

# Predictions of Storage Modulus of Glass Bead-Filled Low-Density-Polyethylene Composites

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## ABSTRACT

The factors affecting storage modulus ( $E_c'$ ) and quantitative characterization of polymer composites filled with inorganic particles were discussed in this paper. On the basis of Eshelby's method and Mori's work, an equation describing the relationship between the  $E_c'$  and the filler volume fraction, particle geometry as well as interfacial morphology was proposed. The  $E_c'$  of the glass bead filled low-density-polyethylene (LDPE/GB) composites was estimated by means of this equation under experimental conditions with temperature range of  $-150-100^\circ\text{C}$ , frequency of 1 Hz and the amplitude of 0.6 mm, and compared with other equations proposed in literature. The results showed that the predictions for this equation were close to the measured data from the LDPE/GB composites.

**Keywords:** Polymer, Composite Materials, Storage Modulus, Prediction

## 1. Introduction

Viscoelasticity is one of important parameters for characterization of processing and use properties of polymeric materials. For polymer blends or inorganic particle-filled polymer composites, the relationship between structure and properties tends towards more complexity owing to the formation of an interface between components, as well as between the fillers and matrix. The viscoelastic parameter of polymer materials may be measured using a dynamic mechanical analysis instrument, such as storage modulus, loss modulus and mechanical damping, etc. In addition, dynamic mechanical measurements over a range of temperatures provide valuable insight into the structure, morphology and properties of polymeric blends and composites. A lot of dynamic mechanical analyses on polymeric blends and composites have been done [1-4]. Zhang *et al.* [1] measured dynamic mechanical properties of composites filled with SMA particles and short fibers, and found that the storage modulus reaches the maximum at the SMA phase transformation temperature of approximate  $120^\circ\text{C}$ . Karoui and Dufour [2] predicted the rheology parameters, such as storage modulus, loss modulus, strain,  $\tan\delta$  and complex viscosity, of ripened semi-hard cheeses using fluorescence spectra in the UV and visible ranges recorded at a young stage. Miyagawa and his colleague [3] studied the characterization and thermophysical properties of un-

saturated polyester-layered silicate nanocomposites. The results showed that a higher storage modulus enhancement was obtained when the organo-clay nanoplatelets were delaminated and more homogeneously dispersed. Kolarik [4] researched the Phase structure and thermal and mechanical properties of heterogeneous polyamide 66/syndiotactic polystyrene blends, and found that storage modulus ( $125^\circ\text{C}$ ) noticeably declined with weight fraction and thus showed that sPS did not improve the dimensional stability of the blends at elevated temperatures. Since 1998, Liang *et al.* [5-9] have investigated the effects of glass bead content and size on the viscoelastic properties of filled polyolefin composites, and get some useful findings.

Storage modulus is an important index for measuring the stiffness and elasticity of polymeric materials, and it has been paid extensively attention by researchers. For particulate filled composites, a number of equations for prediction of the modulus have been derived with different methods. Among these methods, Eshelby's equivalent inclusion method is more noticeable, which is a method to analyze average stress field distribution in the case of only an inclusion an infinite body [10]. It is necessary to modify Eshelby's method in the case of existence of a lot of inclusions and their interaction. Mori and Tanaka [11] proposed a modification method in order that the method was available for the case of con-

taining a number of elliptic sphere inclusions. Taya and Chou [12] further developed Mori-Tanaka method and presented a model including several types of inclusions. To calculate the elastic modulus Benveniste [13] proposed an equation group based on the modified Mori-Tanaka method.

The focus of this paper is to investigate the factors affecting the storage moduli of polymer composites filled with inorganic particles, and to propose a quantitative characterization based on the previous work stated above. Moreover, to verify it some measured data of the dynamic mechanical properties of glass bead-filled low density polyethylene composites will be used.

## 2. Theory

### 2.1. Factors Affecting Storage Modulus

For polymer composites, relative storage modulus ( $E'_R$ ) is usually used to characterize the relationship between storage modulus and other parameters, which is defined by

$$E'_R = E'_c / E'_m \quad (1)$$

where  $E'_c$  and  $E'_m$  are the storage modulus of composite and matrix resin, respectively.

For a given matrix resin, the major factors affecting  $E'_R$  are filler content, geometry, size and its distribution, the distribution and dispersion status of the inclusions in the matrix resin, as well as the interfacial morphology between them. That is

$$E'_R = f(\phi_f, d, \xi, \dots) \quad (2)$$

where  $\phi_f$  is the filler volume fraction,  $d$  is the particle diameter,  $\xi$  is the parameter related to the dispersion of the particles in matrix and interfacial adhesion strength.

### 2.2. Quantitative Description of Storage Modulus

For a random distribution of spherical particles in matrix, if there is no interfacial slide, then  $E'_R$  may be described with the famous Einstein Equation [14]:

$$E'_R = 1 + 2.5\phi_f \quad (3)$$

Guth generalized the Einstein equation concept by introducing a particle interaction term and proposed a following equation for spherical particles [15]:

$$E'_R = 1 + 2.5\phi_f + 14.1\phi_f^2 \quad (4)$$

Halpin and Tsai derived a simple and generalized equation to approximate the results of more exact micromechanics. The Halpin-Tsai equation is as follows [16]

$$E'_R = \frac{1 + \zeta\eta\phi_f}{1 - \eta\phi_f} \quad (5)$$

and

$$\eta = \frac{m-1}{m+\zeta} \quad (6)$$

where  $\zeta$  is a measure of reinforcement, and it depends on filler geometry, packing geometry, and loading conditions. For spherical particles,  $\zeta = 2$ .  $m = E'_f / E'_m$ ,  $E'_f$  is the filler particle storage modulus.

On the basis of Eshelby's method [10] and Mori's work [11], a simplified storage modulus equation may be proposed as follows:

$$E'_R = 1 + \frac{\xi\phi_f}{(1-\phi_f)\lambda} \quad (7)$$

and

$$\lambda = \frac{7-5\nu_m}{15(1-\nu_m)} \quad (8)$$

where  $\xi$  is the coefficient related to filler shape and packing property.  $\nu_m$  is the matrix resin Poisson ratio.

## 3. Experimental

### 3.1. Raw Materials

A matrix resin used in this experimental was a low-density-polyethylene with trade-mark of LDPE G812 (Polyolefin, Singapore). The resin melt flow index and density were 35 g/10 min (2.16 kg, 190°C) and 0.917 g/cm<sup>3</sup>, respectively. The melting temperature was 106°C.

A set of solid glass beads (GB) with different diameter, 114 μm (GB2227), 93 μm (GB2429) and 11 μm (GB 5000), was used as filler in this test. The GB trade mark was Spheriglass<sup>®</sup> and was supplied by Potters Industry Inc. in USA. The GB density was 2.5 g/cm<sup>3</sup>, and the GB surface was pretreated with a silane coupling agent (CP-01) by the supplier.

### 3.2. Specimen Fabrication

The LDPE and glass beads were blended in a twin screw extruder (Brabender) after simply mixing to produce the composites. The blending ratios of LDPE/GB were 90/10, 80/20, 70/30, and 60/40, respectively. The extrusion temperature varied from 160°C to 180°C. The specimens for dynamical testing were molded with an injection machine, with width, thickness, and length of 12.9, 3.2, and 55 mm, respectively. The injection temperature was from 180°C to 200°C.

### 3.3. Apparatus and Methods

The viscoelasticity property measurements of the LDPE/GB composites were conducted using a dynamical mechanical analyzer (DMA 983, Du Pont Instruments, USA). The test temperatures varied from -150°C to

100°C, and the temperatures were increased at 2°C per minute. The fixed frequency was 1 Hz and the amplitude was 0.6 mm.

## 4. Results and Discussion

### 4.1. Dependence of Storage Modulus on Temperature

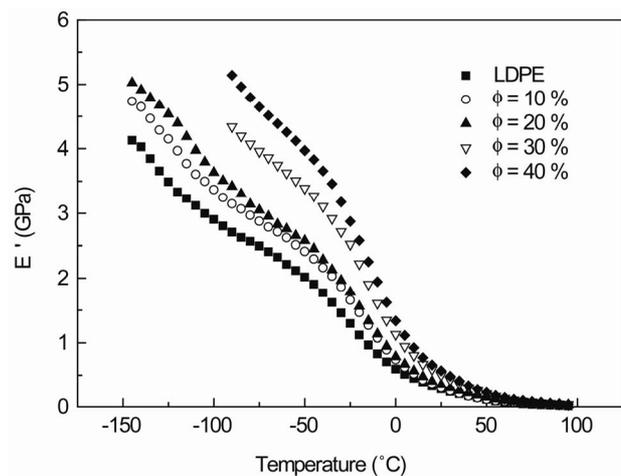
**Figure 1** shows the dependence of the storage modulus ( $E'_c$ ) of LDPE/GB5000 composites on temperature. When temperature is lower than  $-100^\circ\text{C}$  and glass bead content is low (weight fraction ( $\phi$ )  $\leq 20\%$ ),  $E'_c$  decreases rapidly, and then it decreases gently as temperature lower than  $-50^\circ\text{C}$ . In a temperature range of  $-50^\circ\text{C} \sim 25^\circ\text{C}$ ,  $E'_c$  decreases quickly with a rise in temperatures, and then it decrease slightly. In other words, the turning points of storage modulus-temperature curves are at about  $-100^\circ\text{C}$ ,  $-50^\circ\text{C}$ , and  $25^\circ\text{C}$ , respectively. When  $\phi$  is more than 20%, the turning points of storage modulus-temperature curves are at about  $-35^\circ\text{C}$  and  $25^\circ\text{C}$ , respectively. It indicates that when temperature is fixed  $E'_c$  changes with variation of the glass bead content, especially in a case of higher filler concentration.

**Figure 2** shows the dependence of the storage modulus ( $E'_c$ ) of LDPE/GB2429 composites on temperatures. When temperature is lower than  $-100^\circ\text{C}$  and within  $-50 \sim 0^\circ\text{C}$ ,  $E'_c$  decreases rapidly, but it decreases gently in other temperature range with a rise in temperatures. In other words, the turning points of storage modulus-temperature curves were around  $-125^\circ\text{C}$  and  $-25^\circ\text{C}$ , respectively. It was found in further studies that one of peaks of loss modulus-temperature curves of these composites located around  $-25^\circ\text{C}$  [6,9]. This indicates that the glass transition temperature for these composites is about  $-25^\circ\text{C}$ .

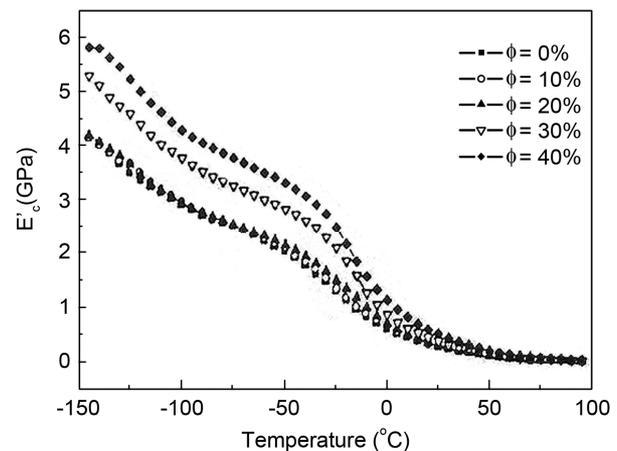
**Figure 3** shows the dependence of the storage modulus ( $E'_c$ ) of LDPE/GB2227 composites on temperatures. When temperature is lower than  $-50^\circ\text{C}$  and glass bead content is low (weight fraction ( $\phi$ )  $\leq 10\%$ ),  $E'_c$  decreases roughly linearly. In a temperature range of  $-50^\circ\text{C} \sim 25^\circ\text{C}$ ,  $E'_c$  decreases quickly with a rise of temperatures, and then it decrease slightly. In other words, the turning points of storage modulus- temperature curves are at about  $-50^\circ\text{C}$  and  $25^\circ\text{C}$ , respectively. When  $\phi$  is more than 20%, the turning points of storage modulus- temperature curves are at about  $-125^\circ\text{C}$ ,  $-50^\circ\text{C}$  and  $25^\circ\text{C}$ , respectively? It also indicates that  $E'_c$  changes with variation of the glass bead content when temperature is fixed, especially in a case of higher filler concentration.

It can be seen from **Figure 1** to **Figure 3** that when temperature is fixed the  $E'_c$  changes with variation of the glass bead content, and the difference increases with

a reduction of temperatures. In general, the interaction between the glass beads and the LDPE matrix increases and the certain elastic shear deformation is generated under dynamic shear load when temperature is constant, leading to forming the elastic storage energy in the composite system. With a rise of temperature, the motion ability of molecular chain in the resin enhances and the relaxation process of the elastic storage energy is quickened, resulting from the reduction of the storage modulus (see **Figures 1-3**). Moreover, the interaction between the glass beads and the LDPE matrix increases is enhanced and the dependence of the storage modulus of the filled systems on temperature is increased with an addition of the glass beads, especially in the case of high filler concentration such as  $\phi = 40\%$  (see **Figures 1 and 2**).



**Figure 1.** Dependence of storage modulus on temperature of LDPE/GB5000 composite.



**Figure 2.** Dependence of storage modulus on temperature of LDPE/GB2429 composite.

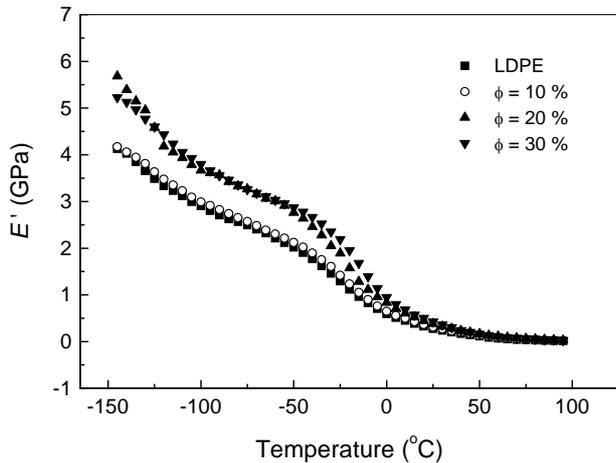


Figure 3. Dependence of storage modulus on temperature of LDPE/GB2227 composite.

#### 4.2. Relationship between Relative Storage Modulus and GB Content

Figure 4 illustrates the relationship between the relative storage modulus ( $E'_R$ ) of the LDPE/GB composites and the glass bead volume fraction ( $\phi_f$ ) as temperature is  $-25^\circ\text{C}$ . It may be seen that the  $E'_R$  increases nonlinearly with an increase of  $\phi_f$ . In addition, the  $E'_R$  is estimated by means of Equation (7) under these test conditions. The results indicate that the calculations and the experimental measured data are roughly close to each other. In this paper,  $\nu_m = 0.38$ ,  $\xi = 2.0$ . For inorganic particles, a relationship between weight fraction and volume fraction is given by [17]:

$$\phi = \frac{\phi_f \chi}{1 - \phi_f + \phi_f \chi} \quad (9)$$

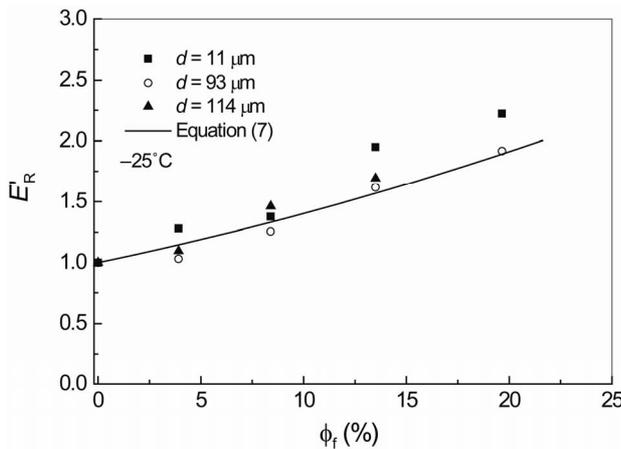


Figure 4. Relationship between relative storage modulus and GB volume fraction at  $-25^\circ\text{C}$ .

where  $\chi = \rho_f / \rho_m$ ,  $\rho_f$  and  $\rho_m$  are the density of the filler and matrix resin, respectively.

When temperature is  $0^\circ\text{C}$ , the relationship between the relative storage modulus of the LDPE/GB composites and the glass bead volume fraction is showed as in Figure 5. Similarly, the  $E'_R$  increases nonlinearly with an addition of  $\phi_f$ . Furthermore, the  $E'_R$  is also estimated by means of Equation (7) under these test conditions. The results show good agreement between the estimations and the experimental measured data.

It can also be observed from Figures 4 and 5 that the relative storage modulus of LDPE filled with small diameter GB is obvious greater than that of LDPE filled with big ones. This because that the smaller the size of particles is, the more specific surface area of the filler is, leading to increase of the contact area between the inclusions and matrix. Furthermore, the particle number increases with an reduction of filler size under the same volume fraction, and the interaction between the inclusions and matrix is enhanced correspondingly, resulting in increase of the storage modulus of polymer composites, especially in a case of uniform dispersion of filler in resin matrix. Figures 6-8 are respectively the fracture surface photographs of the scanning electron microscope (SEM) of the LDPE/GB2227, LDPE/GB2429 and LDPE/GB5000 filled systems when the glass bead weight fraction is 20%. It can be observed that the dispersion of the glass beads in LDPE matrix was roughly uniform.

As stated above, the interaction between the glass beads and the LDPE matrix increases is enhanced and the dependence of the storage modulus of the filled systems on temperature is increased with an addition of the glass beads, especially in the case of high concentration of the fine particles, leading to the difference between the predictions and the measured storage modulus of the

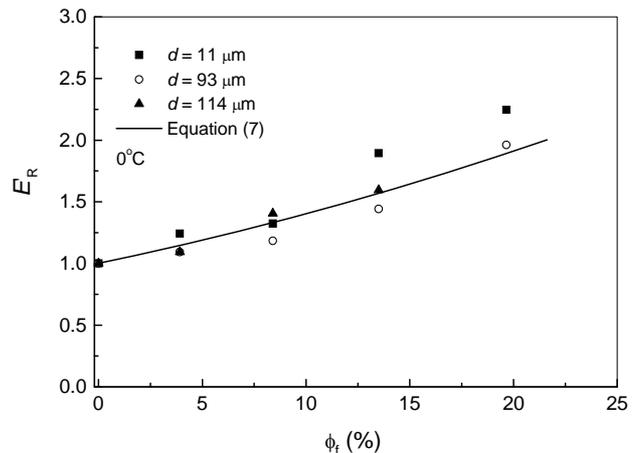


Figure 5. Relationship between relative storage modulus and GB volume fraction at  $0^\circ\text{C}$ .



Figure 6. SEM photograph of fracture surface of LDPE/GB2227 composite.

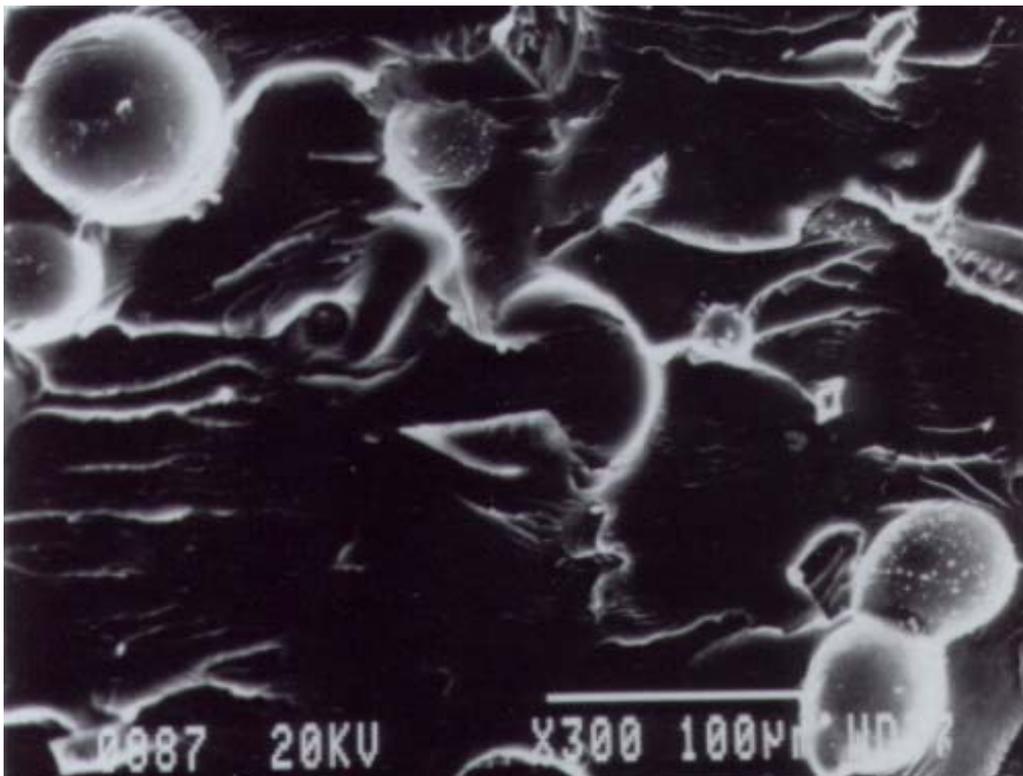


Figure 7. SEM photograph of fracture surface of LDPE/GB2429 composite.

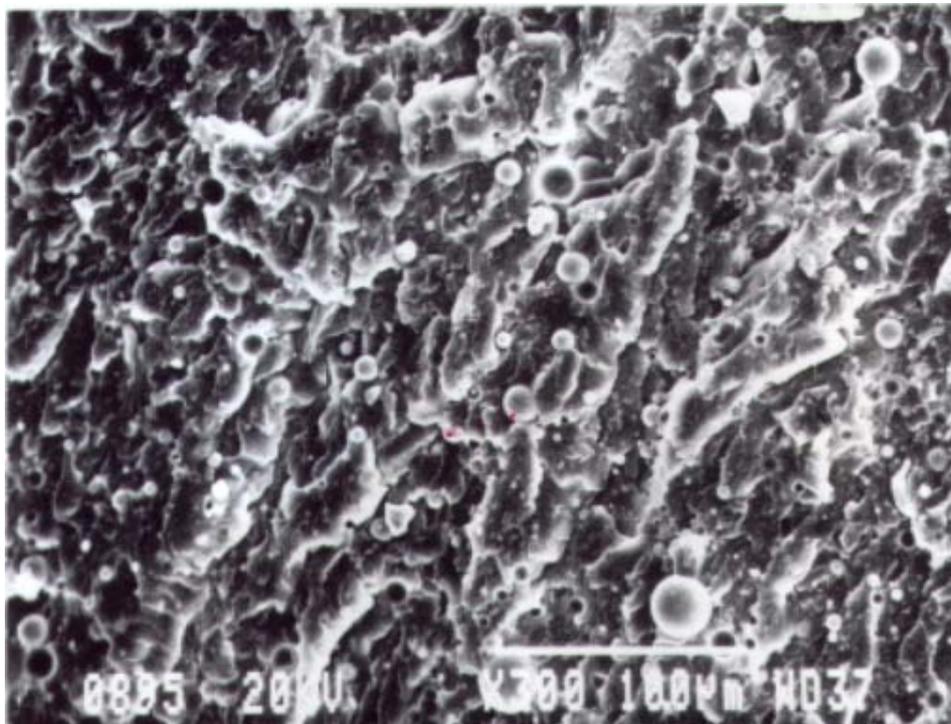


Figure 8. SEM photograph of fracture surface of LDPE/GB5000 composite.

LDPE composites increases (such as LDPE/GB5000 composite, see **Figures 4** and **5**). This indicates that the parameter  $\zeta$  would be greater than 2 for the LDPE composite filled with small size glass beads.

#### 4.3 Comparison between Predictions of Relative Storage Modulus

**Figure 9** shows the relationship between the relative storage modulus of the LDPE/GB2429 composites and

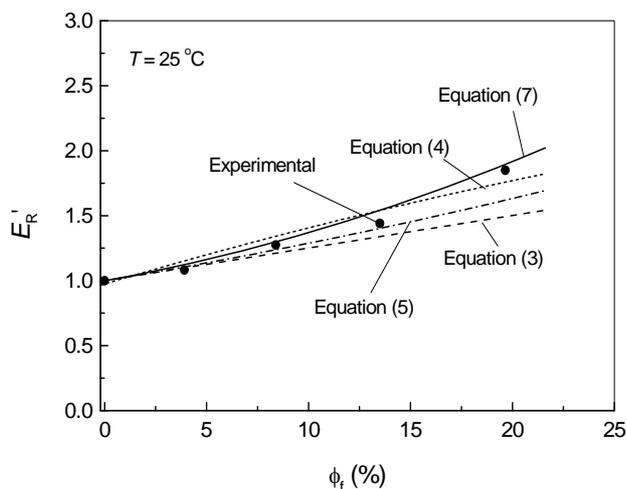


Figure 9. Comparison between predictions of relative storage moduli of LDPE/GB2429 system at 25°C.

the glass bead volume fraction as temperature is 25°C. Similarly, the  $E'_R$  increases nonlinearly with an addition of  $\phi_f$ . In addition, the values of the  $E'_R$  are calculated respectively by using of Einstein equation, Guth equation, Halpin-Tsai equation and Equation (7) under these test conditions, and the results are showed as in **Figure 4**. It can be seen that the predictions by application of Equation (7) were closer to the measured data from the experiments of the composites than the other equations.

When inorganic particles are blended into matrix resin, they will play a role of framework in polymeric composite because their stiffness is much greater than that of the matrix. In addition, they will block the movement of the molecular chains of the matrix resin, leading to increase the stiffness of filled polymer composite materials. Therefore, if the distribution or dispersion of the inclusions in the matrix is uniform, the more the inorganic particles in the matrix, the higher the stiffness of polymeric composites is. In this case, the storage moduli of polymer composites will increase with an increase of the filler particles (see **Figures 4,5,9**).

#### 5. Conclusions

The storage modulus of LDPE/GB composites decreased with rising temperature when the glass bead content was constant, and the turning points of storage modulus-temperature curves were around  $-125^\circ\text{C}$  and  $-25^\circ\text{C}$ , re-

spectively.

The storage modulus of LDPE/GB composites increased nonlinearly with an increase of the volume fraction of the glass beads under given experimental conditions.

Equation (7) describes a relationship between the storage modulus and volume fraction of inorganic particles for filled polymer composites. The relative storage modulus of LDPE/GB composites was estimated by using this equation, and these estimations were compared respectively with the calculations by means of Einstein equation, Guth equation and Halpin-Tsai equation. The results showed that the predictions of the relative storage modulus by means of Equation (7) were closer to the measured data from the experiments of the composites than the other equations.

## REFERENCES

- [1] R. X. Zhang, Q. Q. Ni, T. Natsuki and M. Iwamoto, "Mechanical Properties of Composites Filled with SMA Particles and Short Fibers," *Composite Structures*, 2007, Vol. 79, No. 1, pp. 90-96.
- [2] R. Karoui and E. Dufour, "Prediction of the Rheology Parameters of Ripened Semi-Hard Cheeses Using Fluorescence Spectra in the UV and Visible Ranges Recorded at a Young Stage," *International Dairy Journal*, 2006, Vol. 16, No. 12, pp. 1490-1497.
- [3] H. Miyagawa, A. K. Mohanty, R. Burgueno, L. T. Drzal and M. Misra, "Characterization and Thermophysical Properties of Unsaturated Polyester-Layered Silicate Nanocomposites," *Journal of Nanoscience and Nanotechnology*, 2006, Vol. 6, No. 2, pp. 464-471.
- [4] J. Kolarik, L. Fambri, M. Slouf and D. Konecny, "Heterogeneous Polyamide 66/Syndiotactic Polystyrene Blends: Phase Structure and Thermal and Mechanical Properties," *Journal of Applied Polymer Science*, 2005, Vol. 96, No. 3, pp. 673-684.
- [5] J. Z. Liang, C. Y. Tang, R. K. Y. Li, S. C. Tjong and K. C. Yung, "A Study of the Elastic Storage Moduli of Glass Bead Filled LDPE Composites," *Key Engineering Materials*, 1998, Vol. 145-148, pp. 817-822.
- [6] R. K. Y. Li, J. Z. Liang and S. C. Tjong, "Morphology and Dynamic Mechanical Properties of Glass Beads Filled Low Density Polyethylene Composites," *Journal of Materials Processing Technology*, 1998, Vol. 79, No. 1-3, pp. 59-65.
- [7] J. Z. Liang, R. K. Y. Li and S. C. Tjong, "Effects of Glass Bead Content and Surface Treatment on Viscoelasticity of Filled Polypropylene/Elastomer Hybrid Composites," *Polymer International*, 1999, Vol. 48, No. 11, pp. 1068-1072.
- [8] J. Z. Liang, R. K. Y. Li and S.C. Tjong, "Effects of Glass Bead Size and Content on the Viscoelasticity of Filled Polypropylene Composites," *Polymer Testing*, 2000, Vol. 19, No. 2, pp. 213-220.
- [9] J. Z. Liang, R. K. Y. Li and S. C. Tjong, "Dynamic Mechanical Analysis of Low-Density Polyethylene with Glass Beads," *Journal of Thermoplastic Composite Materials*, 2000, Vol. 13, No. 1, pp. 12-20.
- [10] J. D. Eshelby, "Elastic Inclusion and Inhomogeneities. Progress in Solid Mechanics," *Amsterdam*, 1961, Vol. 2, pp. 89-140.
- [11] T. Mori and K. Tanaka, "Average Stress in Matrix and Average Elastic Energy of Materials with Misfitting Inclusions," *Acta Metallurgica*, 1973, Vol. 21, No. 5, pp. 571-574.
- [12] M. Taya and T. W. Chou, "On Two Kinds of Ellipsoidal Inhomogeneities in an Infinite Elastic Body: An Application to a Hybrid Composite," *International Journal of Solids and Structures*, 1981, Vol. 17, pp. 553-563.
- [13] Y. Benveniste, "A New Approach to the Application of Mori-Tanaka Theory in Composite-Materials," *Mechanics of Materials*, 1987, Vol. 6, pp. 147-157.
- [14] E. Guth, "Theory of Filler Reinforcement," *Journal of Applied Physics*, 1945, Vol. 16, No. 1, pp. 21-25.
- [15] L. E. Nielsen, "Mechanical Properties of Polymer and Composites," Marcel Dekker, New York, 1974.
- [16] L. E. Nielsen, "Generalized Equation for the Elastic Moduli of Composite Materials," *Journal of Applied Physics*, 1970, Vol. 41, No. 11, pp. 4626-4627.
- [17] J. Z. Liang and R. K. Y. Li, "Measurement of Dispersion of Glass Beads in PP Matrix," *Journal of Reinforced Plastics and Composites*, 2001, Vol. 20, No. 8, pp. 630-638.