule. The new approach relies on the MIP model, where the reference schedule is modified to account for energy consumption without changing the jobs' assignments and sequencing provided by the reference schedule. The results demonstrated that a commercial MIP solver and an original MIP heuristic are applicable in practical production.

Enumeration and heuristic methods have been applied for energy saving in previous studies [10]. Integer programming, branch and bound programming, and MIP are the most widely used enumeration methods that can provide appropriate solutions. However, high computational times limit the applicability of enumeration methods to small-scale problems [17]. Thus, heuristics such as the genetic algorithm, simulated annealing algorithm, and ant colony optimization algorithm are commonly used for solving energy-saving problems. Lian [18] obtained the average relative error rates of -28.20% and 60.25% for a combined local and global PSO algorithm against PSO and genetic algorithms, respectively. Zhang *et al.* [19] presented an I-ATTPSO algorithm with an average effectiveness improvement rate of -14% in small-scale problems and 55% in large-scale problems. Liu *et al.* [20] obtained an average relative error rate of 0.65% for the PSO-EDA_PI algorithm against other algorithms. Zhao *et al.* [21] found the average relative error rate of their proposed logistic dynamic PSO algorithm against other algorithms to be approximately $1.19\% - 2.39\%$.

In many industrialized countries, manufacturing industries pay stratified electricity charges depending on the time of the day (*i.e.*, on-peak, mid-peak, and off-peak hours) [22]. China saves energy concerning the impact of internal industrial configuration in terms of size and ownership structure on aggregate energy intensity [23]. Besides, Germany property owners can deduce where they should ideally invest in order to optimize the energy efficiency of their building stock sustainably [24]. By contrast, the emerging smart grid concept may demand that industries pay real-time hourly electricity costs for the efficient usage of energy. To enable decision makers to apply feasible solutions for resolving unrelated parallel machine scheduling problems, Moon *et al.* [25] developed an energy-efficient method by using the weighted sum objective of production scheduling and electricity usage. Reliability models using a hybrid genetic algorithm along with their blank job insertion algorithm consider the energy cost aspect of the problem with the objective function of optimizing the weighted sum of two criteria: the minimization of the production makespan and the minimization of time-dependent electricity costs. The results demonstrated its performance in simulation experiments in practical production.

Energy-saving method relates to fixed costs. Shrouf *et al.* [26] posited that rising energy costs associated with increased production costs at manufacturing facilities encouraged decision makers to tackle this problem in different ways. One crucial step in this trend is to reduce the energy consumption costs of production systems. Considering variable energy prices in a single day, the authors

proposed a mathematical model for minimizing energy consumption costs for single machine production scheduling during production processes. The job processing time consists of the starting time, idle time, and times when the machine must be shut down, turned on, and turned off. The proposed mathematical model enables the operation manager to implement the least expensive production scheduling during a production shift. To obtain feasible solutions by using a genetic algorithm, this study also determined whether the heuristic solution provides the minimum cost and optimal schedule for minimizing energy costs. In addition, an analytical solution was applied to generate the optimal solution. Moreover, analytical solutions and heuristic solutions were compared, and the heuristic solution is considered preferable for larger problems. The results indicate that significant reductions in energy costs can be achieved by avoiding high-energy price periods. The results have a positive environmental effect by reducing energy consumption during peak periods, thereby increasing the possibility of reducing CO₂ emissions from power generator sites. Although a genetic algorithm can efficiently solve energy-saving problems and prevent entrapment at a local optimum, the current study improves the solving process for enhancing performance in practical production and environmental protection.

By applying the nontardy constraint to practical production, the current study attempted to minimize makespan costs. A Cmax minimization genetic algorithm (CGA) and energy minimization genetic algorithm (EGA) are proposed for use in the first stage of solving two-stage multiprocessor flow shop scheduling problems and minimizing makespan costs. Furthermore, an adjusted Cmax minimization genetic algorithm (ACGA) and adjusted energy minimization genetic algorithm (AEGA) used in the second stage were compared for obtaining superior solutions and aiding enterprises in increasing profits and lowering overhead costs. The current study compared the proposed solution with two reported solutions that yielded comparable improvements.

The remainder of the paper is organized as follows: In Section 2, the FFS is formulated. In Section 3, the basic algorithms are introduced briefly. Then, the framework of energy-saving genetic algorithm for solving the FFS is proposed in Section 4. The influence of parameter setting is investigated based on design of experiment testing in Section 4, and computational results and comparisons are provided as well. Finally, we end the paper with some conclusions in Section 5.

2. Problem Definition

According to notation rule of Pinedo [27], the current study formulates the problem as $FF_k | EP_t, State | EC | T_j = 0$. FF_k represents k -stage flexible flow shop scheduling environment. EP_t means different electricity bill in each period. $State$ denotes three conditions of operation: stand-by, or shut-down of machines, and re-operation of machines also consumes power. $EC | T_j = 0$ demonstrates all operations of non-tardy jobs must complete before completion dates in order to minimize electricity costs. **Figure 1** demonstrates the Gantt

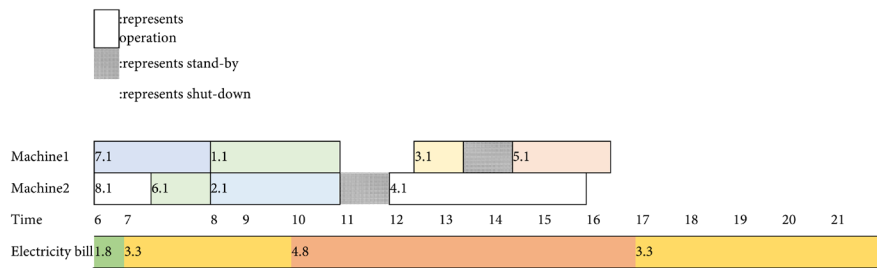


Figure 1. State of machine process.

chart of the attempted problem.

The FFS problem provides multiple identical parallel machines at each station for increasing capacity and reducing costs in practical production. One machine at every station can be selected for each job and the process begins from the first station. After the final job is completed in the second stage, all jobs are completed.

The scope and constraints of this study are demonstrated as follows:

- 1) Number of jobs, machines and stages are known.
- 2) Processing time of each job on each machine is known and constant.
- 3) Each machine in each stage can only process one job simultaneously.
- 4) The sequence through which jobs pass through machines may differ with the sequence of machine receiving job.
- 5) Jobs cannot be preempted.
- 6) There is no permutation, or machine breakdown.
- 7) The job ready time is 0.
- 8) Machines can switch into operation, stand-by, and shut-down.

2.1. Notation

- T = total period set, all jobs in this study
- M = total parallel machines at stage i , all machines in this study
- D = due date set, all jobs completed dates in this study
- J = job set, all jobs waiting for scheduling in this study
- K = stage set, all stages in this study
- C_{max} = the maximal completion time of all jobs
- d_j = the due date of job J_j
- C_{jkm} = the completion time of job J_j processed in the m -th machine at the k -th stage
- S_{jkm} = the starting time of job J_j processed in the m -th machine at the k -th stage
- P_{jkm} = the processing time of job J_j processed in the m -th machine at the k -th stage
- E_t^O = the turn-on energy consumption of all machines at t -th time
- E_t^I = the stand-by energy consumption of all machines at t -th time
- E_t^R = the working energy consumption of all machines at t -th time
- e_{km}^O = the working energy consumption in the m -th machine at the k -th stage

e_{km}^I = the stand-by energy consumption in the m -th machine at the k -th stage
 e_{jkm}^R = the working energy consumption of job J_j processed in the m -th machine at the k -th stage

EP_t = the electricity bill of different time period

α_{jkm_t} = indicator of whether job J_j is scheduled at the k -th stage in m -th machine at t -th time ($\alpha_{jkm_t} = (0, 1)$); if $\alpha_{jkm_t} = 1$, job J_j is processed at the k -th stage in m -th machine at t -th time; otherwise $\alpha_{jkm_t} = 0$)

β_{jkm_t} = indicator of whether job J_j is assigned at the k -th stage in m -th machine at t -th time ($\alpha_{jkm_t} = (0, 1)$); if $\alpha_{jkm_t} = 0$, job J_j is processed at the k -th stage in m -th machine at t -th time; otherwise $\alpha_{jkm_t} = 1$)

Y_{km_t} = indicator of whether at the k -th stage the m -th machine turned on at t -th time ($Y_{km_t} = (0, 1)$); if $Y_{km_t} = 1$, the m -th machine was turned on at t -th time; otherwise $Y_{km_t} = 0$)

δ_{km_t} = indicator of whether at the k -th stage the m -th machine turned off at t -th time ($\delta_{km_t} = (0, 1)$); if $\delta_{km_t} = 0$, the m -th machine was turned off at t -th time; otherwise $\delta_{km_t} = 1$)

2.2. Mathematical Model

1) Objective function

$$\min \sum_{t \in T} EP_t (E_t^R + E_t^I + E_t^O) \quad (1)$$

Equation (1) is the objective formulation and is primarily designed for minimizing energy consumption costs, such as those during operation, standby mode, and working. This equation measures the common criterion of the completion of all jobs and aids enterprises in improving the energy consumption and efficiency of production scheduling.

2) Total energy consumption

$$E_t^I = \sum_{j \in J} \sum_{k \in K} \sum_{m \in M} \beta_{jkm_t} \delta_{km_t} e_{km}^I, \quad t \in T \quad (2)$$

$$E_t^R = \sum_{j \in J} \sum_{k \in K} \sum_{m \in M} \alpha_{jkm_t} e_{jkm}^R, \quad t \in T \quad (3)$$

$$E_t^O = \sum_{m \in M} \gamma_{km_t} e_{km}^O \quad (4)$$

Equation (2) is the standby total energy consumption of all machines at the t -th time. Equation (3) is the total energy consumption of all machines in the t -th time period. Equation (4) is the turn-on total energy consumption of all machines in the t -th time period.

3) Completion time of job

$$C_{jkm} \leq d_j, \quad j \in J, k \in K, m \in M \quad (5)$$

$$C_{jkm} = S_{jkm} + P_{jkm}, \quad j \in J, k \in K, m \in M, t \in T \quad (6)$$

$$C_{jkm} \leq S_{(j+1)km}, \quad j \in J, k \in K, m \in M \quad (7)$$

$$C_{jkm} \leq S_{(k+1)m}, \quad j \in J, k \in K, m \in M \quad (8)$$

Equation (5) is the time for completing job j before the due date. Equation (6)

is the completion time of job j by the m -th machine at the k -th stage and equals the starting time plus the processing time. Equation (7) is the completion time of job j by the m -th machine at the k -th stage and is no longer than the starting time of job $(j + 1)$ for the m -th machine at the k -th stage. Equation (8) is the completion time of job j by the m -th machine at the k -th stage and is no longer than the starting time of job j for the m -th machine at the $(k + 1)$ -th stage. Because of continuous production, the processing time prolongs the completion time and consumes energy. Therefore, minimizing energy consumption can remain the primary objective of machines for further production.

4) The constraints of job processing

$$\sum_{m \in M} \alpha_{jkm} = 1, j \in J, k \in K, t \in T \tag{9}$$

$$\gamma_{kmt} + \delta_{kmt} \leq 1, k \in K, m \in M, t \in T \tag{10}$$

$$\alpha_{jkm} = \delta_{kmt}, j \in J, k \in K, m \in M, t \in T \tag{11}$$

Equation (9) controls all jobs during each stage and ensures that they are processed only once. Furthermore, Equation (10) controls the m -th machine and ensures that only one job can be processed by it. Finally, Equation (11) determines whether the m -th machine is turned off at the t -th time ($\delta_{kmt} = (0, 1)$); if $\delta_{kmt} = 0$, the m -th machine was turned off at t -th time; otherwise $\delta_{kmt} = 1$.

3. Concept of Energy-Saving Genetic Algorithm Solving Procedure

According to $FF_k | EP_t, State | EC | T_j = 0$, this study constructed energy-saving genetic algorithm (ESGA) using two-stage solving procedures: a genetic algorithm for maximizing the makespan and another for minimizing energy consumption in the second stage. **Figure 2** demonstrates the starting time of solutions applied in the first stage to avoid on-peak hours.

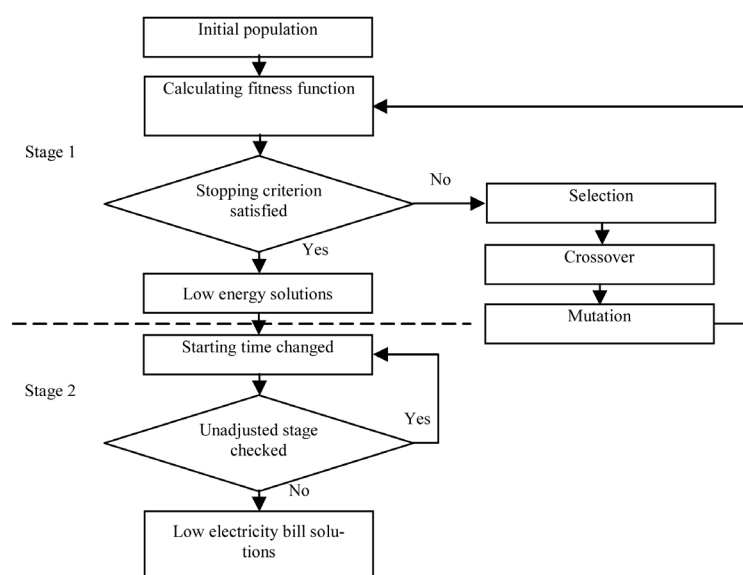


Figure 2. Flow chart of solving procedure of ESGA.

3.1. The First Stage of ESGA

This study utilized two genetic algorithms for solving problems: the CGA for minimizing the makespan and calculating the electricity cost and EGA for determining low energy consumption scheduling and calculating the electricity cost concurrently [6]. The procedures of the proposed method are demonstrated as follows:

3.1.1. Encoding

According to Dai *et al.* [6], a job set, stage set, and machine set ($s = 1, 2, \dots, k$) are present at each stage. This study formulated FFS scheduling as a genetic matrix in which the columns are jobs and stages are rows.

$$A_{k \times j} = \begin{bmatrix} a_{1,1} & \cdots & a_{1,j} \\ \vdots & a_{1,1} & \vdots \\ a_{k,1} & \cdots & a_{k,j} \end{bmatrix} \quad (12)$$

The $a_{m,n}$ ($m = 1, 2, \dots, k, n = 1, 2, \dots, j$) is a real number in the interval $(1, M_s)$. $a_{m,n}$ indicates which machine processes job j , and the decimal indicates the processing sequence; the lower the decimal is, the earlier the job is processed. A coding matrix represents a chromosome in which $k \times j$ genes are present.

$$[a_{1,1}, a_{1,2}, \dots, a_{1,j}, a_{2,1}, a_{2,2}, \dots, a_{k,j}] \quad (13)$$

For example, in FFS scheduling, the coding matrix consists of three stages, in which there are two machines and eight jobs to be processed.

$$A = \begin{bmatrix} 1.301 & 2.533 & 1.415 & 2.76 & 1.824 & 2.351 & 1.113 & 2.204 \\ 1.261 & 1.997 & 2.442 & 1.528 & 2.609 & 1.016 & 2.224 & 2.185 \\ 1.518 & 1.635 & 2.254 & 2.965 & 2.753 & 1.378 & 2.181 & 2.156 \end{bmatrix} \quad (14)$$

Row 1 represents processing conditions of the first stage. The $a_{1,1} = 1.301$ means J_1 processed in machine 1, $a_{1,2} = 2.533$ means J_2 processed in machine 2, and $a_{1,3} = 1.145$ means J_3 processed in machine 1. The decimal of $a_{1,1}$ is 0.301 smaller than 0.415 of $a_{1,3}$, which represents $a_{1,1}$ is processed earlier than $a_{1,3}$.

$$\begin{aligned} & [1.301, 2.533, 1.415, 2.76, 1.824, 2.351, 1.113, 2.204, 1.261, \\ & 1.997, 2.442, 1.528, 2.609, 1.016, 2.224, 2.185, 1.518, 1.635, \\ & 2.254, 2.965, 2.753, 1.378, 2.181, 2.156] \end{aligned} \quad (15)$$

3.1.2. Initial Population

The initial solution is the first population of a genetic algorithm. Generally, two methods can generate initial solutions: one is randomly generated and other requires research. The scale of the initial population affects the efficiency and quality of solutions. A random initial solution was used in this study.

3.1.3. The Fitness Function

The fitness function can identify the quality of chromosomes, enabling inferior solutions to be screened out. The fitness function of the CGA is as follows:

$$f(x) = \frac{1}{C_{\max}} \quad (16)$$

The fitness function of EGA is as below:

$$f(x) = \frac{1}{\sum_{i \in T} EP_i (E_i^T + E_i^I + E_i^O)} \quad (17)$$

3.1.4. Selection

The algorithm selects a favorable parent from chromosomes and proceeds with crossover and mutation. Each chromosome has a fitness value, which determines the possibility for crossover and mutation. This study adopted roulette wheel selection.

3.1.5. Crossover

The proposed algorithm partially exchanges two chromosomes. In this study, the exchange rate was set as, which is a rounded-up approximation of the quantity of exchanged chromosome multiplied by the exchange rate. If the quantity of exchanged chromosome is odd, then one chromosome is added to the total chromosomes and the quantity becomes even. The exchange rate was set at 0.9, and this study adopted a two-point crossover method to solve the considered problem.

3.1.6. Crossover

Mutation can generate multiple and various children. A mutation rate of P_m was set in this study. The proposed method arbitrarily generates a probability value. If the value is below the mutation rate, mutation occurs. The mutation rate was set at 0.1. The mutation rate is uniformly distributed from 0 to 1. If the rate becomes 1, the proposed algorithm regenerates an interval of real numbers $(1, M_s + 1)$.

3.2. The Second Stage of ESGA

Although the genetic algorithm generates scheduling with lower electricity costs, some jobs still generate high electricity costs. The solutions generated from the GCA and EGA in the first stage were adjusted using the ACGA, and problems in the second stage were solved using the AEGA to avoid high-energy price periods.

The adjustment rule begins from the final stage and proceeds in descending order. The proposed approach organizes the operations into the final order. The method gradually schedules operations in the off-peak period and moves the sequence of operation away from the on-peak period until all jobs are scheduled.

Figure 3 illustrates the flow chart.

3.3. A Brief Example

In a job scheduling scheme consisting of three stages, two machines at each stage, and eight jobs to be processed, the total working time is 16 hours and the

factory working period is from 6 a.m. to 10 p.m. on each day. **Table 1** shows the operation time:

Table 2 shows the consumed energy of machines. The starting time of the machines is assumed to be short with sudden turn-on energy consumption.

Table 3 shows the electricity costs of every time period. The parameters of the proposed method are as follows: initial population, 30; exchange rate, 0.9; mutation rate, 0.1; and stopping criterion, 300 iterations.

3.3.1. The First Stage of ESGA

Figure 4 shows the computational result using CGA, and the electricity bill is NT\$ 3277.8.

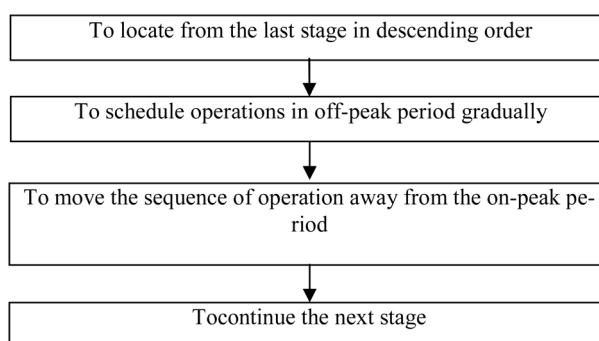


Figure 3. Flow chart of solving procedure of ESGA.

Table 1. The operation working time.

Jobs		The working time of jobs at different stages		
		Stage 1	Stage 2	Stage 3
1	Hour	3	4	1
2	Hour	3	2	2
3	Hour	1	2	3
4	Hour	4	2	3
5	Hour	2	2	0.5
6	Hour	0.5	1	1.5
7	Hour	2	0.5	1
8	Hour	1.5	2	1.5

Table 2. The operation working time.

Conditions of machines	Stage 1	Stage 2	Stage 3
Stand-by (kW)	3	7	6
Operation (kW)	8	18	17
Turn-on (kW)	4	10	8

Remarks: This study assumes the starting time of machine is short with a sudden turn-on energy consumption.

Figure 5 shows the computational result using EGA, and the electricity bill is NT\$ 2900.6.

3.3.2. The Second Stage of ESGA

The adjustment rule begins from the final stage and proceeds in descending order. The proposed approach organizes operations into the final order. The method gradually schedules operations in the off-peak period and moves the sequence of operation away from the on-peak period until all jobs are scheduled. **Figure 6** shows the computational result obtained using the ACGA and the electricity cost is NT\$ 2929.7.

Figure 7 the computational result using AEGA, and the electricity bill is NT\$ 2807.4.

Table 4 lists four computational results obtained using the CGA as the

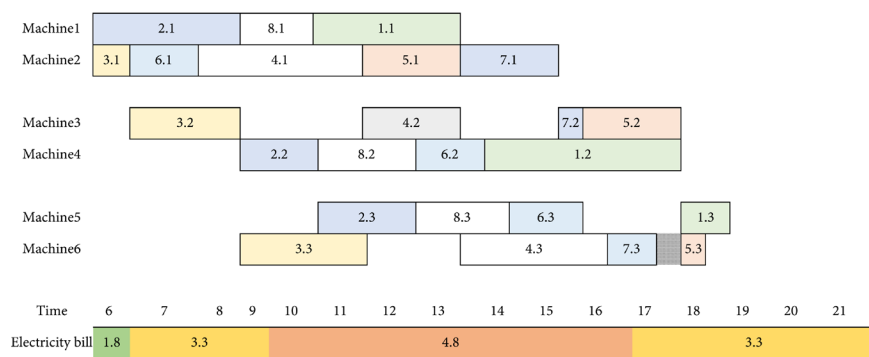


Figure 4. The Gantt chart of computational result using CGA.

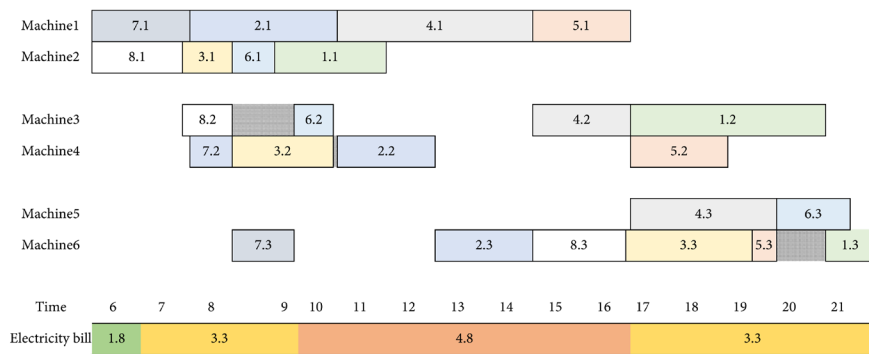


Figure 5. The Gantt chart of computational result using EGA.

Table 3. The electricity bill of time periods.

Factory working period		6:00~20:00
Time period		Summer electricity price (NT\$)
Off-peak	6:00~7:00	1.8
Mid-peak	7:00~10:00	3.3
	17:00~20:00	3.3
On-peak	10:00~17:00	4.8

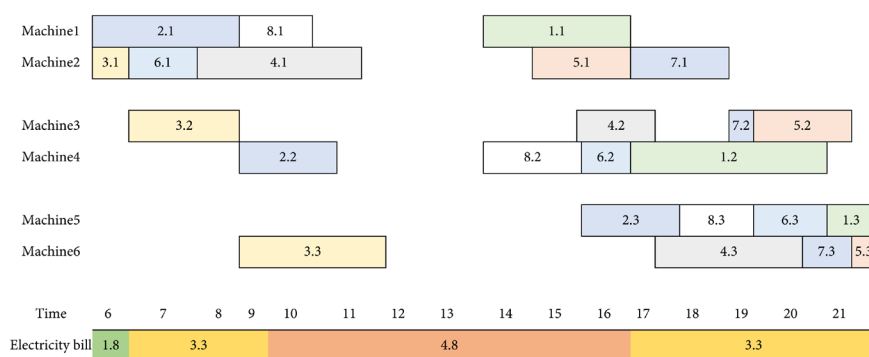


Figure 6. The Gantt chart of computational result using ACGA.

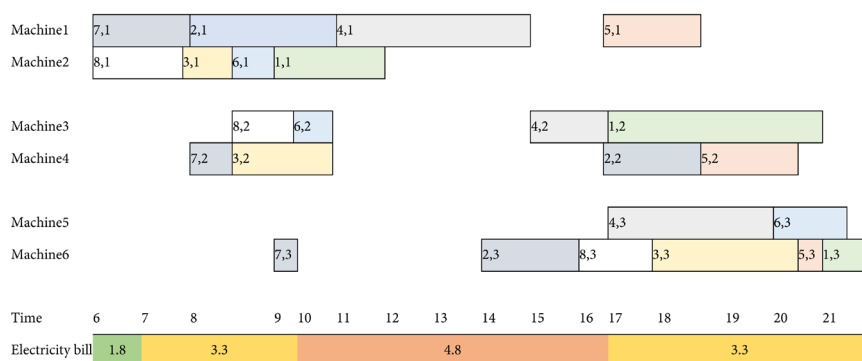


Figure 7. The Gantt chart of computational result using AEGA.

Table 4. Comparison of electricity bills.

	CGA	EGA	ACGA	AEGA
Electricity bills (NT\$)	3277.8	2900.6	2929.7	2807.4
Comparison costs ratio	1	0.88	0.89	0.86

benchmark for comparison. According to **Table 4**, applying the CGA generates the highest electricity cost, because it neglects the costs of standby, shutdown, and different time periods. Furthermore, the EGA considers different conditions of machines and can lower the electricity cost; however, jobs are processed in the on-peak period. The proposed method using ESGA can efficiently avoid processing jobs in the on-peak period. Moreover, ESGA can lower the electricity cost by up to 11% and 14%, respectively, compared with the CGA. The results demonstrate higher energy saving with the AEGA than with the CGA, EGA, and ACGA.

4. Computational Experiments

All tests were conducted on a PC with an Intel® Core™ i5-4300U 1.9-GHz CPU with 8 GB of RAM. The operation system used was Windows® 8.1. The FFS scheduling problem is $FF_k | EP_i, State | EC | T_j = 0$. The parameters of the proposed method are the number of jobs, type of stage, number of machines, energy

consumption of machines, processing time of jobs, and due dates. For the considered problems, the number of jobs was 30, 60, or 90; the type of stage was 3 or 5; and the number of machines in the two stages = 6, 9. **Table 2** and **Table 5** show the energy consumption of machines. Moreover, the processing time of jobs was limited within U [2] [9]; the unit time was 30 minutes; the factory working period was from 6 a.m. to 10 p.m. on each day; and the electricity costs of various time periods are shown in **Table 3**. The formula of the due date $(1-TF)\sum_{i=1}^k \bar{P}_i(1+(k+1)*0.25)$, among which the \bar{P}_i represents the average processing time of machines, and TF is the tardy factor; Type I was 0.3 and Type II was 0.5. The working duration per day was assumed to be 16 hours. Therefore, when the formula of the due date provided a duration of 20 hours, the due date was estimated to be 2 days. Finally, the parameters of the genetic algorithms were set on the basis of a pretest to improve the results; specifically, the initial population was 30; the exchange rate was 0.9; the mutation rate was 0.1; and the stopping criterion was 500 iterations.

4.1. Analysis of Effectiveness

To assess the effectiveness of the proposed algorithm in solving the considered problems, 12 conditions were applied to randomly test 30 generated problem sets; specifically, the number of jobs was 30, 60, or 90; the type of stage was 3 or 5; and the number of machines in the two stages was 6 or 9. **Table 6** provided a comparison of the average solutions and average solving times of the CGA, EGA, ACGA, and AEGA for efficacy analysis under Type I of slacker due dates.

Table 7 provided a comparison of the average solutions and average solving times of the CGA, EGA, ACGA, and AEGA for efficacy analysis under Type II of non-slacker due dates.

Table 6 and **Table 7** illustrate that for different due dates, the cost of energy consumption is lower for the ACGA and AEGA than for the CGA. Type I has slacker due dates than those of Type II, indicating that the EGA and AEGA provide superior solutions. A data set of 30/6/5 has the same due date as that of Type I and Type II; therefore, the improvement is not remarkable. The CGA calculates the electricity cost for the minimal makespan; therefore, the CGA and ACGA might not provide superior solutions in the Type I condition. **Table 8** show comparison cost ratios for electricity costs obtained using all methods under Type I of slacker due dates.

Table 8 and **Table 9** show comparison cost ratios for electricity costs obtained using all methods under Type I of non-slacker due dates.

Table 5. The energy consumption during three time periods of 5-stage machines.

Conditions of machines	Stage 1	Stage 2	Stage 3	Stage 4	Stage 5
Stand-by (kW)	3	7	6	6	5
Operation (kW)	8	18	17	15	14
Turn-on (kW)	4	10	8	7	7

Table 6. The effectiveness of time window Type I.

j/m/k	CGA		EGA		ACGA		AEGA	
	Avg.	CPU time(s)	Avg.	CPU time(s)	Avg.	CPU time(s)	Avg.	CPU time(s)
30/6/3	12673	5.8	8558	7.1	12471	6.6	8314	7.5
30/6/5	22519	9.9	15957	12.1	20681	11.3	15438	12.6
30/9/3	13173	6.4	8721	7.6	12405	7.2	8616	8.2
30/9/5	23098	11.4	16516	13.8	20893	12.2	15706	14.4
60/6/3	26545	15.3	19420	17.6	24187	16.5	18242	18.2
60/6/5	44668	27.4	37244	32.4	42057	30.3	34822	33.2
60/9/3	25903	16	18763	19	24779	18.2	18412	19.7
60/9/5	44647	27	36474	31.7	42664	29.9	34236	32.1
90/6/3	39398	25.7	31909	29.4	37783	28.5	29634	30.8
90/6/5	65787	48.5	57154	53.9	62155	51.3	53657	55
90/9/3	40014	26.7	31456	30.5	37869	29.7	30431	31.1
90/9/5	66557	31.5	57340	37.4	64741	33.6	53933	38

Remarks: The unit cost is NT\$.

Table 7. The effectiveness of time window Type II.

j/m/k	CGA		EGA		ACGA		AEGA	
	Avg.	CPU time(s)	Avg.	CPU time(s)	Avg.	CPU time(s)	Avg.	CPU time(s)
30/6/3	12700	5.7	8650	7.3	12523	6.7	8473	7.8
30/6/5	22243	10.2	16467	11.9	21347	10.9	15992	12.5
30/9/3	13041	6.4	8659	7.5	12597	7	8507	8.1
30/9/5	22773	11.3	17036	14.2	21965	12.7	16325	14.8
60/6/3	27427	15.1	20036	17.5	24911	16.8	18868	18.4
60/6/5	44884	27	37302	32.7	42566	29.6	36043	33.7
60/9/3	26008	15.6	19167	18.9	25348	17.8	18843	19.5
60/9/5	44988	27.5	36825	31.5	42497	30.2	35445	32.1
90/6/3	39286	25.3	33843	28.7	37859	27.6	31830	29.3
90/6/5	67006	47.1	57504	53	63318	51.9	55136	54.8
90/9/3	39850	27.2	33224	30.6	37368	29.4	32200	31.3
90/9/5	67166	32.4	57519	37	65489	34.2	54244	37.9

Remarks: The unit cost is NT\$.

Table 8 and **Table 9** illustrate that the EGA, ACGA, and AEGA yielded lower electricity costs than did the CGA. Moreover, the AEGA provided solutions superior to those of the ACGA method in terms of effectiveness.

4.2. Analysis of Robustness

To assess the robustness of the proposed algorithms in solving the considered problems, 12 conditions were applied to test the same solution 30 times;

Table 8. The comparison costs ratio of electricity bills of time window Type I.

j/m/k	CGA	EGA	ACGA	AEGA
30/6/3	1	0.68	0.98	0.66
30/6/5	1	0.71	0.92	0.69
30/9/3	1	0.66	0.94	0.65
30/9/5	1	0.72	0.90	0.68
60/6/3	1	0.73	0.91	0.69
60/6/5	1	0.83	0.94	0.78
60/9/3	1	0.72	0.96	0.71
60/9/5	1	0.82	0.96	0.77
90/6/3	1	0.81	0.96	0.75
90/6/5	1	0.87	0.94	0.82
90/9/3	1	0.79	0.95	0.76
90/9/5	1	0.86	0.97	0.81
Avg.	1	0.77	0.94	0.73

Table 9. The comparison costs ratio of electricity bills of time window Type II.

j/m/k	CGA	EGA	ACGA	AEGA
30/6/3	1	0.68	0.99	0.67
30/6/5	1	0.74	0.96	0.72
30/9/3	1	0.66	0.97	0.65
30/9/5	1	0.75	0.96	0.72
60/6/3	1	0.73	0.91	0.69
60/6/5	1	0.83	0.95	0.80
60/9/3	1	0.74	0.97	0.72
60/9/5	1	0.82	0.94	0.79
90/6/3	1	0.86	0.96	0.81
90/6/5	1	0.86	0.94	0.82
90/9/3	1	0.83	0.94	0.81
90/9/5	1	0.86	0.98	0.81
Avg.	1	0.78	0.96	0.75

specifically, the number of jobs was 30, 60, or 90; the type of stage = 3, 5; and the number of machines in the two stages $M_s = 6, 9$. **Table 10** and **Table 11** provide a comparison of the average solutions, optimal solutions, and poorest solutions calculated using the CGA, EGA, ACGA, and AEGA in the analysis of robustness.

The test results in **Table 10** and **Table 11** for robustness show that the ACGA and AEGA are affected by original solutions during adjustment procedures,

Table 10. The robustness of time window Type I.

j/m/k	CGA		EGA		ACGA		AEGA	
	Best Worst	Avg. [Std. dev.]	Best Worst	Avg. [Std. dev.]	Best Worst	Avg. [Std. dev.]	Best Worst	Avg. [Std. dev.]
30/6/3	11330	12202	8136	8991	11083	11693	7964	8507
	12687	[492.6]	9105	[356.6]	12249	[422.5]	8832	[307]
30/6/5	21853	22469	16430	17232	21090	21836	15082	16030
	23085	[677.9]	18034	[537.5]	22272	[427.3]	16512	[420.3]
30/9/3	11336	12253	8521	8819	10534	11707	8100	8381
	13170	[684.2]	9118	[353.6]	12430	[686.5]	8864	[497]
30/9/5	20937	22169	16131	16707	19170	21395	15434	15805
	23189	[862.1]	17282	[457.5]	22567	[1304.3]	16172	[295.2]
60/6/3	24779	25987	19118	19822	23062	24515	18267	18945
	27195	[984.5]	20513	[653.2]	25432	[936.9]	19706	[646.8]
60/6/5	42020	43378	35442	35805	39517	41239	34267	35256
	44735	[999.2]	36632	[676.3]	42368	[1065.6]	36301	[758.8]
60/9/3	24565	25913	18209	18920	24124	24719	17415	18288
	27261	[1149.6]	19711	[594.7]	25826	[646.8]	18753	[370.2]
60/9/5	43167	44852	35305	36377	41856	42481	33707	35112
	46538	[1209.4]	37244	[881.6]	43784	[865.1]	36761	[845.2]
90/6/3	38541	39749	32015	33263	37124	37712	27963	29877
	40956	[907.9]	34513	[955.7]	38134	[438]	31085	[1161.7]
90/6/5	65226	66485	55357	56175	61613	62774	52056	53456
	67744	[929.0]	57823	[913.8]	63426	[720.1]	54253	[889.5]
90/9/3	39596	40707	30663	31270	35614	37211	29920	30545
	41817	[839.8]	31878	[436.2]	37759	[941.5]	31085	[416.2]
90/9/5	65027	66754	55440	56450	62526	64235	54006	54620
	68482	[1270.9]	57461	[682.9]	66064	[1878.7]	55744	[674.4]

Remarks: The unit cost is NT\$.

causing the electricity cost to decrease partially. Thus, the robustness of the proposed method was fairly identified.

5. Computational Experiments

This study investigated the use of limited resources of parallel machines to promote practical production and environmental protection. Ideal practical production for better energy using effective scheduling prevents processes from excessive energy consumption and energy price fluctuations. Recent studies on sustainable manufacturing focused on energy saving to reduce the unit production cost and environmental impacts.

Most importantly, the application of the optimization of the scheduling can be respected for costs down and energy-saving simultaneously. Under an operational environment in which electricity costs differ depending on the time period, manufacturing activities in machine shops increase electricity consumption costs. In particular, machine conditions and job processing time periods are crucial factors in making energy-saving decisions during the manufacturing process.

Table 11. The robustness of time window Type II.

j/m/k	CGA		EGA		ACGA		AEGA	
	Best Worst	Avg. [Std. dev.]	Best Worst	Avg. [Std. dev.]	Best Worst	Avg. [Std. dev.]	Best Worst	Avg. [Std. dev.]
30/6/3	11882	12654	8357	8732	11719	12501	8020	8557
	13695	[727.8]	8995	[285.6]	13527	[769.7]	8990	[346.5]
30/6/5	20613	22795	16819	18037	20512	21555	15525	16015
	23183	[794.7]	19539	[939.6]	22919	[791.5]	17692	[983.6]
30/9/3	11685	12432	8435	8641	11414	12287	8211	8490
	13150	[551.6]	8886	[257.9]	13058	652.9	8831	[239.5]
30/9/5	20870	22116	16431	17273	20720	21755	15632	16178
	22629	[764.1]	17863	[483.5]	22232	[552.2]	16812	[444.5]
60/6/3	24996	26199	19632	20292	23821	24872	18579	19216
	27493	[1040]	20944	[409.6]	25713	[741.9]	20105	[563.4]
60/6/5	42195	43873	35972	36790	40297	42243	34933	35929
	45796	[1267.5]	37976	[500.5]	44283	[1425.9]	37009	[657.7]
60/9/3	25168	26187	19257	20118	24323	25308	17821	18603
	27220	[747.1]	20980	[634.1]	26260	[760.3]	19056	[743.8]
60/9/5	42133	44225	35563	37033	40184	42705	34534	35509
	46152	[1551.5]	38106	[1311.8]	44258	[1595.9]	36907	[1163.7]
90/6/3	38663	39708	31907	33670	37485	37807	30927	32197
	41731	[1228.7]	34748	[1059.8]	38319	[341.1]	34023	[1393.3]
90/6/5	65131	66630	56002	57442	62199	64249	53741	54987
	67830	[1007.9]	58882	[1111.8]	65876	[1429.4]	56412	[1180]
90/9/3	38270	39270	32262	33093	36261	37340	30489	31587
	40291	[720.2]	34060	[664.9]	38974	[918.2]	32286	[649.5]
90/9/5	66374	67386	55781	57005	63054	64489	54669	55593
	68401	[737.8]	58106	[896.2]	66193	[1320.7]	56518	[779]

Remarks: The unit cost is NT\$.

According to the analysis, the CGA, EGA, ACGA, and AEGA can efficiently solve problems. The electricity cost ratio for the CGA, EGA, ACGA, and AEGA is 1:0.78:0.95:0.74, demonstrating that the AEGA can efficiently solve the problem. The robustness test results show that the ACGA and AEGA of ESGA are affected by original solutions during adjustment procedures and partially reduce electricity costs. Thus, the robustness of the proposed method was appropriately identified. As a whole, the proposed method can lower electricity bills to fit green energy nowadays.

Finally, enterprises can adopt the proposed method for enhancing practical production in the flexible job shop scheduling environment and generate profits by fully exploiting the advantages of the method in the future. In addition, the proposed method can mitigate the environmental impact of manufacturing processes and protect environment at the same time.

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