

Phase space in EEG signals of women referred to meditation clinic

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ABSTRACT

Poincare plots are commonly used to study the non-linear behavior of physiological signals. In the time series analysis, the width of Poincare plots can be considered as a criterion of short-term variability in signals. The hypothesis that Poincare plot indexes of electroencephalogram (EEG) signals can detect dynamic changes during meditation was examined in sixteen healthy women. Therefore, the aim of this study is to evaluate the effect of different lags on the width of the Poincare plots in EEG signals during meditation. Poincare plots with six different lag (1-6) were constructed for two sets of data and the width of the Poincare plot for each lag was calculated. The results show that during meditation the width of Poincare plots tended to increase as the lag increased. The Poincare plot is a quantitative visual tool which can be applied to the analysis of EEG data gathered over relatively short time periods. The simplicity of the width of Poincare plot calculation and its' adaptation to the chaotic nature of the biological signals could be useful to evaluate EEG signals during meditation.

Keywords: Electroencephalogram; Meditation; Poincare Plots; Nonlinear Dynamics

1. INTRODUCTION

Meditation, a technique that frees the mind from distractions and allows for communication with the Master Within, can lead to numerous physical, mental and spiritual benefits. Meditation is a unique state of consciousness with associated changes in the physiological and psychological functions in the brain. Some research has shown that meditation characterized by marked reductions in metabolic activity, increased orderliness and

integration of brain functioning, decreased peripheral vascular resistance, and increased cerebral blood flow. In addition, meditation produces comprehensive improvements in mental health, enhancing positive features, and reducing various forms of psychological distress [1].

The electroencephalogram (EEG) signals reflect the electrical activity of the brain. The study of the brain electrical activity, through the electroencephalographic records, is one of the most important tools for the diagnosis of neurological diseases. The initial time series analysis based on statistical indexes was soon replaced by more sophisticated analysis capable of extracting more information of the signal.

Since the dynamics of the brain system are chaotic, nonlinear methods have been applied to the analysis of EEG signals. One of these techniques is the Poincare plot. This technique was first used as a qualitative tool and later, the quantification of the Poincare plot geometry was proposed.

In previous studies, Poincare plot is extensively used for qualitative visualization of heart rate signals. Tulppo *et al.* [2] fit an ellipse to the shape of the Poincare plot in order to calculate heart rate indices. Brennan *et al.* [3] demonstrate that the width of the Poincare plot indicates the level of short-term variability in heart rate signals. A number of variations have been proposed, in order to optimize the use of the Poincare plot as a quantitative tool [4,5]. One of them is the lagged Poincare plot. The conventional plot has two dimensions and a lag of one interval, *i.e.*, each point on the plot consists of a pair of successive intervals (RR_i, RR_{i+1}). Lerma *et al.* [6] used longer lags (RR_i, RR_{i+t} with $1 \leq t \leq 8$) to analyze HRV in chronic renal failure patients. Contreras *et al.* [4] showed that lagged Poincare widths and spectral indices might be useful to distinguish normal from pathological heart rate signals. Thakre and Smith [7] used lags from 1 to 10 for heart rate analysis in patients with chronic heart fail-

ure.

Other investigators have reported systematic changes in EEG trajectories associated with the seizure onset [8]. We felt that such changes might also be found in the EEG during meditation. Because of its sensitivity to the state of a system, the Poincare trajectory is potentially valuable for visualizing changes such as the transition from the normal state to meditation. We decided to explore Poincare trajectories associated with this transition, and to describe the changes systematically that were evident, in the Poincare plots. However mathematical manipulations of the EEG have failed to give way to visual inspection as a primary clinical tool. Therefore, we were interested in the possible value of this visual tool, which is based on current concepts from nonlinear dynamic analysis, but has the advantage of providing detailed information that can be scrutinized by the human eye. Since these trajectories may provide a new way to characterize, describe, and quantify EEG dynamics, we wished to evaluate their possible usefulness in the specific psycho-physiological state.

The aim of the present study was to evaluate the width of the Poincare plot with different lags on EEG signals during meditation. For this purpose, we used the EEG signals of two groups of subjects (before meditation and during meditation). Poincare plots with six different lag (1-6) were constructed and the width of the Poincare plot for each lag was calculated.

The outline of this study is as follows. At first, we briefly describe the sets of the EEG signals used in our study. Then, we explain the Poincare plot and its' width. Finally, we present the results of analysis of Poincare plots with six different lags (1-6), and we conclude the study.

2. METHOD

2.1. Data Collection

Subjects were considered to be at an advanced level of meditation training. The sixteen meditators, took part in the study (women, age range 30 - 53, mean 38.19 years). The subjects were in good general health and did not follow any specific heart diseases. The subjects were asked not to eat salty or fat foods before meditation practices or data recording. Informed written consent was obtained from each subject after the experimental procedures had been explained.

The experimental procedure was divided into two different stages: Subjects were first instructed to sit quietly for 5 minutes and kept their eyes closed. After that, they performed meditation. Meditation prescribes a certain bodily posture. They sit on a cushion 5 to 10 centimeters thick that is placed on blanket. They cross their legs so that one foot rests on the opposite thigh with the sole of

their foot turned up and with their knees touching the blanket (lotus or half-lotus position). The torso should be kept straight, but it should not be strained. The head should be kept high with eyes closed. During this session, the meditators sat quietly, listening to the guidance of the physician and focusing on the breath.

The meditation EEG signals were recorded in meditation clinic using 16-channel Powerlab (manufactured by ADInstruments). EEG activity was recorded using three electrodes (*i.e.*, Fz, Cz and Pz) according to the International 10-20 System, referenced to linked ear lobe electrodes. The monitoring system hardware filters band passed data in range: 0.1 - 50 Hz for EEG time series. A digital notch filter was applied to the data at 50 Hz to remove any artifacts caused by alternating current line noise. The sampling rate was 400 Hz.

2.2. Poincare Plots

Poincare plot is a geometrical representation of a time series in a Cartesian plane. A two dimensional plot constructed by plotting consecutive points is a representation of time series on phase space or Cartesian plane [5]. A standard Poincare plot of EEG signal is shown in **Figure 1**. Two basic descriptors of the plot are SD_1 and SD_2 . The line of identity is the 45° imaginary diagonal line on the Poincare plot and the points falling on the imaginary line has the property $X_n = X_{n+1}$. SD_1 measures the dispersion of points perpendicular to the line of identity, whereas SD_2 measures the dispersion along the line of identity.

Fundamentally, SD_1 and SD_2 of Poincare plot is directly related to the basic statistical measures, standard deviation of time series (SDX), and standard deviation of the successive difference of time series ($SDSD$), which is given by the relation shown in (1) and (2).

$$SD_1^2 = \frac{1}{2}SDSD^2 = \gamma_X(0) - \gamma_X \quad (1)$$

$$SD_2^2 = 2SDX^2 - \frac{1}{2}SDSD^2 = \gamma_X(0) + \gamma_X(1) - 2\bar{X}^2 \quad (2)$$

Where $\gamma_X(0)$ and $\gamma_X(1)$ is the autocorrelation function for lag 0 and lag 1 of data intervals and \bar{X} is the mean of time series intervals. From (1) and (2), it is clear that the measures SD_1 and SD_2 are actually derived from the correlation and mean of the time series with lag 0 and lag 1. The above equation sets are derived for unit time delay Poincare plot. Researchers have shown interest in plots with different time delays to get a better insight in the time-series signal. Usually the time delay is multiple of the cycle length or the sampling time of the signal [3]. The dependency among the variables is controlled by the choice of time delay, and the most conventional analysis is performed with higher order linear correlation be-

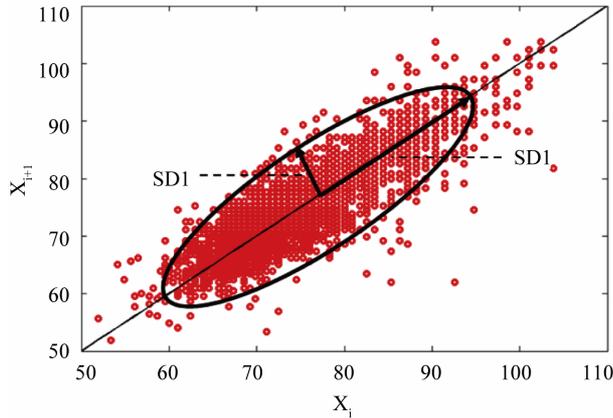


Figure 1. Standard Poincare plot (lag 1). SD_1 and SD_2 represent the dispersion along minor and major axis of the fitted ellipse.

tween points.

In case of plotting the 2D phase space with lag m the equations for SD_1 and SD_2 can be represented as:

$$SD_1^2 = \gamma_X(0) - \gamma_X(m) \Rightarrow SD_1 = F(\gamma_X(0), \gamma_X(m)) \tag{3}$$

$$SD_2^2 = \gamma_X(0) + \gamma_X(m) - 2\bar{X}^2 \Rightarrow SD_2 = F(\gamma_X(0), \gamma_X(m)) \tag{4}$$

Where $\gamma_X(m)$ is the autocorrelation function for lag m time series. This implies that the standard descriptors for any arbitrary m lag Poincare plot is a function of autocorrelation of the signal at lag 0 and lag m .

3. RESULTS

Poincare plots with six different lag (1-6) were constructed and the width of the Poincare plot for each lag was calculated. There is a significant difference between two measures of the transversal and longitudinal dispersion of the cloud of points in Poincare plots. After we constructed Poincare plots, SD_1 was calculated for each lag. **Figure 2** shows the influence of different lags on SD_1 within each group.

In both groups, SD_1 tended to increase as the lag increased. The SD_1 value of two different lags (1 and 6) for all subjects during meditation are shown in **Figure 3**. As shown in **Figure 2** and **Figure 3**, the relative changes of SD_1 with increasing lag were also significantly higher during meditation.

The mean value of SD_1 for Poincare plot in Fz, Cz and Pz channels with two different lags (1-6) are shown in **Table 1**. The values of SD_1 with lag 1 are about 1.53 - 1.94, but they are at around 8.52 - 10.95 with lag 6 in all channels. According to the results, as the lag increases the shape of the plots becomes more circular during meditation.

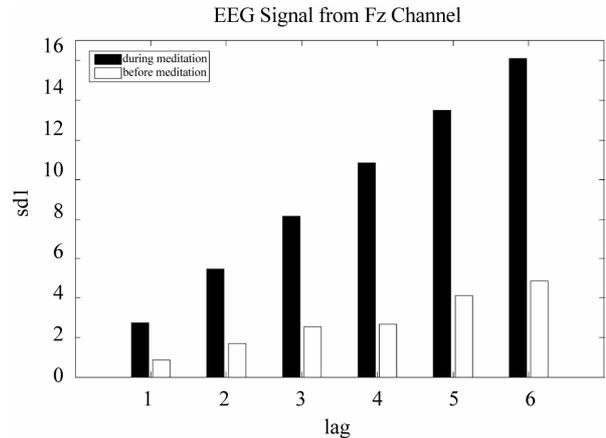


Figure 2. SD_1 for different lags (1-6) in Fz channel before and during meditation (record S7).

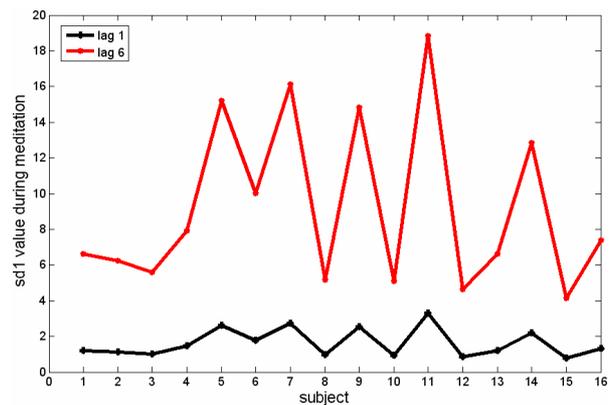


Figure 3. SD_1 value of sixteen subjects with two different lags (1 and 6) during meditation.

Table 1. The average value of SD_1 during meditation.

EEG Channel	The average value of SD_1 during meditation	
	Lag 1	Lag 6
Fz	1.63	9.20
Cz	1.94	10.95
Pz	1.53	8.52

4. DISCUSSION

Poincare plot is one of the important techniques used for visually representing the signals' variability. It is valuable due to its ability to display nonlinear aspects of the data sequence. In this study, we examined the influence of different lags on the Poincare plots of EEG signals in three channels (Fz, Cz and Pz) in the specific psycho-physiological state. The results show that the Poincare plots with different lags have different shapes during meditation. The Poincare plots are cigar-shaped plots for lag 1, whereas round clouds of points are shown for

higher lags. The reason of this change is, when points are plotted against immediately preceding points (lag 1), the correlation between these will be increased if they were more widely separated. Cigar-shaped plots expressed the high correlation, whereas round clouds of points are typical of lack of correlation.

On a lag 1 Poincare plot, SD_1 measures the variability from one point of time series to the next. However, when we consider SD_1 from Poincare plots with longer lags, the term of the variability is extended, from one point of time series to another separated from it by many intervals. The longer the distance between these points, the higher the mean time interval between the Poincare plots points which are being summarized by SD_1 .

The major advantage of the Poincare plots lies in their relative insensitivity to artifacts. In addition, the simplicity of the width of Poincare plot calculation and its' adaptation to the chaotic nature of the biological signals could be useful to evaluate EEG signals during meditation.

5. CONCLUSION

In this study, we have shown that SD_1 tended to increase as the lag increased. The rate of changes in SD_1 with increasing lags was also significantly higher during meditation (Figure 2). These changes provide supplementary information about the activity of brain.

The comparative dynamic measures of the lagged Poincare plots give more insight of the EEG signals in a specific psycho-physiological state. We propose that these approaches of analysis can be used to improve the analysis of EEG signals.

Other indices of Poincare plots like the ratio of SD_1/SD_2 or asymmetry in the Poincare plot can be studied in the future. Furthermore, the influence of different lags on Poincare plots during meditation could be analyzed in other biological signals like electrocardiogram and respiration.

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