Fading Effects on the Lower Shifting of Mode Switching Thresholds in the Rate Adaptive IEEE 802.11a/g WLANs

Chie Dou, Li-Shin Wang

Department of Electrical Engineering, National Yunlin University of Science and Technology, Touliu, Taiwan, China E-mail: {douc, g9851710}@yuntech.edu.tw Received May 3, 2010; revised June 29, 2010; accepted August 2, 2010

Abstract

In this paper we used the probability distribution of the average channel gain of the fading channel to analyze the degree of fading effects on both the PER (packet error rate) and the throughput in OFDM systems. Instead of solely examining the average received SNR (signal-to-noise ratio) value of a packet, considering the whole distribution of the average received SNR allows us to aggregate a better selection of the mode switching thresholds in the rate adaptive 802.11 a/g WLAN. This paper demonstrates that the set of mode switching thresholds can be determined for each individual target E_b / N_0 , so that the optimal throughput performance is obtained on a per target E_b / N_0 basis. Numerical results show that mode switching thresholds should be reduced with the lowering of target E_b / N_0 values. This conclusion could have significant implications for improving the performances of location (distance)-dependent mobile applications, since the determinations of target E_b / N_0 values are closely related to the distances between mobile devices and the access point.

Keywords: 802.11a/g, Fading Channels, Packet Error Rate, Channel Gain, Link Adaptation

1. Introduction

THE IEEE 802.11 a/g WLAN is an OFDM (orthogonal frequency division multiplexing)-based basic service set (BSS) in which stationary devices and an access point (AP) communicate. The multipath channel effect causes a communicating pair of devices to experience a particular fading realization which may be different from those of other communicating pairs in the BSS. The transmiting device determines a target signal quality by setting an initial SNR or a target E_b / N_0 , so that a certain qualityof-service (QoS) may be satisfied at the receiver side. The determination of the target signal quality is often dependent on the distance between the pair of communicating devices. An example of the correspondence between the distance and the initial SNR under 802.11 a standard [1] was given in [2]. In this paper, we first determine the target E_b / N_0 , which can subsequently be used to directly calculate the initial SNR value per subcarrier for different rate modes. Furthermore, we clarify the relationship between the target E_b / N_0 and the received SNR of the packet in the rate adaptive IEEE 802.11 a/g WL-AN over frequency selective fading channels. In OFDM systems, a carrier frequency offset (CFO) can give rise to amplitude reduction and phase rotation of the desired signal, inducing inter-carrier interference (ICI) [3]. Consequently, the signal-to-interference-and-noise ratio (SINR) should be considered at the receiver [4,5]. The SINR for frequency selective fading channels with a CFO has already been investigated [4]. Evidently the average SINR will be reduced to the average SNR if the ICI can be ignored. In this paper, we assumed conditions of perfect synchronization with no timing and frequency offsets. Thus, we examine the received SNR of each subcarrier and the average received SNR of a packet instead of the SINR.

The channel transfer functions (or channel gains) of fading channels significantly impact both the received SNR and the PER of received packets in OFDM-based WLANs [2,6-8]. An analytical PER calculation method was developed in [2] for OFDM-based systems using a hard decoder. This paper also derives the PER expression for convolutional-coded hard-decision decoded OFDM systems on a fading realization basis. The PER calculation method presented in this paper differs from that of [2] by introducing a more simple yet effective analysis process in that both methods provide only an analytical upper bound. The average PER expression captures the PER versus initial SNR for all data rates in [2]. However,



it does not provide insight into the influence that the distribution of the channel transfer function (or channel gain) over the subcarriers has on the PER. This paper uses the probability distribution of the average channel gain of the fading channel to analyze the degree of fading effects on both the PER and the throughput in OFDM systems. The average channel gain of a fading realization is obtained by averaging the channel gains over all subcarriers. A similar definition of the average channel gain can be found in [9]. Estimation schemes based on an "indicator" concept obtain accurate predictions of the PER via evaluations of the channel transfer function [6,7]. The estimated variance of the transfer function amplitude serves as a simple but effective indicator. However, indicatoraided SNR estimations and direct PER predictions must take into account some complex optimizations of parameters that may cause errors in channel estimation. A conventional link adaptation algorithm takes the measured SNR as the only input from the PHY layer; there exists the possibility that it ignores the stochastic variability of the multipath fading channel and does not exploit the full potential of the link adaptation [6,7]. Instead of solely examining the average received SNR value of a packet, this paper considers the whole distribution of the average received SNR in a way that facilitates a better performance of link adaptation by exploiting the stochastic variability of the multipath fading channel. Previously, two analytical methods have been presented for estimating the bit error rate (BER) of coded multicarrier systems operating over frequency-selective quasi-static channels with non ideal interleaving [8]. However, explicit knowledge of Rayleigh-distributed frequency-domain subcarrier channel gains and their correlation matrices are prerequisites for finding the BER.

In this paper, the average PER of individual average received SNR value is obtained for different rate modes both by an analytical approach and by the simulation on a per target E_b / N_0 basis. The influences of the probability distribution of average channel gain on the average PER are investigated and compared between ETSI (European telecommunications standards institute) BRAN A and C channel models [10]. Performance result of the average PER performance is obtained with the same average received SNR by lowering the target E_b / N_0 value. This observation has significant impact on the determination of mode switching thresholds in 802.11a/g link adaptation.

For conventional link adaptation techniques, a set of mode switching thresholds for the received SNR is chosen for different rate modes based on the achieved throughput taking the PER for each rate mode into account [11,12] or based on the delay performance of a certain target PER for all rate modes [13]. Unlike conventional link adaptation techniques, in this paper an optimal set of mode switching thresholds is determined for each target E_b / N_0 . Numerical results show that mode switching thresholds should be shifted downwards with the lowering of target E_b / N_0 values. This conclusion is useful in improving the performances of location (distance)-dependent mobile applications, such as distributed camera network (DCN). In a DCN, digital cameras using 802.11 protocol for video transmissions may have different target E_b / N_0 values according to the distances between their locations and the access point. The performances of video transmissions in a DCN can be improved if each particular digital camera can use the optimal set of mode switching thresholds determined by the corresponding target E_b / N_0 .

The rest of this paper is organized as follows. Section 2 presents the channel fading effects in OFDM-based svstems. The impact of channel gains over subcarriers on the average received SNR of a received packet is investigated. For the rate adaptive 802.11a/g WLAN, an analytical approach is proposed to obtain the average PER of individual average received SNR value for different rate modes on a per target E_h / N_0 basis. Instead of just looking at the average received SNR value of a packet. we consider the whole distribution of the average received SNR, which leads to a better average PER and also throughput performances. Section 3 presents the simulation model and the channel estimation technique. The average PER derived from the analytical upper bound is compared to the simulation. Numerical results and their applications to the throughput-based link adaptation in 802.11a/g WLAN are presented in Section 4. We demonstrate that the set of mode switching thresholds can be determined for each individual target E_{h}/N_{0} for optimal throughput performance. Numerical results show that mode switching thresholds should be reduced with the lowering of target E_h / N_0 values. Finally, Section 5 states the conclusions.

2. Fading Effects in OFDM-Based Systems

Figure 1 shows a block diagram of OFDM-based systems using *N*-point IFFT/FFT in an equivalent low-pass



Figure 1. Block diagram of OFDM-based systems in an equivalent low-pass system.

system. Basically, in an OFDM system the serial bit stream is transformed to a parallel form. The bits to be transmitted are first mapped onto constellation points with the M-ary PSK (phase shift keying) or QAM (quadrature amplitude modulation) scheme, then those parallel data are modulated by means of an IFFT (inverse fast Fourier transform) on N parallel subcarriers. In 802.11a, different combinations of the code rate and modulation type results in eight rate modes specified in the standard [1]. These rate modes and their corresponding code rates and modulation types and coded bits per subcarrier are listed in **Table 1**. Let $d_{i}[i]$ be the modulation symbol of the *i*-th subcarrier for the nth OFDM symbol. Without timing and frequency offset, the baseband discrete-time data signal of the k-th sample of the n-th transmitted OFDM symbol can be given by

$$x_n[k] = \sum_{i=0}^{N-1} d_n[i] \cdot e^{j2\pi ki/N}, \quad k = 0, 1, \dots, N-1.$$
(1)

The output signal s(t) of the transmitter traverses through a multipath channel. To accurately measure the delay and fading caused by multipath, the Naftali model, which is a consistent channel model to compare different WLAN systems in an indoor radio environment is commonly used [14]. Using Naftali model, we can compose the channel impulse response of complex samples using random uniformly distributed phase and Rayleigh distributed magnitude. We assume the time-varying channel consists of *L* multipath components, and each path component is characterized by an amplitude h_l and a delay time τ_l . The model has the form

$$h(t) = \sum_{l=0}^{L-1} h_l \delta(t - \tau_l) \,. \tag{2}$$

The channel impulse response of the *l*-th path is given by

$$h_{l} = N(0, \frac{1}{2}\sigma_{l}^{2}) + jN(0, \frac{1}{2}\sigma_{l}^{2}), \qquad (3)$$

where $N(0, \sigma_l^2/2)$ is a Gaussian random variable with zero mean and variance $\sigma_l^2/2$, where

$$\sigma_l^2 = \sigma_0^2 \cdot e^{-\tau_l / T_{RMS}} , \qquad (4)$$

where σ_0^2 is selected so that the summation of all σ_l^2 must be normalized to one to ensure the average received power be the same. Here T_{RMS} is the root mean square delay spread of the channel response. Due to the exponential decaying term expressed in (4), the Naftali model is usually called exponential channel model.

After the multipath channel, the received signal r(t) is further corrupted by an Additive White Gaussian Noise (AWGN) as follows:

$$r(t) = s(t) * h(t) + n(t),$$
(5)

 Table 1. Rate mode dependent parameters in 802.11a/g standard.

Rate mode (<i>RM</i>)	Data rate (Mb/s)	Modulation type	Coding rate (CR)	Coded bits per subcarrier (N_{BPSC})
1	6	BPSK	1/2	1
2	9	BPSK	3/4	1
3	12	QPSK	1/2	2
4	18	QPSK	3/4	2
5	24	16-QAM	1/2	4
6	36	16-QAM	3/4	4
7	48	64-QAM	2/3	6
8	54	64-QAM	3/4	6

where '*' represents the convolution operation and n(t) is AWGN with the two-side power spectral density, $N_0/2$.

At the receiver, the received signal is down-converted to the baseband signal and enters FFT. In this process, we assume that the synchronization in frequency and timing are perfect and the delay spread is smaller than the guard interval (GI), so that ICI and ISI (inter symbol interference) are ignored. After taking an N point FFT on the nth OFDM symbol, we have the received signal for subcarrier *i* over a slowly time-varying time-dispersive channel given by

$$Y_{n}[i] = d_{n}[i]H_{i} + Z_{n}[i], \qquad (6)$$

where H_i is the channel transfer function of subcarrier *i* in frequency domain and $Z_n[i]$ is the noise term of the *i*-th subcarrier due to AWGN. The channel frequency response H_i can be given by [15-17]:

$$H_{i} = \sum_{l=0}^{L-1} h_{l} \cdot e^{\frac{-j2\pi i \epsilon_{l}}{N T_{s}}}, i = 0, 1, \dots, N-1,$$
(7)

where $1/T_s$ is the total bandwidth of the system. In the IEEE 802.11a/g standard, the total bandwidth of the system is 20 MHz.

2.1. Impact of Channel Gains on Received SNR

For different rate modes of 802.11 a/g, the initial SNR value of subcarrier i can be given by

$$SNR_{SC_i} = 10^{\frac{(E_b/N_0)}{10}} \times CR \times N_{BPSC}, \qquad (8)$$

where E_b is the transmitted signal energy per bit, and *CR* is the code rate of the given rate mode and N_{BPSC} is the corresponding coded bits per subcarrier as listed in **Table 1**. From (8), it is clear that the initial SNR value of subcarrier *i* will not be the same for different rate modes of 802.11a/g under the same E_b / N_0 , due to different code rates and number of coded bits per subcarrier. If we further assume that the average energy of an OFDM symbol is equal to 1 and the initial SNR values of all

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subscribers are equal, then the average energy of the signal constellation for each subcarrier is equal to 1/N (N = 64), and the initial SNR value per subcarrier, denoted by η , can be defined as

$$\eta \equiv SNR_{SC_i} = \frac{1/N}{N_0} = \frac{1}{N \times 2\sigma_Z^2},$$
(9)

where $\sigma_z^2 = N_0 / 2$ is the noise variance of AWGN.

From (8) and (9), the E_b / N_0 can be expressed as

$$\frac{E_b}{N_0} = 10 \cdot \log_{10} \frac{1}{N \times CR \times N_{BPSC} \times (2\sigma_Z^2)} .$$
(10)

From (10) it shows that when E_b / N_0 is the same, the rate mode should be decreased if the variance of AWGN increases. For different rate modes, noise power can be calculated to generate AWGN that will be used in the simulation model presented in the next section.

Let γ_i be the received SNR of the *i*-th subcarrier, which is dependent on the initial SNR value of the *i*-th subcarrier in the transmitter side and the channel gain $|H_i|^2$ in frequency domain. It can be given by [18,19]:

$$\gamma_i = \left| H_i \right|^2 SNR_{SC_i} = \left| H_i \right|^2 \eta \,. \tag{11}$$

In [1], the 802.11a/g system uses 52 subcarriers that are modulated using *M*-ary PSK or QAM scheme, including 48 data subcarriers and 4 pilot subcarriers. Let $\overline{\gamma}$ be the average received SNR after demodulation over all these 52 subcarriers and *I* be the set of coefficient indices corresponding to these 52 subcarriers. We have

$$\overline{\gamma} = \left| \overline{H} \right|^2 \eta \,, \tag{12}$$

where $\left|\overline{H}\right|^2$ is the average channel gain over all subcarriers [9]:

$$\left|\overline{H}\right|^{2} = \frac{1}{52} \sum_{\text{all } i \in I} \left|H_{i}\right|^{2}$$
 (13)

If we assume the channel is static for each transmitted packet (that is, the channel gain is the same for a given subcarrier between consecutive OFDM symbols), then the average received SNR of the packet is also $\overline{\gamma}$ given by (12).

2.2. Fading Realization of Channel Models

In this paper, PER performance comparisons are made between ETSI/BRAN A and C channel models. Fading realizations of both channel models are discussed in this subsection. ETSI/BRAN A channel (18-ray) was defined to represent a typical small office NLOS (non line-of-sight) indoor environment with a small RMS delay spread (50 ns). ETSI/BRAN C channel (18-ray) was defined to represent a typical large office NLOS indoor environment with a large RMS delay spread (150 ns). The power delay profile (PDP) of ETSI/BRAN A and C channels are shown in **Table 2** and **Table 3**, respectively.

Since BRAN A and C channel models are not truly exponential channel models, the variance $\sigma_l^2/2$ of the Gaussian random variable $N(0, \sigma_l^2/2)$ used in (3) could not be calculated by (4) directly. In this study, we use the power level (in dB) specified for each ray in the PDP of the channel model to calculate the desired σ_l^2 . First, the decibel measure for each ray is converted to its relative power ratio, for example, 0 dB is converted to power ratio 1. Let v_l^2 denote the relative power ratio converted from the power level (dB) specified for the *l*-th ray. Since the summation of all σ_l^2 must be normalized to one to ensure the average received power is the same thus we have

$$\sigma_l^2 = v_l^2 / \sum_{k=1}^{L-1} v_k^2 .$$
 (14)

Now, we can use (3) and (14) to generate the channel impulse response of the *l*-th path for BRAN A and C channel models. Fading realizations of both channel models are generated by (7) and the average channel gain of each fading realization is give by (13).

Figure 2 shows the probability distribution of average channel gain over 100,000 samples of fading realization

Table 2. Power delay profile of BRAN A channel.

Delay (µs)	Power (dB)	Delay (µs)	Power (dB)
0.00	0.00	0.09	-7.80
0.01	-0.90	0.11	-4.70
0.02	-1.70	0.14	-7.30
0.03	-2.60	0.17	-9.90
0.04	-3.50	0.20	-12.5
0.05	-4.30	0.24	-13.7
0.06	-5.20	0.29	-18.0
0.07	-6.10	0.34	-22.4
0.08	-6.90	0.39	-26.7

	Table 3.	Power	delay	profile	of BR	AN C	channel.
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Delay (µs)	Power (dB)	Delay (µs)	Power (dB)
0.00	-3.30	0.23	-3.00
0.01	-3.60	0.28	-4.40
0.02	-3.90	0.33	-5.90
0.03	-4.20	0.40	-5.30
0.05	0.00	0.49	-7.90
0.08	-0.90	0.60	-9.40
0.11	-1.70	0.73	-13.2
0.14	-2.60	0.88	-16.3
0.18	-1.50	1.05	-21.2

for two channel models. A rectangle-based integration method with equally spaced "bins" has been employed to derive the curves. Here the width of each "bin" is 0.05. From Figure 2, it shows that the mean value of both probability distributions is equal to one. We see that for small $|\overline{H}|^2$, say smaller than 0.5, BRAN A channel has higher probability distribution than that of BRAN C channel. For instance, it gives $Pr(|\overline{H}|^2 \le 0.5) = 0.2316$ for BRAN A channel and $Pr(|\overline{H}|^2 \le 0.5) = 0.0913$ for BRAN C channel. For large $\left|\overline{H}\right|^2$, say larger than 2, BRAN A channel also has higher probability distribution than that of BRAN C channel. For instance, it gives $\Pr(|\overline{H}|^2 \ge 2) = 0.0788$ for BRAN A channel and $\Pr(|\bar{H}|^2 \ge 2) = 0.0258$ for BRAN C channel. The impacts of $|\overline{H}|^2$ in its full statistics on the PER performance under BRAN A and C channel models are discussed in the following.

Figure 3 shows the probability distribution of average received SNR under two channel models given that the rate mode RM = 3 and the target E_b / N_0 , denoted by *T*, is 16 dB. Rectangle-based integration method with equally spaced "bins" has also been employed to derive the probability distribution of average received SNR. For a particular integer-valued average received SNR. For a particular integer-valued average received SNR, *R*, the range of the corresponding sampling bin is (R - 0.5, R + 0.5]. In this paper, only integer-valued average received SNR is considered. However, fractionary average received SNR can be treated by reducing the width of each sampling bin. From (8) and (12), the average received SNR of a packet for a certain rate mode can also be written as

$$\overline{\nu} = \left|\overline{H}\right|^2 T + 10\log_{10}(CR \times N_{BPSC}) \tag{15}$$

Because of the code rate multiplied by the coded bits per subcarrier is 1 for RM = 3, a simple relationship $\overline{\gamma} = |\overline{H}|^2 T$ holds in deriving the result of Figure 3. Although the probability distribution of average received SNR shown in Figure 3 has similarity to the probability distribution of average channel gain shown in Figure 2, **Figure 3** depicts more clearly the influence of $|\overline{H}|^2$ on average received SNR. The conclusions that have been drawn from Figure 2 on the differences between BRAN A and BRAN C channel models can be observed from Figure 3 more apparently. In Figure 3, the pattern of the probability distribution function defines the effective range of average received SNR. The "effective" range means that the probability distribution of average received SNR falling outside of this range is negligible. From Figure 3 we observe that the effective ranges of average received SNR are different for two channel models. The effective ranges are [7,22] dB and [10,21] dB



Figure 2. The probability distribution of average channel gain over 100,000 samples of fading realization for BRAN A and C channel models, respectively.



Figure 3. The probability distribution of average received SNR in terms of average channel gain for two channel models given that RM = 3 and the target E_b/N_0 is 16 dB.

for BRAN A and C channel models, respectively, for T = 16 dB. Clearly, BRAN A channel has longer tails on both sides than BRAN C channel. Note that if the selected rate mode and the target E_b / N_0 are changed, only the effective ranges of average received SNR are shifted according to (15) but the patterns of the probability distribution for both channel models remain unchanged.

2.3. PER Calculation for a Received Packet

The symbol error probability for an *M*-ary QAM [20] with the average SNR per symbol, *s*, can be calculated by

$$p_M(s) = 1 - \left[1 - \left(1 - \frac{1}{\sqrt{M}}\right) \operatorname{erfc}\left(\sqrt{\frac{3}{2(M-1)} \cdot s}\right)\right]^2. \quad (16)$$

In 802.11a/g, an OFDM data symbol consists of N_{SD} = 48 data subcarriers. The average symbol error probability for an *M*-ary QAM over all these data subcarriers can be given by

$$\overline{p}_{e,M} = \frac{1}{N_{SD}} \sum_{i=1}^{N_{SD}} p_M(\gamma_i), \qquad (17)$$

where γ_i is the received SNR of the *i*-th subcarrier. With a Gray coding, the average bit error probability for an *M*-ary QAM after demodulation is given by

$$p_b = \frac{1}{\log_2 M} \,\overline{p}_{e,M}.\tag{18}$$

In [21], an upper bound was given on the PER under the assumption of binary convolutional coding and harddecision Viterbi decoding with independent errors into the decoder. For a *B*-octet long packet to be transmitted using PHY mode ϕ , this bound is

$$p_{e,pkt} \le 1 - (1 - P_u^{\varphi})^{8B},$$
 (19)

where the union bound P_u^{ϕ} of the first-event error probability is given by, $P_u^{\phi} = \sum_{d=d_{free}}^{\infty} a_d P_d$ with d_{free} being the minimum free distance of the convolutional code for the given code rate, a_d the total number of error events of weight d [22], and P_d the probability of error in the pair-wise comparison of two paths that differ in d bits. When the hard-decision decoding is applied, P_d is given by

$$P_{d} = \begin{cases} \sum_{k=(d+1)/2}^{d} \binom{d}{k} p_{b}^{k} (1-p_{b})^{d-k}, \\ d = odd \\ \sum_{k=d/2+1}^{d} \binom{d}{k} p_{b}^{k} (1-p_{b})^{d-k} + \binom{d}{\frac{d}{2}} \frac{p_{b}^{d/2} (1-p_{b})^{d/2}}{2}, \\ d = even \end{cases}$$
(20)

where P_d is the average bit error probability given by (15).

2.4. Average PER of an Average Received SNR

For an *B*-octet long packet to be transmitted using rate mode ϕ , given that the target E_b / N_0 is *T*, total 100,000 samples of such packet are generated to derive the average PER (an upper bound) of an average received SNR by the following steps.

Step 1: Calculate the initial SNR value per subcarrier using (8).

Step 2: Calculate the average channel gain of each sampling packet using (13).

Step 3: Calculate the average received SNR ($\overline{\gamma}$) of

each sampling packet using (12).

Step 4: Count the number of received packets, denoted by $N_{pkt}(R)$, falling in the given sampling bin belonging to the average received SNR *R*.

Step 5: Calculate the PER of each packet counted in step 4 using (19).

Step 6: The average PER of the average received SNR R, denoted by $\overline{PER}(R)$, is given by

$$\overline{PER}(R) = \frac{1}{N_{pkt}(R)} \sum_{i=1}^{N_{pkt}(R)} p_{e,pkt}[i]$$
(21)

where $p_{e,pki}[i]$ is the PER of the *i*-th packet calculated in step 5.

2.5. Average PER Performance Comparisons

Figure 4 presents the performance comparisons of average PER derived in (21) between BRAN A and C channel models for four different rate modes defined in 802.11a/g, given that T = 16 dB and B is 196-octet long. The effective range of average received SNR that can be measured by (15) is considered for every PER curve of different rate mode. For example, these ranges are [15, 30] dB and [18,29] dB for BRAN A and C channels, respectively, given that RM = 8. From Figure 4 we observe that BRAN C channel has better performance than BRAN A channel for RM = 1 (6 Mb/s) and RM = 3 (12 Mb/s) if the values of average received SNR are lower. On the contrary, BRAN A channel outperforms BRAN C channel for RM = 6 (36 Mb/s) and RM = 8 (54 Mb/s) if the values of average received SNR are higher. These results agree with our observation from Figure 2 and Figure 3



Figure 4. Performance comparisons of average PER between BRAN A and C channels for four different rate modes in 802.11a/g given that the target E_b/N_0 is 16 dB.

that BRAN A channel has higher probability to have smaller values $\left|\overline{H}\right|^2$ than BRAN C channel. Thus, BR-AN A channel degrades PER performance more severely than BRAN C channel as channel conditions are bad. **Figure 2** and **Figure 3** also show that BRAN A channel has higher probability to have larger values of $\left|\overline{H}\right|^2$ than BRAN C channel. So that BRAN A channel outperforms BRAN C channel on PER performance as channel conditions are good.

The results and observations depicted above are rarely found in the literature. Although many researchers have focused on the performance evaluation of different channel models in HiperLAN/2 and 802.11a, such as [12,23], and it is commonly recognized that BRAN channel C has better performance than channel A. For example, Haider and Raweshidy in [23] concluded that BRAN C channel has better performance than channel A due to the increase of frequency diversity of the channels. Frequency diversity [24] due to delay spread provides the receiver with several (ideally independent) replica of the transmitted signal and is therefore a powerful means to combat fading and interference. Surely BRAN C channel has larger RMS delay spread (150 ns) than that of BRAN A channel (50 ns). The ray (multipath) number of BRAN C channel could be larger than that of BRAN A channel if ideal exponential channel model was considered. But actually both channel models have the same ray number (18-ray) and their PDPs are quite different as shown in Table 2 and Table 3. In this paper, we provide a different approach to compare the average PER performance between two channel models. Our approach provides more insight into the performance differentiation between BRAN A and BRAN C channel models by firstly taking the whole power delay profiles of each channel model into account, secondly by performing performance comparisons on a per target E_b / N_0 basis, and thirdly by considering the effects of the probability distribution of average channel gain on the average PER performances. Our approach for average PER performance comparisons between different channel models can be applied to other channel models as well, on a per target E_h / N_0 basis.

3. Simulation Model

Figure 5 shows the simulation model of OFDM-based systems that we used in this paper. The inputs of the simulation model are target E_b / N_0 , selected rate mode, and packet length. The output of the simulation model is the estimation of packet error rate. For a given target E_b / N_0 and a certain selected rate mode, the initial SNR value per subcarrier, η , is obtained by (8). Noise power





Figure 5. The simulation model of OFDM-based systems.

is calculated by (10) to generate AWGN noise in the simulation. In the IEEE 802.11a/g WLAN, there are two long training symbols for each packet that can be used for coherent detection. In this study training-sequence based channel estimation method is used for stationary mobile stations in slowly time-varying environments. The two long training symbols in the PLCP (physical layer convergence procedure) preamble are rate mode independent and are used for the channel estimation of every received PPDU (physical protocol data unit). Other channel estimation methods, such as pilot symbol aided scheme [25-27], and blind estimation technique [28-30], were not considered.

3.1. Channel Estimation

After taking an N point FFT at the receiver, the two long training symbols have the same form of the received signal for subcarrier i given by

$$Y_{n}[i] = F_{i}H_{i} + Z_{n}[i], \quad n = 0$$
(22)

where $\{F_i\}$ is the set of training sequence defined in 802.11a standard and is both known by the transmitter and the receiver. In [31], a channel estimation value \hat{H}_i of the *i*-th subcarrier in a conventional equalizer can be estimated by

$$\hat{H}_{i} = (Y_{0}[i] + Y_{1}[i]) / 2F_{i}, \qquad (23)$$

where $Y_0[i]$ and $Y_1[i]$ are both complex Gaussian random variables with the same mean H_iF_i . In [32], it has been proved that the optimal estimator of H_i is just \hat{H}_i defined in (23) by using the likelihood function of H_i . The likelihood function of H_i can be written as

$$f(Y_{0}[i] + Y_{1}[i]; H_{i}) = \frac{1}{\left(2\pi\sigma_{Z}^{2} / N\right)^{2}} \exp\left[-\frac{1}{2\sigma_{Z}^{2} / N}\left(\left|Y_{0}[i] - H_{i}F_{i}\right|^{2} + \left|Y_{1}[i] - H_{i}F_{i}\right|^{2}\right)\right] + \left|Y_{1}[i] - H_{i}F_{i}\right|^{2}\right)].$$
(24)

662

The optimal estimator of H_i is hence

$$\hat{H}_{i} = \arg \max_{H_{i}} f(Y_{0}[i] + Y_{1}[i]; H_{i})$$

$$= \arg \min_{H_{i}} |Y_{0}[i] - H_{i}F_{i}|^{2} + |Y_{1}[i] - H_{i}F_{i}|^{2} \quad (25)$$

$$= (Y_{0}[i] + Y_{1}[i]) / 2F_{i}.$$

Thus, the estimation of the received SNR γ_i of the *i*th subcarrier can be expressed as

$$\hat{\gamma}_i = \left| \hat{H}_i \right|^2 \eta. \tag{26}$$

The estimation of the average channel gain over all subcarriers is given by

$$\left|\hat{\bar{H}}\right|^{2} = \frac{1}{52} \sum_{\text{all } i \in I} \left|\hat{H}_{i}\right|^{2}.$$
(27)

And the estimation of average received SNR of a packet for a certain rate mode is given by

$$\hat{\overline{\gamma}} = \left|\hat{\overline{H}}\right|^2 T + 10\log_{10}(CR \times N_{BPSC}).$$
(28)

3.2. Analytical Upper Bound and Simulation Results

In our simulation the size of the physical service data unit (PSDU) is assumed 196-octet long. During transmission, the PSDU is provided with a PLCP preamble and header to create the PPDU. The simulation result of the average PER for a particular average received SNR R is obtained by first counting the number of those received packets (PPDUs) whose estimated average received SNRs falling within the range (R - 0.5, R + 0.5] but they could not be decoded correctly, and then divided that number by the value of $N_{pkt}(R)$ defined in Subsection 2.4. Figure 6 shows the results of average PER versus average received SNR for three different values of target $E_h/$ N_0 under BRAN A channel model and RM = 7 (48 Mb/s). The results of average PER derived both from the analytical upper bound and the simulation are presented for comparison. From Figure 6, we can see that the results derived from the analytical upper bound and derived from the simulation can be fitted quite well for each case of different target E_b / N_0 values, if the curve derived from the analytical upper bound is shifted leftward by a small amount less than 2 dB. The shifting amounts for T= 22 dB, 19 dB and 16 dB are 2 dB, 1.8 dB and 1.5 dB, respectively. A similar conclusion concerning the fitting between PER curves derived from the analytical upper bound and derived from the simulation in OFDM-based systems can be found in [2].

In **Figure 6**, we also see that the PER curve of T = 16 dB performs the best, and that of the T = 22 dB performs the

worst. This implies better PER performance is obtained with the same average received SNR by lowering the value of target E_h / N_0 . This phenomenon has close relationship to the fading effects represented by $\left|\overline{H}\right|^2$, as illustrated by the following example. For RM = 7, the average received SNR value of a packet given by (20) becomes $\overline{\gamma} = \left|\overline{H}\right|^2 T + 6 \text{ dB}$. For the case of T = 16 dB, the average received SNR will be 25 dB if we let $\left| \vec{H} \right|^2$ = 2. The same average received SNR can be derived if we let $|\overline{H}|^2 = 1$ and $|\overline{H}|^2 = 1/2$ for the cases of T = 19dB and 22 dB, respectively. Though the average received SNR for the above three cases are the same, the smallest average PER is obtained by the case of T=16 dB under better channel condition ($\left|\overline{H}\right|^2 = 2$), and the largest average PER is obtained by the case of T = 22 dB under worse channel condition $(\left|\overline{H}\right|^2 = 1/2)$. The impact of this phenomenon on the link adaptation of 802.11a will be presented in the next section.

4. Numerical Results and Applications

For the rate adaptive 802.11a/g WLAN systems, this section determines a set of mode switching thresholds for each individual target E_b / N_0 using the results derived above for the average PER, so that the optimal throughput performance can be obtained on a per target E_b / N_0 basis. The lower shifting of mode switching thresholds with the lowering of target E_b / N_0 values is presented by exploiting the phenomenon that we have observed from **Figure 6**.



Figure 6. Performance comparisons of average PER between the analytical upper bound and the simulation for three different target E_b/N_0 values under BRAN A channel model and RM = 7.

4.1. Throughput-Based Link Adaptation

For throughput-based link adaptation, physical link is adapted to the rate mode that gives the highest throughput. For different rate modes used in 802.11 a/g, the relationship between the achieved throughput and the corresponding average PER, denoted by \overline{PER} , can be obtained as follows. During transmission, the PSDU is provided with a PLCP preamble and header to create the PPDU. The transmission time of a PPDU frame (in us) can be calculated as

$$T_{PPDU} = T_{PREAMBLE} (16 \text{ us}) + T_{SIGNAL} (4 \text{ us}) + N_{DATA SVM} \times T_{SVM},$$
(29)

where T_{SYM} is the OFDM symbol interval, and N_{DATA_SYM} is the number of OFDM symbols in the DATA portion of the PPDU frame format and its value is dependent on the data rate used. The value of N_{DATA_SYM} is calculated by

$$N_{DATA_SYM} = \left\lceil \frac{16 + PSDU_size \times 8 + 6}{N_{DBPS}} \right\rceil, \quad (30)$$

where PSDU_size is the size of the PSDU in bytes, and N_{DBPS} is the number of data bits per OFDM symbol which is dependent on the rate mode used. To obtain the net throughput of 802.11a/g physical layer, only the payload bits of successful transmitted PPDU frames are considered. Thus, the throughput (in Mb/s) is calculated by

Throughput = PSDU_size
$$\times 8 \times (1 - PER) / T_{PPDU}$$
. (31)

We choose two target E_b / N_0 values T = 12 dB and 18 dB to illustrate the throughput-based link adaptation of 802.11 a on a per target E_h / N_0 basis. Average PER derived from the simulation under BRAN A channel model is used for all the cases presented in this section. Both average PER and throughput versus average received SNR for different rate modes under T = 12 dB and 18 dB are shown in Figure 7 and Figure 8, respectively. Five contour lines for connecting points where $|\overline{H}|^2$ = 1/4, 1/2, 1, 2, and 4 on different average PER curves are plotted in Figure 7(a). When compare Figure 7(a) to Figure 8(a), firstly, we notice that contour lines with smaller values of $|\overline{H}|^2$ which are absent in Figure 7(a) are now appearing in Figure 8(a); secondly, the contour lines that are of the same values of $\left| \overline{H} \right|^2$ are shifted right toward higher average received SNR in Figure 8(a). This is because for a particular rate mode to achieve a certain average PER, the channel conditions, represented by $|\bar{H}|^2$, experienced by the packets with lower target E_{b}/N_{0} is better than that experienced by the packets with higher target E_h / N_0 . For example, to achieve average PER = 10^{-2} for RM = 5 (24 Mb/s) in Figures 7(a) and 8(a), the corresponding values of $|\overline{H}|^2$ are larger than 2 for T = 12 dB and within [1/2, 1] for T = 18 dB.



Figure 7. Throughput-based link adaptation for target E_b / N_0 = 12 dB.

Figure 7(b) shows the throughput performances of different rate modes under T = 12 dB. Mode switching between neighboring rate modes are clear except that there has no definite rate adaptation between RM = 7 and RM = 8. This exception is due to the right-most boundary of the effective ranges of average received SNR for RM = 7 and RM = 8 are 24 dB and 25 dB, respectively. In Figure 7(b), the mode selection ranges for RM = 1 is [0, 7] dB, for RM = 3 is [8,13] dB, for RM = 5 is [14,18] dB, for RM = 6 is [19,21] dB, for RM = 7 is [22,24], and for RM = 8 is [25,-]. Figure 8(b) shows the result of link adaptation for T = 18 dB. Simulation result shows that there has no need for rate adaptation between RM = 3(12 Mb/s) and RM = 1 (6 Mb/s). Therefore the throughput curve for RM = 1 was not shown in Figure 8(b). This also means that there has no possibility to use RM = 1



Figure 8. Throughput-based link adaptation for target E_b /N₀ = 18 dB.

for T = 18 dB under BRAN A channel model. In **Figure 8(b)**, the mode selection ranges for RM = 3 is [9,13] dB, for RM = 5 is [14,20] dB, for RM = 6 is [21,22] dB, for RM = 7 is [23,27], and for RM = 8 is [28,31]. Note that the effective ranges of average received SNR for different rate modes are considered in both **Figure 7** and **Figure 8**. Also in **Figure 8**, the two PHY rate modes RM = 2 (9 Mb/s) and RM = 4 (18 Mb/s) were not included. Because in our simulation, the throughput performance of RM = 4 is worse than that of RM = 3 and the throughput performance of RM = 2 is worse than that of RM = 1.

4.2. Lower Shifting of Mode Switching Thresholds

As we have observed from **Figure 6** that better PER performances with the same average received SNR are obtained by lowering the values of target E_b / N_0 . By exploiting this phenomenon this subsection presents the lower shifting of mode switching thresholds with the

lowering of target E_b / N_0 values. An example is given as below for illustrative purpose. Consider the results of average PER for RM = 7 in both Figures 7(a) and 8(a). For RM = 7, we have already known that $\overline{\gamma} = |\overline{H}|^2 T +$ 6 dB. For the case of T = 12 dB, the average received SNR will be 21 dB if we let $|\overline{H}|^2 = 2$. The same average received SNR is obtained if we let $|\overline{H}|^2 = 1/2$ for the case of T = 18 dB. From Figure 7(a), we see that the average PER of average received SNR = 21 dB is about 0.3 for RM = 7 under T = 12 dB. However, from Figure **8(a)** we observe that this value is about 0.5 under T = 18dB. Accordingly, the achieved net throughputs of average received SNR = 21 dB for RM = 7 are about 19 Mb/s and 14 Mb/s under T = 12 dB and T = 18 dB, respectively, as that shown in Figures 7(b) and 8(b). Therefore we have shown that by lowering the value of T, better throughput performance with the same average received SNR can be achieved; consequently, rate adaptation to the next lower rate mode can be shifted downwardly. Compare the mode switching thresholds between RM = 6and RM = 7 in Figures 7(b) and 8(b), we see that this threshold is shifted downward from 22 dB under T = 18dB to 21 dB under T = 12 dB.

Figure 9 provides a full view of the lower shifting of mode switching thresholds for the link adaptation of 802.11a over BRAN A channel model under different target E_b / N_0 values. In Figure 9, the X-axis denotes the average received SNR and the Y-axis denotes the desired target E_{h} / N_{0} . Six rate modes are considered in the rate adaptation of 802.11a. The set of mode switching thresholds for target $E_b / N_0 = T \, dB$ can be obtained from Figure 9 by drawing a horizontal line on T (Y-axis) and finding the intersections between this horizontal line and the vertical lines (mode switching boundaries). For every given target E_{h}/N_{0} , the effective range of average received SNR is confined by the cross points plotted on the both sides. The cross point on the right-hand side is determined by the effective range of the highest rate mode that the given target E_b / N_0 may achieve; and the cross point on the left-hand side is determined by the effective range of the lowest rate mode that the given target E_b / N_0 may reach. Ideally, for every given value of T there should have five mode switching thresholds corresponding to all the pairs of neighboring rate modes. However, this may not be the case due to the rate modes that can be adapted to under a specific value of T may not cover all six rate modes. For example, the set of mode switching thresholds under T = 18 dB is [-,13,20, 22,27] dB since there has no rate adaptation between RM = 1 and RM = 3.

An interesting phenomenon that can be observed from

Figure 9 is that the lower shifting of mode switching thresholds occurred more frequently between neighboring rate modes RM = 7 and RM = 8 and also between RM = 5 and RM = 6. Coincidentally, each pair of neighboring rate modes has the same and high modulation level. The first pair, RM = 7 and RM = 8, uses the same modulation scheme 64 QAM, and the second pair, RM = 5 and RM = 6, uses the same modulation scheme 16 QAM. The lower shifting of mode switching thresholds occurred less frequently between neighboring rate modes with different modulation levels, for example RM = 3 with QPSK and RM = 5 with 16 QAM. Moreover, there has no lower shifting of mode switching thresholds between RM = 1 with BPSK and RM = 3 with QPSK. More investigations are needed to further understand this phenomenon.

4.3. System Throughput Optimization

In this subsection, we show that no other sets of mode switching thresholds can achieve higher system throughput than the optimal set which is determined on a per target E_{h}/N_{0} basis. The following example is given for illustrative purpose. From Figure 9, we have the optimal set of mode switching thresholds under T = 18 dB is [-,13,20, 22,27] dB. Here we purposely choose two other sets of mode switching thresholds [-,16,23,25,29] dB and [-,12, 18,20,24] dB. The thresholds in the first set are tending towards right, so we called them upward-shifted thresholds. On the contrary, the thresholds in the second set are tending towards left, so we called them downward-shifted thresholds. The comparisons of achieved system throughputs between the optimal set and these two sets of mode switching thresholds under T = 18 dB are presented in Figures 10(a) and 10(b), respectively. In Figure 10(a), the throughput achieved by the optimal set of mo-



Figure 9. A full view of the lower shifting of mode switching thresholds for the link adaptation of 802.11a over BRAN A channel model under different target E_b/N_0 values.

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de switching thresholds is expressed by the solid curves, and that achieved by the upward-shifted thresholds is expressed by the dotted curves. Obviously, the solid curves are always higher than or equal to the dotted curves for every average received SNR. In **Figure 10(b)** we observe that rate adaptations using downward-shifted thresholds always occurred at smaller average received SNR values than that using the optimal thresholds. So that solid curves are also higher than or equal to dotted curves for every average received SNR in **Figure 10(b)**.

5. Conclusions

For the rate adaptive 802.11a/g WLAN, an analytical approach is proposed to obtain the average PER of individual average received SNR value for different rate modes on a per target E_b / N_0 basis. Instead of just looking



Figure 10. The comparisons of achieved system throughputs between the optimal set and the other two sets of mode switching thresholds: (a) Upward-shifted thresholds; (b) Downward-shifted thresholds, under T = 18 dB.

at the average received SNR value of a packet, this paper considers the whole distribution of the average received SNR, which leads to a better average PER and throughput performances. In this paper we also showed that the probability distribution of average channel gain can affect the average PER over the effective range of average received SNR for different rate modes on a per target E_b / N_0 basis. Furthermore, we have shown that better PER performances with the same average received SNR can be obtained by lowering the values of target E_h / N_0 . By exploiting this phenomenon, the mode switching thresholds for optimal throughput performance of each target E_{h}/N_{0} can be determined. Numerical results show that mode switching thresholds can be shifted downwards with the lowering of target E_h / N_0 values. A full view of the lower shifting of mode switching thresholds for the link adaptation of 802.11a over BRAN A channel model under different target E_b / N_0 values is presented. From this an interesting phenomenon is observed, that is, the lower shifting of mode switching thresholds can occur more frequently between neighboring rate modes with the same and high modulation level - e.g. 64 OAM or 16 OAM. The lower shifting of mode switching thresholds occurred less frequently between neighboring rate modes with different modulation levels - e.g. QPSK and 16 QAM. Further investigations are needed to have a better understanding of this phenomenon

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