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# Calibrating Remotely Sensed Ocean Chlorophyll Data: An Application of the Blending Technique in Three Dimensions (3D)

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#### **Abstract**

In this article, the extension to three dimensions (3D) of the blending technique that has been widely used in two dimensions (2D) to calibrate ocean chlorophyll is presented. The results thus obtained revealed a very high degree of efficiency when predicting observed values of ocean chlorophyll. The mean squared difference between the predicted and observed values of ocean chlorophyll when 3D technique was used fell far below the tolerance level which was set to the difference between *satellite* and observed *in-situ* values. The resulting blended field did not only provide better predictions of the *in situ* observations in areas where bottle samples cannot be obtained but also provided a smooth variation of the distribution of ocean chlorophyll throughout the year. An added advantage is its computational efficiency since data that would have been treated at least four times would be treated only once. With the advent of these results, it is believed that the modelling of the ocean life cycle will become more realistic.

#### **Keywords**

*In-Situ*, 3D-Blending, Satellite, Over-Relaxation Method, Calibration, Remotely Sensed Data

#### 1. Introduction

The ocean environment can be considered as a continuous physical system subject to changes depending on atmospheric and weather conditions. To describe changes in a continuous physical system, there is a need to study partial differential equations. [1] and [2] who have done much work on representation of physical systems using partial differential equations (PDE) make it clear that all physical systems exist in three space dimensions, and that representations in one or two space dimensions entails a large degree of approximations. It is on this basis that this research was motivated. Therefore

in this research, the two dimensional blending technique that was implemented by [3] in the case of predicting Sea Surface Temperature (SST) and also used by [4] who pioneered the calibration of Ocean Chlorophyll, is extended to three-dimensions (3D). The inspiration for this is that, since the *in situ* field is expected to have a smooth relationship with satellite as one move from one location to another, this smoothness may also apply across time (*day of data collection*) since the data fields run throughout the year. Thus time was seen as a possible additional dimension which could influence the relationship between *satellite* and *in situ* data fields. The idea of including time as a third variable had been proposed and implemented by [5] in their attempt to calibrate remotely sensed ocean chlorophyll-a data using the non-parametric approach of penalized regression spline described by [6]. In another instance, [7] also suggested the extension of the blending technique to three dimensions in order to render it more realistic. With the inclusion of time as a third variable, the blending problem now becomes a three-dimensional problem.

To perform the three-dimensional blending will require that the data fields are extracted in three-dimensions. In order to achieve this, data are required throughout the period of a year. Extraction and processing of the data were done using latitude, longitude and time (averaged over weeks) as variables for both the *satellite* and *in situ* fields, following the same procedure as in the two-dimensional case described in [8]. Using the successive 8-day interval approach, the year has 46 weeks. Thus the dimensions of the extracted working fields were  $241 \times 67 \times 46$ . The external latitudes and longitudes that had very few or no observations were removed, leaving a real working area of  $230 \times 65 \times 46$ . After extraction, the number of observations in the *in situ* field was 3999, and after some pre-processing the number dropped to 3450, the others being identified by the *satellite* as land. The total number of points in the working arena is 687,700, out of which 374,164 points are on the sea surface, with the *in situ* observations contributing only about 0.9% of the total observations in the ocean area.

#### 2. The Blending Procedure

During the blending process, we employ the use of the partial differential equation (PDE) in three-dimensions. This was necessary since the intension was to perform blending in three dimensions. This was achieved by introducing the time variable as the third dimension. By doing this, the belief is that the resulting blended field will be a better predictor since it is expected that chlorophyll concentration could also vary as the seasons or times of the year changes.

The general linear equations governing physical fields take the form:

$$A\frac{\partial^{2}U}{\partial x^{2}} + 2B\frac{\partial^{2}U}{\partial x \partial y} + C\frac{\partial^{2}U}{\partial y^{2}} = D\frac{\partial U}{\partial x} + E\frac{\partial U}{\partial y} + FU + G$$
 (1)

where U is the final blended field. From here the various types of PDE (that is; Parabolic, Elliptic and Hyperbolic) can be formed by attributing values which may be negative, positive or zero to each of the parameters from A to G.

In this article, emphasis is laid on the elliptic type of the partial differential equation and most importantly the Poisson equation. [9] states that the most often encountered of the elliptic PDE and indeed of all PDEs in applied physical sciences and physics, is

the Laplace's equation. This is a special case of the Poisson equation and it arises when all the terms on the right hand side of the Poisson equation equal zero. The prototypical elliptic equation in three dimensions is the Poisson equation of the form:

$$\frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} + \frac{\partial^2 U}{\partial z^2} = \rho(x, y, z), \qquad (2)$$

where the source term  $\rho$  is given. Thus, if this source term is equal to zero, the equations become Laplace's equation. The cross product term is not included because there is no theoretical foundation to expect convergence in such a case as seen in [10]. [3], who used the Poisson equation in the analysis of Sea Surface Temperature, stated that the advantage of the Poisson equation lies in its mode of solution and it also has the important benefit of behaving well numerically. Thus, when the equations are expanded by finite differencing into a set of linear algebraic equations, they can be solved iteratively to obtain a unique solution. This behaviour is especially convenient since the set of equations varies as the boundary points respond to changes.

Since the resulting matrix arising from this finite-differencing is sparse, it can be solved easily using the successive over-relaxation method. A somewhat more physical way of looking at the method, which also enhances convergence, is by making use of the diffusion equation. Therefore writing Equation (2) as a diffusion equation, with t as the time-step, the following equation is obtained.

$$\frac{\partial U}{\partial t} = \frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} + \frac{\partial^2 U}{\partial z^2} - \rho(x, y, z). \tag{3}$$

As  $t \to \infty$ , the solution to this problem is a solution to original elliptic Equation (2). Equation (3) can then be represented using finite differencing as:

$$\begin{split} U_{i,j,k}^{n+1} &= U_{i,j,k}^n \\ &\quad + \frac{\Delta t}{\Lambda^2} \Big( U_{i+1,j,k}^n + U_{i-1,j,k}^n + U_{i,j+1,k}^n + U_{i,j-1,k}^n + U_{i,j,k+1}^n + U_{i,j,k-1}^n - 6 U_{i,j,k}^n \Big) - \Delta t \rho_{i,j,k} \end{split}$$

where  $\Delta$  represents the difference between two points in either the i, j or k directions and  $\Delta t$  represents the time-step from one iteration to another. The solution of the system of linear simultaneous equations, resulting from this expression when all the boundary conditions have been applied, can be obtained by the over-relaxation method. [11] has established the procedures for obtaining the stability criterion and the over-relaxation parameter which are the two determinant elements used in facilitating convergence to the solution when solving PDEs by the successive over-relaxation (SOR) method in three dimensions.

After having obtained the stability criterion and the over-relaxation parameter for the three-dimensional case, the Gauss-Seidel scheme for solving the system of simultaneous equations resulting from this can be written in its extrapolated Liebmann form as follows:

$$\begin{split} U_{i,j,k}^{n+1} &= U_{i,j,k}^{n} + \alpha \bigg( \frac{1}{6} \Big( U_{i+1,j,k}^{n} + U_{i-1,j,k}^{n+1} + U_{i,j+1,k}^{n} + U_{i,j-1,k}^{n+1} + U_{i,j,k+1}^{n} + U_{i,j,k-1}^{n+1} - 6U_{i,j,k}^{n} \Big) \\ &- \frac{\Delta^{2}}{6} \rho_{i,j,k} \bigg). \end{split}$$

As seen in [12], this can be written in short form as

$$U_{i,j,k}^{n+1} = U_{i,j,k}^{n} + \alpha R_{i,j,k}^{n}$$

where

- 1)  $R_{i,j,k}^n = \nabla^2 U_{i,j,k} \rho_{i,j,k}$  is the residual which must be less than a stated tolerance limit  $\varepsilon$  for convergence to be attained, and  $\nabla^2 U_{i,j,k}$  is calculated from the recently obtained U as  $\nabla^2 U_{i,j,k} = U_{i+1,j,k}^n + U_{i-1,j,k}^{n+1} + U_{i,j+1,k}^n + U_{i,j-1,k}^{n+1} + U_{i,j,k+1}^{n+1} + U_{i,j,k-1}^{n+1}$ ,
  - 2) The superscript *n* is the iteration number, while
  - 3)  $\alpha$  is the over-relaxation parameter.

This scheme is then iterated until convergence is attained. The convergence set thus obtained is the blended field of the process. [13] provides some guidelines on how to build computer codes to solve systems of algebraic equations. Meanwhile a general idea of how to write programs in Fortran is provided by [14] while [15] provides an engineering approach to Fortran programming. Program written were then interfaced in the R programming environment for statistical analysis and graphical display of the results obtained. [16] [17] [18] were used as guides to writing the R-codes.

#### 3. Blending in 3D

Following the procedure for solving the three-dimensional PDE using the relaxation method as described in [12], the blending process was carried out using the observed data fields. In addition [8] had shown that the "corrector factor" method performs better than the original blending technique in the prediction of ocean chlorophyll, hence this technique was also employed. The image plots in **Figures 1-12** show the distribution

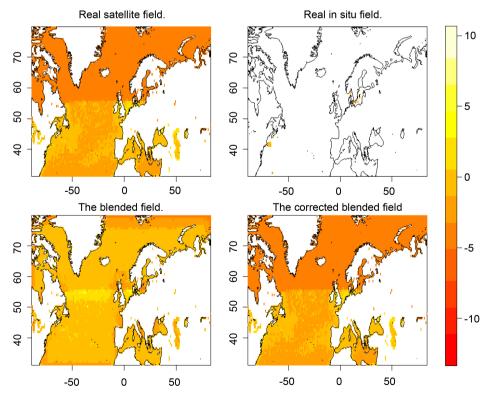


Figure 1. Predictions for month of January.

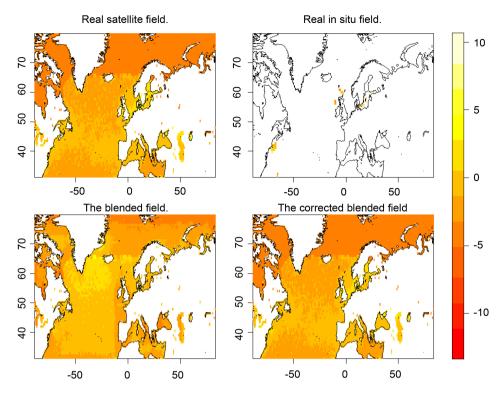


Figure 2. Predictions for month of February.

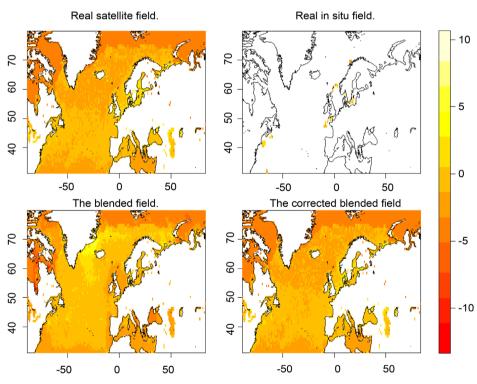


Figure 3. Predictions for month of March.

of chlorophyll density from the satellite, *in situ*, the normal blended and corrector factor blended fields for the twelve months of the year using the 3D blending method.

These plots are not monthly means, but are selected weeks which fall within the

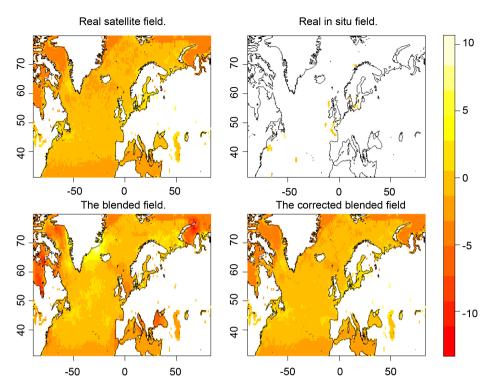


Figure 4. Predictions for month of April.

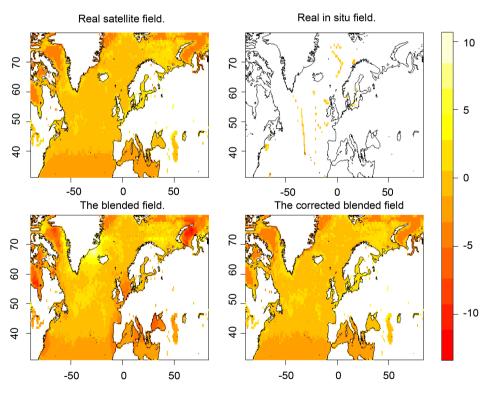


Figure 5. Predictions for month of May.

months and have been selected in such a way that each week should fall approximately in the middle of the month. The motivation behind this is to see how the availability of observations from both the satellite and *in situ* fields could influence the resulting

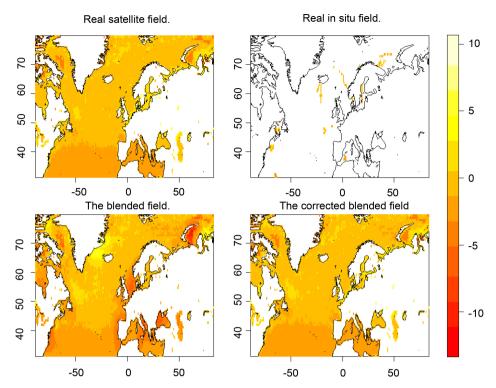


Figure 6. Predictions for month of June.

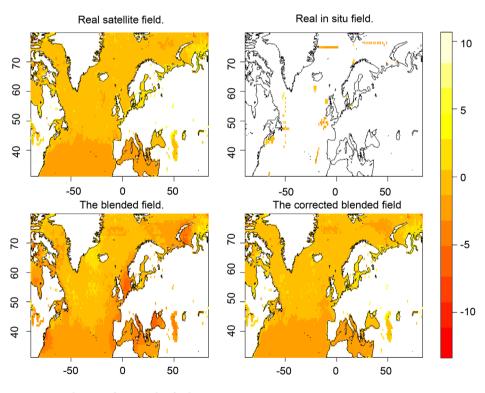


Figure 7. Predictions for month of July.

blended fields from both the normal blending and the corrector factor methods. This will also be able to indicate any existing trend in the ocean chlorophyll concentration from month to month throughout the whole year. This objective is achieved in the case

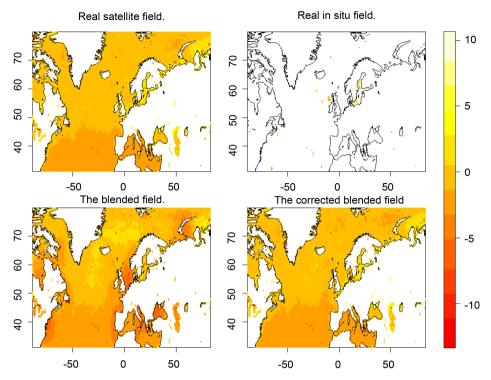


Figure 8. Predictions for month of August.

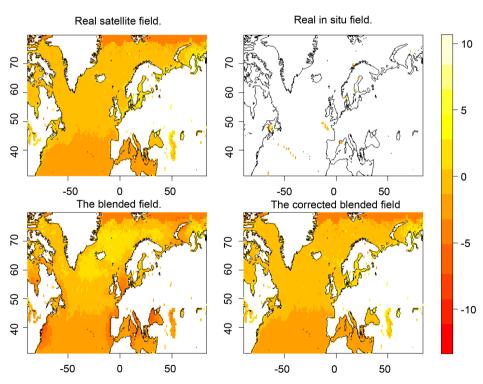


Figure 9. Predictions for month of September.

of three-dimensions; *in situ* and satellite observations from neighbouring weeks have some influence on the chosen week since the blending process moves across data for the whole year. Thus the effects of the observed values cut across the whole year resulting in a smooth transition from month to month. This trend can be seen in the gradual

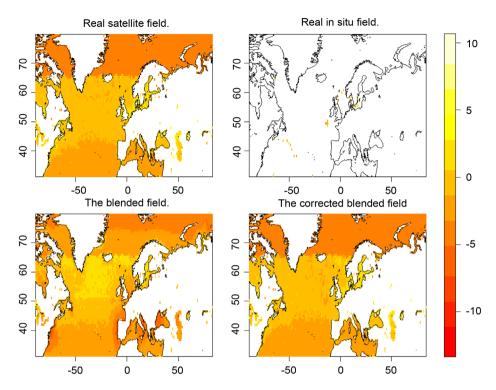


Figure 10. Predictions for month of October.

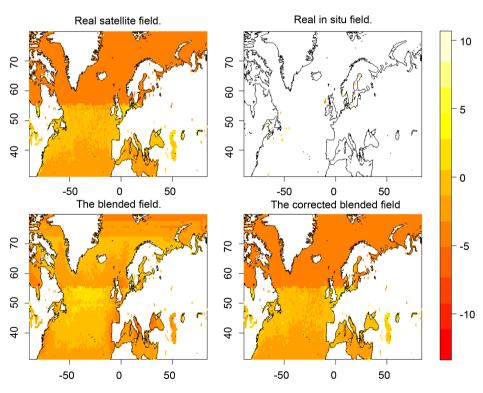


Figure 11. Predictions for month of November.

change of colour in the plots of the density of chlorophyll plots from Figures 1-12. Lower values are seen during the winter and autumn periods with higher densities in spring and summer as expected.

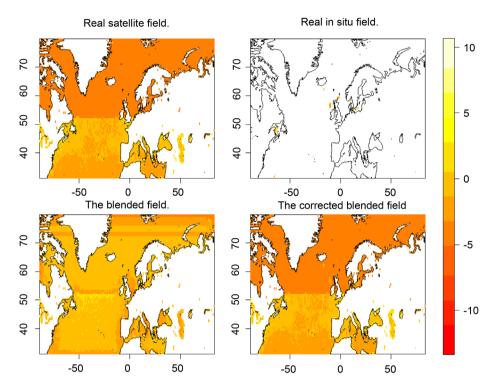


Figure 12. Predictions for month of December.

#### 4. Validating the Performance of the 3D Blending Technique

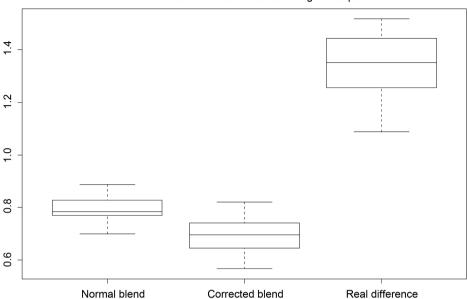
The resulting blended field from both the original blending method and the corrector factor blending method were then subjected to a validation study to assess their ability to predict the observed *in situ* chlorophyll. Randomly selected test sets each of size 500 were taken from the *in situ* field. The remaining field is then introduced into the blending process. The box plots in **Figure 13** show the range of the mean squared differences between predictions from both methods and the observed *in situ* values.

The range of the mean squared differences between the real satellite and *in situ* fields in the samples is also plotted to give an indication of the improvements provided by both processes.

From the validation study, it is clear that the resulting blended field from the corrector factor method is still the best even in the case of the three dimensional blending. To prove its power of prediction over the original blending method, the corrector factor predictions were much closer to the observed *in situ* values than the predictions from the original blending method though both methods show a great improvement on the prediction of *in situ* as opposed to the raw satellite field. The codes for running the validation study and plotting of the results were written in R as developed by [19].

#### 5. Comparing 2D and 3D

The idea here is to verify the authenticity of the three-dimensional blending which has been introduced. The expectation is that the predictions from the three-dimensional blending should closely match the predictions from the two-dimensions at any chosen point. In this case, the monthly predictions from the three-dimensions are plotted and



### Mean squared differences between predicted and observed in situ values from the normal and corrector factor blending techniques

**Figure 13.** A box plot of the mean squared difference between predicted and observed *in situ* values from both the normal blending and the corrector factor methods using blending in three-dimensions; this can be compared with the corresponding box plot from the differences between the observed satellite and *in situ* samples.

to be compared with monthly blended fields obtained from the two-dimensional blending. The images are shown in Figure 14 and Figure 15. Recall that the data fields in three dimensions contain data for the whole year divided into 46 weeks. Hence the selection of monthly data is based on the weeks that fall in the middle of the month and not on monthly averages. Since the selected data fields are maintained for both processes, the effect is expected to be the same. Data used for the two-dimensional blending here were extracted from the three dimensional data fields according to the selected weeks described above. The images plotted here are from the three-dimensional blended field selected according to the weeks chosen to represent each month in the two-dimensional blending.

From the image plots, it is very clear that the predictions from both methods are very close to each other in areas where observations exist for both data fields. In the case where observations are present only from the *in situ* field, their effect on the predicted field is more prominent in the two-dimensional case than in the three-dimensions. This can be seen from the plots of predictions for the months of November, December and January where there are some *in situ* observations around the North East Atlantic in areas where satellite could not provide readings during these periods. This feature is not outstanding in the three-dimensional case. The reason for this difference is that in two-dimensional blending these observed *in situ* values stand independently as the only boundary values in an area where the satellite field initially had no observations, thus their effect dominates the blending process for that chosen week, whereas in the case of three-dimensions, *in situ* and satellite observations from neighbouring weeks have some influence on the chosen week since the blending process moves across data for

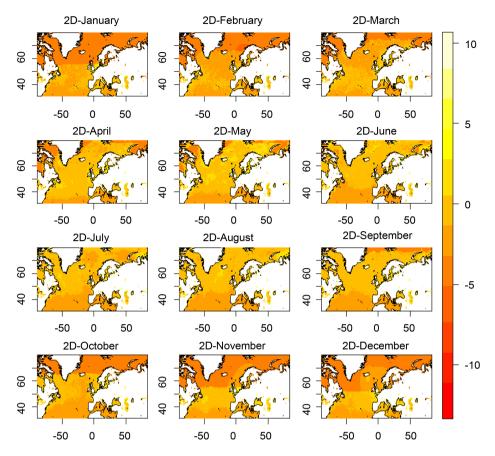


Figure 14. Predictions from the 2D blending technique.

the whole year. Thus the effects of the observed values cut across the whole year resulting in a smooth transition from month to month. This can be seen from the gradual change of colour within and between the monthly plots. A trend can be seen with respect to the density of chlorophyll throughout the year. Lower values are seen during the winter and autumn periods with higher densities in spring and summer as expected.

#### 6. Conclusions

In this research, the blending technique traditionally used in two dimensions to predict ocean chlorophyll concentration in areas where ship and buoy could not obtain values has been successfully extended to three dimensions. This was based on the fact that most physical and environmental problems exist in three dimensions, thus representing blending procedure in three dimensions would render it more realistic. The "corrector factor" method which was shown by [8] to be a better way of implementing the blending technique was used. The resulting blended field did not only provide better predictions of the *in situ* observations in areas where bottle samples could not be obtained but also provide a smooth variation of the distribution of ocean chlorophyll throughout the year.

In addition, the three-dimensional technique has the advantage that it reduces computer time and memory since a process that could have been done twelve times by months or at least four times by season if the normal two-dimensional method was to

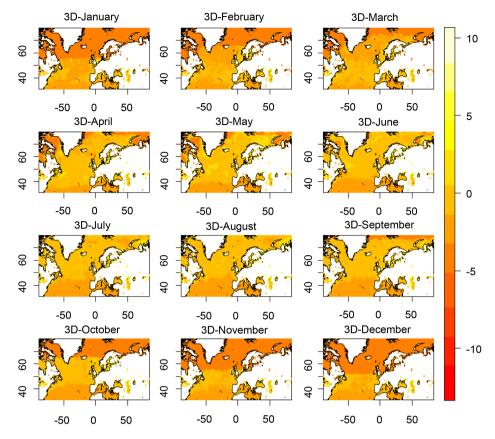


Figure 15. Predictions from the 3D blending Technique.

be used will simply be done once by employing the three-dimensional technique. Apart from this computational advantage, the physical advantage was seen when predictions over a year's period were made using both the two and three-dimensional blending.

Another advantage of the three-dimensional blending over two dimensions is that it maintains a smooth variation between data from month to month thus providing a trend for the whole year rather than producing independent monthly or quarterly trend which is obtained when using the two-dimensional technique.

This implies that the three-dimensional blending method can serve as a better approach to the blending procedure in particular and to all other processes which employ the use of the elliptic partial differential equations in their operations. With the advent of these results, it is believed that the modelling of the ocean life cycle will become more realistic.

#### 7. Future Work

The improvement realised by the 3D Technique could be made more realistic by introducing the penalised technique. This could render these results more accurate as shown by [7].

#### References

[1] Vemuri, V. and Karplus, W. (1981) Digital Computer Treatment of PDE. Prentice Hall Inc., New Jersey.

- [2] Ames, W.F. (1972) Numerical Methods for Partial Differential Equation. 2nd Edition, Thomas and Sons Limited, Port of Spain.
- [3] Reynolds, R.W. (1988) A Real-Time Global Sea Surface Temperature Analysis. *Journal of Climate*, 1, 75-86. https://doi.org/10.1175/1520-0442(1988)001<0075:artgss>2.0.co;2
- [4] Gregg, W.W. and Conkright, M.E. (2001) Global Seasonal Climatologies of Ocean Chlorophyll; Blending in Situ and Satellite Data for Coastal Zone Colour Scanner era. Journal of Geophysical Research, 106, 2499-2515. https://doi.org/10.1029/1999JC000028
- [5] Clarke, E., Speirs, D., Heath, M., Wood, S., Gurney, W. and Holmes, S. (2006). Calibrating Remotely Sensed Chlorophyll-A Data by Using Penalized Regression Splines. *Journal of Royal Statistics Society*, 55, 331-353. <a href="https://doi.org/10.1111/j.1467-9876.2006.00540.x">https://doi.org/10.1111/j.1467-9876.2006.00540.x</a>
- [6] Wood, S.N. (2003) Thin Plate Regression Splines. *Journal of Royal Statistical Society, Series B*, **65**, 95-114. https://doi.org/10.1111/1467-9868.00374
- [7] Onabid, M.A. and Wood, S. (2014) Modeling Ocean Chlorophyll Distributions by Penalizing the Blending Technique. *Open Journal of Marine Science*, 4, 25-30. https://doi.org/10.4236/ojms.2014.41004
- [8] Onabid, M.A. (2011) Improved Ocean Chlorophyll Estimate from Remote Sensed Data: The Modified Blending Technique. African Journal of Environmental Science and Technology, 5, 732-747.
- [9] Brandt and Diskin, B. (1999) Multigrid Solvers for Non-Aligned Sonic Flows. SIAM Journal on Scientific Computing, 13, 273-501. https://doi.org/10.1137/S1064827598332205
- [10] Kallin, S. (1971) Numerical Methods and FORTRAN Programming. AUERBACH publisher Inc., Boca Raton.
- [11] Onabid, M.A. (2012) Solving Three-Dimensional (3D) Laplace Equations by Successive Over-Relaxation Method. *African Journal of Mathematics and Computer Science Research* 5, 204-208.
- [12] Oort, A.H. (1983) Global Atmospheric Circulation Statistics. NOAA Professional Paper 14, Nat. Oceanic and Atmospheric Administration (Silver Spring. Md.), 180 p.
- [13] Edgar, S.L. (1992) FORTRAN for the '90s Problem Solving for Scientists and Engineers. Computer Science Press, USA.
- [14] Calderbank, V. (1990) Programming in Fortran. 3rd Edition, Chapman and Hall, London.
- [15] Forsythe, C. (1997) Contemporary Computing for Engineers and Scientists Using Fortran90. PWS Publishing Company.
- [16] Dalgaard, P. (2002) Introductory Statistics with R. Springer, Boston.
- [17] Venables, W., Smith, D.M. and the R Development Core Team (2003) An Introduction to R. A Programming Environment for Data Analysis and Graphics. Version 1.8.0 Ed.
- [18] Wood, S.N. (2006) Generalized Additive Models: An Introduction with R. Chapman and Hall, CRC, London.
- [19] R-Core (2004) A Language and Environment for Statistical Computing. Version 2.0.1 Ed.



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