

Exact Solutions of a Power Law Fluid Model in Posttreatment Analysis of Wire Coating with Linearly Varying Boundary Temperature

Rehan Ali Shah^{1*}, Saeed Islam², Abdul Majeed Siddiqui³, Tahira Haroon⁴

¹Department of Basic Sciences and Islamiat, University of Engineering and Technology, Peshawar, Pakistan

²Department of Mathematics, Abdul Wali Khan University, Mardan, Pakistan

³Department of Mathematics, Pennsylvania State University, York Campus, York, USA

⁴Department of Mathematics, COMSATS Institute of Information Technology, Islamabad, Pakistan

Email: *mmrehan79@yahoo.com

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ABSTRACT

In this paper, analysis of post-treatment of wire coating is presented. Coating material satisfies power law fluid model. Exact solutions for the velocity field, volume flow rate and average velocity are obtained. Moreover, the heat transfer results are presented for different cases of linearly varying on the boundaries. The variations of velocity, volume flow rate, radius of coated wire, shear rate and the force on the total wire are presented graphically and discussed.

Keywords: Exact Solution; Wire Coating; Power Law Fluid Model; Linearly Varying Temperature at Boundaries

1. Introduction

The wire coating process is basically an extrusion operation in which either the molten polymer, in the form of tubing, is extruded continuously over axially moving wire, or the wire is pulled through the extruded molten polymer. Polymer extrudate is an important industrial process used for coating a wire for primary insulation of conducting wires with molten polymers for mechanical strength and environmental protection purposes. Wire coating have many application in the field of chemical and industrial engineering. Many authors have studied the wire coating phenomena.

The basic concept of modeling the wire coating for viscous fluid is given in the books by Denn and middleman [1,2]. McKelvey [3] and Paton *et al.* [4] have analyzed the flow of Newtonian and power law fluid model in wire coating process, and obtained expressions for the flow rate, shear rate and the velocity distribution along the radial direction. Gagley and storey [5] provided numerical simulations for a Newtonian fluid in the form of dimensionless parameters characterizing the wire speed, die dimensions, radial position, shear rate, and melt viscosity. Akhter and Hashmi [6,7] have developed the mathematical model for wire coating using power law model and investigated the effect of the change in viscosity. A.M Siddiqui, T.Haroon and H. Khan [8] studied

the wire coating extrusion in a pressure-type die in flow of third grade fluid. Fenner and Williams [9] carried out an analysis of the flow in the tapering section of a pressure type die. They obtained the numerical solutions for the pressure and velocity profiles in the die. M. Sajjid *et al.* [10] studied the wire coating with Oldroyd 8-constant fluid and gave the solution for velocity field in the series form.

The coated wire after leaving the die is effected by the quality of the material used in coating process, the wire drawing velocity and the temperature. There are very few disclosures presenting theoretical analysis of flow in the posttreatment process subsequent to the die.

The analysis of the drag flow of the coated polymer outside pressure die was carried out by Kasajima and Katsuhiko Ito [11]. They derived the expression for velocity and temperature field. Moreover, they found the volume flow rate, average velocity and discussed some cases for constant velocity and constant temperature on the boundaries. We work under the same geometry as by Masayuki Kasajima and Katsuhiko with the assumption that the polymer obeys the power law fluid model and derived the velocity field, volume flow rate, thickness of coated wire, average velocity, the force on the total wire surface and linearly varying temperature distribution in the direction of flow. As the posttreatment problem is mainly concern with temperature for cooling the coated wire therefore due to its importance and realization of

*Corresponding author.

physical problem we discussed some cases of linearly varying temperature for analysis of temperature distribution as follows:

- Temperature of the wire is constant while it is varying linearly on the surface of the coated wire.
- Temperature of the wire varying linearly while it is constant on the surface of the coated wire.
- Temperature of the wire and the surface of coated wire are varying linearly at the same temperature gradient.

The non-linear differential equations governing the model are made dimensionless and solved for velocity and temperature distribution. Theoretical analysis on the drag flow mechanism of polymer extrudate, in the heat treatment process, is presented.

2. Basic Governing Equations

The basic equations governing the flow of an incompressible fluid with thermal effects are:

$$\nabla \cdot \underline{u} = 0, \tag{1}$$

$$\rho \frac{D\underline{u}}{Dt} = \text{div} \underline{T} + \rho \underline{f}, \tag{2}$$

$$\rho c_p \frac{D\Theta}{Dt} = k \nabla^2 \Theta + \underline{S} \cdot \underline{L} \tag{3}$$

where \underline{u} is the velocity vector, ρ is the constant density, \underline{f} is the body force, \underline{T} is the Cauchy stress tensor, D/Dt denote the material derivative, Θ is the fluid temperature, k is the thermal conductivity, c_p is the specific heat and \underline{L} is the gradient of velocity vector \underline{u} .

The Cauchy stress tensor \underline{T} is defined as

$$\underline{T} = -p \underline{I} + \underline{S}, \tag{4}$$

In which p is the pressure, \underline{I} is the identity tensor and \underline{S} is the extra stress tensor. For power law fluid model \underline{S} is defined as

$$\underline{S} = \eta \underline{A}_1, \tag{5}$$

where

$$\eta = \eta_0 \left[\frac{\Delta : \Delta}{2} \right]^{\frac{n-1}{2}}; \Delta = 0.5 (\nabla \underline{u} + (\nabla \underline{u})^T) \tag{6}$$

where $(\Delta : \Delta)$ is the scalar invariant, η is the coefficient of viscosity of the fluid, T in superscript denotes the transpose of the matrix $\nabla \underline{u}$, η_0 is the consistency index and n is the power law index. The index n is non-dimensional and the dimension of η_0 depends on the value of n . The parameter n subdivide fluids into pseudoplastic fluids ($n < 1$), dilatant fluids ($n > 1$) and Newtonian fluid For $n = 1$. Therefore the deviation of n from unity indicates the degree of deviation from Newtonian behavior [12].

3. Formulation and Solution of the Problem

In wire coating process, the quality of the polymer and wire drawing velocity are important within the die, after leaving the die temperature and the shape of the transverse sectioning is also very important. Consider the flow of the polymer extrudate given in **Figure 1**, denoted by the solid line. To analyze the flow behavior of a polymer used in wire coating, it is convenient to divide the flow transversely into many short sections as shown by broken lines in **Figure 1** with the assumption that each section has almost the same shape, we analyze only one section because each section can be assumed to be approximately of the shape shown in **Figure 2** and readily analyzable.

Consider the wire of radius R_1 is dragged in the z direction with velocity V_1 through an incompressible polymer satisfying power law fluid model (II) and the gas (III) surrounding the polymer (II) is flowing with a velocity V_2 in the z direction.

Consider the cylindrical coordinates (r, θ, z) such that r is perpendicular to the direction of flow.

Assume that:

1) The flow is incompressible due to the high viscosity of the polymer.

2) Polymer II holds the power law fluid model for shear rate.

3) In **Figure 2** the wire I, the polymer II and gas III are in contact with each other and consider no slippage occurs along the contacting surfaces of the wire, polymer, and the gas.

Also assume that the flow is steady, laminar, unidirectional and axisymmetric:

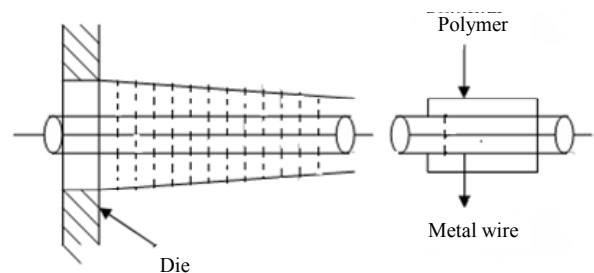


Figure 1. Schematic profile of polymer extrudate in wire coating.

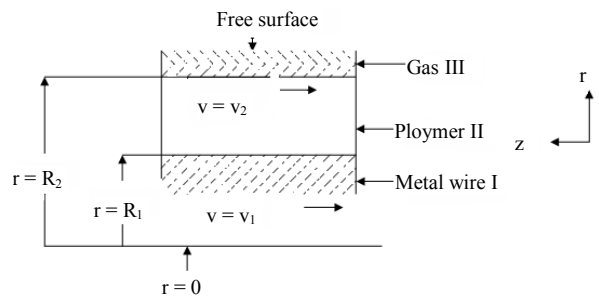


Figure 2. Drag flow in wire coating.

We seek the velocity field of the form

$$\underline{u} = [0, 0, w(r)], \underline{S} = \underline{S}(r). \quad (7)$$

then the boundary conditions for the problem become

$$\begin{aligned} w &= V_1 \text{ at } r = R_1, \\ w &= V_2 \text{ at } r = R_2. \end{aligned} \quad (8)$$

In the flow through the tube, the scalar invariant is:

$$(\Delta : \Delta) = 2 \left(\frac{\partial w}{\partial r} \right)^2 \quad (9)$$

Substituting Equation (9) into Equation (6) one obtains:

$$\eta = \eta_0 \left[\frac{\partial w}{\partial r} \right]^{n-1}. \quad (10)$$

Using the velocity field (7) the continuity Equation (1) is satisfied identically, and the non zero components of Equation (5) with the help of Equation (10) become:

$$S_{rz} = \eta_0 \left(\frac{dw}{dr} \right)^n \quad (11)$$

Substituting the velocity field and Equation (11) in the momentum Equation (2) neglecting the body force take the form:

$$\frac{\partial p}{\partial r} = 0 \quad (12)$$

$$\frac{\partial p}{\partial \theta} = 0 \quad (13)$$

$$\frac{\partial p}{\partial z} = \frac{d}{dr} \left(r \eta_0 \left| \frac{dw}{dr} \right|^n \right) \quad (14)$$

If the z -axis is chosen correspond to the direction of increasing pressure, polymer (II) moves in the minus direction of the z -axis and the shear rate $\gamma^0 = \frac{dw}{dr}$, becomes plus for all value of r . Therefore, the absolute value of Equation (5) can be discarded.

Equation (14) represents the flow due to pressure gradient. After leaving the die, there is only drag flow. Hence, we consider

$$\frac{d}{dr} \left(r \eta_0 \left(\frac{dw}{dr} \right)^n \right) = 0 \quad (15)$$

and the energy Equation (3) becomes:

$$\rho c_p \frac{D\Theta}{Dt} = k \nabla^2 \Theta + \eta_0 \left(\frac{dw}{dr} \right)^{n+1}. \quad (16)$$

For linearly varying temperature, consider

$$\Theta(r, z) = Az + g(r), \quad (17)$$

where A is the temperature gradient.

Substituting Equation (17) into Equation (16), we have

$$\rho c_p w A = k \left(\frac{d^2}{dr^2} + \frac{1}{r} \frac{d}{dr} \right) g + \eta_0 \left(\frac{dw}{dr} \right)^{n+1}. \quad (18)$$

Now first the velocity field is determined from Equation (15) and then the temperature distribution can be easily calculated using Equation (18).

The average velocity is

$$w_{ave} = \frac{2}{R_1^2 - R_2^2} \int_{R_1}^{R_2} r w(r) dr \quad (19)$$

At some control surface downstream, the volume flow rate of coating is

$$Q = \pi V_1 (R_c^2 - R_1^2) \quad (20)$$

where R_c is the radius of the coated wire.

The volume flow rate of the polymer is

$$Q = \int_{R_1}^{R_2} 2\pi r w(r) dr \quad (21)$$

The thickness of the coated wire can be obtained from Equations (16) and (17) as

$$R_c = \left[R_1^2 + \frac{2}{V_1} \int_{R_1}^{R_2} r w(r) dr \right]^{\frac{1}{2}}. \quad (22)$$

The force on the wire is computed by determining the shear stress at the wire surface. This is given by

$$S_{rz} \Big|_{r=R_1} = \eta_0 \left(\frac{dw}{dr} \right)^n \Big|_{r=R_1}. \quad (23)$$

The force on the total wire surface is

$$F_w = 2\pi R_1 L S_{rz} \Big|_{r=R_1} \quad (24)$$

Introduce the dimensionless parameters

$$r^* = \frac{r}{R_1}, w^* = \frac{w}{V_1}, G = \frac{g}{\left(\eta_0 V_1^{n+1} / k R_1^{n-1} \right)}, \quad (25)$$

$$S = \frac{\rho c_p A R_1^{n+1}}{\eta_0 V_1^n}, \frac{R_2}{R_1} = \delta > 1, \frac{V_2}{V_1} = U$$

Equations (8), (15) and (18)-(25) after dropping the “*” take the following form:

$$\frac{d}{dr} \left(r \left(\frac{dw}{dr} \right)^n \right) = 0, \quad (26)$$

$$w(1) = 1, \text{ and } w(\delta) = U, \quad (27)$$

$$r \frac{d^2 G}{dr^2} + \frac{dG}{dr} + r \left(\frac{dw}{dr} \right)^{n+1} = S r w, \quad (28)$$

$$\hat{w}_{ave} = \frac{w_{ave}(R_2^2 - R_1^2)}{2R_1^2V_1} = \int_1^\delta rw(r)dr, \tag{29}$$

$$\hat{Q} = \frac{Q}{2\pi R_1^2V_1} = \int_1^\delta rw(r)dr, \tag{30}$$

$$\hat{R}_c = \frac{R_c}{R_1} = \left[1 + 2 \int_1^\delta rw(r)dr \right]^{\frac{1}{2}}, \tag{31}$$

$$S_{rz}|_{r=1} = \frac{S_{rz}R_1^n}{\eta_0V_1^n} \Big|_{r=1} = \left(\frac{dw}{dr} \right)^n \Big|_{r=1}, \tag{32}$$

$$\hat{F}_w = \frac{F_w R_1^{n-1}}{2\pi\mu LV_1^n} = \left(\frac{dw}{dr} \right)^n \Big|_{r=1}, \tag{33}$$

The solution to (26) corresponding to the boundary conditions (27) are:

$$w(r) = (U-1) \left(\frac{r^{\frac{n-1}{n}} - 1}{\delta^{\frac{n-1}{n}} - 1} \right) + 1, \text{ for } n \neq 1 \tag{34}$$

For $n = 1$, the velocity field can be obtain from Equation (26).

$$w^*(r) = (U-1) \frac{\ln r}{\ln \delta} + 1, \tag{35}$$

where the superscript “*” means the case of $n = 1$.

For $n \neq 1$ the average velocity is obtained from Equations (29) and (34):

$$\hat{w}_{ave} = \frac{1}{2}(\delta^2 - 1) \left(1 + (U-1) \left(\delta^{\frac{n-1}{n}} - 1 \right)^{-1} \cdot \left(\frac{2n}{(3n-1)(\delta^2 - 1)} \left(\delta^{\frac{n-1}{n}} - 1 \right) - 1 \right) \right) \tag{36}$$

For $n = 1$ the average velocity is obtained from Equations (29) and (35):

$$\hat{w}_{ave}^* = \frac{1}{2}(\delta^2 - 1) \left(1 + (U-1) \left(\left(1 - \frac{1}{\delta^2} \right)^{-1} + \frac{1}{2 \ln \delta} \right) \right) \tag{37}$$

For $n \neq 1$ the shear rate can be obtained from Equation (34):

$$\gamma = \frac{dw}{dr} = \left(\frac{n-1}{n} \right) \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) r^{-\frac{1}{n}} \tag{38}$$

For $n = 1$ the shear rate is obtained from Equation (35) as:

$$\gamma^* = \frac{dw}{dr} = \left(\frac{n-1}{n} \right) \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) r^{-\frac{1}{n}} \tag{39}$$

The thickness of the coated wire for $n \neq 1$ is obtained from Equations (31) and (34):

$$\hat{R}_c = \left[1 + 2 \left(\frac{1}{2}(\delta^2 - 1) \left(1 + (U-1) \left(\delta^{\frac{n-1}{n}} - 1 \right)^{-1} \cdot \frac{2n}{(3n-1)(\delta^2 - 1)} \left(\delta^{\frac{n-1}{n}} - 1 \right) - 1 \right) \right) \right]^{\frac{1}{2}}, \tag{40}$$

Similarly, the thickness of the coated wire for $n = 1$ is obtained from Equations (31) and (35):

$$\hat{R}_c^* = \left[1 + 2 \left(\frac{1}{2}(\delta^2 - 1) \left(1 + (U-1) \cdot \left(\left(1 - \frac{1}{\delta^2} \right)^{-1} + \frac{1}{2 \ln \delta} \right) \right) \right) \right]^{\frac{1}{2}}. \tag{41}$$

In a similar manner, the force on the total wire surface for power law index n is not equal to 1 is

$$\hat{F}_w = \left(\frac{n-1}{n} \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) \right)^n, \tag{42}$$

and the force on the total wire surface for the case when the power law index n is equal to 1 is given by

$$\hat{F}_w^* = \left(\frac{U-1}{\ln \delta} \right)^n. \tag{43}$$

In dimensionless form the volume flow rate for n is or is not equal to 1 are the same as the average velocity in Equations (37) and (36) respectively.

In case of transformation of our problem to original parameters the results of velocity field, volume flow rate, average velocity and rate of shear stress are transformed to the results of Kasajima and Katsuhiko Ito [11] for n is or is not equal to 1.

Figure 3 illustrates the well known effect of n on the velocity profile; *i.e.* for pseudoplastic the profile becomes progressively flatter; and for dilatant fluids the profile becomes progressively linear.

Keeping the importance of temperature in our problem we are seeking the temperature distribution with different cases.

Case 1. Temperature of the wire is constant while it is varying linearly on the surface of the coated wire:

Here, consider the temperature of the wire is Θ_0 , and it is Az on the surface of the coated wire, so from Equation (17) we have

$$\begin{aligned} \Theta(1, z) &= Az + g(1) = \Theta_0, \\ \Theta(\delta, z) &= Az + g(\delta) = Az \end{aligned} \tag{44}$$

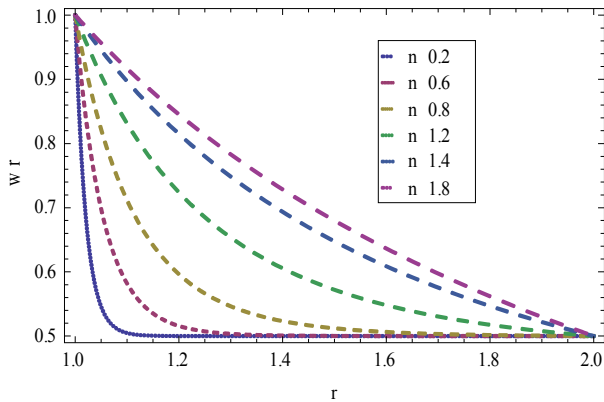


Figure 3. The velocity profile for different index n taking $\delta = 2, U = 0.5$.

After transformation we obtain

$$G(1) = H, G(\delta) = 0 \tag{45}$$

where

$$H = \frac{\Theta_0 - Az}{(\eta_0 V_1^{n+1} / k R_1^{n-1})}$$

For $n \neq 1$ the velocity field from Equation (23) is substitute in Equation (22) and solved corresponding to the boundary conditions (45), we obtain the expression for temperature distribution in form of G as:

$$\begin{aligned} G(r) = & \frac{S}{2} \left(1 - \frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) \left(r^2 - 1 - \frac{\ln r}{\ln \delta} (\delta^2 - 1) \right) \\ & + S \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) \left(\frac{n}{3n-1} \right)^2 \left(r^{\frac{3n-1}{n}} - 1 - \frac{\ln r}{\ln \delta} \left(\delta^{\frac{3n-1}{n}} - 1 \right) \right) \\ & - \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right)^{n+1} \left(\frac{n}{n-1} \right)^2 \left(r^{\frac{n-1}{n}} - 1 - \frac{\ln r}{\ln \delta} \left(\delta^{\frac{n-1}{n}} - 1 \right) \right) \\ & + H \left(1 - \frac{\ln r}{\ln \delta} \right) \end{aligned} \tag{46}$$

For $n = 1$ the velocity field from Equation (24) is substitute in Equation (22) and solved corresponding to the boundary conditions (45), the explicit function for G is obtained for temperature field as:

$$\begin{aligned} G^*(r) = & \frac{S}{4} \left(1 - \frac{U-1}{\ln \delta} \right) \left(r^2 - 1 - \frac{\ln r}{\ln \delta} (\delta^2 - 1) \right) \\ & + \frac{S}{4} \left(\frac{U-1}{\ln \delta} \right) (r^2 - \delta^2) \ln r + H \left(1 - \frac{\ln r}{\ln \delta} \right) \end{aligned} \tag{47}$$

Case 2. Temperature of the wire varying linearly while it is constant on the surface of the coated wire:

In this case, consider the temperature at the surface of wire is Θ_1 , and Az on the surface of continuum.

Under the above consideration Equation (17) gives

$$\begin{aligned} \Theta(1, z) &= Az + g(1) = Az, \\ \Theta(\delta, z) &= Az + g(\delta) = \Theta_1 \end{aligned} \tag{48}$$

After transformation of the boundary conditions (48) for the non-dimensional temperature distribution G takes the following form

$$G(1) = 0, G(\delta) = J \tag{49}$$

where

$$J = \frac{\Theta_1 - Az}{(\eta_0 V_1^{n+1} / k R_1^{n-1})}$$

For $n \neq 1$ the velocity field from Equation (22) is substitute in Equation (22) and solved corresponding to the boundary conditions (49), we have

$$\begin{aligned} G(r) = & \frac{S}{2} \left(1 - \frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) \left(r^2 - 1 - \frac{\ln r}{\ln \delta} (\delta^2 - 1) \right) \\ & + S \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) \left(\frac{n}{3n-1} \right)^2 \left(r^{\frac{3n-1}{n}} - 1 - \frac{\ln r}{\ln \delta} \left(\delta^{\frac{3n-1}{n}} - 1 \right) \right) \\ & - \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right)^{n+1} \left(\frac{n}{n-1} \right)^2 \left(r^{\frac{n-1}{n}} - 1 - \frac{\ln r}{\ln \delta} \left(\delta^{\frac{n-1}{n}} - 1 \right) \right) \\ & + J \frac{\ln r}{\ln \delta} \end{aligned} \tag{50}$$

For $n = 1$ the velocity field from Equation (24) is substitute in Equation (22) and solved corresponding to the boundary conditions (49), we have

$$\begin{aligned} G^*(r) = & \frac{S}{4} \left(1 - \frac{U-1}{\ln \delta} \right) \left(r^2 - 1 - \frac{\ln r}{\ln \delta} (\delta^2 - 1) \right) \\ & + \frac{S}{4} \left(\frac{U-1}{\ln \delta} \right) (r^2 - \delta^2) \ln r + J \frac{\ln r}{\ln \delta} \end{aligned} \tag{51}$$

Case 3. Temperature of the wire and the surface of coated wire are varying linearly at the same temperature gradient:

Consider the temperatures at the surface of wire and on the surface of continuum are Az .

From Equation (17), we have

$$\begin{aligned} \Theta(1, z) &= Az + g(1) = Az, \\ \Theta(\delta, z) &= Az + g(r) = Az \end{aligned} \tag{52}$$

After simplification according to demand of our problem, we obtain

$$G(1) = 0, G(\delta) = 0 \tag{53}$$

For $n \neq 1$ the velocity field from Equation (22) is substitute in Equation (22) and solved corresponding to

the boundary conditions (53), we have

$$\begin{aligned}
 G(r) = & \frac{S}{2} \left(1 - \frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) \left(r^2 - 1 - \frac{\ln r}{\ln \delta} (\delta^2 - 1) \right) \\
 & + S \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right) \left(\frac{n}{3n-1} \right) \\
 & \cdot \left(r^{\frac{3n-1}{n}} - 1 - \frac{\ln r}{\ln \delta} \left(\frac{3n-1}{\delta^{\frac{n-1}{n}} - 1} \right) \right) \\
 & - \left(\frac{U-1}{\delta^{\frac{n-1}{n}} - 1} \right)^{n+1} \left(\frac{n}{n-1} \right) \\
 & \cdot \left(r^{\frac{n-1}{n}} - 1 - \frac{\ln r}{\ln \delta} \left(\frac{n-1}{\delta^{\frac{n-1}{n}} - 1} \right) \right)
 \end{aligned} \tag{54}$$

For $n=1$ the velocity field from Equation (24) is substitute in Equation (22) and solved corresponding to the boundary conditions (53), after simplification we have

$$\begin{aligned}
 G^*(r) = & \frac{S}{4} \left(1 - \frac{U-1}{\ln \delta} \right) \left(r^2 - 1 - \frac{\ln r}{\ln \delta} (\delta^2 - 1) \right) \\
 & + \frac{S}{4} \left(\frac{U-1}{\ln \delta} \right) (r^2 - \delta^2) \ln r
 \end{aligned} \tag{55}$$

4. Conclusion

The posttreatment of wire coating analysis are carried out for power law model fluid. The velocity field, volume flow rate, average velocity, force on the total wire, thickness of coated wire and shear rate have been derived for n is or is not equal to 1. In posttreatment problem the temperature is extremely important for cooling the wire. Therefore, regarding the importance of temperature we have discussed three cases for linearly varying temperature. Expression for temperature distributions in non-dimensional form are obtained for $n=1$ and $n \neq 1$. The interpretations of the results are carried out under the influence of non-dimensional parameters. It is concluded that the velocity decreases as the power law index n increases. In addition, the non-Newtonian parameter ε decrease the fluid velocity. Also, it is concluded that the force on the coated wire increases as the velocity ratio increases and decreases while increases δ . It is observed that for $(n > 1)$ the thickness of coated wire increases. Moreover, with a linearly varying wall temperature along the direction of flow the highest temperature rise in the centre of the channel depends on the dimensionless number S . One can see the behavior of the physical quantities such as velocity function, non-dimensional function of temperature profile and the differential form of these functions from Figures 3-15.

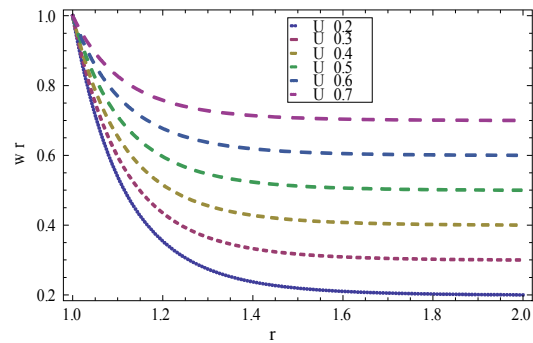


Figure 4. The velocity profile for different values of velocity ratio U taking index $n = 0.1$ and $\delta = 2$.

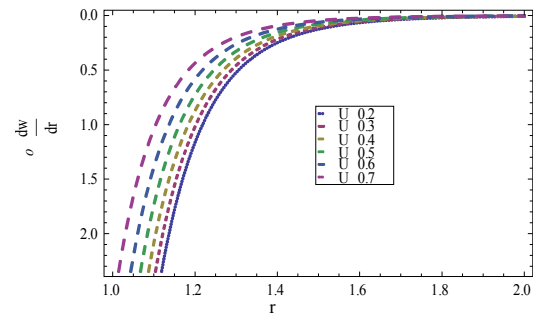


Figure 5. The shear rate for different values of velocity ratio U taking index $n = 0.1$ and $\delta = 2$.

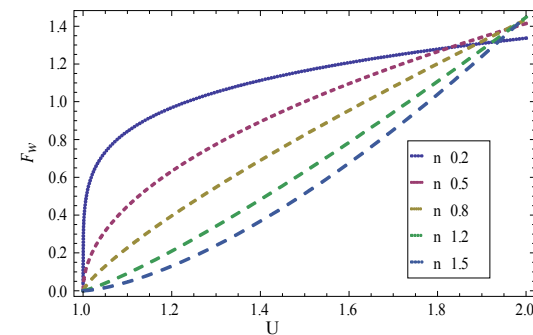


Figure 6. Force \hat{F}_w is plotted against U for different values of n by taking $\delta = 2$.

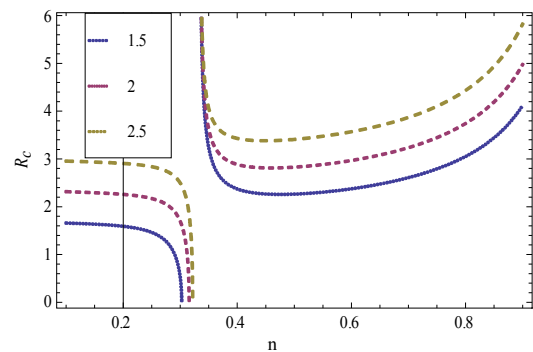


Figure 7. Radius of coated wire \hat{R}_c is plotted against n for different values of δ by taking $U = 1.2$.

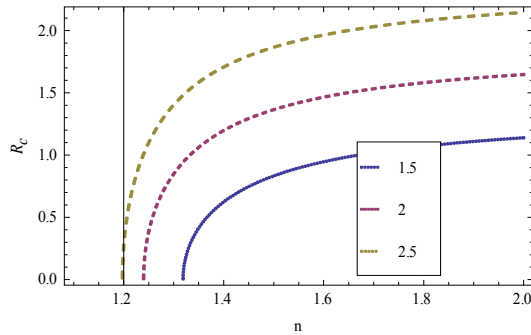


Figure 8. Radius of coated wire \hat{R}_c is plotted against n for different values of δ by taking $U = 1.2$.

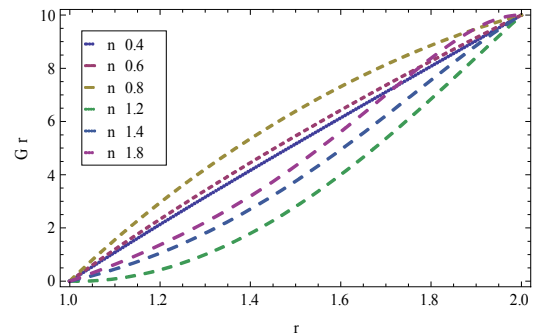


Figure 12. The non-dimensional function G for different values of n taking $J = 10, U = 0.6, S = 5$ and $\delta = 2$.

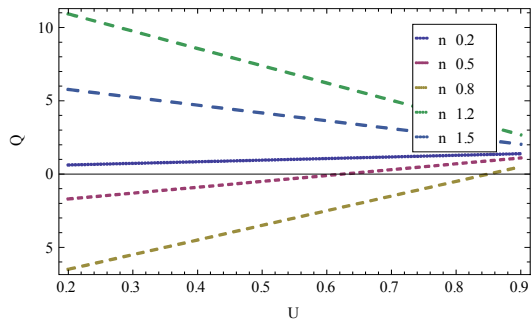


Figure 9. Volume flow rate is plotted against U for different values of power law index n by taking $\delta = 2$.

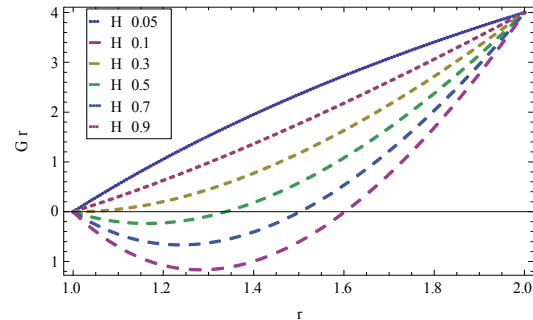


Figure 13. The non-dimensional function G for different values of H taking $J = 4, U = 0.6, S = 25, n = 0.5$ and $\delta = 2$.

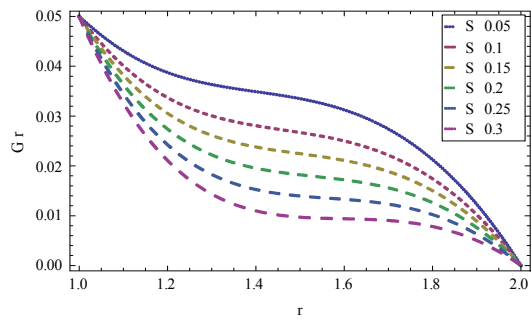


Figure 10. The non-dimensional function G for different values of non-dimensional parameter S taking $n = 0.5, u = 0.5, H = 0.05$ and $\delta = 2$.

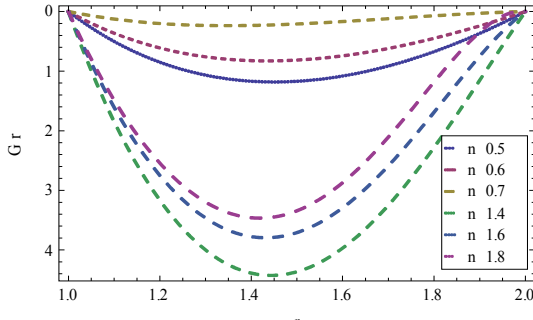


Figure 14. The non-dimensional function G for different values of n taking $J = 0.5, U = 0.6, S = 10$ and $\delta = 2$.

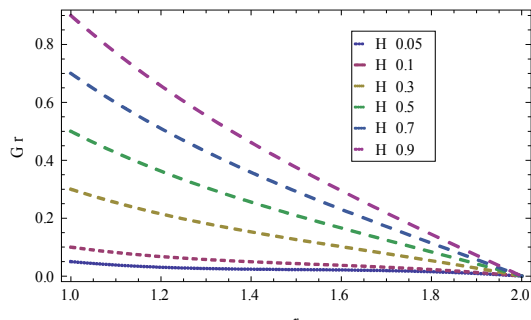


Figure 11. The non-dimensional function G for different values of H taking $n = 0.5, u = 0.5, H = 0.15$ and $\delta = 2$.

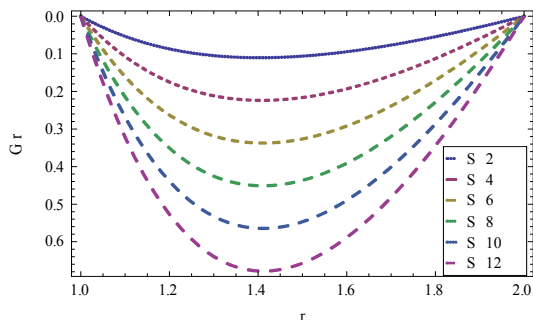


Figure 15. The non-dimensional function G for different values of non-dimensional parameter S taking $J = 2, U = 0.3, n = 0.4$ and $\delta = 2$.

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