

# Brain Function Diagnosis Enhanced Using Denoised fNIRS Raw Signals

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## Abstract

Nowadays, brain function evaluation using Functional Near Infrared Spectroscopy (*fNIRS*) is one of the most potential non-invasive monitoring techniques. This paper concerns usefulness of the *NIRS* signals denoising using the *Hemodynamic Evoked Response (HomER)* as graphical user interface displays the *NIRS* data, fast independent component analysis (*FASTICA*) method to reduce data dimension and the combined *Wavelet & PCA* method for enhancing *NIRS* signals. *NIRS* signals include many types of noise, spread across a broad spectrum of frequencies, such as: low frequency noise from respiratory interference, 0.1 - 0.3 Hz, *Mayer* wave, about 0.1 Hz, cardiac interference, 0.8 - 2.0 Hz, and other artifacts from head and facial motions. Meanwhile, electronic components generate high frequency noise. *Multi-resolution wavelet and PCA* was applied successfully to enhance the *NIRS* signals. It consists of adaptively modifying the wavelet coefficients based on the degree of noise contamination of the processed *NIRS* signal. This is done subsequently to the signal pre-processing by reducing data dimension using the *FASTICA* method. We demonstrate, using *signal-to-noise ratio* and *correlation* indicators, that the technique used is superior to the wavelet and moving average filter and outperforms the proposed denoising *NIRS* signal.

## Keywords

fNIRS; FASTICA; PCA; Wavelet

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## 1. Introduction

*NIRS* is a new medical device that can be used for long term monitoring of brain activity in several diseases of the human brain. Recently several laboratories have focused on *NIRS* for functional imaging. Among the most common methods used in the clinical setting are the traditional methods of *magnetic resonance imaging (MRI)* and *positron emission tomography (PET)*. *NIRS* is a new technique in the medical imaging field. *NIRS* is gaining

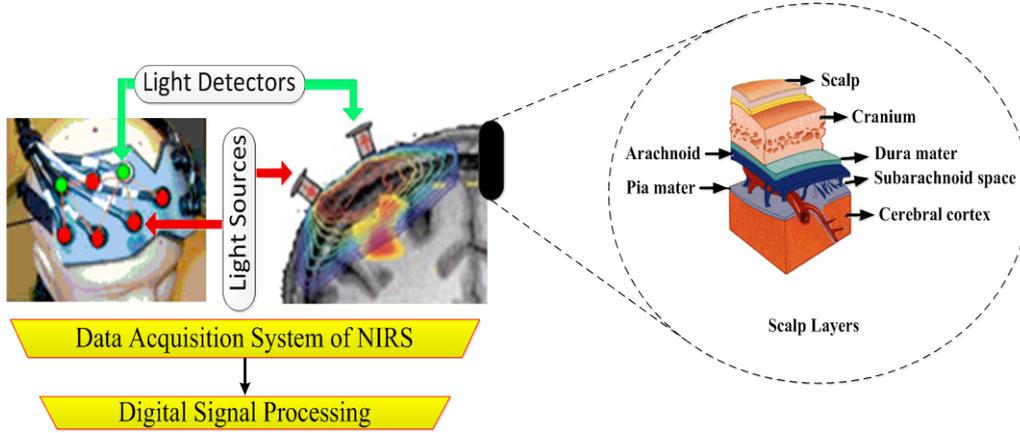
recognition amongst clinicians as it has enabled functional studies of most areas of the brain. These studies focus on research for the prevention and treatment of strokes [1] [2], the observation of the state of newborn and adult brains, and the rehabilitation [3] of the brain after strokes. Additionally, research is exploring its application to the study of certain psychiatric disorders. *NIRS* works primarily by sensing the oxygen variation in the blood through the absorption of red and near-infrared light [4]. In *NIRS*, a light with a wavelength ranging from 630 nm to 1000 nm is applied to the head and passes through the brain. The amount of light detected corresponds directly to the amount of oxygen present, which is of course a function of the oxy-deoxy hemoglobin concentration and the amount of blood present in the brain. Oxy-deoxyhemoglobin based on the absorption and diffusion computation of light in the near infrared spectrum [5]; thus, the corresponding wavelengths can be determined. In last 10 years, *NIRS* has become the focus of several laboratories' research. The goal is to improve it for use in medical equipment for monitoring brain function. When using *NIRS* to study changes in oxy-deoxygenated hemoglobin in brain and scalp tissue, noise signals will reflect the subject (patient) movements since such motion will cause changes in scalp blood circulation. This type of noise is typically present in *NIRS* signals and results in significant distortion of *NIRS* data. Unfortunately, such noise appears quite regularly but without constant amplitude or location, meaning that it can be found anywhere in the spectrum. This noise is random and we have no prior information about such artifacts; however, several methods have been proposed for de-noising and/or removal of interference and motion artifacts from *NIRS* signals. Additionally, numerous methods exist to reduce global interference, which causes physiological noise effects. These methods consist of the subtraction of an average "noise" (cardiac) waveform [6], low-pass filtering, principal components analysis and adaptive filtering using a pulse oximetry reference waveform [7] [8]. Unfortunately simple low-pass filtering is a weak method in *NIRS* signals de-noising, because the frequency bands of physiological noise and stimulus evoked activations are highly overlapping. Subtraction of an average "noise" method corrects one type of oscillation but does not consider the non-stationarity of the oscillation shape. Recently, adaptive filtering has been proposed as a possible method to *NIRS* noise removal. This latest method requires a reference signal correlated with the noise signal that should be removed [9] [10]. This method is also applicable to the removal of motion artifacts. To achieve this, we apply "Sources-Detectors", which are co-located sources and detectors in each optode [11]. Additionally, some people suggest the application of wavelet decomposition for the detection and removal of interference from the *NIRS* signal [12]-[14]. All of these methods of denoising a *NIRS* signal are applied, but their success depends upon several factors such as "Sources-Detectors" positions, distance, and type of electronic components and the status of subjects.

In this paper, we address the task of *NIRS* signal denoising to enhance quality of diagnosis based on the new *NIRS* system. We consider the following candidate technique to obtain *NIRS* dataset: *HomER* toolbox, *FASTICA*, and wavelet with *PCA*. These techniques are the most commonly used *NIRS* based data. A toolbox *HomER* is applied to be the brain-computer interface and analyse the data in real time. We employ a *FASTICA* method to reduce the dimension of the data. Followed by the wavelet and *PCA* method to denoising the *NIRS* signals, performance measurements are employed to evaluate the denoising signals in terms of signal quality enhancement.

This paper is organized as follows: Section 2 briefly reviews and presents the extract *NIRS* signal using optical measurement via a continuous wave. Section 3 displays sources and types of noise. We describe methods and materials used in *ICA* for reducing data dimension, *Multivariate Wavelet* with *PCA* for denoising data, and the steps of our algorithm with performance measurements in Section 4. Experimental results and discussions based on a comparative study are presented in Section 5. Finally, conclusion is provided in Section 6.

## 2. Extract *NIRS* Signals

While many techniques exist for creating *NIRS* signals, in our work, we focus on optical measurement by *continuous wave (CW)*. *CW* is most commonly used to evaluate brain function imaging. It consists of high temporal resolution and low cost photon detectors. Alternative types of *NIRS* creation are more complex. Some use light sources to measure the phase of the recovered signals (Frequency domain) or the temporal distribution of photons (Time domain). The Frequency and Time domain method is advantageous as it creates a three-dimensional (3D) image. *NIRS* by *CW* uses light sources to emit a continuous permanent beam at a specific location point in the tissue. Near infrared light can enter deep into the scalp via transfusion through the scalp layers: cranium, dura mater, arachnoids, subarachnoid space, pia mater and cerebral cortex (see [Figure 1](#)). The light penetration is a function of the separation between the source and the detector. As the distance increases the light transfuses



**Figure 1.** Schemas of CW-NIRS data acquisition system and the position of light sources and detectors.

deeper; however, the common limit on separation is usually *interoptode distance (IOD)* of 3 cm. While we have described a single source-single detector system, in actuality we used a network of sources and detectors on the subject's head, each separated by approximately 3 cm. The measured quantity is directly related to the change in optical density  $\Delta OD$  that occurs between the source and the detector. Each detector reports a voltage linearly varying with the amount of light detected. To obtain the *chromophore concentration* ( $C_i$ ) for each detector, we often used *Beer-Lambert law* to convert light intensity to  $C_i$  according to the mathematical model shown in the following equation:

$$\log \frac{I_0}{I_1} = \left( \sum_i^n \alpha_i(\lambda) c_i \right) L \quad (1)$$

where  $I_0$  is an input light intensity and  $I_1$  is an output light intensity.  $\lambda$  is the wavelength of source light,  $\alpha_i$  is the corresponding in tissue absorption,  $L$  is the path length between the optodes emission and detection, and  $c$  is the chromophore concentration. There are two major issues inherent to the basic form of *Beer-Lambert* equation. First, it does not consider diffusion, which would of course give rise to significant errors in the study. Second, the distance between the optodes does not correspond exactly to the distance traveled by light. To correct this error, a *Differential path Length Factor (DPF)* is added to the *Beer-Lambert* equation. Additionally a constant must be added to the equation for the diffusion model. This constant, however, creates a new problem in that *CW-NIRS* cannot evaluate this constant. In order to solve this problem, it is necessary to transform this equation to differential form. This does not obtain absolute concentrations; rather, it provides changes in concentration over time [15]. Using two different wavelengths, we construct a system of two linear equations with two unknowns:

$\Delta[HbO_2]$  and  $\Delta[HbR]$  as shown in the following equation:

$$\begin{bmatrix} \Delta C_{HbO_2}(t) \\ \Delta C_{HbR}(t) \end{bmatrix} = \begin{bmatrix} \epsilon_{HbO_2}^{\lambda_1} & \epsilon_{HbR}^{\lambda_1} \\ \epsilon_{HbO_2}^{\lambda_2} & \epsilon_{HbR}^{\lambda_2} \end{bmatrix}^{-1} \begin{bmatrix} \Delta OD(t, \lambda_1) \\ \Delta OD(t, \lambda_2) \end{bmatrix} \quad (2)$$

where  $\Delta[HbO_2]$  and  $\Delta[HbR]$  are the chromophore concentration changes of oxyhemoglobin and de-oxyhemoglobin respectively.  $\epsilon_{HbO_2}(\lambda)$  and  $\epsilon_{HbR}(\lambda)$  are extinction coefficients, and  $\Delta OD(\lambda)$  is the change in optical density measured at a given wavelength.

There are several factors that influence the accuracy of the measurements such as: choice of illumination wavelength, optodes positions, noise from electrical interferences, physiology noise and environmental subjectivity. Due to this, a signal processing is a necessary step to reduce noise from the light intensity signal. Noise sources will be discussed in detail in the following section.

### 3. Noise Types

#### 3.1. Physiological Noise

*NIRS* physiological noise is the internal noise that arises while the patient is immobile. Though we find noise on *NIRS* signal, we can't delete this type of noise because we have almost no information about it. To deal with it,

we use an average filter to reduce the power of the noise. Sources of this noise found in the *NIRS* signal is the frequency of the heartbeat, about 0.7 to 1.5 Hz, the frequency of blood pressure or Mayer wave, 0.1 Hz, and the frequency of breathing, between 0.13 and 0.33 Hz. These frequencies appear in the signal as noise. Additionally, hemodynamic fluctuation cycle is considered noise; however, this particular noise is useful in identifying normal and sick subjects.

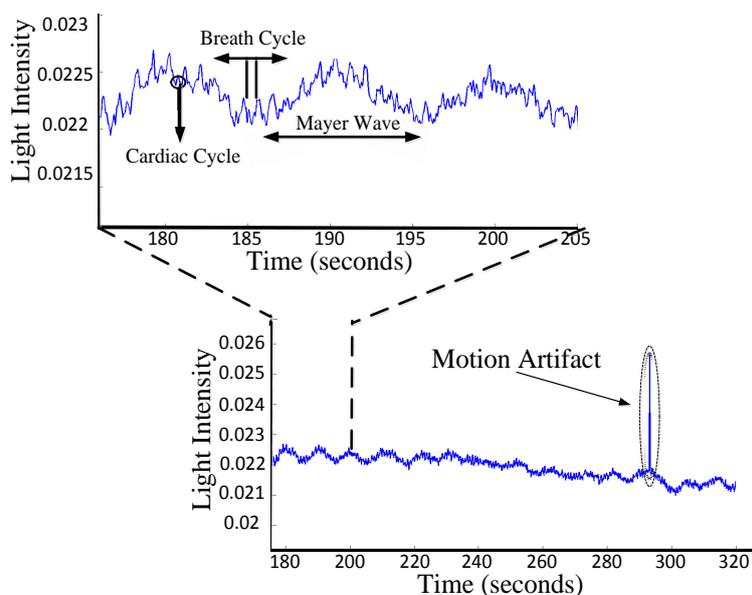
### 3.2. Electronics Components and Experimental Noise

Electronic noise results from the electronic components used in the experiment and is generally found in the frequency domain. To eliminate it, we always use a low-pass filter. Interference light can be minimized by modulating the emitted light and demodulating the detected signal. Additional experimental noise is motion artifact. This noise is difficult to handle because motion artifact appears as appropriate information. This is due to optode position and weak contact between electrodes and head. Recently several methods have been proposed to reduce the impact of motion artifact using *Wiener*, *Kalman* filtering and *Wavelet*-based [16]-[18], to add to the filtering proposed in the introduction. Finally, to improve the quality of our data, it's necessary to ensure we have good coupling with the skin. With all this, if there are no physiological oscillations present, meaning there is no signal detection from our optical receiver, then it is clear that we have a problem in optode. **Figure 2** presents types of signals and noises from *NIRS*.

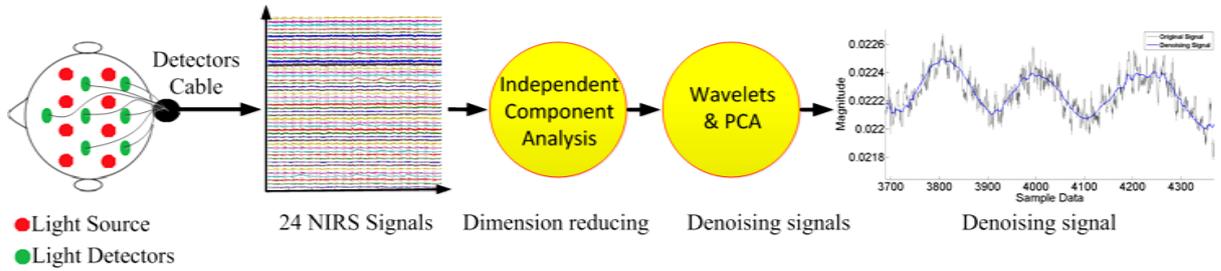
## 4. Materials and Methods

Schematic representation of a *NIRS* system for brain functional evaluation is shown in **Figure 1**. The dataset is obtained from *Polystim laboratory, Montreal, Canada*. Raw data of 47 patients have a stroke disease has been analyzed to test the performance of the proposed approach. The age of the patients in the dataset ranges from 20 to 70 years. In the following, a brief description of signals extraction using the *NIRS* system and their enhancement signals. Here, the *NIRS* signals were analyzed in preprocessing to get the  $\Delta[HbO_2]$  and  $\Delta[HbR]$ .

As mentioned above, each type of filter discussed can help in de-noising *NIRS* signal; however, we have no filter to efficiently remove all noise types because we have a variable frequency *NIRS* signal with variable magnitude. To accommodate such variability, we need a filter with adaptability. Each recorder consists of 24 *NIRS* signals (12 by  $\lambda 735$  nm and 12 by  $\lambda 850$  nm). We used *independent component analysis (ICA)* to reduce large dimension data, and then we applied multivariate de-noising using wavelets and principal component analysis. **Figure 3** presents our methodology for the signal processing to evaluate brain function based on *NIRS* data.



**Figure 2.** Schemas of physiological oscillations including the cardiac cycle, breath cycle, motion artifact (right side) and Mayer waves.



**Figure 3.** Schematic of the NIRS data analysis, The NIRS data from detectors, then 24 signals, is reduced by ICA method and after which de-noising by wavelets and principal component analysis occurs.

We extracted 24 NIRS signals; this refers to the coupling of source-detector ( $S1D1$ ,  $S1D2$ ,  $S1D3$ ... $S4D1$ ... etc.). We obtained a matrix [ $24 \times \text{number of samples}$ ] and reduced it by ICA method. This step can reduce the global noise when it appears only in independent signals.

#### 4.1. Independent Component Analysis Method

ICA is a multivariate data analysis that has been studied recently in the signal processing community for blind source separation. This work proposes to demonstrate the interest of ICA in a particular to reduce the dimension of the original data. The concept of ICA assumes that data is linearly mixed via a set of separate independent sources and then separates these signal sources according to their statistical independency as measured by mutual information [19]-[22]. The model for ICA can be expressed with the following mathematical equation:

$$x = A * s \quad (3)$$

where  $x$  is the mixed signal source vector,  $A$  is the mixing matrix and  $s$  is the signal source. The goal of ICA method is to find a demixing matrix  $A^{-1}$  that separates the signal source vector  $S$  into a set of sources that are statistically independent, meaning  $A^{-1}$  is the inverse matrix to go from the source vector  $S$  to the signal vector  $X$ . The estimated independent source signals should be equal to the original independent source signals. Our computed  $S$  depends upon the following expression:

$$S = A^{-1} * X \quad (4)$$

Our algorithm is based on the *FASTICA* in which *negentropy* is utilized as it is an excellent measurement of *non-Gaussianity*. This method can be reduced our NIRS data ( $24 \text{ signals} * \text{number of samples}$ ) without negatively affecting of the appropriate information in each signal. A limiting factor of ICA methods, as with all methods, is that it cannot give the same performance with high dimensionality because it will not diffuse the internal structure of NIRS data [23] [24]. **Figure 4** presents a model of the ICA method and its implementation will present in algorithm subsection.

#### 4.2. Multivariate Wavelet Denoising NIRS Signals Using PCA

The wavelet transform method effectively applies with many different types of signals in order to detect frequencies as a function of time. Due to the aforementioned NIRS channels characteristics, multivariate wavelet denoising is a good method to reduce global noise from signals. The concept uses principal component analysis to kill insignificant principal components in order to obtain an additional denoising effect. This method does not aim to discover new variables of interest, but to simply eliminate insignificant components. A multiscale of PCA has been proposed by *Bakshi* in order to fine tune the limits in statistical process control and dimensionality reduction of data. Classically, we make PCA based on the symmetric covariance or correlation matrix. This matrix can be computed from the data matrix where the covariance matrix is scaled by sums of squares and cross products. We apply the same methodology for computing the correlation matrix. PCA solves the eigenvalues and eigenvectors of a square symmetric matrix with sums of squares and cross products. The eigenvector associated with the largest eigenvalue reflects the same orientation as the first principal component and the eigenvector associated with the second largest eigenvalue determines the orientation of the second principal component. The trace of this square matrix represents the sum of the eigenvalues, while the number of columns in the matrix represents the number of eigenvectors. *Multiscale PCA* begins with a multivariate signal, “NIRS Signals”, and

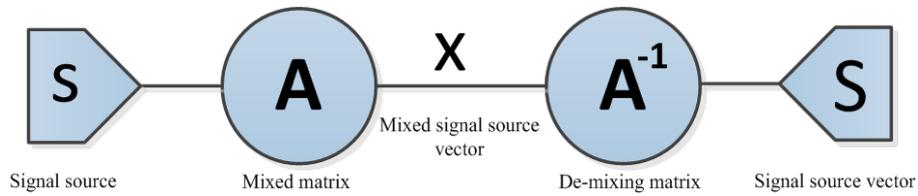


Figure 4. Model of ICA method in general case.

uses a simple representation at each resolution level. By this step, we can generalize a normal *PCA* of a multivariate signal represented as a matrix of different levels simultaneously. We used *PCA* to perform an approximation of the coefficients matrix in the wavelet, and finally we reconstructed *NIRS* signals by selecting the number of retained principal components [25]-[30].

### 4.3. Algorithm

The *Matlab* algorithm we developed includes two consecutive parts. First it receives 24 to 32 channels of Near Infrared Spectroscopy from a portable *NIRS* device, which is data based on a *HomER* toolbox that records and processes in real time. Specification of the Toolbox allows the algorithm to perform the 24 or 32 signals and apply different signals and image processing techniques. In the second part, the algorithm extracts and reduces the data using *FASTICA* toolbox, and then applies a *Multivariate Wavelet* denoising with *PCA* in order to produce data with as minimal noise as possible. Finally, it measures several performance indicators: Signal to Noise Ratio and correlation in order to evaluate enhanced data or signals [31]. We used 24 signals including 12 signals based on  $\lambda 735$  and 12 signals based  $\lambda 850$ . We reduced and observed data, with the percent of data reduction set to 33.4%. Our algorithm, shown below, is divided into the following three steps:

1) We use *homer* Toolbox to extract signals from our data acquisition system and perform our analysis. We save our data as *NIRS* format “*nirs*” for independent processing. Additionally, this toolbox possesses the capability to reconstruct an image from obtained signals.

2) Next, we use *FASTICA* for reducing the dimension of our data using *negentropy* technique according to the following stages:

- a) Center the data “signal” or take the mean of the data,  $E\{signal\}$
- b) Whiten signal to maximize *non-Gaussian* characteristics: “filtering”,  $E\{xx^T\}$ , ...
- c) Choose an initial random vector,  $\|A\|=1$ , ...
- d) Normalize the *non-Gaussian* where  $A=A/\|A\|$ , ...
- e) Iterate until convergence
- f) Compute the final independent component where  $S=[A_1 A_2 A_3 \dots A_n] * X$
- g) Separate the sources where  $S_1 S_2 S_3 S_4 \dots S_n$  are source signals.

3) Lastly, we use *Multivariate Wavelet* denoising with *PCA* to reduce the global noise because simply performing step 2 is not sufficient to enhance the quality of the *NIRS* signals. The technique used here is divided into the following stages:

- a) Read multivariate signals ( $S_1 \dots S_n$ )
- b) Determine the level of wavelet decomposition
- c) Choose retained number of principal components based on *Kaiser’s* rule and perform *multiscale of PCA*.

In order to evaluate our performance algorithm for enhancing *NIRS* signals, we computed the signal to noise ratio *SNR* and *correlation* coefficient between signals processed and the original signals. These indicators can be expressed by the following equations:

$$SNR = 10 \text{Log} \left( \frac{\sum_{i=1}^N s_i^2}{\sum_{i=1}^N (x_i - s_i)^2} \right) \quad (5)$$

The *SNR* indicator computed represents a comparison between the original signal power and the noise signal power. *SNR* value reflects enhancement by signal processing.

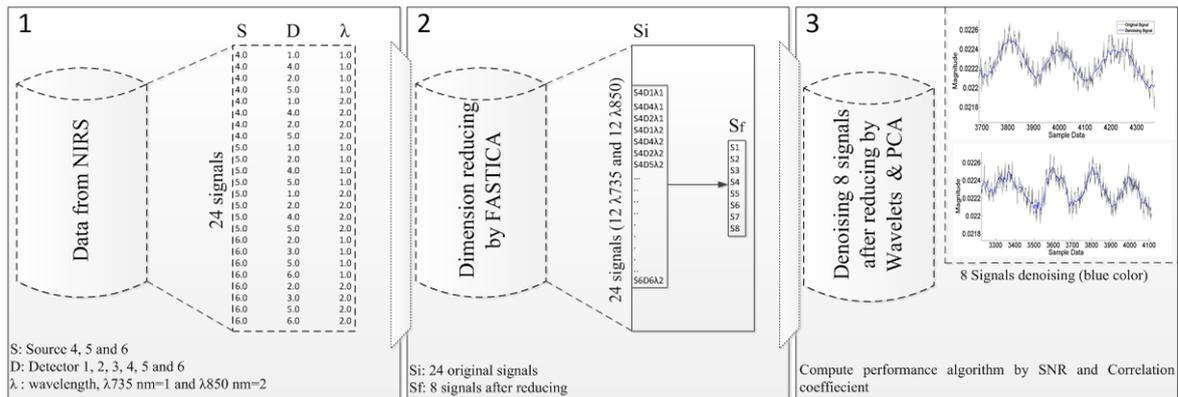
$$\text{Corr}(s, x) = \frac{\text{cov}(s, x)}{\sigma_s \sigma_x} \quad (6)$$

where  $\sigma_s$  and  $\sigma_x$  are the standard deviations of source signal and output signal respectively.

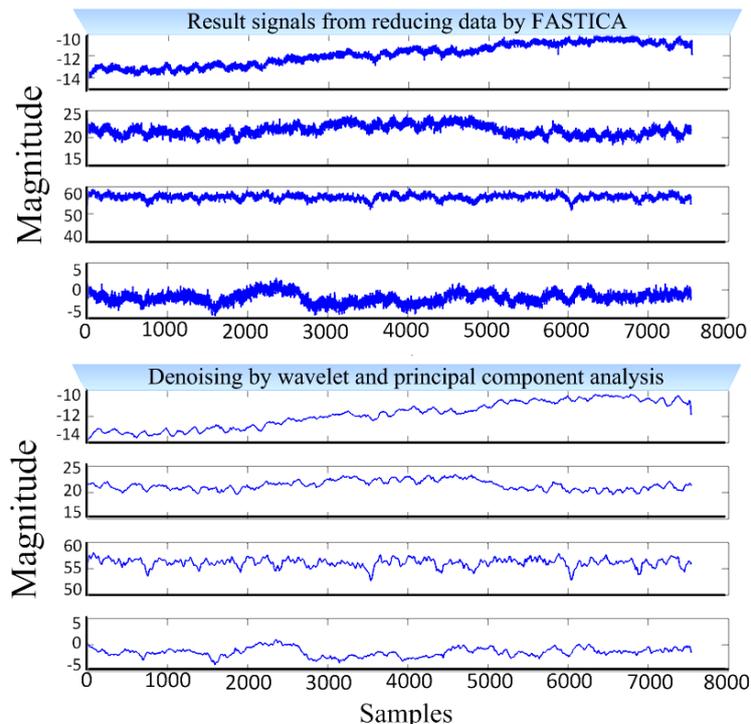
We computed the correlation coefficient as a second indicator for evaluating the relationship between source signal ( $s$ ) and output signal ( $x$ ), where  $s$  is the original signal and  $x$  is the signal after noises cancelation. **Figure 5** illustrates in details the processing of the 3 initial steps of the general algorithm.

### 5. Experimental Results and Discussions

We first provide some results on natural *NIRS* signals in order to understand the improvements obtained using our methodology. All the experiments were done on Matlab v. 2012a, run on an *Intel core i7, 3.2 GHz processor*. As we mentioned above, our algorithm divides into 3 principal steps. Via empirical computation, we arrived at 33.4% reduction of data dimension. *FASTICA* is efficient for pre-denoising and strong for reducing data dimension. Based on this, we present results of denoising signals by Wavelet and principal component analysis as illustrated in **Figure 6**. Evaluation of the performance of denoising the signal is presented in **Table 1**. It presents



**Figure 5.** Scheme of general algorithm applied on NIRS system.



**Figure 6.** Result of denoising applied to NIRS signals after FASTICA reduced dimension processing.

**Table 1.** Results of signal to noise ratio and the correlation.

	Signal	SNR/Wavelet	SNR/moving average filter	SNR/wavelet & PCA	Correlation/Wavelet	Correlation/moving average filter	Correlation/wavelet & PCA
λ735 nm	S1	39.90	33.43	38.63	0.98	0.96	0.99
	S2	37.50	35.06	34.11	0.89	0.15	0.9
	S3	32.86	29.33	40.2	0.81	0.74	0.83
	S4	20.83	5.35	29.91	0.83	0.50	0.85
	S5	16.63	10.55	12.49	0.91	0.57	0.75
	S6	38.60	24.38	39.19	0.89	0.96	0.99
	S7	39.39	32.84	39.78	0.99	0.41	0.90
	S8	3.20	4.31	2.34	0.98	0.55	0.98
	S9	33.26	36.64	33.70	0.93	0.41	0.94
	S10	47.11	35.40	48.27	0.96	0.65	0.94
	S11	40.51	39.03	41.25	0.92	0.82	0.96
	S12	3.9	32.94	7.59	0.69	0.34	0.72
	S13	32.8	33.43	38.63	0.81	0.96	0.99
	S14	39.9	32.9	7.6	0.7	0.6	0.74
λ850 nm	S15	32.7	33.4	38.6	0.84	0.95	0.9
	S16	39.9	33.4	38.66	0.91	0.96	0.99
	S17	37.51	35.02	34.14	0.9	0.89	0.91
	S18	32.8	29.3	40.22	0.83	0.83	0.85
	S19	20.82	5.32	29.9	0.85	0.84	0.86
	S20	25.1	12.12	32.91	0.88	0.8	0.86
	S21	38.61	24.39	39.2	0.9	0.96	0.99
	S22	46.2	29.8	34.1	0.98	0.73	0.90
	S23	45.6	34.9	40.20	0.89	0.76	0.93
	S24	6.2	6.07	30.36	0.83	0.70	0.95
Average	30.3	26.5	31.92	0.88	0.7	0.9	

signal to noise ratio (*SNR*) and correlation (*Corr*) applied on three denoising techniques. These indicators demonstrated good average results for *SNR* (31.9252) and *correlation* (0.9005) of *multivariate wavelet & PCA*. It is clear from our *SNR* and *Correlation* values for *wavelet and multivariate wavelet & PCA* that these are, in principle, more adapted to the *NIRS* data. The results of **Table 1** show the variation between adaptive methods (*wavelet and multivariate wavelet & PCA*) and a non-adaptive denoising method (*moving average filter*). Note, adaptive methods are not limited to the two methods applied to *NIRS* data. However, in the case of our *NIRS* device we have no ideal signal as reference to apply other adaptive methods. In addition, the noise quantity on *NIRS* signals reflects the type of light sources and detectors. When we have good light quantity emitted, these light detectors will give us quality information represented by high magnitude signals. We choose to do a compromise among the following constraints in order to get minimum noise and thus receive accurate medical diagnoses: miniaturized *NIRS* device, reduced power consumption, minimized electronic component noise [32] [33]. Miniaturized *NIRS* device used a low power consumption which provides weak amplitude of *NIRS* signals.

## 6. Conclusions

In this paper, we presented a new algorithm dedicated to processing *NIRS* signals based on *HomER* toolbox for extracting *NIRS* signals, a *FASTICA* method for reducing *NIRS* data, and *Wavelet & PCA* for efficiently denoising *NIRS* signals, while all sub-algorithms used *Matlab* v. 2012a.

Simulation results of the *FASTICA* method displayed an efficiency in data reducing at 33.4% (3 signals taken from 12 signals based on wavelength 735 nm and 3 signals taken from 12 signals based on wavelength 850 nm). Denoising achieved using *Multivariate wavelet & PCA*. We provided a performance indicator using *SNR* (31.9252) and *correlation* (0.9005). These indicators displayed an advantage to our methods relative to conventional methods in denoising signals. Our algorithm is adaptive to several types of biomedical signals such as *EEG* and *ECG*. Furthermore, the three steps composing our algorithm are relatively simple. *Multivariate wavelet & PCA* uses the principle of thresholding, which makes no complicated assumptions on the structure of the signal; thus, no particular model of the *NIRS* signal is needed to be assumed. The denoising method should, therefore, be chosen according to the signals in hand. So, in our case, we found *Multivariate wavelet & PCA* is a successful, fully adaptive method for our type of *NIRS* signals. With this in mind, further work will focus on developing a hardware implementation of *FPGA* in order to achieve robustness and extract high quality information for proper medical diagnoses.

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