

Comparison between Simple and Advanced Data Analysis to Pure Oxygen Absorption Spectrum at the 1270 nm Band

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Abstract

Simple and advanced data analysis was carried out on the pure oxygen absorption spectrum by Voigt deconvolution method between 1200 - 1300 nm, which represented the near-infrared spectrum. Pressures were 1, 5, 10, 15, 20, and 25 bars at 298 K. Experimental spectral lines showed two peaks at 1264 nm belong to O_2 dimol and 1268 nm wavelength belong to O_2 monomer, but advanced analysis of spectral lines gave many peaks around those two peaks. The total number of energy levels (peaks) decreases when pressure increases.

Keywords

 O_2 Monomer, O_2 Dimol, Voigt Deconvolution, Gaussian Width, Lorentzian Width, Voigt FWHM

1. Introduction

The famous paper, which was written to treat the comprehensive oxygen spectrum, belonged to Krupenie [1], and a huge amount of data could be taken from The HITRAN molecular spectroscopic database [2]. And a group of Smith *et al.* published many excellent papers about oxygen spectrum, especially, at 1270 nm band, and another band [3]-[10].

In the near-IR, experimental lines of pure oxygen absorption at 1270 nm band show, apparently, two kinds of absorptions: the first is a discrete line from individual O_2 molecules (O_2 monomer), and the second is a continuum band, which arises from collision complexes of O_2 , such as O_2 - O_2 (O_2 dimol (oxygen binary of O_2 - O_2)). A continuous absorption band is characterized by O_2 dimol, which is a consequence of collision-induced absorp-

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The lowest singlet electronic excitation energy from the O₂ ground state is:

$$a^{1}\Delta_{g}\left(0\right) \leftarrow X^{3}\Sigma_{g}^{-}\left(0\right) + h\upsilon\left(1268.4\,\mathrm{nm}\right) \tag{1}$$

The ground state of O₂-O₂ is ${}^{3}\Sigma_{g}^{-}(\upsilon = 0) {}^{3}\Sigma_{g}^{-}(\upsilon = 0)$, and the first lowest electronic excitation energy from the O₂ dimol ground state due to the following processes:

$${}^{3}\Sigma_{g}^{-}(\nu=0)a^{1}\Delta_{g}(\nu=0) \leftarrow 1264.5 \text{ nm} + {}^{3}\Sigma_{g}^{-}(\nu=0) {}^{3}\Sigma_{g}^{-}(\nu=0)$$
(2)

Mechanisms of relation (1) are different from the relation (2), because the first comes from O_2 discrete line where the second comes from O_2 - O_2 band spectra.

Most excitations come from natural width according to Heisenberg's uncertainty principle that is subject to Lorentzian or natural line. Collisional broadening contributes to the collision line shape by Lorentz distribution function, and the Doppler broadening depends on the Maxwell velocity distribution in a gas, where the Doppler line shape is Gaussian. In many sometimes, conditions require consideration of all effects as the convolution of Voigt profile.

The Gaussian temperature (Doppler)-broadened profile and a collision (Lorentzian)-broadened profile are given as follows:

$$I_{\text{Gauss}} = I_0 \left(\text{offset} \right) + \frac{A}{\Gamma_G \sqrt{\pi/2}} e^{-2\frac{(\lambda - \lambda_c)^2}{\Gamma_G^2}} \left(\text{Gaussian intensity profile} \right)$$
(3)
$$I_{\text{Lorentz}} = I_0 \left(\text{offset} \right) + \frac{2A}{\pi} \frac{\Gamma_L}{4(\lambda - \lambda_c)^2 + \Gamma_L^2} \left(\text{Lorentzian intensity profile} \right)$$

Whereas, a Voigt profile, mathematically, is the convolution of the Gaussian and the Lorentzian intensities:

$$I_{\text{Voigt}} = I_0 \left(\text{offset} \right) + A \frac{2 \ln 2}{\pi^{3/2}} \frac{\Gamma_L}{\Gamma_G^2} \int_{-\infty}^{\infty} \frac{e^{-t^2}}{\left(\sqrt{\ln 2} \frac{\Gamma_L}{\Gamma_G}\right)^2} + \left(\sqrt{4 \ln 2} \frac{\lambda - \lambda_c}{\Gamma_G} - t\right)^2} dt \left(\text{Voigtian intensity profile}\right)$$
(4)

I = absorption intensity, I_0 = offset absorption intensity, A = absolute area under the spectral line (integrated absorption intensity), Γ_G = Gaussian width, Γ_L = Lorentzian width, λ = wavelength, λ_c = central wavelength.

Humlíček [14] developed a Voigt profile, and gave the equation of the Voigt spectral line width (Voigt FWHM (full width at half-maximum height) as follows:

$$\Gamma_{\rm FWHM} \cong 0.5346\Gamma_L + \left(0.2166\Gamma_L^2 + \Gamma_G^2\right)^{\frac{1}{2}}$$
(5)

When Doppler (Gaussian) component is constant and small, Lorentzian distribution will prevail.

Voigt deconvolution method is the opposite of Voigt convolution method. It aims to analyze every spectral line to their components. The simple method denotes to analyzing one or two of visible peaks, whereas the advanced method is a full survey to all peaks and analyzes all appeared and disappeared peaks to their components.

The aim of this paper is to analyze the experimental results of pure oxygen spectrum at 1270 nm band by a simple and advanced Voigt deconvolution method.

2. Experimental

All spectra measurements of pure oxygen were carried out at the spectroscopy laboratory. Absorption spectrum in the NIR was recorded under the mode of baseline corrections by using Cary5000 UV-VIS-NIR spectrophotometer, VARIAN Company, equipped with long-pathlength absorption cell (LPAC). The LPAC contains multipass optics in the White cell configuration with a fixed path length of 9.6 m, and its constant volume equal 1.7 L. The temperature was constant at 298 K and pressures of gas were 1, 5, 10, 15, 20, 25 bar. Experimental measurements were chosen to measure the absorbance as a function of wavelength in the near infrared region ex-

tended between 1200 - 1300 nm.

3. Data Analysis

Origin pro Lab program was used for simple and advanced data analysis. The absolute area under the spectral line (A), central wavelength (X_c),Gaussian (WG), Lorentzian (WL) width and full width at half-maximum height (FWHM) in each spectral line were exactly defined through the deconvolution method of the Voigt profile function.

Simple and advanced analysis of six samples from twenty-five samples was subjected to pressures extended from 1 to 25 bars at 298 K, 323 K, 348 K, and 373 K. In this paper, pressures, which were chosen, are 1, 5, 10, 15, 20, 25 bar at only 298 K, where other pressures will be dealt with in other papers.

Figure 1 shows tough data analysis to total oxygen spectrum between 1200 - 1300 nm. Figures 1(a)-(f) inside Figure 1 show the peaks number for each line, where the number of peaks decreases with pressures increasing.

4. Results and Discussion

Because of the highly density of peaks number between 1200 - 1300 nm, only peaks(lines) between 1260 - 1270 nm were taken into account, where the interested lines (1268 nm, 1264 nm) exist between these lines. All results and values were taken based on the absorbance intensity $(A = \sigma c \ell)$ as a function of wavelength (nm).

In addition, mathematical absolute area (integrated absorbance) under each main line was calculated to equal to sum of mathematical absolute areas for all separated lines by advanced data analysis, and absolute area (integrated absorbance) increases with increasing of pressure (see Figures 2-7).

All Figure 2(a), Figure 3(a), Figure 4(a), Figure 5(a), Figure 6(a), Figure 7(a) show how the main spectral line was separated from the Voigt deconvolution method to two spectral lines, the first belongs to O_2 monomer at 1268 nm central wavelength, and the second to O_2 binary absorbance at 1264 nm central wavelength. Whereas all Figure 2(b), Figure 3(b), Figure 4(b), Figure 5(b), Figure 6(b), Figure 7(b) show many spectral lines



Figure 1. Advanced analysis of spectral lines by Voigt deconvolution method (black line indicates the main spectral line, red line denotes to cumulative fit peak to main line, and the green line denotes to all analyzed spectral lines which came from analysis of main line (black line).







Figure 3. Simple and advanced data analysis at 5 bar and 298 K.







Figure 5. Simple and advanced data analysis at 15 bar and 298 K.



Figure 6. Simple and advanced data analysis at 20 bar and 298 K.



Figure 7. Simple and advanced data analysis at 25 bar and 298 K.

were made by advanced analysis between 1260 nm - 1270 nm, each line consist of two regions: the first belongs to discrete region, and the second belongs to continuous region.

Figures 2-4 show comparison between simple and advanced data analysis at 1, 5, 10 bar and constant temperature (298 k). The most important thing in advanced analysis, that there is a real discrete region with many wavelengths around the central wavelength (1268 nm) for O_2 monomer with R and P branches, which belong to rotational spectrum. Whereas, the continuous region is wide and filled with spectral line around the central wavelength (1264 nm) for O_2 dimol, where collision induced absorption (CIA) prevails in this region with a variety of energy levels (peaks).

Figure 5 and **Figure 6** show, also, the comparison between simple and advanced data analysis at 15 and 20 bar and constant temperature (298 k). The main notices at these figures that the simple analysis gave factious values for central discrete line (1268 nm) and central continuous line (1264 nm), which mean that the discrete region was disappeared under pressures between 10 - 20 bar.

Figure 7 shows a strange result, where a very small initial discrete region began to appear, which needs to follow for pressures more than 25 bar.

Finally, it seems that at low pressures, the interactions and the competition between thermal effect (Doppler) and collisional effect (Lorentz) are very sensitive and active, and peaks number (energy levels) are very large. Whereas, at pressures higher than 10 bar the density of peaks will be more little. **Figure 8** shows an exponential decay function between peaks number as a function of pressure (1 - 25 bar).

5. Conclusions

Voigt deconvolution method to separate two peaks from each other's is a very successful method, and this method is able to give the values of Gaussian width (WG), Lorentzian width (WL), Voigt FWHM, and the integrated absorbance intensity for each peak.

Figure 2(a), Figure 3(a), Figure 4(a), Figure 5(a), Figure 6(a), Figure 7(a) reflect the simple analysis of each spectral line, which analyzes only two peaks belonging to central O_2 discrete line (1268 nm) and central O_2 - O_2 continuous line (1264 nm).

Whereas Figure 2(b), Figure 3(b), Figure 4(b), Figure 5(b), Figure 6(b), Figure 7(b) reflect the advanced analysis, which separates all energy levels (peaks), and each peak gives all information that is found in a two-



Figure 8. Peaks (energy levels) number as a function of pressure (1 - 25 bar).

peak method, which may belong to discrete or continuous bands.

The simple analysis may give factious values for some spectral lines under pressures between 10 - 20 bar, whereas advanced analysis gives almost real values for all spectral lines.

The pressure is very effective on absorption energy levels where their numbers exponentially decay with high pressures.

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