

# **Evaluation of the Gas Turbine Inlet Temperature with Relation to the Excess Air**

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# Abstract

This paper shows the effect of excess air on combustion gas temperature at turbine inlet, and how it determines power and thermal efficiency of a gas turbine at different pressure ratios and excess air. In such a way an analytic Equation that allows calculating the turbine inlet temperature as a function of excess air, pressure ratio and relative humidity is given. Humidity Impact on excess air calculation is also analyzed and presented. Likewise it is demonstrated that dry air calculations determine a higher level for calculations that can be performed on wet air.

Keywords: Gas Turbine, Excess Air, Turbine Inlet Temperature, Dry Air, Wet Air

# **1. Introduction**

Evolution of gas turbines has evolved together with aero thermodynamics and metallurgy, such relationship has made possible for today's gas turbines to withstand temperatures in the 1700°C range [1,2], pressure ratios up to 34:1 [1,2], internal compressor and turbine efficiency up to 90% [3] and overall thermal efficiency up to 40% [3]. In the same way, it has been possible to reduce the number of stages required in a compressor to achieve a specific pressure ratio, hence the number of stages in a turbine to drive the compressor, and consequently the overall gas turbine size has been reduced allowing to have more compact and efficient gas turbines for a required power.

However, the most spectacular improvement that the gas turbine has even experimented is, perhaps, the increase of the gas turbine inlet temperature. This has been possible thanks to improvements on the turbine blade cooling techniques, and of course, metallurgical advances. The turbine inlet gas temperature implicitly makes reference to exhaust temperature from combustion chamber. It is known that the temperature during steady combustion in the combustion zone, greatly exceeds the maximum allowable temperature by the turbine blades on the first stage, therefore an increase in excess air is needed to bring down the combustion gas temperature to allowable values at the turbine inlet. In other words, utilize more excess air in order to cool down the combustion

gas temperature.

excess air in the combustion chamber to reach an exhaust gas temperature allowable by the turbine first stages blades. To achieve this, it is needed to consider the humidity on the atmospheric air, which is taken as the work fluid at the compressor process, and entering then to the combustion chamber. Due to the humidity effect is considered on the excess wet air calculations, the calculations considering dry air are also presented showing that it is required a greater quantity of dry air to reach a determined gas temperature. The effect of relative humidity on the gas turbine is wide discussed at the paper of I.

The objective of this work is to calculate the required



Figure 1. Schematic diagram of a continuous combustion chamber.

Usiyama [3], where the effect of ambient condition is analyzed: temperature, pressure and humidity over the gas turbine performance. Usiyama's work concludes that the humidity effect must be considered on accurate calculations when the ambient temperature is up to 30°C and the relative humidity is up to 70%. The paper presented by I. G. Rice [4] meets the conclusions presented in [3]. It was decided to include the relative humidity on the excess air calculations because of the importance of this parameter at the gas turbine performance. It must be noted that works traditionally including relative humidity parameter, generally, is included and analyzed its effect over the plant global thermal efficiency, however is not shown the effect on the turbine inlet temperature, which is shown in this article, as well as an analysis of how the thermal efficiency and the work output as a function of pressure ratio and excess air. Work also considers a stationary gas turbine for analysis.

## 2. Methodology

#### 2.1. System Description

Figure 1 [5] shows a schematic diagram of a combustion chamber with its main components, combustion and cooling zones. Usually, the combustion gas temperature at turbine inlet is on the range of 800°C to 1700°C, depending on turbine blade materials and whether or not they have cooling systems. In order to achieve these temperatures a 600% to 100% excess air is required. However, these excess air values make combustion un-steady. That's why combustion chambers are divided in combustion zone and mixture and dilution zone, as Figure 1 shows. In the combustion zone, fuel is sprayed and stabilized by swirling vanes, primary air is mixed with fuel making a mixture approximately stechiometric, which ignites the flame and keeps a steady temperature of approximately 2500°C depending on fuel. In the mixture zone, secondary air is forced into the flame tube through small holes on the tube wall in order to achieve a complete combustion. In this zone, more secondary air is added in order to low down the temperature in the combustion zone. At the dilution zone, the tertiary air is added to the flow coming from the mixture zone in order to combustion gas temperature low down to reach a permissible value for the turbine first stage blades. It must be generated a turbulence enough to cool and hot streams mix themselves getting an homogeneous distribution of gas temperature at combustion chamber outlet, therefore hot stream lines are avoided, which could damage the turbine blades.

Figure 1 also depicts a swirling vane, which objective is to facilitate the heat and mass transfer by vortex generating. A Thoroidal vortex is generated getting a low pressure zone through combustion chamber axis. The net result is that burned gases tend to go into the low pressure zone and a part of them goes to the combustible spout and primary air entering at combustion zone. That way, an auto guided flame is obtained at the air stream, which speed is higher than flame speed at combustion mixture, getting so, the combustion stabilizing.

The atmospheric pressure is a function of the altitude. In accordance with the definition of static pressure, the following differential Equation is obtained.

$$\frac{\mathrm{d}p}{\mathrm{d}z} = -g\rho \tag{1}$$

The air at low pressures behaves as ideal gas, so we can get to the following Equation

$$dp/p = -(\rho_{atm}g/p_{atm})dz$$
 (2)

#### 2.2. Dry Air

Atmospheric air is an Oxygen and Nitrogen mixture with slight quantities of Carbon Anhydrous, Argon and Water Steam. Its composition slightly varies with humidity and altitude. When water steam presence is not considered in atmospheric air composition, it is known as dry air. This work considers the dry air composition as follows 21% Oxygen and 79% Nitrogen. Thus the 79% N<sub>2</sub> fraction refers to N<sub>2</sub>, CO<sub>2</sub> and Ar mixture, which is known as atmospheric Nitrogen. That way, there is 0.21 mol of Oxygen and 0.79 mol of Nitrogen in each dry air mol. That is to say:  $1DA = 0.21O_2 + 0.79N_2$ .

#### 2.3. Wet Air

Wet air is a dry air and water steam mixture. The air in atmosphere, which is taken as work fluid in internal combustion machines, is a kind of that mixture. For its thermodynamic analysis, it must be considered the ambient humidity effect in order to get a real analysis, otherwise, there will be a mistake into the excess air calculations.

The thermodynamics analysis of dry air and water steam mixture can be made in an easy and accurate way just with the next two assumptions: 1) the gas phase lays on the ideal gases law; 2) liquid phase does not have dissolved gas. Since wet air is a dry air and water steam mixture, the composition of a wet airmol can be written as follows:

$$1WA = x_{DA}DA + x_{H_2O}H_2O$$
 (3)

where  $x_{DA}$  and  $x_{H_{2}O}$  are the dry air and water steam mol fractions in the wet air. The results of these fractions from pressure, temperature and relative humidity at ambient conditions are very important to establish the com-

bustion reaction when wet air is considered.

#### 2.4. Relative Humidity

The wet air composition can be showed in terms of relative humidity  $\phi$ , it can be written as follows:

$$\varphi = \frac{p_{\rm H_2O}}{p_{\rm sat}} \tag{4}$$

The *T*-*s* diagram in **Figure 2** [6] shows processes at dew temperature, which are key parameters to consider: constant pressure process (0-3) to reach dew temperature, as well as the constant temperature process (0-1) to reach the saturation pressure. Point 0 is for the water steam present on the atmospheric air, which is known as superheated steam under ambient temperature  $T_0$  and partial pressure  $p_{\rm H_2O}$  conditions. If atmospheric air is cool down at a constant pressure, then the water steam temperature decreases until reach the saturation phase (point 2). This saturation temperature is known as dew temperature and corresponds to the partial pressure  $p_{\rm sat}$  of water steam corresponding at atmospheric air temperature  $T_0$ , that is to say,  $p_{\rm sat} = p_{\rm sat}(T_0)$ .

### 2.5. Specific Humidity

Wet air composition can also be showed using the specific humidity  $\omega$ , that is to say:

$$\omega = \frac{m_{\rm H_2O}}{m_{\rm DA}} \tag{5}$$

The specific humidity can be written as a term of relative humidity,  $\phi$ :

$$\omega = 0.622 \frac{\varphi p_{sat}}{p_0 - \varphi p_{sat}} \tag{6}$$



Figure 2. Temperature entropy diagram for relative humidity and dew temperature.

It is useful to show the specific humidity in terms of dry air and water steam mol fractions:

$$\omega = \frac{x_{\rm H_2O} P M_{\rm H_2O}}{x_{\rm DA} P M_{\rm DA}} \tag{7}$$

The relation between water steam molfraction as a function of specific humidity is:

$$x_{\rm H_2O} = \frac{\omega}{\omega + 0.622} \tag{8}$$

and the relation between dry air mol fraction as a function of specific humidity is:

$$x_{\rm DA} = \frac{0.622}{\omega + 0.622} \tag{9}$$

Using the Equation (4) on Equations (6) and (7), the formulas for dry air and water steam mol fractions as a function of relative humidity, can be obtained:

$$x_{\rm H_2O} = \frac{\varphi p_{\rm sat}}{p_0} \tag{10}$$

$$x_{\rm DA} = 1 - \frac{\varphi p_{sat}}{p_0} \tag{11}$$

Both Equations show that volumetric composition of wet air depends on the relative humidity  $\phi$ , as well as the pressure and temperature ambient conditions. Note that  $p_{\text{sat}} = p_{\text{sat}}(T_0)$ .

Curves on Figure 3 [7] are generated based on Equation (8). The Figure 3 depicts the variation of humidity present in atmospheric air as a function of relative humidity for different ambient temperature values. It depicts that for a given atmospheric pressure and, increasing the ambient temperature, the humidity content increases too. However, it can be seen that humidity content increases is higher for high ambient temperature values. It is interesting to note how for a 40°C temperature and 80% humidity, the water fraction content reaches values of 7% in the atmospheric air. Last point out that the water mol fraction is a variable which impacts on calculations of the excess air required for gas turbine combustion when there ambient temperature values up to 30°C and relative humidity values up to 45% for a given atmospheric pressure.

**Figure 4** [8] depicts the effect that ambient pressure has over the humidity contained in atmospheric air for a given ambient temperature. It can be seen from **Figure 4** that keeping the ambient temperature constant, an atmospheric pressure increase results in a humidity content increasing. For instance, for a relative humidity value of 60%, there is a lower humidity content at an atmospheric pressure of 0.672 bar, instead of atmospheric pressure values of 0.872 and 1.01 bar.

Figures 3 and 4 depict that variation of ambient pres-



Figure 3. Water steam mol fraction wet air varying relative humidity.



Figure 4. Humidity content in atmospheric air as a function of relative humidity for different values of ambient pressure.

sure has a lower effect on the water fraction contained in the atmospheric air, then varying the ambient temperature. It also can be seen that humidity content in atmospheric air increases as ambient pressure decreases and the ambient temperature increases. That is to say, the condition in which a higher water volume can be operated is when ambient condition presents high temperature and low pressure. The water fraction contained in atmospheric air impacts the value of specific heat at constant pressure. The humidity effect takes importance at high atmospheric temperatures and compression ratio.

If combustion is incomplete or excess air is used, the mixture temperature is lower than adiabatic combustion temperature.

## 2.6. Excess Air

The minimum air quantity needed to get a complete oxidation of reactants is known as theoretic air [9]. Ideally, if combustion would be made with theoretic air, it could be a complete combustion and oxygen should not appear in products. At practice, this is impossible; because of the short time of combustion process is not enough to achieve a complete reaction of Oxygen and combustible molecules. That is why more Oxygen is needed than the theoretically necessary to achieve a complete combustion of reactants. Thus it is required excess air in order to assure the Oxidation of hydrocarbon molecules. Using excess air means that a quantity of air higher than theoretically necessary (100%) was used. 200% of excess air means the double of theoretically necessary air to achieve a complete combustion. It is 100% of excess air.

Industrial gas turbines generally use excess air values from 100% to 600%. This work considers natural gas as combustible due to the general use of this one in gas turbines and combined cycles plants. Natural gas composition varies from deposit to deposit and even with the time. It is useful to represent the combustion reaction of any hydrocarbon combustible with the form *CnHm*, using atmospheric air as oxidation element, that is to say, considering the humidity in ambient.

The elemental composition of fuel is Carbon and Hydrogen as reactant elements, with other elements such as Nitrogen and Oxygen. The main combustion products are Carbon Anhydrous,  $CO_2$ , and the Water Steam,  $H_2O$ .

The combustion reaction is the following:

$$\left(\sum_{i=1}^{k} x_i C_{n,i} H_{m,i}\right) + N_{\text{WA},\lambda} \text{WA} \rightarrow \text{ACO}_2$$
$$+ \left\lfloor N_{\text{WA},\lambda} x_{\text{H}_2\text{O}} + B \right\rfloor \text{H}_2\text{O} \qquad (12)$$
$$+ \left[ 0.21 N_{\text{WA},\lambda} x_{\text{DA}} - C \right] \text{O}_2 + 0.79 N_{\text{WA},\lambda} x_{\text{DA}} N_2$$

where:

WA = 
$$x_{DA} [0.21O_2 + 0.79N_2] + x_{H_2O}H_2O$$
 (13)

$$A = \sum_{i=1}^{k} x_i n_i \quad B = \sum_{i=1}^{k} \frac{x_i m_i}{2} \quad C = \sum_{i=1}^{k} x_i \left( n_i + \frac{m_i}{4} \right)$$
(14)

$$N_{\rm WA,\lambda} = (1+\lambda) \frac{C}{0.21 x_{\rm DA}}$$
(15)

It is known that the hot part temperatures at gas turbine inlet are a metallurgical limitation for each gas turbine model. These temperatures vary from 800°C to 1700°C depending on construction and turbine blades cooling system. By analyzing Equation (10) and knowing the combustible composition, the only variable is the excess air  $\lambda$ , because combustion gas temperature (products) is a known parameter, it is, turbine inlet temperature  $T_3$ .

Excess air value  $\lambda$ , necessary to get a given combustion gas temperature  $T_3$ , is found as follows. It is considered that reactants enter to the combustion chamber at air

temperature reached after the compression process and that the product exit from combustion chamber at turbine inlet gas temperature  $T_3$ . Following the adiabatic combustion principles, the next energy balance is presented having in mind a steady state process, adiabatic conditions, work absence and without kinetic energy change for the reaction process described by Equation (10):

$$\sum_{P} N_{i} \overline{h}_{i} \left( T_{2} \right) = \sum_{R} N_{j} \overline{h}_{j} \left( T_{3} \right)$$
(16)

Using Equation (14) into combustion reaction Equation (10), the required quantity of wet air with excess air  $(N_{\text{WA}\lambda})$  necessary to reach the desired temperature inlet turbine  $(T_3)$ ,

$$N_{\mathrm{WA}_{\lambda}} = \frac{\overline{h}_{f}\left(T_{0}\right) - A\overline{h}_{\mathrm{CO}_{2}(T_{3})} - B\overline{h}_{\mathrm{H}_{2}\mathrm{O}(T_{3})} - C\overline{h}_{\mathrm{O}_{2}}}{\left[\overline{h}_{\mathrm{WA}(T_{3})} - \overline{h}_{\mathrm{WA}(T_{2})}\right]} \qquad (17)$$

From Equation (15), denominator corresponds to the enthalpy change of wet air between combustion chamber inlet temperature  $T_2$  and combustion gas temperature at combustion chamber outlet  $T_3$ . According to wet air composition, its enthalpy is determined as follows:

$$\bar{h}_{WA}(T) = x_{DA} \left[ 0.21 \bar{h}_{o_2}(T) + 0.79 \bar{h}_{N_2}(T) \right]$$

$$+ x_{H_2O} + \bar{h}_{H_2O}(T)$$
(18)

Finally, excess air is given by the next Equation:

$$\lambda = \left(\frac{N_{WA_{\lambda}}}{N_{WA_{st}}} - 1\right) 100\%$$
(19)

Equation (17) is the mathematical model to find the excess air as function of turbine inlet temperature T<sub>3</sub>, fuel composition, relative humidity and pressure ratio. For instance, for a given T<sub>3</sub> value using Equation (17) it is possible to calculate the corresponding value of excess air, in the other hand, for a given value of excess air it is also possible to calculate the corresponding value of T<sub>3</sub>using ad iterative method. In Equation (17)  $N_{WA_{sf}}$  term, corresponds to stoichiometric quantity of wet air, it is,  $\lambda = 0$ , and is given by the next Equation:

$$N_{\mathrm{WA}_{st}} = \frac{C}{0.21x_{\mathrm{DA}}} \tag{20}$$

## 3. Results

The natural gas composition used in this work and the operation conditions of the gas turbine cycle are presented on the Appendix 1. From the Equations (17) and (18), it is possible to calculate the excess wet air necessary to reach an specific combustion gas temperature at turbine inlet. The **Figure 5** depicts that decreasing the design

|     |          | Res     | ulfados  | o de la    | a Simulaci  | ón   |           |
|-----|----------|---------|----------|------------|-------------|--|-----------|
|     |          |         |          |            |             | ₩c<br>(kJ/kg)                              | 451.704   |
|     | T(°C)    | P(bar)  | h(kJ/kg) | S(kJ/kg K) | Cp(kJ/kg K) | Wt<br>(kJ/kg)                              | 779.864   |
| g1  | 37.2     | .86406  | 310.556  | 6.73617    | 1.00443     | Wmotor<br>(kJ/kg)                          | 343.732   |
| g2s | 386.2242 | 13.1337 | 669.352  | 6.73617    | 1.06445     | Flujo Comb.                                | 6.646     |
| g2  | 472.2856 | 13.1337 | 762.260  | 6.86331    | 1.08518     | (kg/s)                                     | 000.047   |
| g3  | 1245.    | 12.7397 | 1747.04  | 7.64559    | 1.29626     | Flujo de<br>Aire (kg/s)                    | 332.817   |
| g4s | 539.5576 | .90078  | 873.456  | 7.64559    | 1.16312     | Flujo Gases<br>(kg/s)<br>Eficiencia<br>(%) | 339.463   |
| g4  | 619.4181 | .90078  | 967.176  | 7.76116    | 1.18376     |  | 34.904    |
|     |          |         |          |            |             | Exceso de aire                             | 292.52298 |

Figure 5. Excess wet air variation as a function of the turbine inlet temperature.

temperature of combustion gas at turbine inlet; the required excess air will be greater. For instance, when the gas temperature is 1200°C at the inlet of a turbine, the excess air will be 198.79%, otherwise, if the temperature is 1000°C, the excess air increases to 324.51%. On the other hand, a high turbine inlet gas temperature will require a lower quantity of secondary and tertiary air to cool down the combustion gas to the specified temperature.

It is also possible from the Equations (17) and (18) to determine the excess dry air, making  $x_{DA} = 1$  y  $x_{H_2O} = 0$  in the Equation (10). Based on that, the **Figure 6** depicts the variation between the excess dry air and the wet air respect to the turbine inlet temperature. It can be seen in the **Figure 6** that to reach a given turbine inlet temperature, it's required a dry air quantity greater than the wet air quantity. This difference between the excess dry and wet air increases as turbine inlet temperature increases. For instance, to get a  $T_3 = 1000$  °C temperature it is required 5.24% dry air more than wet air. The last is shown in the **Table 1**.

The **Figures 5** [10] and **6** [11] depict the dependency of the turbine inlet temperature according to the excess air value required to reach that temperature. It is also shown in the **Figure 6** that the atmospheric air gives a decrease in the excess air to reach the same turbine inlet gas temperature. However, the **Figure 7** depicts the effect that relative humidity and ambient temperature have over the excess air values required to reach a combustion gas temperature of 1243°C at the turbine inlet by varying the ambient temperature. The **Figure 7** also depicts that increasing the relative humidity to a determined ambient temperature value, then the excess air decreases to reach a 1243°C combustion gas temperature at the turbine inlet.

However, it is interesting to note that excess air variation

Table 1. Excess dry air and excess wet air.

| $T_3(^{\circ}C)$ | Dry air $\lambda$ (%) | Wet Air $\lambda$ (%) | Relative (%) |
|------------------|-----------------------|-----------------------|--------------|
| 800              | 629.51                | 600.29                | 4.64         |
| 900              | 453.08                | 430.78                | 4.92         |
| 1000             | 342.48                | 324.51                | 5.24         |
| 1100             | 266.72                | 251.72                | 5.62         |
| 1200             | 211.631               | 198.79                | 6.07         |
| 1300             | 169.79                | 158.59                | 6.59         |
| 1400             | 136.96                | 127.06                | 7.23         |
| 1500             | 110.53                | 101.68                | 8.00         |



Figure 6. Required excess air values to reach a given temperature between wet air and dry air.



Figure 7. Excess air as a function of the relative humidity at different ambient temperature values.

as a function of relative humidity variation, increases as the ambient temperature increases, see **Table 2**. When dry air is considered, it means  $\phi = 0$ , it can be seen that the excess

air increases as the ambient temperature increases, however, considering wet air, the last is not necessary true for relative humidity values up to 60% and ambient temperature values up to 30°C.

The **Figure 8** depicts that by increasing the compression ratio, a greater excess air is required in order to reach a given combustion gas temperature at the turbine inlet. The last assumption is due to the increase of the compression ratio, the temperature at the end of the compression process increases; therefore it has a lower cooling effect at the dilution zone, **Figure 1**, of the combustion chamber. It has seen that increasing the compression ratio, the excess air required to reach a given temperature at the turbine inlet increases too, as the **Figure 8** depicts is increased. Given that the atmospheric pressure is not constant at any level of altitude, variations are had in the quantity of mass of water and enthalpy.

The excess air decreasing (increasing of combustion gas temperature at turbine inlet) has a direct relationship with the cycle thermal efficiency. This is known at certain values of pressure ratios, it means, that the thermal efficiency of the gas turbine cycle is in function of excess air (combustion gas temperature at turbine inlet) and the pressure ratio. This is as follows:

 Table 2. Excess air in function of the relative humidity for different values of the ambient temperature.

| $\phi$ | 0°C    | 10°C   | 20°C   | 30°C   | 40°C   | 50°C   |
|--------|--------|--------|--------|--------|--------|--------|
| 0      | 170.90 | 177.55 | 184.54 | 191.88 | 199.61 | 207.75 |
| 20     | 170.38 | 176.48 | 182.42 | 187.92 | 192.51 | 195.52 |
| 40     | 169.86 | 175.4  | 180.32 | 183.99 | 185.51 | 183.58 |
| 60     | 169.34 | 174.33 | 178.22 | 180.09 | 178.61 | 171.92 |
| 80     | 168.82 | 173.26 | 176.13 | 176.23 | 171.80 | 160.53 |
| 100    | 168.30 | 172.19 | 174.05 | 172.39 | 165.09 | 149.40 |



Figure 8. Excess air as function of the combustion gas temperature.

$$\eta t = \eta t \left(\lambda, \pi\right) \text{ or } \eta t = \eta t \left(T_3, \pi\right)$$
 (21)

However, thermal efficiency can be expressed in a general form as follows:

$$\eta = \frac{y\eta_{SIT} \left(1 - \frac{1}{\pi^{Z}}\right) - \frac{1}{\eta_{SIC}} (\pi^{Z} - 1) - \frac{Z\pi^{Z}}{\eta_{SIC}} (\varepsilon_{1} + \varepsilon_{2})}{y - 1 - \frac{1}{\eta_{SIC}} (\pi^{Z} - 1) - \frac{Z\pi^{Z}}{\eta_{SIC}} (\varepsilon_{1} + \varepsilon_{2})}$$
(22)

where:

$$z = \frac{R}{c_p} = \frac{k-1}{k}; y = \frac{T_3}{T_1}$$

Equation (20) expresses thermal efficiency as function of work output,  $W_m$ , turbine inlet temperature,  $T_3$ , pressure ratio,  $\pi$ , compressor inlet temperature,  $T_1$  and implicitly excess air,  $\lambda$ . It means:

$$\eta = \eta \left( W_m, T_3, T_1, \pi, \lambda \right)$$

According to Equation (20), the **Figure 9** [12] depicts the network output variation as a function of the cycle thermal efficiency at different excess air values (combustion gas temperature at turbine inlet), as well as to different pressure ratios. It can be seen in the **Figure 9**.

That the thermal efficiency of gas turbine cycle increases as the excess air decreases (increasing the combustion gas temperature at turbine inlet) keeping a constant compression ratio. However, it must be noted that for a given excess air (a given combustion gas temperature at turbine inlet), there is a pressure ratio which makes maximum the thermal efficiency. In the **Figure 9** can be noted these excess air values at 600.29%, 324.51% and 198.8% (for turbine inlet temperatures of 800°C, 1000°C and 1200°C).



Figure 9. Performance map showing the effect of pressure ratio and excess air (turbine inlet temperature) on a simple cycle.

## 4. Conclusions

The methodology shown here is a useful tool to determine the turbine inlet gas temperature using the excess air and the pressure ratio. The methodology is also an alternative to calculate the turbine inlet temperature respect to direct methods used to measure the turbine inlet temperature, which are complex and expensive.

The mathematical model shown in this work can be coupled to empirical correlation in such a way the turbine inlet temperature can be predicted depending on the characteristics of each gas turbine model.

Increasing the turbine inlet temperature, the required excess air decreases. The result is a secondary and tertiary air used to cooling process. Therefore the machine size will be smaller for the same power generated.

The difference between the calculations for the excess air using dry air and wet air is just little. Therefore the generalized assumption to use dry air is good, however, if more accurate is required for the calculations, the ambient humidity must be considered, much more when the ambient conditions are temperature up to 30°C and the relative humidity up to 60%.

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## Nomenclature

- DA dry air, [mol];
- *Cp* specific heat at constant pressure, [kJ/(kgK)];
- *h* specific enthalpy, [kJ/kg];
- *m* mass flow rate, [kg/s];
- *N* number of moles, [mol];
- *p* pressure, [bar];
- *rf/a* fuel/air ratio, [kgC / kg];
- R gas constant, [kJ/(kgK)];
- *s* specific entropy, [kJ/(kgK)];
- T temperature, [°C];
- v specific volume, [m3/kg];
- WA wet air, [mol];
- *x* mole fraction, [-];
- y mass fraction, [-];
- h Efficiency, [%];
- *f* Relative humidity, [%];
- l Excess air, [%];
- *p* Pressure ratio, [-].

#### Subscripts

- *c* compressor; *cc* combustion chamber;
- DA dry air;
- *dew* dew temperature;
- *gc* combustion gas;
- $H_2O$  water;
- *i i*-esimo component;
- *m* hydrogen atoms number;
- *n* carbon atoms number;
- *P* products;
- *R* reactants;
- *s* isentropic process;
- st stoichiometric;
- t thermal;

- T turbine;
- *GT* gas turbine;
- WA wet air;
- *l* with excess air;
- 0 atmospheric conditions;
- 1 compressor inlet;
- 2 compressor outlet;
- 3 turbine inlet;
- 4 turbine outlet.

# **APPENDIX 1**

Gas Turbine Cycle Operations Conditions

- The ambient condition in cite are as follows: Ambienttemperature,  $T_0 = 32.2^{\circ}$ C; Ambient pressure,  $p_0 = 0.872$  bar; Relative humidity,  $\phi = 45\%$ ; Site elevation, 1260 mosl.
- Pressure ratio,  $\pi = 15.2$ ;
- Compressor efficiency,  $\eta_{\text{PIC}} = 86\%$ ;
- Pressure difference at the compressor inlet,  $\Delta p_c = 0.9174\%$ ;
- Pressure difference at the combustion chamber,  $\Delta p_{cc} = 2.3\%$ ;
- Pressure difference at the turbine exit,  $\Delta p_{GT} = 3.326\%$ ;
- Turbine inlet temperature,  $T_3 = 1243$ °C;
- Turbine efficiency,  $\eta_{\text{PIT}} = 85\%$ ;
- Power output P = 114400 kW
- Natural gas volumetric composition: Methane (CH<sub>4</sub>), 96.87%; Ethane (C<sub>2</sub>H<sub>6</sub>), 2.85%; Propane (C<sub>3</sub>H<sub>8</sub>) 0.24%; Butane (C<sub>4</sub>H<sub>10</sub>), 0.03%;. Isobutane (C<sub>4</sub>H<sub>10</sub>), 0.01%.