

# Buffer Standards for the Biochemical pH of the Zwitterionic Buffer *N*-Tris-(Hydroxymethyl)Methyl-2-aminoethanesulfonic Acid (TES) from 5°C to 55°C

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## ABSTRACT

The authors have undertaken the determination of pH values for one buffer solution of TES without NaCl and nine buffer solutions with NaCl yielding an ionic strength  $I = 0.16 \text{ mol}\cdot\text{kg}^{-1}$  similar to that of blood. These buffer solutions have been evaluated in the temperature range of 5°C to 55°C using an extended version of the Debye-Hückel equation. The pH values are reported using 1) the Debye-Hückel extension of the Bates-Guggenheim convention in the temperature range 5°C to 55°C and 2) with and without liquid junction correction at 25°C and 37°C. These TES buffer solutions are recommended as secondary standard references for pH measurements in the range of pH 7.2 to 7.5 for physiological application with an ionic strength of  $I = 0.16 \text{ mol}\cdot\text{kg}^{-1}$ .

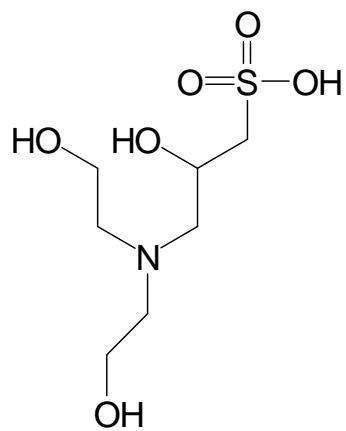
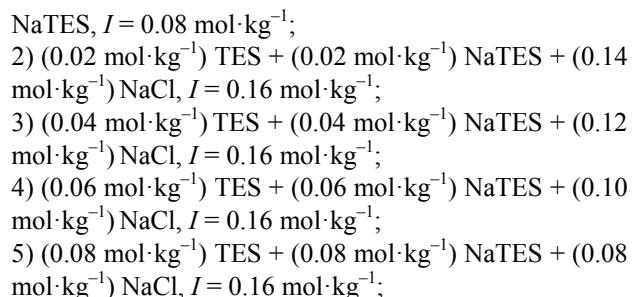
**Keywords:** Ionic Strength; Liquid Junction Potentials; Second Dissociation Constant; Buffer Solutions; Activity Coefficients

## 1. Introduction

Good *et al.* [1,2] have proposed a select group of zwitterionic buffers for physiological use. The authors have previously reported the pH values of *N*-[tris(hydroxymethyl)methyl-3-amino]propansulfonic acid (TAPS) [3] from 5 to 55°C, including 37°C. Vega and Bates [4] have reported the second dissociation constant,  $pK_2$ , and related thermodynamic data of TES from 5°C to 55°C. Roy and associates [5] also determined  $pK_2$  values of TES with thermodynamic quantities from 5°C to 55°C. The purpose of the current investigation is to provide pH values for the amino acid TES, the structure of which is given in **Figure 1**.

The universally used NIST certified physiological phosphate primary standard buffer solution has pH values of 7.415 and 7.395 at 25°C and 37°C, respectively [6]. This phosphate buffer contains  $0.008695 \text{ mol}\cdot\text{kg}^{-1}$   $\text{KH}_2\text{PO}_4$  and  $0.03043 \text{ mol}\cdot\text{kg}^{-1}$   $\text{Na}_2\text{HPO}_4$ . Because of problems associated with the current phosphate buffer [7-9], we have been prompted to investigate some zwitterionic buffers including TES for use in physiological pH range 6.5 - 7.5.

The following compositions were used for the determination of  $p\alpha_{\text{H}}$ : 1)  $(0.08 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.08 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES}$ ; 2)  $(0.02 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.02 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES} + (0.14 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaCl}$ ; 3)  $(0.04 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.04 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES} + (0.12 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaCl}$ ; 4)  $(0.06 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.06 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES} + (0.10 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaCl}$ ; 5)  $(0.08 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.08 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES} + (0.08 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaCl}$ ; 6)  $(0.16 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.16 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES}$ ; 7)  $(0.20 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.20 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES}$ ; 8)  $(0.24 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.24 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES}$ ; 9)  $(0.28 \text{ mol}\cdot\text{kg}^{-1}) \text{ TES} + (0.28 \text{ mol}\cdot\text{kg}^{-1}) \text{ NaTES}$ .



**Figure 1.** *N*-tris-(hydroxymethyl)methyl-2-aminoethanesulfonic acid (TES).

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- 6) ( $0.05 \text{ mol}\cdot\text{kg}^{-1}$ ) TES + ( $0.05 \text{ mol}\cdot\text{kg}^{-1}$ ) NaTES + ( $0.11 \text{ mol}\cdot\text{kg}^{-1}$ ) NaCl,  $I = 0.16 \text{ mol}\cdot\text{kg}^{-1}$ ;  
 7) ( $0.02 \text{ mol}\cdot\text{kg}^{-1}$ ) TES + ( $0.04 \text{ mol}\cdot\text{kg}^{-1}$ ) NaTES + ( $0.12 \text{ mol}\cdot\text{kg}^{-1}$ ) NaCl,  $I = 0.16 \text{ mol}\cdot\text{kg}^{-1}$ ;  
 8) ( $0.03 \text{ mol}\cdot\text{kg}^{-1}$ ) TES + ( $0.06 \text{ mol}\cdot\text{kg}^{-1}$ ) NaTES + ( $0.10 \text{ mol}\cdot\text{kg}^{-1}$ ) NaCl,  $I = 0.16 \text{ mol}\cdot\text{kg}^{-1}$ ;  
 9) ( $0.04 \text{ mol}\cdot\text{kg}^{-1}$ ) TES + ( $0.08 \text{ mol}\cdot\text{kg}^{-1}$ ) NaTES + ( $0.08 \text{ mol}\cdot\text{kg}^{-1}$ ) NaCl,  $I = 0.16 \text{ mol}\cdot\text{kg}^{-1}$ ;  
 10) ( $0.05 \text{ mol}\cdot\text{kg}^{-1}$ ) TES + ( $0.10 \text{ mol}\cdot\text{kg}^{-1}$ ) NaTES + ( $0.06 \text{ mol}\cdot\text{kg}^{-1}$ ) NaCl,  $I = 0.16 \text{ mol}\cdot\text{kg}^{-1}$ .

## 2. Experimental

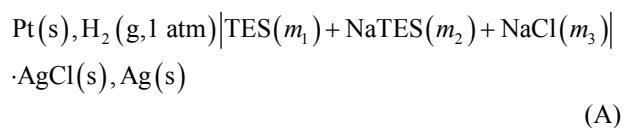
The TES was obtained from Research Organics in Cleveland, OH. The experimental method for further crystallization and the assay have been previously reported in detail [5]. Buffer solutions 1) to 10) were prepared by weighing recrystallized TES buffer, ACS reagent grade NaCl, a standard NaOH solution, and calculated amounts of double distilled CO<sub>2</sub>-free water. Vacuum corrections were made for all masses.

The cell design, preparation of the chloroplatinic acid, hydrogen gas purification, silver-silver chloride, solution preparation, and other experimental details have been described previously [10-13].

## 3. Methods and Results

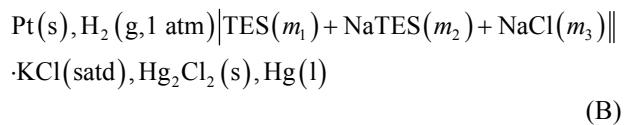
Cell (A) contains one solution without the Cl<sup>-</sup> and nine solutions containing NaCl to yield an ionic strength of  $I = 0.16 \text{ mol}\cdot\text{kg}^{-1}$ . The emf values have been corrected to a hydrogen pressure of 1 atm. The values for the  $p_{\text{aH}}$  calculations are given in **Table 1**. The error in the emf, on an average of two readings, lies within 0.02 mV.

For accurate calculations of the pH values of the buffer solutions, the following Cell (A) was used:



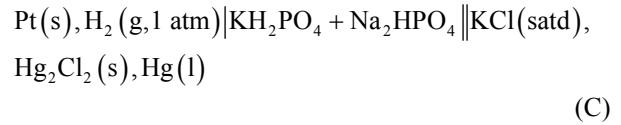
where  $m_1$ ,  $m_2$ , and  $m_3$  denote the molalities of the respective species at 1 atm. The Harned-type cell was employed.

Cell (B) involves liquid junction as shown with a double vertical line:



where the abbreviations “s”, “l”, and “g” indicate the solid, liquid, and gaseous states, respectively.

For Cell (C), the phosphate salts were NIST standard reference materials. Its solutions are recommended for pH measurements in physiological media. The schematic diagram of the Cell (C) is shown below:



The  $E_{\text{SCE}}^{\circ}$  values of the saturated calomel electrode were taken as  $-0.2415$  and  $-0.2335$  at  $25^{\circ}\text{C}$  and  $37^{\circ}\text{C}$ , respectively [12,14]. The  $\delta E_j$  values of the buffer solution for Cell (B) were calculated using the following equation:

$$\delta E_j = E + E_{\text{SCE}}^{\circ} - kp\text{H} \quad (1)$$

where  $k = 0.059156$  and  $\text{pH} = 7.415$  at  $25^{\circ}\text{C}$ ;  $k = 0.061538$  and  $\text{pH} = 7.395$  at  $37^{\circ}\text{C}$ . These values are for phosphate primary standard and buffer solutions. The operational definition of pH is denoted as  $\text{pH}(x)$  which can be calculated by use of the equation:

**Table 1. Electromotive force of Cell A: Pt(s); H<sub>2</sub>(g, 1 atm) | TES( $m_1$ ), NaTES( $m_2$ ), NaCl ( $m_3$ ) | AgCl(s), Ag(s).**

$m_1^{\text{a}}$	$m_2^{\text{a}}$	$m_3^{\text{a}}$	5°C	10°C	15°C	20°C	25°C	30°C	35°C	37°C	40°C	45°C	50°C	55°C
0.08	0.08	0.005	0.79716	0.79847	0.79946	0.80037	0.80099	0.80206	0.80295	0.80296	0.80380	0.80417	0.80532	0.80577
0.08	0.08	0.010	0.78204	0.78302	0.78377	0.78449	0.78480	0.78585	0.78633	0.79628	0.78673	0.78697	0.78740	0.78765
0.08	0.08	0.015	0.77406	0.78302	0.77540	0.77587	0.77594	0.77698	0.77715	0.77712	0.77747	0.77740	0.77747	0.77738
0.08	0.08	0.020	0.76875	0.76939	0.76996	0.77034	0.77000	0.77120	0.77128	0.77105	0.77131	0.77110	0.77105	0.77078
0.02	0.02	0.14	0.72121	0.72111	0.72087	0.72050	0.71991	0.71933	0.71864	0.71839	0.71783	0.71692	0.71591	0.71466
0.04	0.04	0.12	0.72597	0.72594	0.72576	0.72547	0.72506	0.72450	0.72385	0.72358	0.72307	0.72224	0.72129	0.72019
0.06	0.06	0.10	0.73153	0.73162	0.73149	0.73122	0.73085	0.73034	0.72975	0.72949	0.72903	0.72823	0.72734	0.72634
0.08	0.08	0.08	0.73804	0.73830	0.73825	0.73808	0.73781	0.73741	0.73688	0.73666	0.73627	0.73553	0.73467	0.73377
0.05	0.05	0.11	0.72998	0.72980	0.72939	0.72890	0.72809	0.72735	0.72640	0.72624	0.72566	0.72492	0.72404	0.72288
0.02	0.04	0.12	0.73954	0.73974	0.73986	0.73989	0.73960	0.73935	0.73898	0.73883	0.73853	0.73798	0.73733	0.73674
0.03	0.06	0.10	0.74487	0.74523	0.74544	0.74547	0.74527	0.74515	0.74481	0.74468	0.74440	0.74395	0.74337	0.74263
0.04	0.08	0.08	0.75155	0.75189	0.75223	0.75236	0.75232	0.75224	0.75205	0.75193	0.75165	0.75140	0.75087	0.75036
0.05	0.10	0.06	0.75903	0.75958	0.76027	0.76050	0.76080	0.76088	0.76087	0.76078	0.76060	0.76038	0.76004	0.75969

<sup>a</sup>Units of  $m$ ,  $\text{mol}\cdot\text{kg}^{-1}$ .

$$\text{pH}(x) = \text{pH}(s) + \frac{E_x - E_s + \delta E_j}{k} \quad (2)$$

where "x" refers to the unknown buffer solution (TES + NaTES in this case), "s" is the NIST standard phosphate buffer solution of known pH, and  $\delta E_j = E_{j(s)} - E_{j(x)}$ .

To calculate the pH values for the buffer solutions, the determination of the acidity function,  $p(a_{\text{H}\gamma_{\text{Cl}}})$ , in the temperature range 5°C to 55°C is required. These calculations were made using the emf ( $E$ ) values listed in **Table 1**. The following equation was used:

$$p(a_{\text{H}\gamma_{\text{Cl}}}) = \frac{E - E^\circ}{k} + \log m_{\text{Cl}} \quad (3)$$

where "k" is the Nernst slope.

The plot of  $p(a_{\text{H}\gamma_{\text{Cl}}})$  as a function of  $m_{\text{Cl}^-}$ , a linear plot was obtained. The y-intercept gives a  $p(a_{\text{H}\gamma_{\text{Cl}}})^\circ$  value at  $m_{\text{Cl}^-} = 0$ . The  $p(a_{\text{H}\gamma_{\text{Cl}}})^\circ$  values for the chloride-free buffer solution are listed in **Table 2**. The  $p(a_{\text{H}\gamma_{\text{Cl}}})$  values for the buffer solutions of high ionic strength containing  $\text{Cl}^-$  are entered in **Tables 2** and **3** from 5°C to 55°C.

**Table 2.**  $p(a_{\text{H}\gamma_{\text{Cl}}})^\circ$  of (TES + NaTES) buffer solutions from 5°C to 55°C, computed using Equation 5<sup>a</sup>  $p(a_{\text{H}\gamma_{\text{Cl}}})$  of (TES + NaTES) buffer solutions from 5°C to 55°C, computed using Equation (4)<sup>a</sup>.

$t$ (°C)	0.08 m TES + 0.08 m NaTES + 0.00 m NaCl $I = 0.08 \text{ m}$	0.02 m TES + 0.02 m NaTES + 0.14 m NaCl $I = 0.16 \text{ m}$	0.04 m TES + 0.04 m NaTES + 0.12 m NaCl $I = 0.16 \text{ m}$	0.06 m TES + 0.06 m NaTES + 0.10 m NaCl $I = 0.16 \text{ m}$	0.08 m TES + 0.08 m NaTES + 0.08 m NaCl $I = 0.16 \text{ m}$
5	7.867	7.971	7.991	8.012	8.033
10	7.759	7.861	7.881	7.902	7.924
15	7.650	7.756	7.774	7.795	7.817
20	7.550	7.654	7.673	7.692	7.713
25	7.455	7.555	7.575	7.594	7.615
30	7.364	7.462	7.481	7.499	7.520
35	7.277	7.372	7.390	7.407	7.427
37	7.241	7.338	7.355	7.372	7.392
40	7.194	7.285	7.302	7.319	7.339
45	7.115	7.202	7.219	7.235	7.254
50	7.043	7.121	7.138	7.153	7.171
55	6.972	7.041	7.059	7.074	7.091

<sup>a</sup>Units of  $m$ , mol·kg<sup>-1</sup>.

**Table 3.**  $p(a_{\text{H}\gamma_{\text{Cl}}})$  of (TES + NaTES) buffer solutions from 5°C to 55°C, computed using Equation (4)<sup>a</sup>.

$t$ (°C)	0.05 m TES + 0.05 m NaTES + 0.11 m NaCl $I = 0.16 \text{ m}$	0.02 m TES + 0.04 m NaTES + 0.12 m NaCl $I = 0.16 \text{ m}$	0.03 m TES + 0.06 m NaTES + 0.10 m NaCl $I = 0.16 \text{ m}$	0.04 m TES + 0.08 m NaTES + 0.08 m NaCl $I = 0.16 \text{ m}$	0.05 m TES + 0.10 m NaTES + 0.06 m NaCl $I = 0.16 \text{ m}$
5	8.026	8.237	8.254	8.278	8.289
10	7.912	8.126	8.145	8.166	8.178
15	7.800	8.021	8.039	8.061	8.077
20	7.694	7.921	7.937	7.959	7.974
25	7.589	7.821	7.838	7.860	7.879
30	7.491	7.728	7.745	7.766	7.785
35	7.394	7.637	7.654	7.675	7.694
37	7.361	7.603	7.619	7.640	7.659
40	7.306	7.551	7.566	7.586	7.605
45	7.224	7.468	7.484	7.505	7.522
50	7.143	7.389	7.404	7.424	7.442
55	7.062	7.313	7.324	7.346	7.364

<sup>a</sup>Units of  $m$ , mol·kg<sup>-1</sup>.

The pH(s) values for solutions without liquid junction in the absence of NaCl were determined using the next Equation:

$$\text{pH}(s) = p(a_{\text{H}} \gamma_{\text{Cl}}^{\circ}) + \log \gamma_{\text{Cl}}^{\circ} \quad (4)$$

where the single-ion activity coefficient,  $\gamma_{\text{Cl}}^{\circ}$ , cannot be experimentally measured. A previous publication gives the method used for obtaining  $\gamma_{\text{Cl}}^{\circ}$  [10,15,16]. The pH values from the liquid junction cell are indicated by pH whereas the "conventional" pH calculated from Equayon. 5 is designated as pH(s). The Bates-Guggenheim convention [10,15] is commonly known as "pH convention" and is expressed by the Equation:

$$\log_{10} \gamma_{\text{Cl}}^{\circ} = -\frac{A\sqrt{I}}{1 + Ba^{\circ}\sqrt{I}} \quad (5)$$

where Equation (5) is valid only up to  $0.1 \text{ mol}\cdot\text{kg}^{-1}$ . Since blood and other physiological solutions have  $I = 0.16$

$\text{mol}\cdot\text{kg}^{-1}$ , there is a need for a better choice to calculate  $\log \gamma_{\text{Cl}}^{\circ}$ . Thus, a linear-dependent " $CI$ " term is added in the Bates-Guggenheim convention as shown in Equation (6):

$$\log_{10} \gamma_{\text{Cl}}^{\circ} = -\frac{A\sqrt{I}}{1 + Ba^{\circ}\sqrt{I}} + CI \quad (6)$$

where " $I$ " is the ionic strength of the buffer solution, the constants " $A$ ", " $B$ ", and  $a^{\circ}$  have the usual physical significances. The following empirical equation is used for the calculation of the adjustable parameter " $C$ " [8,10].

$$C = C_{25} + (6.2 \times 10^{-4})(t - 25) - (8.7 \times 10^{-6})(t - 25)^2 \quad (7)$$

where  $C_{25} = 0.032 \text{ kg}\cdot\text{mol}^{-1}$  at  $25^{\circ}\text{C}$  and  $t$  is the temperature in degrees Celsius.

The  $pa_{\text{H}}$  values listed in **Tables 4** and **5** for the TES buffer solution with and without the presence of NaCl

**Table 4.**  $pa_{\text{H}}$  of (TES + NaTES) buffer solutions from  $5^{\circ}\text{C}$  to  $55^{\circ}\text{C}$ , computed using Equations (4)-(6)<sup>a</sup>.

$t$ ( $^{\circ}\text{C}$ )	0.08 m TES + 0.08 m NaTES + 0.00 m NaCl $I = 0.08 \text{ m}$	0.02 m TES + 0.02 m NaTES + 0.14 m NaCl $I = 0.16 \text{ m}$	0.04 m TES + 0.04 m NaTES + 0.12 m NaCl $I = 0.16 \text{ m}$	0.06 m TES + 0.06 m NaTES + 0.10 m NaCl $I = 0.16 \text{ m}$	0.08 m TES + 0.08 m NaTES + 0.08 m NaCl $I = 0.16 \text{ m}$
5	7.767	7.846	7.865	7.887	7.908
10	7.659	7.736	7.755	7.777	7.799
15	7.549	7.630	7.649	7.669	7.691
20	7.450	7.529	7.548	7.567	7.588
25	7.354	7.429	7.449	7.468	7.488
30	7.262	7.335	7.354	7.372	7.393
35	7.174	7.224	7.262	7.279	7.299
37	7.138	7.210	7.227	7.244	7.264
40	7.091	7.156	7.174	7.190	7.210
45	7.011	7.073	7.090	7.105	7.124
50	6.938	6.991	7.008	7.023	7.041
55	6.867	6.909	6.927	6.943	6.960

<sup>a</sup>Units of  $m$ ,  $\text{mol}\cdot\text{kg}^{-1}$ .

**Table 5.**  $pa_{\text{H}}$  of (TES + NaTES) buffer solutions from  $5^{\circ}\text{C}$  to  $55^{\circ}\text{C}$ , computed using Equations (4)-(6)<sup>a</sup>.

$t$ ( $^{\circ}\text{C}$ )	0.05 m TES + 0.05 m NaTES + 0.11 m NaCl $I = 0.16 \text{ m}$	0.02 m TES + 0.04 m NaTES + 0.12 m NaCl $I = 0.16 \text{ m}$	0.03 m TES + 0.06 m NaTES + 0.10 m NaCl $I = 0.16 \text{ m}$	0.04 m TES + 0.08 m NaTES + 0.08 m NaCl $I = 0.16 \text{ m}$	0.05 m TES + 0.10 m NaTES + 0.06 m NaCl $I = 0.16 \text{ m}$
5	7.900	8.111	8.128	8.153	8.163
10	7.786	8.001	8.019	8.041	8.053
15	7.674	7.895	7.914	7.937	7.951
20	7.569	7.796	7.812	7.834	7.849
25	7.462	7.695	7.711	7.734	7.752
30	7.364	7.601	7.618	7.639	7.658
35	7.266	7.510	7.526	7.547	7.567
37	7.233	7.475	7.491	7.512	7.531
40	7.178	7.423	7.438	7.458	7.477
45	7.094	7.339	7.354	7.376	7.393
50	7.013	7.258	7.273	7.293	7.311
55	6.931	7.182	7.193	7.215	7.233

<sup>a</sup>Units of  $m$ ,  $\text{mol}\cdot\text{kg}^{-1}$ .

were calculated using the following equation:

$$1) \text{pa}_H = 7.35 - (1.90 \times 10^{-2})(t-25) - (8.98 \times 10^{-5})(t-25)^2 \quad (8)$$

in the temperature range of 5°C to 55°C. The standard deviation of regression for the  $\text{pa}_H$  of the chloride-free buffer solution was obtained using Equations (3), (4), (6), and (7). The standard deviation was 0.0012.

For the buffer solutions containing NaCl, with an isotonic saline media ionic strength of

$I = 0.16 \text{ mol} \cdot \text{kg}^{-1}$ , the  $\text{pa}_H$  values were also calculated using Equations. 3 - 7. The acidity function data,  $p(a_H \gamma_{\text{Cl}})$  from **Tables 2** and **3** were used to generate the  $\text{pa}_H$  data entered in **Tables 4** and **5**. These  $\text{pa}_H$  values are expressed by use of the quadratic equations:

$$2) \text{pa}_H = 7.431 - (1.93 \times 10^{-2})(t-25) - (6.80 \times 10^{-5})(t-25)^2 \quad (9)$$

$$3) \text{pa}_H = 7.449 - (1.94 \times 10^{-2})(t-25) - (1.22 \times 10^{-5})(t-25)^2 \quad (10)$$

$$4) \text{pa}_H = 7.468 - (1.95 \times 10^{-2})(t-25) - (6.86 \times 10^{-5})(t-25)^2 \quad (11)$$

$$5) \text{pa}_H = 7.489 - (1.96 \times 10^{-2})(t-25) - (6.66 \times 10^{-5})(t-25)^2 \quad (12)$$

$$6) \text{pa}_H = 7.463 - (2.02 \times 10^{-2})(t-25) - (8.46 \times 10^{-5})(t-25)^2 \quad (13)$$

$$7) \text{pa}_H = 7.696 - (1.93 \times 10^{-2})(t-25) - (7.20 \times 10^{-5})(t-25)^2 \quad (14)$$

$$8) \text{pa}_H = 7.713 - (1.94 \times 10^{-2})(t-25) - (6.91 \cdot 10^{-5})(t-25)^2 \quad (15)$$

$$9) \text{pa}_H = 7.735 - (1.94 \times 10^{-2})(t-25) - (7.12 \times 10^{-5})(t-25)^2 \quad (16)$$

$$10) \text{pa}_H = 7.752 - (1.92 \times 10^{-2})(t-25) - (6.42 \times 10^{-5})(t-25)^2 \quad (17)$$

The observed standard deviations of regression from Equations. 9 - 17 are 0.0014, 0.0009, 0.0006, 0.0006, 0.0009, 0.0008, 0.0010, 0.0009, and 0.0009, respectively.

The emf values of Cells (B) and (C), pH values with and without liquid junction, an the values of  $\delta E_j$  at 25 and 37°C are given in **Table 6**. These are various sources of error: 1) extrapolation of the  $p(a_H \gamma_{\text{Cl}})$  plot for  $\text{Cl}^-$  free solutions; 2) the calculation of the single ion activity coefficient  $\log \gamma_{\text{Cl}}^0$  using Equation (6); 3) the error in the experimental emf measurement; and 4) in the estimation of the liquid junction potential. For the four buffer solutions in **Table 6** the pH values obtained from the extended Debye-Hückel equations and liquid junction correction are in very good agreement ( $\pm 0.001$  pH unit). Thus these TES buffer solutions are recommended as useful secondary pH standard for blood serum and physiological application in the pH range 7.2 - 7.5. The authors have undertaken the calculation of the single ion

**Table 6. Emf of Cell B and pH values with  $\delta E_j$  correction at 25°C and 37°C for TES buffer.**

$m_1$	$m_2$	$m_3$	$I$	E/V		$\delta E_j^b / \text{mV}$		Without <sup>c</sup> $\delta E_j$ corr	With <sup>d</sup> $\delta E_j$ corr	Extended D-H eqn.	Without <sup>c</sup> $\delta E_j$ corr	With <sup>d</sup> $\delta E_j$ corr	Extended D-H eqn.
				25°C	37°C	25°C	37°C						
0.08	0.08	0.00	0.08	0.67873	0.67515	2.2	2.4	7.347	7.354	7.354	7.131	7.138	7.138
0.04	0.04	0.12	0.16	0.68263	0.67889	0.5	0.7	7.413	7.448	7.449	7.191	7.226	7.227
0.06	0.06	0.10	0.16	0.68375	0.67991	0.5	0.7	7.432	7.467	7.468	7.208	7.243	7.244
0.08	0.08	0.08	0.16	0.68491	0.68117	0.5	0.7	7.452	7.487	7.488	7.227	7.263	7.264
Emf of Cell C <sup>a</sup>													
0.008695 m KH <sub>2</sub> PO <sub>4</sub> + 0.03043 m Na <sub>2</sub> HPO <sub>4</sub>				0.68275	0.69147	2.6	2.9						

<sup>a</sup>Published data [4,6,8] for physiological phosphate buffer solutions; units of  $m$ , mol · kg<sup>-1</sup>. <sup>b</sup>  $E_j = E + -k \text{pH}(s)$  from Equation (1) and the residual liquid junction potential,  $\delta E_j = E_j(s) - E_j(x)$ , which can be calculated from the values of **Tables 4** and **5**. The pH of the primary standard phosphate buffer is 7.415 and 7.395 at 25°C and 37°C, respectively. <sup>c</sup>Values obtained from Equation (3) and **Table 6**. <sup>d</sup>Obtained from Equation (2) and emf values from **Table 6**. <sup>e</sup>Obtained from extended Debye-Hückel (DH) equation of the Bates-Guggenheim convention.

activity coefficient need for accurate pH calculation of several buffer solutions using Pitzer formalism [17,18].

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