

ISSN: 2327-4352 Volume 11, Number 5, May 2023



# Journal of Applied Mathematics and Physics



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ISSN 2327-4352 (Print) ISSN 2327-4379 (Online)

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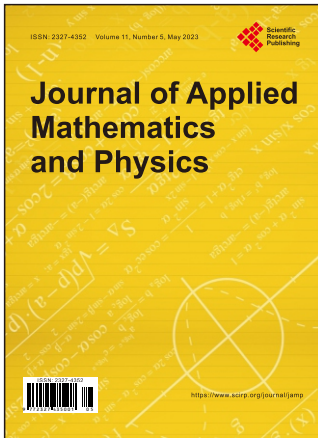
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ISSN Print: 2327-4352 ISSN Online: 2327-4379  
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