

An Antilock-Braking Systems (ABS) Control: A Technical Review

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Abstract

Many different control methods for ABS systems have been developed. These methods differ in their theoretical basis and performance under the changes of road conditions. The present review is a part of research project entitled "*Intelligent Antilock Brake System Design for Road-Surfaces of Saudi Arabia*". In the present paper we review the methods used in the design of ABS systems. We highlight the main difficulties and summarize the more recent developments in their control techniques. Intelligent control systems like fuzzy control can be used in ABS control to emulate the qualitative aspects of human knowledge with several advantages such as robustness, universal approximation theorem and rule-based algorithms.

Keywords: ABS, Intelligent Control, Fuzzy Control

1. Introduction

Since the development of the first motor driven vehicle in 1769 and the occurrence of first driving accident in 1770, engineers were determined to reduce driving accidents and improve the safety of vehicles [1]. It is obvious that efficient design of braking systems is to reduce accidents. Vehicle experts have developed this field through the invention of the first mechanical antilock-braking system (ABS) system which have been designed and produced in aerospace industry in 1930 [2,3].

In 1945, the first set of ABS brakes were put on a Boeing B-47 to prevent spin outs and tires from blowing and later in the 1950s, ABS brakes were commonly installed in airplanes [4,5]. Soon after, in the 1960s, high end automobiles were fitted with rear-only ABS, and with the rapid progress of microcomputers and electronics technologies, the trend exploded in the 1980s. Today, all-wheel ABS can be found on the majority of late model vehicles and even on select motorcycles [6-10].

ABS is recognized as an important contribution to road safety as it is designed to keep a vehicle steerable and stable during heavy braking moments by preventing wheel lock. It is well known that wheels will slip and lockup during severe braking or when braking on a slippery (wet, icy, etc.) road surface. This usually causes a long stopping distance and sometimes the vehicle will lose steering stability [11-13]. The objective of ABS is to manipulate the wheel slip so that a maximum friction is obtained and the steering stability (also known as the lateral stability) is maintained. That is, to make the vehicle stop in the shortest distance possible while maintaining the directional control. The ideal goal for the control design is to regulate the wheel velocity. The technologies of ABS are also applied in traction control system (TCS) and vehicle dynamic stability control (VDSC) [14].

Typical ABS components include: vehicle's physical brakes, wheel speed sensors (up to 4), an electronic control unit (ECU), brake master cylinder, a hydraulic modulator unit with pump and valves as shown in **Figure 1**. Some of the advanced ABS systems include accelerometer to determine the deceleration of the vehicle. This paper is intended to present a literature review of research works done by many researchers concerning various aspects of ABS technology in an effort to improve the performance of its applications.

2. Principles of Antilock-Brake System

The reason for the development of antilock brakes is in essence very simple. Under braking, if one or more of a vehicle's wheels lock (begins to skid) then this has a



Figure 1. Typical ABS components [4].

number of consequences: a) braking distance increases, b) steering control is lost, and c) tire wear will be abnormal. The obvious consequence is that an accident is far more likely to occur. The application of brakes generates a force that impedes a vehicles motion by applying a force in the opposite direction.

During severe braking scenarios, a point is obtained in which the tangential velocity of the tire surface and the velocity on road surface are not the same such that an optimal slip which corresponds to the maximum friction is obtained. The ABS controller must deal with the brake dynamics and the wheel dynamics as a whole plant [15]. The wheel slip, *S* is defined as:

$$s = \frac{V - \omega R}{V} \tag{1}$$

where ω , *R*, and *V* denote the wheel angular velocity, the wheel rolling radius, and the vehicle forward velocity, respectively. In normal driving conditions, $V = \omega R$, therefore S = 0. In severe braking, it is common to have $\omega = 0$ while S = 1, which is called wheel lockup. Wheel lockup is undesirable since it prolongs the stopping distance and causes the loss of direction control [16,17].

Figure 2 shows the relationship between braking coefficient and wheel slip. It is shown that the slide values for stopping/traction force are proportionately higher than the slide values for cornering/steering force. A locked-up wheel provides low road handling force and minimal steering force. Consequently the main benefit from ABS operation is to maintain directional control of the vehicle during heavy braking. In rare circumstances the stopping distance may be increased however, the directional control of the vehicle is substantially greater than if the wheels are locked up.

The main difficulty in the design of ABS control arises from the strong nonlinearity and uncertainty of the problem. It is difficult and in many cases impossible to solve this problem by using classical linear, frequency domain methods [17]. ABS systems are designed around system hydraulics, sensors and control electronics. These systems are dependent on each other and the different system components are interchangeable with minor changes in the controller software [18].

The wheel sensor feeds the wheel spin velocity to the electronic control unit, which based on some underlying control approach would give an output signal to the brake actuator control unit. The brake actuator control unit then controls the brake actuator based on the output from the electronic control unit. The control logic is based on the objective to keep the wheels from getting locked up and to maintain the traction between the tire and road surface at an optimal maximum. The task of keeping the wheels operating at maximum traction is complicated given that the friction-slip curve changes with vehicle, tire and road changes. The block diagram in Figure 3. shows the block representation of an antilock brake system. It shows the basic functionality of the various components in ABS systems and also shows the data/information flow.

The ABS (shown in **Figure 4**) consists of a conventional hydraulic brake system plus antilock components.



Figure 2. Illustration of the relationship between braking coefficient and wheel slip [14].



Figure 3. Block representation of an ABS.

The conventional brake system includes a vacuum booster, master cylinder, front disc brakes, rear drum brakes, interconnecting hydraulic brake pipes and hoses, brake fluid level sensor and the brake indicator. The ABS components include a hydraulic unit, an electronic brake control module (EBCM), two system fuses, four wheel speed sensors (one at each wheel), interconnecting wiring, the ABS indicator, and the rear drum brake.

Most ABS systems employ hydraulic valve control to regulate the brake pressure during the anti-lock operation. Brake pressure is increased, decreased or held. The amount of time required to open, close or hold the hydraulic valve is the key point affecting the brake efficiency and steering controllability.



Figure 4. Anti-lock braking system [14].

3. ABS Control

ABS brake controllers pose unique challenges to the designer: a) For optimal performance, the controller must operate at an unstable equilibrium point, b) Depending on road conditions, the maximum braking torque may vary over a wide range, c) The tire slippage measurement signal, crucial for controller performance, is both highly uncertain and noisy, d) On rough roads, the tire slip ratio varies widely and rapidly due to tire bouncing, e) brake pad coefficient of friction changes, and f) The braking system contains transportation delays which limit the control system bandwidth [19].

As stated in the previous section of this paper, the ABS consists of a conventional hydraulic brake system plus antilock components which affect the control characteristics of the ABS. ABS control is a highly a nonlinear control problem due to the complicated relationship between friction and slip. Another impediment in this control problem is that the linear velocity of the wheel is not directly measurable and it has to be estimated. Friction between the road and tire is also not readily measurable or might need complicated sensors. Researchers have employed various control approaches to tackle this problem. A sampling of the research done for different control approaches is shown in **Figure 5**. One of the technologies that has been applied in the various aspects of ABS control is soft computing. Brief review of ideas

of soft computing and how they are employed in ABS control are given below.

3.1. Classical Control Methods Based on PID Control

Out of all control types, the well known PID has been



Figure 5. Sampling of ABS control.

used to improve the performance of the ABS. Song, et al. [20] presented a mathematical model that is designed to analyze and improve the dynamic performance of a vehicle. A PID controller for rear wheel steering is designed to enhance the stability, steerability, and driveability of the vehicle during transient maneuvers. The braking and steering performances of controllers are evaluated for various driving conditions, such as straight and J-turn maneuvers. The simulation results show that the proposed full car model is sufficient to predict vehicle responses accurately. The developed ABS reduces the stopping distance and increases the longitudinal and lateral stability of both two- and four-wheel steering vehicles. The results also demonstrate that the use of a rear wheel controller as a yaw motion controller can increase its lateral stability and reduce the slip angle at high speeds.

The PID controller is simple in design but there is a clear limitation of its performance. It does not posses enough robustness for practical implementation. For solving this problem, Jiang [21] applied a new Nonlinear PID (NPID) control algorithm to a class of truck ABS problems. The NPID algorithm combines the advantages of robust control and easy tuning. Simulation results at various situations using TruckSim show that

NPID controller has shorter stopping distance and better velocity performance than the conventional PID controller and a loop-shaping controller.

3.2. Optimal Control Methods Based on Lyapunov approach

The optimal control of nonlinear system such as ABS is one of the most challenging and difficult subjects in control theory. Tanelli *et al.* [22] proposed a nonlinear output feedback control law for active braking control systems. The control law guarantees bounded control action and can cope also with input constraints. Moreover, the closed-loop system properties are such that the control algorithm allows detecting without the need of a friction estimator, if the closed-loop system is operating in the unstable region of the friction curve, thereby allowing enhancing both braking performance and safety. The design is performed via Lyapunov-based methods and its effectiveness is assessed via simulations on a multibody vehicle simulator. The change in the road conditions implies continuous adaptation in controller parameter.

In order to resolve this issue, an adaptive control-Lyapunov approach is suggested by R. R. Freeman [23] and similar ideas are pursued in [24,25]. The use of Sontag's formula is applied in the adaptive control Lyapunov approach in [26], which includes gain scheduling on vehicle speed and experimental testing. Feedback linearization in combination with gain scheduling is suggested by Liu and Sun [27]. PID-type approaches to wheel slip control are considered in [28-32]. A gain scheduled LQ control design approach with associated analysis, and, except [26] and [32], is the only one that contains detailed experimental evaluation using a test vehicle. In [33], an optimum seeking approach is taken to determine the maximum friction, using sliding modes. Sliding mode control is also considered in [34,35].

Another nonlinear modification was suggested by Ünsal and Kachroo [36] for observer-based design to control a vehicle traction that is important in providing safety and obtaining desired longitudinal vehicle motion. The direct state feedback is then replaced with nonlinear observers to estimate the vehicle velocity from the output of the system (*i.e.*, wheel velocity). The nonlinear model of the system is shown locally observable. The effects and drawbacks of the extended Kalman filters and sliding observers are shown via simulations. The sliding observer is found promising while the extended Kalman filter is unsatisfactory due to unpredictable changes in the road conditions.

3.3. Nonlinear Control Based on Backstepping Control Design

The complex nature of ABS requiring feedback control to obtain a desired system behavior also gives rise to dynamical systems. Ting and Lin [37] developed the anti-lock braking control system integrated with active suspensions applied to a quarter car model by employing the nonlinear backstepping design schemes. In emergency, although the braking distance can be reduced by the control torque from disk/drum brakes, the braking time and distance can be further improved if the normal force generated from active suspension systems is considered simultaneously. Individual controller is designed for each subsystem and an integrated algorithm is constructed to coordinate these two subsystems. As a result, the integration of anti-lock braking and active suspension systems indeed enhances the system performance because of reduction of braking time and distance.

Wang, *et al.* [38] compared the design process of backstepping approach ABS via multiple model adaptive control (MMAC) controllers. The high adhesion fixed model, medium adhesion fixed model, low adhesion fixed model and adaptive model were four models used in MMAC. The switching rules of different model controllers were also presented. Simulation was conducted for ABS control system using MMAC method basing on quarter vehicle model. Results show that this method can control wheel slip ratio more accurately, and has higher robustness, therefore it improves ABS performance ef-

fectively.

Tor Arne Johansen, [39] provided a contribution on nonlinear adaptive backstepping with estimator resetting using multiple observers A multiple model based observer/estimator for the estimation of parameters was used to reset the parameter estimation in a conventional Lyapunov based nonlinear adaptive controller. Transient performance can be improved without increasing the gain of the controller or estimator. This allows performance to be tuned without compromising robustness and sensitivity to noise and disturbances. The advantages of the scheme are demonstrated in an automotive wheel slip controller.

3.4. Robust Control Based on Sliding Mode Control Method

Sliding mode control is an important robust control approach. For the class of systems to which it applies, sliding mode controller design provides a systematic approach to the problem of maintaining stability and consistent performance in the face of modeling imprecision. On the other hand, by allowing the tradeoffs between modeling and performance to be quantified in a simple fashion, it can illuminate the whole design process.

Several results have been published coupling the ABS problem and the VSS design technique [40,41]. In these works design of sliding-mode controllers under the assumption of knowing the optimal value of the target slip was introduced. A problem of concern here is the lack of direct slip measurements. In all previous investigations the separation approach has been used. The problem was divided into the problem of optimal slip estimation and the problem of tracking the estimated optimal value. J.K. Hedrick, et al. [42,43] suggested a modification of the technique known as sliding mode control. It was chosen due to its robustness to modeling errors and disturbance rejection capabilities. Simulation results are presented to illustrate the capability of a vehicle using this controller to follow a desired speed trajectory while maintaining constant spacing between vehicles. Therefore a sliding mode control algorithm was implemented for this application. While Kayacan [44] proposed a grey sliding-mode controller to regulate the wheel slip, depending on the vehicle forward velocity. The proposed controller anticipates the upcoming values of wheel slip and takes the necessary action to keep the wheel slip at the desired value. The performance of the control algorithm as applied to a quarter vehicle is evaluated through simulations and experimental studies that include sudden changes in road conditions. It is observed that the proposed controller is capable of achieving faster convergence and better noise response than the conventional

approaches. It is concluded that the use of grey system theory, which has certain prediction capabilities, can be a viable alternative approach when the conventional control methods cannot meet the desired performance specifications. In real systems, a switched controller has imperfections which limit switching to a finite frequency. The oscillation with the neighborhood of the switching surface cause chattering. Chattering is undesirable, since it involves extremely high control activity, and furthermore may excite high-frequency dynamics neglected in the course of modeling. Chattering must be reduced (eliminated) for the controller to perform properly.

3.5. Adaptive Control Based on Gain Scheduling Control Method

Ting and Lin [45] presented an approach to incorporate the wheel slip constraint as a priori into control design so that the skidding can be avoided. A control structure of wheel torque and wheel steering is proposed to transform the original problem to that of state regulation with input constraint. For the transformed problem, a low-and-high gain technique is applied to construct the constrained controller and to enhance the utilization of the wheel slip under constraint. Simulation shows that the proposed control scheme, during tracking on a snow road, is capable of limiting the wheel slip, and has a satisfactory coordination between wheel torque and wheel steering.

3.6. Intelligent Control Based on Fuzzy Logic

FC has been proposed to tackle the problem of ABS for the unknown environmental parameters [46-50]. However, the large amount of the fuzzy rules makes the analysis complex. Some researchers have proposed fuzzy control design methods based on the sliding-mode control (SMC) scheme. These approaches are referred to as fuzzy sliding-mode control (FSMC) design methods [51,52]. Since only one variable is defined as the fuzzy input variable, the main advantage of the FSMC is that it requires fewer fuzzy rules than FC does. Moreover, the FSMC system has more robustness against parameter variation [52]. Although FC and FSMC are both effective methods, their major drawback is that the fuzzy rules should be previously tuned by time-consuming trial-anderror procedures. To tackle this problem, adaptive fuzzy control (AFC) based on the Lyapunov synthesis approach has been extensively studied [52-55]. With this approach, the fuzzy rules can be automatically adjusted to achieve satisfactory system response by an adaptive law.

Kumar et al. [56] investigated the integrated control of ABS System and collision avoidance system (CAS) in

electric vehicle. Fuzzy logic techniques are applied for integral control of two subsystems. Control algorithm is implemented and tested in a prototype electric vehicle in laboratory environment using free scale HCS12 microcontroller. A high level network protocol CAN is applied to integrate all sensors, ABS and CAS. The results show that integrated control of ABS and CAS maintains the safe distance from obstacle without sacrificing the performance of either system. Different researcher [57-59] developed an adaptive PID-type fuzzy controller for the ABS system. A platform is built to accomplish a series of experiments to control the ABS. A commercial ABS module controlled by a controller is installed and tested on the platform. The vehicle and tire models are deduced and simulated by a personal computer for real time control. Road surface conditions, vehicle weight and control schemes are varied in the experiments to study braking properties.

Lin and Hsu [60] proposed a self-learning fuzzy sliding-mode control (SLFSMC) design method for ABS. In the proposed SLFSMC system, a fuzzy controller is the main tracking controller, which is used to mimic an ideal controller; and a robust controller is derived to compensate for the difference between the ideal controller and the fuzzy controller. The SLFSMC has the advantages that it can automatically adjust the fuzzy rules, similar to the AFC, and can reduce the fuzzy rules, similar to the FSMC. Moreover, an error estimation mechanism is investigated to observe the bound of approximation error. All parameters in SLFSMC are tuned in the Lyapunov sense, thus, the stability of the system can be guaranteed. Finally, two simulation scenarios are examined and a comparison between a SMC, an FSMC, and the proposed SLFSMC is made.

The ABS system performance is examined on a quarter vehicle model with nonlinear elastic suspension. The parallelism of the fuzzy logic evaluation process ensures rapid computation of the controller output signal, requiring less time and fewer computation steps than controllers with adaptive identification. The robustness of the braking system is investigated on rough roads and in the presence of large measurement noise. The simulation results present the system performance on various road types and under rapidly changing road conditions. While conventional control approaches and even direct fuzzy/ knowledge based approaches [61-67] have been successfully implemented, their performance will still degrade when adverse road conditions are encountered. The basic reason for this performance degradation is that the control algorithms have limited ability to learn how to compensate for the wide variety of road conditions that exist.

Laynet et al. [68] and Laynet and Passino [69] intro-

duced the idea of using the fuzzy model reference learning control (FMRLC) technique for maintaining adequate performance even under adverse road conditions. This controller utilizes a learning mechanism which observes the plant outputs and adjusts the rules in a direct fuzzy controller so that the overall system behaves like a "reference model" which characterizes the desired behavior. The performance of the FMRLC-based ABS is demonstrated by simulation for various road conditions (wet asphalt, icy) and "split road conditions" (the condition where, e.g., emergency braking occurs and the road switches from wet to icy or vice versa). Precup et al. [70] developed a Takagi-Sugeno fuzzy controller and an interpolative fuzzy controller for tire slip control in ABS systems. By employing local linearized models of the controlled plant, the local controllers are developed in the frequency domain. Development methods for the two fuzzy controllers are also offered. Simulation results show that the control system performance enhancement ensured by the fuzzy controllers in comparison with the conventional PI ones.

Stan, *et al.* [71] performed a critical analysis of five fuzzy control solutions dedicated to ABS systems. The detailed mathematical model of controlled plant is derived and simplified for control design with focus on tire slip control. A new fuzzy control solution based on a class of Takagi-Sugeno fuzzy controllers is proposed. This class of fuzzy controllers combines separately designed PI and PID controllers corresponding to a set of simplified models of controlled plant linearized in the vicinity of important operating points. Simulation results validate the suggested fuzzy control solution in controlling the relative slip of a single wheel.

R. Keshmiri and A.M. Shahri [72] designed an intelligent fuzzy ABS controller to adjust slipping performance for variety of roads. There are two major features in the proposed control system: the first is a fuzzy logic controller providing optimal brake torque for both front and rear wheels; and the second is also a FLC provides required amount of slip and torque references properties for different kinds of roads. Simulation results show more reliable and better performance compared with other brake systems. While Karakose and Akin [73] proposed a different fuzzy control algorithm, which used dynamical fuzzy logic system and block based neural network, for dynamical control problems. The effectiveness of the proposed method is illustrated by simulation results for dc motor position control problem. In the same direction Ayman A. Aly [74] designed an intelligent fuzzy ABS controller to adjust slipping performance for variety of roads. The fuzzy optimizer finds immediately the optimal wheel slips for the new surface and forces the actual wheel slips to track the optimal reference wheel slips. The simulation results show that the proposed ABS algorithm ensures avoiding of wheel's blockage, even in different road conditions. Moreover, as a free model strategy, the obtained fuzzy control is advantageous from viewpoint of reducing design complexity and, also, antisaturating, antichattering and robustness properties of the controlled system.

4. Conclusions

ABS control is highly nonlinear control problem due to the complicated relationship between its components and parameters. The research that has been carried out in ABS control systems covers a broad range of issues and challenges. Many different control methods for ABS have been developed and research on improved control methods is continuing. Most of these approaches require system models, and some of them cannot achieve satisfactory performance under the changes of various road conditions. While soft computing methods like Fuzzy control doesn't need a precise model. A brief idea of how soft computing is employed in ABS control is given.

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