

# Application of the Cross Wavelet Transform to Solar Activity and Major Earthquakes Occurred in Chile

Patricia Alejandra Larocca

Instituto de Geodesia y Geofísica Aplicadas, Facultad de Ingeniería, Universidad de Buenos Aires, Buenos Aires, Argentina

Email: patri.larocca@gmail.com

**How to cite this paper:** Larocca, P.A. (2016) Application of the Cross Wavelet Transform to Solar Activity and Major Earthquakes Occurred in Chile. *International Journal of Geosciences*, 7, 1310-1317. <http://dx.doi.org/10.4236/ijg.2016.711095>

**Received:** September 9, 2016

**Accepted:** November 5, 2016

**Published:** November 8, 2016

Copyright © 2016 by author and Scientific Research Publishing Inc.

This work is licensed under the Creative Commons Attribution International License (CC BY 4.0).

<http://creativecommons.org/licenses/by/4.0/>



Open Access

---

## Abstract

Historical earthquakes registered in Chile (from 1900 up to 2015) with epicenters located between 17°30'S and 56°0'S latitude and yearly mean total sunspot number have been considered in order to evaluate a significant linkage between them. The occurrence of strong earthquakes along Chile and the sunspots activity are analyzed to inspect possible influence of solar cycles on earthquakes. The cross wavelet transform and wavelet coherence analysis were applied for sequences of sunspots and earthquakes activity. An 8 - 12 years modulation of earthquakes activity has been identified.

## Keywords

Cross Wavelet Transform, Earthquakes Activity, Solar Activity, Sunspots Number, Periodicities

---

## 1. Introduction

Many terrestrial processes show trends and changes in the long-term: global temperature, geomagnetic activity and Earth's rotation. It is a challenge to find a relationship between them and also to identify possible extraterrestrial factors that may contribute to these changes in the long-term.

The major source of energy near the Earth is the Sun, therefore it is natural to think about a connection between different elements of solar activity and terrestrial processes.

The aim of this work is to find statistical relationships between the number of sunspots and earthquakes in Chile.

Earthquakes distribution on the earth's surface is not homogeneous; they generally

occur in areas with different tectonic boundaries. One example is the largest earthquake of magnitude  $M_s = 9.5$  which occurred in Valdivia on May 22, 1960 (the largest in the history of mankind), originated due to the sudden movement of the Nazca plate beneath the South American plate. The contact zone between the plates was located about 130 km from the coast to the west. Chile is one of the countries with the most seismic activity in the world. One destructive earthquake occurred every ten years in the last century [1].

In previously published work, seismic periodicities in different countries were analyzed as in [2] [3] [4].

Several authors have researched solar activity and its connection with seismic activity [5] [6] [7]. Reference [8] studied the relationship between solar activity and great earthquakes ( $M_s \geq 8$ ) in China. They observed an increase in the number of earthquakes in the years of maximum solar activity. References [9] and [10] proposed the existence of an interaction between the solar wind, particle radiation and earthquakes.

Reference [11] found relationships between increased solar events during the last half of the twentieth century and the intensification of earthquake events. Reference [12] linked the maximum frequency of earthquakes during periods of moderate and high solar activity.

Statistical studies related to solar activity were previously published by [13] and [14].

Reference [15] studied the transitions of solar dynamo and its link to rapid climate changes, presenting some of the solar-terrestrial variables as the causes of triggering seismic activity.

In this paper, surface seismic magnitude values ( $M_s$ ) for earthquakes in Chile and the yearly mean total sunspots number (SSN) were studied using:

- Periodograms obtained by fast Fourier transform;
- Cross Wavelet Transform and wavelet coherence analysis.

## 2. Data

The number of sunspots (SSN) is the index that measures the number and size of sunspots. Yearly mean total sunspot number is obtained by taking a simple arithmetic mean of the daily total sunspot number over all days of each year. The values were obtained by the World Data Center for the production, preservation and dissemination of the international sunspot number (WDC-SILSO, Royal Observatory of Belgium, Brussels) and are shown in **Figure 1(a)**.

The  $M_s$  magnitude is the surface wave magnitude of earthquakes. It is a measure of seismic activity. The annual seismic data were obtained through the *Servicio Sismológico* from the *Universidad de Chile* (<http://www.sismologia.cl/>). Annual averages of earthquakes with  $M_s \geq 7$  for the period 1900-2015 were considered, see **Figure 1(b)**.

## 3. Analysis of the Series

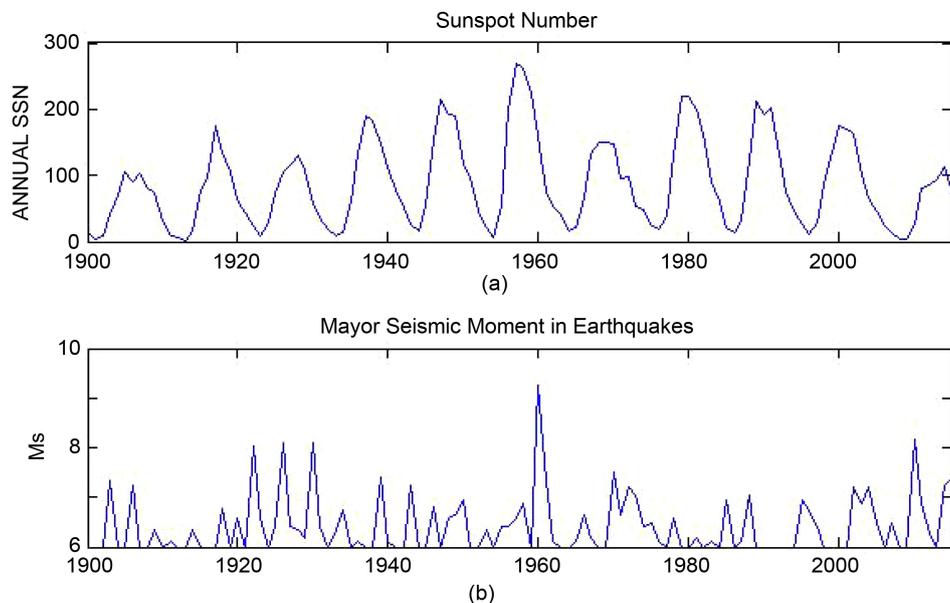
### 3.1. Sunspots Number and Surface Wave Magnitude of Earthquakes Periodograms Obtained by Fast Fourier Transform

To estimate the periodicities of  $M_s$  and SSN, power spectra were performed. In **Figure**

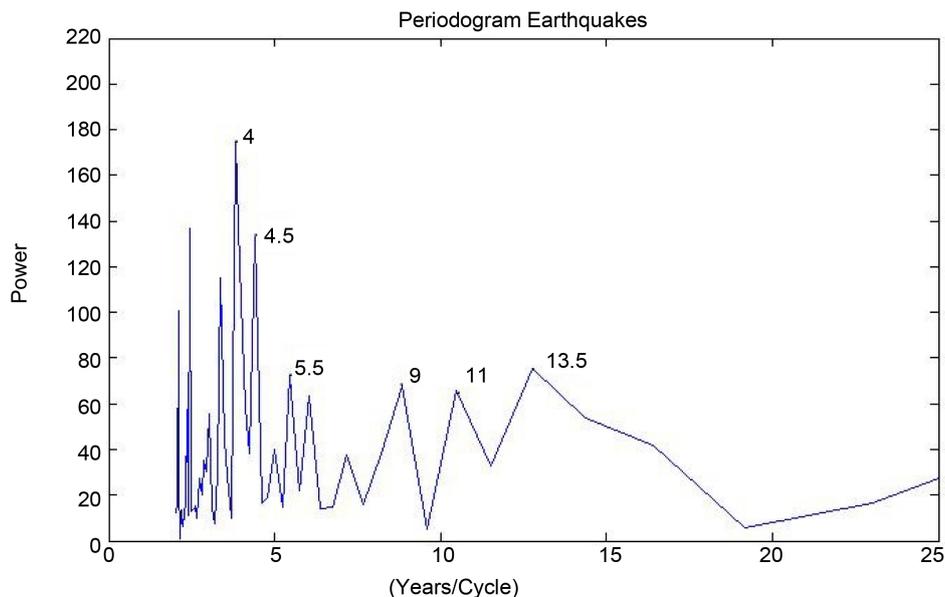
2, power spectrum of  $M_s$  series is presented in the terms of time. Predominant peaks around 4; 4.5; 5.5; 9; 11 and 13.5 are observed.

In **Table 1** periodicities obtained by different authors are shown.

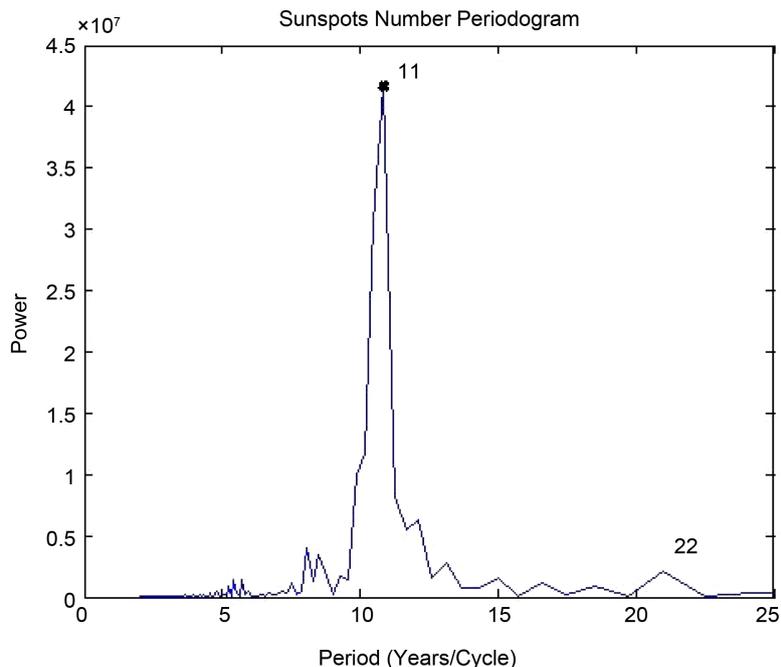
**Figure 3** shows the power spectrum for SSN series. Two picks are observed in 10.5 and 20 years. These picks correspond to the ones cited by Schawabe and Hale respectively. Periodicity of 11 years was observed for the first time by Heinrich Schwave (1789-1875) and periodicity of 22 years takes the name of George Ellery Hale (1868-



**Figure 1.** (a) Number of sunspots (annual average) from 1900-2015. (b) Mayor Seismic moment of earthquakes in Chile (annual average) from 1900-2015.



**Figure 2.** Periodogram for  $M_s$  for the period 1900-2015.



**Figure 3.** Periodogram corresponding to SSN for period 1900-2015 (the maximum corresponds to 11 years).

**Table 1.** Periodicities for  $M_s$  previously published.

	Other papers		
	Du Xinxing, 1997	Madhava Rao and Kaila, 1986	Liritzis and Tsapanos, 1992
Periodicities	7; 14; 22 and 42 years.	3 to 12 years.	3; 4.5; 6.5; 8; 9; 14 - 20 and 31 - 34 years.

1938) who discovered solar spots due to the action of the solar magnetic field limiting the sun radiation emission. In 1961, Harold Babcock and Horace Babcock observed that this magnetic field has two perpendicular components between them: the polar and toroidal that invert the polarity after each Schwave cycle, therefore a whole cycle corresponds to Hale cycle [15].

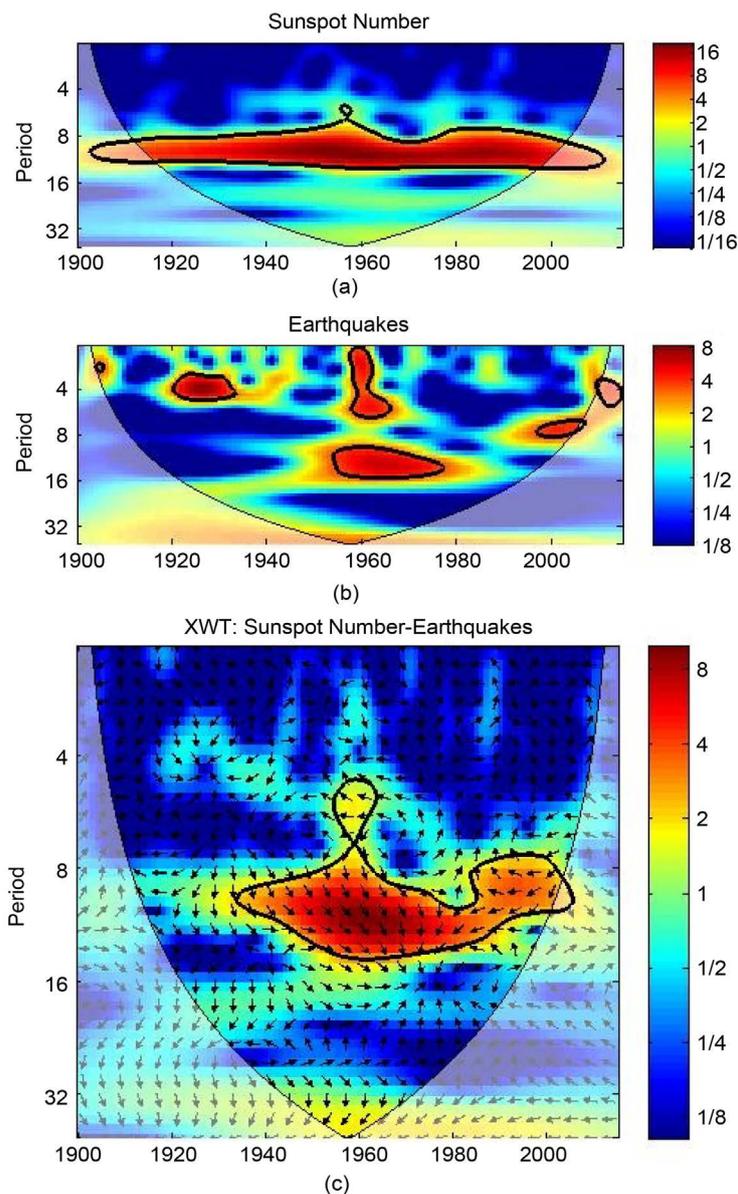
### 3.2. Wavelet Analysis of Sunspot Number and Surface Wave Magnitude of Earthquakes Considering Annual Maximum Values

The temporal correlation between annual averages  $M_S$  (energy release sequences of strong earthquakes in Chile) and SSN (Sunspots Number) were analyzed using the Continuous Wavelet Transform (CWT) as a band-pass filter. A wavelet is a function that is localized in time and frequency. Morlet wavelet (1) (with  $\omega_0 = 6$ ) was utilized because it provides a good balance between time and frequency localization:

$$\psi_0(\eta) = \pi^{-1/4} e^{i\eta\omega_0} e^{-\eta^2/2} \tag{1}$$

where  $\omega_0$  is dimensionless frequency and  $\eta$  is dimensionless time.

**Figure 4(a)** and **Figure 4(b)** show the periodic oscillation of the annual seismic moment of mayor earthquakes in Chile and the sunspot numbers. **Figure 4(a)** remarks the 11 yrs. periodicity of Sunspot Numbers along the complete period of time analyzed. **Figure 4(b)** shows an 11 years periodicity on 1995 to 1980, a small 8 - 11 yrs. periodicity between 1990-2000; 3 - 6 yrs. between 1925-1935 and 1955-1965 of MsSerie.



**Figure 4.** (a) The wavelet real part contour of annual sunspot numbers series. (b) The wavelet real part contour of seismic energy release series. (c) The thick black contour designates the 5% significance level against red noise and the cone of influence (COI) where edge effects might distort the picture is shown as lighter shade. The relative phase is shown as arrows (with in-phase pointing right, anti-phase pointing left and SSN leading Ms by 90° pointing straight down).

We examined the two time series together to find a link in some way. From two CWTs we constructed the Cross Wavelet Transform (XWT) which will expose their common power and relative phase in time-frequency space. We used the cross wavelet transform (XWT) for examining relationships in time frequency space between both time series. The theoretical distribution of cross wavelet transform of two time series is given in [16]. We used the corresponding software at <http://noc.ac.uk/using-science/crosswavelet-wavelet-coherence>. The result is showed in **Figure 4(c)**.

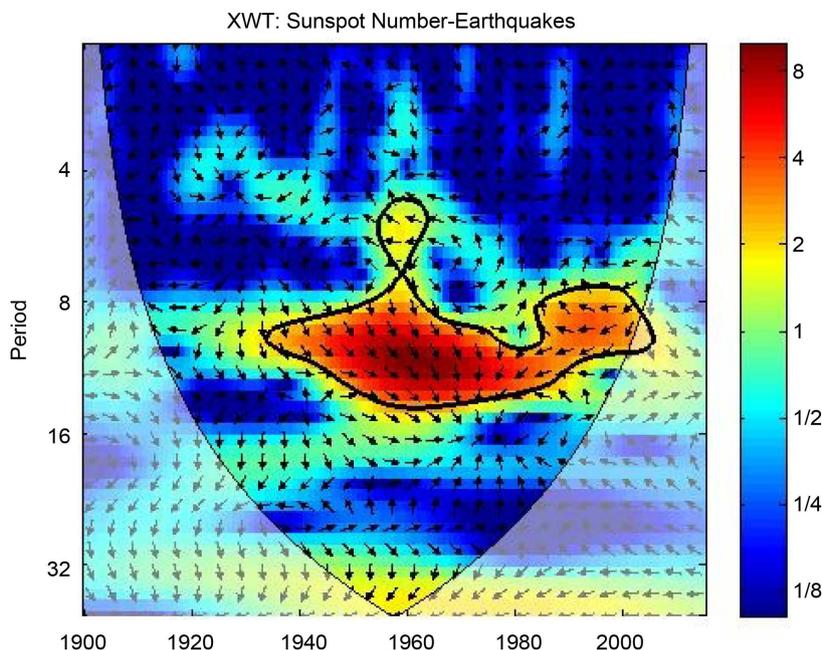
We applied a measure of Wavelet Transform Coherence (WTC) between the two CWTs, to find significant coherence, if the two series are physically related we would expect a consistent or slowly varying phase. Monte Carlo methods are used to calculate the statistical significance against red noise backgrounds.

Wavelet Transform Coherence (WTC) of the SSN and Ms are shown in **Figure 5**. There are clearly common features in the wavelet power of the two series such as the significant peak in the ~11 year band around 1959 (Maximum of 19-Solar Cycle). This coherence seems to be stable between 1930 and 2000.

#### 4. Results and Discussions

From the above analysis, it can conclude that wavelets provide a new tool for the comparison of the periods of earthquakes activity and solar activity.

It could be a possible qualitative mechanism caused by solar activity that would influence seismic activity (proposed [17]).



**Figure 5.** Squared WTC coherence between SSN and Ms series. It confirms the coherence's intermittency around 8 - 12 years band. The horizontal dashed lines are the approximated bounds of 95% confidence level zones.

A summary of the effects of solar activity on the seismic activity should include the following elements:

- pressure pulses associated with fast solar wind or CME that compresses the magnetosphere;
- auroralelectrojet would be strengthened;
- atmospheric gravity waves would be generated and transmitted to lower altitudes;
- zonal winds would be strengthened westward;
- changes in surface air pressure;
- pressure balance of tectonic plates would be interrupted and tension accumulation is enough to trigger seismic activity.

## 5. Conclusions

By using the method of Fast Fourier Transform to study the periodicity in  $M_s$  for the last hundred years, periodicities of 4; 4.5; 5.5; 9; 11 and 13.5 were found for earthquakes. Some of these results were previously obtained (see **Table 1**).

According to the statistical study done, periodicities of approximately 8 - 12 years are observed in both SSN and  $M_s$ . Similar periodicities are also observed in the orbital movements and orbital synodical of large planets. Reference [18] showed evidence that seismic activity could be caused by internal tides produced by the gravitational force of large planets and the moon.

From the study of the temporal correlation between SSN y  $M_s$ , it was applied an independent method based on Wavelet Transform (squared WTC) [19]. It confirms the coherence's intermittency around 8 - 12 years band.

It can be inferred that there is a connection between solar and seismic activities.

This study does not include the prediction of earthquakes. In order to do so, it should also be taken into account the Sun-Earth interaction as an extra variable.

## Acknowledgements

This research work is part of project No. 20020090100131 (UBACYT), Argentina.

## References

- [1] Comte, D. and Pardo, M. (1991) Reappraisal of Great Historical Earthquakes in the Northern Chile and Southern Peru Seismic Gap. *Natural Hazards*, **4**, 23-44.  
<http://dx.doi.org/10.1007/BF00126557>
- [2] Du, X.X. (1997) Wavelets Data Based Analysis of Dynamic Seismicity Period. *Earthquake*, **17**, 259-264.
- [3] Liritzis, I. and Tsapanos, T.M. (1992) Probable Evidence for Periodicities in Global Seismic Energy Release. *Earth, Moon and Planets*, **60**, 93-108.  
<http://dx.doi.org/10.1007/BF00614377>
- [4] Madhava Rao, N. and Kaila, K.L. (1986) Model of Earthquake Energy Periodicity in the Al-pide-Himalayan Seismotectonic Belt. *Tectonophysics*, **124**, 261-270.
- [5] Ritz, M. (1984) Short Communication: A High Conductivity Anomaly on the West African Craton (MALI). *Journal of Geophysics*, **55**, 182-184.

- [6] Serrano, I., Zhao, D., Morales, J. and Torcal, F. (2003) Seismic Tomography from Local Crustal Earthquakes beneath Eastern Rif Mountains of Morocco. *Tectonic Physics*, **367**, 187-201. [http://dx.doi.org/10.1016/S0040-1951\(03\)00100-8](http://dx.doi.org/10.1016/S0040-1951(03)00100-8)
- [7] Mazzarella, A. and Palumbo, A. (1988) Solar Geomagnetic and Seismic Activity. *NuovoCimento C*, **1**, 353-364. <http://dx.doi.org/10.1007/bf02533129>
- [8] Han, Y.B., Guo, Z.J., Wu, J. and Ma, L.H. (2004) Possible Triggering of Solar Activity to Big Earthquakes ( $M_S \geq 8$ ) in Faults with Near West-East Strike in China. *Science in China Series G Physics, Mechanics and Astronomy*, **47**, 173-181. <http://dx.doi.org/10.1360/03yw0103>
- [9] Sobolev, G.A., Shestopalov, I.P. and Kharin, E.P. (1998) Geoeffective Solar Flashes and Seismic Activity of the Earth. *Fizika Zemli*, **7**, 85-90. (In Russian)
- [10] Zolotov, O.V., Namgaladze, A.A., Zkharenkova, I.E., Shagimuratov, I.I. and Martynenko, O.V. (2010) Modeling of Ionospheric Earthquake Precursors Generated by Various Electric Field Sources. *Natural Hazards Earth System Sciences*, **10**, 7-18.
- [11] Tavares, M. and Azevedo, A. (2011) Influences of Solar Cycles on Earthquakes. *Natural Science*, **36**, 436-443. <http://dx.doi.org/10.4236/ns.2011.36060>
- [12] Simpson, J.F. (1967) Solar Activity as a Triggering Mechanism for Earthquakes. *Earth and Planetary Science Letters*, **3**, 417-425. [http://dx.doi.org/10.1016/0012-821X\(67\)90071-4](http://dx.doi.org/10.1016/0012-821X(67)90071-4)
- [13] Silbergleit, V. and Larocca, P. (2001) Estimate of the Upper Limit of Amplitude of Solar Cycle No.23. *Atmósfera*, **3**, 139-145.
- [14] Silbergleit, V. and Larocca, P. (2005) Geomagnetic Activity and Solar Cycles. *Advances in Space Research*, **36**, 2384-2387. <http://dx.doi.org/10.1016/j.asr.2003.08.084>
- [15] Duhau, S. and Martinez, E.A. (2012) Solar Dynamo Transitions as Driver of Sudden Climate Changes. In: Singh, B.R., Ed., *Global Warming-Impacts and Future Perspective*, In-Tech, Croatia, 185-204. <http://dx.doi.org/10.5772/51814>
- [16] Torrence, C. and Compo, G.P. (1998) A Practical Guide to Wavelet Analysis. *Bulletin of the American Meteorological Society*, **79**, 61-78. [http://dx.doi.org/10.1175/1520-0477\(1998\)079<0061:APGTWA>2.0.CO;2](http://dx.doi.org/10.1175/1520-0477(1998)079<0061:APGTWA>2.0.CO;2)
- [17] Odintsov, S., Boyarchuk, K., Georgieva, K., Kirov, B. and Atanasov, D. (2006) Long-Period Trends in Global Seismic and Geomagnetic Activity and Their Relation to Solar Activity. *Physics and Chemistry of the Earth*, **31**, 88-93. <http://dx.doi.org/10.1016/j.pce.2005.03.004>
- [18] Barkin, Y., Ferrandiz, J., Garcia Ferrandez, M. and Navarro, J. (2007) Prediction of Catastrophic Earthquakes in 21 Century. *Geophysical Research Abstracts*, **9**, A-08643. SRef-ID: 1607-7962.EGU2007.
- [19] Grinsted, A., Moore, J.C. and Jevrejeva, S. (2004) Application of the Cross Wavelet Transform and Wavelet Coherence to Geophysical Time Series. *Nonlinear Processes in Geophysics*, **11**, 561-566. <http://dx.doi.org/10.5194/npg-11-561-2004>



**Submit or recommend next manuscript to SCIRP and we will provide best service for you:**

Accepting pre-submission inquiries through Email, Facebook, LinkedIn, Twitter, etc.

A wide selection of journals (inclusive of 9 subjects, more than 200 journals)

Providing 24-hour high-quality service

User-friendly online submission system

Fair and swift peer-review system

Efficient typesetting and proofreading procedure

Display of the result of downloads and visits, as well as the number of cited articles

Maximum dissemination of your research work

Submit your manuscript at: <http://papersubmission.scirp.org/>

Or contact [ijg@scirp.org](mailto:ijg@scirp.org)