

# Stochastic Modeling and Power Control of Time-Varying Wireless Communication Networks

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## Abstract

Wireless networks are characterized by nodes mobility, which makes the propagation environment time-varying and subject to fading. As a consequence, the statistical characteristics of the received signal vary continuously, giving rise to a Doppler power spectral density (DPSD) that varies from one observation instant to the next. This paper is concerned with dynamical modeling of time-varying wireless fading channels, their estimation and parameter identification, and optimal power control from received signal measurement data. The wireless channel is characterized using a stochastic state-space form and derived by approximating the time-varying DPSD of the channel. The expected maximization and Kalman filter are employed to recursively identify and estimate the channel parameters and states, respectively, from online received signal strength measured data. Moreover, we investigate a centralized optimal power control algorithm based on predictable strategies and employing the estimated channel parameters and states. The proposed models together with the estimation and power control algorithms are tested using experimental measurement data and the results are presented.

# Keywords

Wireless Networks, Time-Varying Wireless Fading Channel, Impulse Response, Doppler Power Spectral Density, Stochastic State-Space Model, Stochastic Modeling, Optimal Power Control, Expectation Maximization, Kalman Filter

# **1. Introduction**

Time varying (TV) wireless channel models capture both the space and time variations of wireless systems,

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In [4], the TV channel parameters are estimated from approximating the Doppler power spectral density (DPSD) of the wireless fading channel. However, in reality one does not have access to the TV DPSD at all times during the estimation process. Since these models are based on state-space forms, we propose to estimate the channel parameters as well as the inphase and quadrature components directly from received signal measurements, which are usually available or easy to obtain in any wireless network. A filter-based expectation maximization (EM) algorithm [8] and Kalman filter [9] are employed in estimating the channel parameters as well as the inphase and quadrature components, respectively. These recursive filters use only the first and second order statistics and therefore can be implemented online. These algorithms have been recently utilized in [1] and [2] to estimate the wireless channel parameters and states, and therefore the formulations of these algorithms are not presented in this paper. The proposed models and estimation algorithms are tested using received signal strength measurement data and the results are presented.

The developed stochastic channel models from received signal strength measurements are useful in most wireless applications. In this paper, these models are used to develop an optimal power control algorithm (PCA). Power control (PC) is important to improve performance of wireless communication systems. The benefits of power minimization are not just increased battery life, but also increased overall network capacity. The power allocation problem has been studied extensively as an eigenvalue problem for non-negative matrices [10] [11], resulting in iterative PCAs that converge each user's power to the minimum power [12] [13], and as optimization-based approaches [14]. Much of this previous work deals with static time-invariant channel models.

The proposed PCA is based on predictable power control strategies (PPCS) that were first introduced in [4]. PPCS basically means updating the transmitted powers at discrete times and maintaining them fixed until the next power update begins. The PPCS mechanism is proven to be effectively applicable to such dynamical models for an optimal PC. The outage probability (OP) is used as a performance measure. Since few TV dynamical channel models have so far been investigated with the application of any PCA, the suggested dynamical models and PCA thus provide a far more realistic and efficient optimal control of wireless networks.

The remainder of this paper is organized as follows. In Section 2, stochastic modeling and online estimation of TV wireless fading communication channels are presented. Section 3 introduces an optimal PCA based on predictable strategies and employing the estimated channel parameters and states. Section 4 presents numerical results that validate the proposed models together with the estimation and power control algorithms. Finally, Section 5 provides concluding remarks.

#### 2. Stochastic Modeling and Estimation of Time-Varying Wireless Channels

The general TV model of a wireless channel is typically represented by the following multipath band-pass impulse response [6]

$$H(t;\tau) = \sum_{j=1}^{J(t)} \left( I_j(t,\tau) \cos(\omega_c t) - Q_j(t,\tau) \sin(\omega_c t) \right) \delta(\tau - \tau_j(t))$$
(1)

where  $H(t;\tau)$  is the band-pass response of the channel at time t, due to an impulse applied at time  $t-\tau$ ,

J(t) is the random number of multipath components,  $\omega_c$  is the carrier frequency,  $\delta(\cdot)$  is the Dirac delta function, and the set  $\{I_j(t,\tau), Q_j(t,\tau), \tau_j(t)\}_{j=1}^{J(t)}$  describes the random TV inphase component, quadrature component, and arrival time of the different paths, respectively. Let  $s_l(t)$  be the low-pass equivalent representation of the transmitted signal, then the band-pass representation of the received signal is given by

$$y(t) = \sum_{j=1}^{J(t)} \left( I_j(t,\tau) \cos(\omega_c t) - Q_j(t,\tau) \sin(\omega_c t) \right) s_l(t-\tau_j(t)) + v_I(t) \cos(\omega_c t) - v_Q(t) \sin(\omega_c t)$$
(2)

where  $\{v_I(t)\}_{t\geq 0}$  and  $\{v_Q(t)\}_{t\geq 0}$  are two independent and identically distributed (iid) white Gaussian noise processes.

It is shown in [4] and [15] that the DPSD of a wireless fading channel, denoted by S(s), can be approximated by an even, stable, rational, and factorizable transfer function,  $\tilde{S}(s) = H(s)H(-s)$ , where H(s) is given by

$$H(s) = \frac{b_{n-1}(t)s^{n-1} + \dots + b_1(t)s + b_0(t)}{s^n + a_{n-1}(t)s^{n-1} + \dots + a_1(t)s + a_0(t)}$$
(3)

Consequently, the inphase and quadrature components can be realized using the following stochastic statespace representation [16]

$$dX_{I,j}(t) = A_{I}(t)X_{I,j}(t)dt + B_{I}(t)dW_{j}^{T}(t)$$

$$I_{j}(t) = C_{I}X_{I,j}(t) + f_{j}^{T}(t)$$

$$dX_{Q,j}(t) = A_{Q}(t)X_{Q,j}(t)dt + B_{Q}(t)dW_{j}^{Q}(t)$$

$$Q_{j}(t) = C_{Q}X_{Q,j}(t) + f_{j}^{Q}(t)$$
(4)

where

$$\mathbf{X}_{I,j}(t) = \begin{bmatrix} X_{I,j}^{1}(t), X_{I,j}^{2}(t), \cdots, X_{I,j}^{n}(t) \end{bmatrix}^{\mathrm{T}}, \\
\mathbf{X}_{Q,j}(t) = \begin{bmatrix} X_{Q,j}^{1}(t), X_{Q,j}^{2}(t), \cdots, X_{Q,j}^{n}(t) \end{bmatrix}^{\mathrm{T}}, \\
\mathbf{A}_{I}(t) = \mathbf{A}_{Q}(t) = \begin{bmatrix} 0 & 1 & 0 & \cdots & 0 \\ 0 & 0 & 1 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \cdots & 1 \\ -a_{0}(t) & -a_{1}(t) & -a_{2}(t) & \cdots & -a_{n-1}(t) \end{bmatrix}, \\
\mathbf{B}_{I}(t) = \mathbf{B}_{Q}(t) = \begin{bmatrix} b_{n-1}(t) \\ \vdots \\ b_{2}(t) \\ b_{1}(t) \\ b_{0}(t) \end{bmatrix}, \quad \mathbf{C}_{I} = \mathbf{C}_{Q} = \begin{bmatrix} 1 & 0 & 0 & \cdots & 0 \end{bmatrix}$$
(5)

 $X_{I,j}(t)$  and  $X_{Q,j}(t)$  are the state vectors corresponding to the inphase and quadrature components, respectively.  $\{W_j^I(t)\}_{t\geq 0}, \{W_j^Q(t)\}_{t\geq 0}$  are independent standard Brownian motions, which correspond to the inphase and quadrature components of the  $j^{th}$  path respectively,  $f_j^I(t)$  and  $f_j^Q(t)$  are arbitrary functions representing the presence or absence of line-of-sight (LOS) of the inphase and quadrature components for the  $j^{th}$  path respectively, and T denotes matrix or vector transpose. Without loss of generality, we consider the case of flat fading, in which the fading channel has purely a multiplicative effect on the signal and the multipath components are not resolvable, and, thus, can be considered as a single path [6]. We also consider the non-line-of-sight (NLOS) case, *i.e.*,  $f_j^I(t) = f_j^Q(t) = 0$ , which represents an environment with large obstructions. The

time-varying state space model described in (4) has a solution given by

$$X_{L}(t) = \Phi_{L}(t,t_{0})X_{L}(t_{0}) + \int_{t_{0}}^{t} \Phi_{L}(t,u)B_{L}(u)dW_{L}(u)$$

$$\tag{6}$$

where L = I or Q,  $\Phi_L(t, t_0)$  is the state transition matrix associated to  $A_L(t)$ , and  $\dot{\Phi}_L(t, t_0) = A_L(t) \Phi_L(t, t_0)$ . Therefore, the mean of  $X_L(t)$  is

$$E\left[X_{L}(t)\right] = \Phi_{L}(t,t_{0})E\left[X_{L}(t_{0})\right]$$
<sup>(7)</sup>

and the covariance matrix of  $X_{L}(t)$  is

$$\Sigma_{L}(t) = \Phi_{L}(t,t_{0}) Var \Big[ X_{L}(t_{0}) \Big] \Phi_{L}^{\mathrm{T}}(t,t_{0}) + \int_{t_{0}}^{t} \Phi_{L}(t,u) B_{L}(u) B_{L}^{\mathrm{T}}(u) \Phi_{L}^{\mathrm{T}}(t,t_{0}) \mathrm{d}u$$

$$\tag{8}$$

For the time-invariant case,  $A_I(t) = A_I, A_Q(t) = A_Q, B_I(t) = B_I$ , and  $B_Q(t) = B_Q$ , then (6), (7), and (8) simplify to

$$X_{L}(t) = e^{A_{L}(t-t_{0})} X_{L}(t_{0}) + \int_{t_{0}}^{t} e^{A_{L}(t-u)} B_{L} dW_{L}(u)$$

$$E[X_{L}(t)] = e^{A_{L}(t-t_{0})} E[X_{L}(t_{0})]$$

$$\Sigma_{L}(t) = e^{A_{L}(t-t_{0})} Var[X_{L}(t_{0})] e^{A_{L}^{T}(t-t_{0})} + \int_{t_{0}}^{t} e^{A_{L}(t-u)} B_{L} B_{L}^{T} e^{A_{L}^{T}(t-u)} du$$
(9)

It can be observed in (7) and (8) that the mean and variance of the inphase and quadrature components are functions of time. Thus, the statistics of the inphase and quadrature components, and therefore the statistics of the channel, are times varying.

Similarly, following the state space representation in (4) and the received signal in (2), the fading channel can be represented using general stochastic state-space representation of the form

$$dX(t) = A(t)X(t)dt + B(t)dW(t)$$
  

$$y(t) = C(t)X(t) + D(t)v(t)$$
(10)

where

$$\boldsymbol{X}(t) = \begin{bmatrix} X_{I}(t) & X_{Q}(t) \end{bmatrix}^{\mathrm{T}}, \quad \boldsymbol{A}(t) = \begin{bmatrix} A_{I}(t) & 0\\ 0 & A_{Q}(t) \end{bmatrix}, \quad \boldsymbol{B}(t) = \begin{bmatrix} B_{I}(t) & 0\\ 0 & B_{Q}(t) \end{bmatrix},$$
$$\boldsymbol{C}(t) = \begin{bmatrix} \cos(\omega_{c}t)C_{I} & -\sin(\omega_{c}t)C_{Q} \end{bmatrix}, \quad \boldsymbol{D}(t) = \begin{bmatrix} \cos(\omega_{c}t) & -\sin(\omega_{c}t) \end{bmatrix}$$
(11)
$$\boldsymbol{v}(t) = \begin{bmatrix} v_{I}(t) & v_{Q}(t) \end{bmatrix}^{\mathrm{T}}, \quad d\boldsymbol{W}(t) = \begin{bmatrix} dW^{I}(t) & dW^{Q}(t) \end{bmatrix}^{\mathrm{T}}$$

In this case, y(t) represents the received signal measurements, X(t) is the state variable of the inphase and quadrature components, and v(t) is the measurement Gaussian noise.

In [4] and [15], the channel parameters  $\{a_{n-1}(t), \dots, a_0(t), b_{n-1}(t), \dots, b_0(t)\}$  are obtained from approximat-

ing the DPSD. However, in reality one does not have access to the DPSD at all times during the estimation process. Therefore, we propose estimating the channel parameters as well asinphase and quadrature components directly from received signal measurements, which are usually available or easy to obtain in any wireless network. A filter-based expectation maximization (EM) algorithm combined with the Kalman filter is employed to estimate the channel model parameters and states in (10). These filters use only the first and second order statistics and are also recursive, and therefore can be implemented online. These algorithms have been recently utilized in [1] and [2] to estimate wireless channel parameters and states, and therefore the formulations of these algorithms are not presented in this paper. Experimental results demonstrating the applicability of these algorithms in conjunction with the proposed stochastic wireless models are discussed in Section 4. In the next sec-

tion, we introduce an important application based on the developed models; that is stochastic PC in wireless networks.

#### 3. Optimal Power Control Based on the Stochastic Wireless Channel Models

In this section, an optimal PCA is investigated based on the estimated wireless channel models. Since the channel model parameters are estimated from received signal measurements, PC can be performed solely from having these measurements. The aim of the PCA described here is to minimize the total transmitted power of all users while maintaining acceptable quality-of-service (QoS) for each user. The measure of QoS is defined by the signal-to-interference ratio (SIR) for each link to be larger than a target SIR.

By generalizing the wireless channel model in (10), the state-space representation of a wireless network with M transmitters and N receivers can be described as

$$dX_{ij}(t) = A_{ij}X_{ij}(t)dt + B_{ij}dW_{ij}(t)$$
  

$$y_{i}(t) = \sum_{k=1}^{M} \sqrt{p_{k}(t)}s_{k}(t)C_{ik}(t)X_{ik}(t) + v_{i}(t)$$
(12)

where  $y_i(t)$  is the received signal at the  $i^{th}$  receiver at time t,  $X_{ik}(t)$  is the states of the channel between transmitter k and the receiver assigned to transmitter i,  $p_k(t)$  is the transmitted power of transmitter k at time t, which acts as a scaling on the information signal  $s_k(t)$ ,  $v_i(t)$  is the channel disturbance or noise at receiver i, and  $1 \le i, j \le M$ .

Consider the wireless network described in (12), the centralized PC problem for TV channels over a time interval [0,T] can be stated as follows [4]

$$\min_{\substack{(p_{1}\geq0,\cdots,p_{M}\geq0)}} \left\{ \sum_{i=1}^{M} \int_{0}^{T} p_{i}(t) dt \right\},$$
subject to
$$\frac{\int_{0}^{T} p_{i}(t) s_{i}^{2}(t) \left[ C_{ii}(t) X_{ii}(t) \right]^{2} dt}{\sum_{k\neq i}^{M} \int_{0}^{T} p_{k}(t) s_{k}^{2}(t) \left[ C_{ik}(t) X_{ik}(t) \right]^{2} dt + \int_{0}^{T} v_{i}^{2}(t) dt} \geq \varepsilon_{i}$$
(13)

where  $\varepsilon_i$  is the target SIR at receiver *i* and  $i = 1, \dots, M$ . A solution to (13) is presented by first introducing the communication meaning of predictable power control strategies (PPCS). In wireless cellular networks, it is practical to observe and estimate channels at the base stations and then send the information back to the mobiles to adjust their power signals  $\{p_i(t_k)\}_{i=1}^M$ . Since channels experience delays, and power control is not feasible continuously in time but only at discrete time instants, the concept of predictable strategies is introduced [4]. Consider a set of discrete time strategies  $\{p_i(t_k)\}_{i=1}^M$ ,  $0 = t_0 < t_1 < \dots < t_k < t_{k+1} < \dots \le T$ . At time  $t_{k-1}$ , the base stations estimate the channel information  $\{I_{ij}(t_{k-1}), Q_{ij}(t_{k-1}), s_i(t_{k-1})\}_{i,j=1}^M$  as illustrated in Section 2. Using the concept of predictable strategy, the base stations determine the control strategy  $\{p_i(t_k)\}_{i=1}^M$  for the next time instant  $t_k$ . The latter is communicated back to the mobiles, which hold these values during the time interval  $[t_{k-1}, t_k)$ . At time  $t_k$ , a new set of channel information  $\{I_{ij}(t_k), Q_{ij}(t_k), s_i(t_k)\}_{i,j=1}^M$  is estimated at base stations and the time  $t_{k+1}$  control strategies  $\{p_i(t_{k+1})\}_{i=1}^M$  are computed and communicated back to the mobiles which hold them constant during the time interval  $[t_k, t_{k+1}]$ . Such decision strategies are called predictable. Using the concept of PPCS over any time interval  $[t_k, t_{k+1}]$ , Expression (13) is equivalent to

$$\min_{\boldsymbol{p}(t_{k+1})>0} \sum_{i=1}^{M} p_i(t_{k+1}), \text{ subject to } \boldsymbol{p}(t_{k+1}) \ge \boldsymbol{\Gamma} \boldsymbol{G}_I^{-1}(t_k, t_{k+1}) \times \left(\boldsymbol{G}(t_k, t_{k+1}) \boldsymbol{p}(t_{k+1}) + \boldsymbol{\eta}(t_{k+1})\right)$$
(14)

where

$$g_{ij}(t_{k}, t_{k+1}) \coloneqq \int_{t_{k}}^{t_{k+1}} s_{j}^{2}(t) \Big[ C_{ij}(t) X_{ij}(t) \Big]^{2} dt,$$
  

$$\eta_{i}(t_{k}, t_{k+1}) \coloneqq \int_{t_{k}}^{t_{k+1}} v_{i}^{2}(t) dt, \ 1 \le i, \ j \le M,$$
  

$$G_{I}(t_{k}, t_{k+1}) \coloneqq \operatorname{diag}(g_{11}(t_{k}, t_{k+1}), \cdots, g_{MM}(t_{k}, t_{k+1})),$$
  

$$G(t_{k}, t_{k+1}) \coloneqq \begin{cases} 0 & \text{if } i = j \\ g_{ij}(t_{k}, t_{k+1}) & \text{if } i \ne j \end{cases},$$
  

$$\eta(t_{k}, t_{k+1}) \coloneqq (\eta_{1}(t_{k}, t_{k+1}), \cdots, \eta_{M}(t_{k}, t_{k+1}))^{\mathrm{T}},$$
  

$$p(t_{k+1}) \coloneqq (p_{1}(t_{k+1}), \cdots, p_{M}(t_{k+1}))^{\mathrm{T}},$$
  

$$\Gamma \coloneqq \operatorname{diag}(\varepsilon_{1}, \cdots, \varepsilon_{M}),$$
  
(15)

and diag(·) denotes a diagonal matrix with its argument as diagonal entries. The optimization in (14) is a linear programming problem in  $M \times 1$  vector of unknowns  $p(t_{k+1})$ . Here  $[t_k, t_{k+1}]$  is a time interval such that the channel model does not change significantly, *i.e.*,  $[t_k, t_{k+1}]$  should be smaller than the coherence time of the channel. Throughout this section, we assume that the PC problem is feasible, *i.e.*, there exists a power vector  $p(t_k)$  that satisfies the inequality in (14) for all  $[t_k, t_{k+1}]$  in [0, T].

In the next section, a numerical example is presented to determine the performance of the proposed PCA under the estimated wireless channel models.

#### 4. Numerical Results

In this section, two numerical examples are presented. In Example 1, the EM algorithm combined with Kalman filtering is performed to estimate the channel parameters as well as inphase and quadrature components from received signal measurements. In Example 2, the performance of the proposed PCA based on the estimated channel models in Example 1 is determined and compared with fixed transmitted powers.

#### 4.1. Example 1: Wireless Channel Estimation

In this numerical example, a  $4^{th}$  order channel model as described in (10) and (11) is considered. Therefore, the system parameters  $\theta_t = \{A_t, B_t, C_t, D_t\}$  can be represented as

$$\boldsymbol{A}_{t} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ a_{1} & a_{2} & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & a_{3} & a_{4} \end{bmatrix}, \quad \boldsymbol{B}_{t} = \begin{bmatrix} b_{1} & \delta_{12} & \delta_{13} & \delta_{14} \\ b_{2} & \delta_{22} & \delta_{23} & \delta_{24} \\ \delta_{31} & \delta_{32} & b_{3} & \delta_{34} \\ \delta_{41} & \delta_{42} & b_{4} & \delta_{44} \end{bmatrix},$$
(16)  
$$\boldsymbol{C}_{t} = \begin{bmatrix} \cos(\omega_{c}t) & 0 & -\sin(\omega_{c}t) & 0 \end{bmatrix}, \quad \boldsymbol{D}_{t} = \begin{bmatrix} d_{1} & d_{2} \end{bmatrix}$$

Experimental data for a cellular network is provided by the Canadian Communication Research Center (CRC) and include measurement samples for the inphase and quadrature components and received signal strength.

As previously mentioned, the estimation of a flat fading wireless channel from received signal measurement data is considered. In particular, the estimation includes the channel parameters, inphase and quadrature components, and the received signal, which are then compared to the ones obtained from the provided measurement data. It is also assumed that the received signal measurement data are corrupted by white Gaussian noise sequences.

**Figure 1** shows the measured and estimated inphase and quadrature components as well as the received signal using the EM algorithm together with the Kalman filter for 400 sampled data taken from the measurements of one channel chosen at random. At a certain time instant, the system parameters are estimated as

$$\hat{\boldsymbol{A}} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -0.0756 & -0.0474 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & -0.6638 & 0.0717 \end{bmatrix},$$

$$\hat{\boldsymbol{B}}^{2} = \begin{bmatrix} 0.0484 & -0.0029 & -0.0453 & 4.0686 \times 10^{-4} \\ -0.0029 & 0.0462 & 0.0013 & -0.0438 \\ -0.0453 & 0.0013 & 0.0573 & 0.0047 \\ 4.0686 \times 10^{-4} & -0.0438 & 0.0047 & 0.0564 \end{bmatrix},$$

$$\hat{\boldsymbol{C}} = \begin{bmatrix} \cos(\omega_{c}t) & 0 & -\sin(\omega_{c}t) & 0 \end{bmatrix}, \quad \hat{\boldsymbol{D}}^{2} = \begin{bmatrix} 0.0119 \end{bmatrix}.$$
(17)

From **Figure 1**, it can be observed that the inphase and quadrature components of the wireless fading channel as well as the received signal have been estimated with very high accuracy. It can also be noticed that the estimation error decreases as the number of samples increases; this is because the algorithm is recursive and the channel parameters converge to the actual values as more samples are being estimated. **Figure 2** shows the received signal estimates root mean square error (RMSE) for 100 runs. It can be noticed that it takes just few iterations (less than 15) for the filter to converge, and the steady state performance of the proposed channel estimation algorithm is excellent. Since we consider  $4^{th}$  order channel model, the computational cost of the proposed estimation algorithm is moderate and can be implemented in real time. Moreover, the filters of the expectation step are recursive and decoupled and hence are easy to implement in parallel on a multi-processor system [17].



**Figure 1.** The measured and estimated inphase and quadrature components, and received signal for the  $4^{th}$  order channel model in Example 1, using the EM algorithm combined with the Kalman filter.



Figure 2. Received signal estimates RMSE for 100 runs using the EM algorithm combined with the Kalman filter.

#### 4.2. Example 2: Optimal Power Control

In this numerical example, the received signal measurement data for 24 users are collected experimentally. They represent flat Rayleigh fading environment where the signal envelope at the receivers exhibit Rayleigh distributed density. The channel model parameters as well as the inphase and quadrature components for all users are estimated online from the measurement data using the EM algorithm together with the Kalman filter as illustrated in Example 1. The PCA described in (14) is performed using the estimated channel parameters and states. The outage probability (OP) is used as a performance measure for the PCA. A link with a received SIR,  $R_i$ , less than or equal to a target SIR,  $\varepsilon_i$ , is considered a communication failure. The OP,  $O(\varepsilon_i)$ , is expressed as  $O(\varepsilon_i) = \text{Prob} \{R_i \le \varepsilon_i\}$ , where  $R_i$  is the received SIR at receiver i.

It is assumed that the targets SIR,  $\varepsilon_i$  for all users are the same, and varied from 5 dB to 25 dB with step 5 dB. For each value of  $\varepsilon_i$  the OP is computed every 15 millisecond, *i.e.*,  $[t_k, t_{k+1}] = 15$  millisecond. The simulation is performed for 4.5 seconds, *i.e.*, [0,T] = 4.5 seconds. The OP is computed using Monte-Carlo simulations. The performance of the proposed PCA is compared with the one of constant transmitted powers (CTP).

The OP for both the CTP and the proposed PCA based on PPCS are demonstrated in Figure 3(a) and Figure 3(b), respectively. Figure 3 shows how the OP changes with respect to target SIR and time. As the target SIR increases the OP increases. This is obvious since we expect more users to fail. The OP also changes as a function of time, since users move in different directions and velocities while gathering the measurements.



Figure 3. The outage probability for the dynamical flat Rayleigh wireless network in Example 2. (a) Using CTP; (b) Using PC based on PPCS.



Figure 4. Average outage probability of the PC case based on PPCS and the CTP case in Example 2. Performance comparison.

The average OP versus target SIR for both cases over the whole simulation time (4.5 seconds) is demonstrated in **Figure 4**, which shows that the performance of the proposed PCA based on PPCS is on average much better than that of the CTP. For example, at 10 dB target SIR, the OP is reduced from 0.51 for the CTP algorithm to 0.37 for the PCA; this represents an improvement of over 27%.

# **5.** Conclusion

This paper describes a general scheme for extracting mathematical wireless channel models from noisy received signal measurements, and performing power control based on the estimated channel parameters. The channel models are represented in stochastic state-space form. The proposed estimation algorithm consists of filtering based on the Kalman filter to remove noise from data, and identification based on the EM algorithm to determine the parameters of the model which best describe the measurements. Numerical results indicate that the measured data can be regenerated through a simple 4<sup>th</sup> order discrete-time stochastic state-space model. Moreover, a stochastic PCA based on the estimated parameters and channel states is investigated. Numerical results indicate that there is potentially large gain to be achieved by using the proposed PCA, which can be used as long as the channel model does not change significantly; that is  $[t_k, t_{k+1}]$  is a subset of the coherence time of the channel.

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