

Empirical Modeling of Annual Fishery Landings

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Received 12 March 2016; accepted 18 April 2016; published 21 April 2016

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Abstract

Forecasting plays an essential role in policy formulation and implementation especially in the management of fisheries resources. In this paper, various techniques of forecasting using time series analysis were evaluated on annual fishery production data. In addition to the Box-Jenkins approach, other methods such as the feed forward neural network and exponential smoothing approaches were also examined. A parsimonious model for each forecasting approach was then selected using penalized likelihoods. The chosen models were then evaluated based on their ability to produce accurate forecasts. Implications of the findings as discussed revealed that no particular method was ideal for modeling all landings. Hence when forecasting fishery landings, it is recommended that different structural approaches be compared before selecting an appropriate one for use.

Keywords

Artificial Neural Network, ARIMA, Exponential Smoothing, Forecasting, Fish, Ghana

1. Introduction

Rising fishing efforts (and/overexploitation) as well as climate change and their resultant impacts on fisheries stocks are most widely felt by local fisher folks who rely on fishing for their livelihoods. The impacts of these factors on fish stocks (e.g. species abundance, local extinction/disappearance) are discussed elsewhere [1]-[4]. Generally, fluctuations in a country's annual landings may lead to varying levels of fish imports to augment production shortfalls due to increasing demand. It is therefore imperative that the dynamics of fishery production be understood to allow for efficient management of the local resource base. Hence, estimation of future domestic supply/landings and demand is vital in this regard.

Scientists and policy makers widely rely on predictive models especially, for issues concerning management decisions in relation to fisheries resources. Two different approaches namely deterministic and stochastic models have been developed vis-à-vis forecasting of fisheries landings. Whereas the former is based primarily on the population dynamics theory, stochastic models emanate from the econometric and business literature. Since unobservable variables or unknown lagged processes may be involved in model building procedures, stochastic models are widely employed due to this specific comparative advantage over deterministic models [5].

Over the past decades, many stochastic models have been developed in both the time (Box-Jenkins and smoothing methods) and frequency (spectral and wavelength analysis) domains. Also, artificial neural networks have been proposed recently and successfully applied to modeling time series data. The applications of time series are diverse including but not limited to disciplines such as ecology [6]-[8], economics [9]-[11] and medicine [12] [13] among others. In fisheries research however, time series approaches such as artificial neural network and Autoregressive Moving Average models have been used in some studies [14]-[16]. Due to the principal role predictive models play in key management decisions; this work examined the comparative accuracies of different univariate time series approaches in forecasting annual fishery landings.

2. Data and Methods

This study employed yearly data on total fish (TFL) and *Sardinella maderensis* (SML) landings in Ghana to demonstrate the efficacies of the different time series models used herein. Annual totals of fish production from 1950 to 2013 were obtained from the Food and Agriculture Organization (FAO) fisheries statistics database [17]. However, annual landings of *S. maderensis* were obtained from the work of [18]. The data constituted a portion of the reconstruction of marine fish catches in Ghana from 1950 to 2010. Each data was subsequently split into a training set (minimum of 50 points) and a test set (10 points). The training set was used to estimate the parameters of the various structural models whereas the test set was used to evaluate their performance.

The ensuing sections briefly describe the theoretical concepts of the techniques employed in the study. Since the data are annual production estimates, only non-seasonal models were considered and elaborated on. All analyses were performed using “R” statistical software [19].

2.1. Exponential Smoothing Models (ETS)

2.1.1. Naïve

Basically, the naïve forecasting approach was employed in order to compare forecasting improvements made by the other methods. This technique always predicts a flat horizontal line in that the best one-step-ahead forecast is the value of the current period. The equation is expressed as:

$$\hat{F}_t(m) = y_t \quad (1)$$

2.1.2. Simple Exponential Smoothing (NN)

This technique is best suited for time series data that do not exhibit prevalent trend and seasonality. The general form of the equation is expressed as:

$$L_t = \alpha Y_t + (1 - \alpha) L_{t-1} \quad (2a)$$

$$\hat{F}_t(m) = L_t \quad (2b)$$

Both the “NN” and Naïve models are equivalent when the value of $\alpha = 1$.

2.1.3. Holt’s Linear Method (AN)

This two parameter exponential smoothing model was developed to appropriately handle time series exhibiting a prevalent linear trend [20]. The recursive form of the equation is given by:

$$L_t = \alpha Y_t + (1 - \alpha)(L_{t-1} - T_{t-1}) \quad (3a)$$

$$T_t = \beta(L_t - L_{t-1}) + (1 - \beta)T_{t-1} \quad (3b)$$

$$\hat{F}_t(m) = L_t + mT_t \quad (3c)$$

However, this method is equivalent to Brown's double exponential smoothing model only if the values of α and β are the same.

2.1.4. Modified Holt's Method (A_dN)

A study by [21] revealed that the "AN" often over estimated trend hence, they introduced a dampening constant (δ) to diminish it. The recursive form of this modified equation is given by:

$$L_t = \alpha Y_t + (1 - \alpha)(L_{t-1} - \delta T_{t-1}) \quad (4a)$$

$$T_t = \beta(L_t - L_{t-1}) + (1 - \beta)\delta T_{t-1} \quad (4b)$$

$$\hat{F}_t(m) = L_t + \sum_{i=1}^m \phi^i T_t \quad (4c)$$

2.1.5. Pegels' Method (MN)

Time series that show either a multiplicative or exponential trend are best modeled using Pegels approach [22]. The method is characterized by the equations below:

$$L_t = \alpha Y_t + (1 - \alpha)(L_{t-1} R_{t-1}) \quad (5a)$$

$$R_t = \beta(L_t / L_{t-1}) + (1 - \beta)R_{t-1} \quad (5b)$$

$$\hat{F}_t(m) = L_t R_t^m \quad (5c)$$

2.1.6. Modified Pegels' Method (M_dN)

Similar to the "A_dN", the "MN" was modified by adding a dampening parameter (δ) to control exponential growth [23]. The general form of the equation is written as:

$$L_t = \alpha Y_t + (1 - \alpha)(L_{t-1} R_{t-1}^\delta) \quad (6a)$$

$$R_t = \beta(L_t / L_{t-1}) + (1 - \beta)R_{t-1}^\delta \quad (6b)$$

$$\hat{F}_t(m) = L_t R_t^{\sum_{i=1}^m \delta^i} \quad (6c)$$

where applicable for each exponential smoothing model, Y_t = the time series at the period t ; L_t = level, T_t = trend; R_t = growth rate; α = smoothing coefficient for level; β = smoothing coefficient for trend/growth rate; and $\hat{F}_t(m)$ = smoothed forecast value for Y .

2.2. Autoregressive Integrated Moving Average (ARIMA) Model

This model takes into account past values of the data, prediction errors and a random term [24]. Thus, the Autoregressive (p) portion indicates that the current value of the series can be explained as a function of past values while the Moving Average (q) part also shows that the present has a relationship with past shocks. The ARIMA (p, d, q) process is mathematically expressed as:

$$\phi(B)(\Delta^d Y_t - \mu) = \theta(B)e_t \quad (7)$$

where Y_t = the time series at period t ; μ = mean of $\Delta^d Y_t$; $\phi(B) = 1 - \phi_1 B - \dots - \phi_p B^p$; $\theta(B) = 1 - \theta_1 B - \dots - \theta_q B^q$; ϕ_i and θ_i denote the i th autoregressive and moving average parameters respectively; d is the differenced order parameter of the process; B and Δ represent lag and difference operators respectively. In fitting the model, a three-step procedure namely identification, estimation and diagnosis was followed.

2.2.1. Unit Root Test

Before building the ARIMA models, a test of stationarity was performed on the fishery landing data using the Kwiatkowski-Phillips-Schmidt-Shin (KPSS) test [25]. The KPSS test is based on the model:

$$Y_t = X_t + \varepsilon_t \quad (8)$$

$$X_t = X_{t-1} + v_t, \quad v_t \sim \text{iid}(0, \sigma_v^2) \quad (9)$$

where X_t is a random walk with white noise ε_t . The null hypothesis that Y_t is $I(0)$ is simply given as $H_0 : \sigma_v^2 = 0$ while the alternative is $H_A : \sigma_v^2 > 0$. The test statistic is written as

$$\text{KPSS} = T^{-2} \sum_{t=1}^T S_t^2 / \hat{\sigma}_\infty^2 \quad (10)$$

where $t = 1, 2, \dots, T$ is the number of observations; $S_t = \sum_{j=1}^t \hat{\omega}_j$, $\hat{\omega}_j = Y_t - \bar{Y}$ is the residual of Y_t and;

$\hat{\sigma}_\infty^2 = \lim_{T \rightarrow \infty} T^{-1} \text{var} \left(\sum_{t=1}^T \varepsilon_t \right)$ is a consistent estimate of the long-run variance of ε_t .

The null hypothesis of stationarity is rejected if the calculated test statistic is larger than the critical value at a significance level of 5%.

2.3. Artificial Neural Network (ANN) Model

ANNs are simplified models of the biological neural system. The operating principles of this method are fully documented elsewhere [26]. However, in this study, a feed forward network with a single hidden layer was employed due to its general applicability to a variety of different problems [27]. Thus, the Neural Network Autoregression (NNAR) model fitted with lagged values of the series as inputs was used [28]. The general form of the prediction equation [29] for computing forecasts may be written as:

$$\hat{x}_t = \phi_o \left[w_{co} + \sum_h w_{ho} \phi_h \left(w_{ch} + \sum_i w_{ih} x_{t-j_i} \right) \right] \quad (11)$$

where $x_{t-j_1}, \dots, x_{t-j_k}$ are the input terms at lags j_1, \dots, j_k ; $\{w_{ch}\}$ are the weights for the connections between the constant input and the hidden neurons; $\{w_{co}\}$ is the weight of the direct connection between the constant input and the output; $\{w_{ih}\}$ and $\{w_{ho}\}$ respectively represent the weights for other connections between the input and hidden neurons and between the hidden and output neurons; ϕ_h and ϕ_o respectively symbolize the activation functions that define mappings from inputs to hidden nodes and from hidden nodes to output(s).

2.4. Model Selection and Diagnostics

Penalized likelihood methods like Akaike's Information Criterion (AIC), Corrected Akaike's Information Criterion (AICC) and Bayesian Information Criterion (BIC) were used to select the most appropriate model within groups of competing models. This approach was preferred to measures of forecast error since it penalizes against models with too many parameters. However, due to inconsistent estimators produced by the AIC and AICC, BIC was preferred during model selection.

An overall check of adequacy for the selected models was then conducted using both Ljung-Box and Box-Pierce tests to determine whether residuals are random and independent over time. An ARCH-LM test was also performed on the final models to check for homoscedasticity of model residuals. After selecting and diagnosing the most parsimonious model within each group of competing models, the different structural models were compared using measures of forecast accuracy such as Mean Percent Error (MPE), Mean Absolute Error (MAE), Root Mean Square Error (RMSE), Mean Absolute Percent Error (MAPE) and Mean Absolute Scaled Error (MASE). For each forecast error estimation lower values are preferred. However, much preference was given to MASE during model comparisons since it was proposed to handle deficiencies in both MAPE and scale-dependent (RMSE, MAE) error measures [30].

3. Results

3.1. Model Building and Diagnostics

The various techniques outlined in the previous section have been applied to model annual fishery production

data (Figure 1). With regards to the exponential smoothing approach, the selection criteria favored Pegels' method ($\alpha = 0.8140$, $\beta = 0.1008$) for total fishery landings (TFL). In modeling annual landings of *S. maderensis* (SML) however, the simple exponential smoothing ($\alpha = 0.1216$) method was preferred based on information theoretic approaches (Table 1).

In order to fit the ARIMA models, the stationarity of the two series were first investigated. The results of the KPSS test revealed that both total (KPSS = 2.6541, $P = 0.01$) and *S. maderensis* (KPSS = 1.6118, $P = 0.01$) series were not stationary. Hence, each dataset was first differenced to make it stationary such that it fluctuated about the zero point indicating constant mean and variance (TFL – KPSS = 0.0644, $P = 0.1$; SML – KPSS = 0.0218, $P = 0.1$; see Figure 2). The rapid decay in the autocorrelation function (ACF) and partial autocorrelation function (PACF) further affirmed the stationarity of the differenced series (TFL and SML) (Figure 3). Various tentative models were then fitted and compared as presented in Table 1 using identified orders of ARIMA ($p, 1, q$) based on the ACF and PACF plots. For total landings, an ARIMA (0, 1, 0) with drift was chosen since it recorded minimum values for all information criteria values (i.e. drift = 7089.094, SE = 4696.534). However, ARIMA (0, 1, 1) with drift was suitable for modeling annual *S. maderensis* landings (i.e. MA1 = -1.000, SE = 0.0541; drift = -0.741, SE = 0.136) based on the selection criteria.

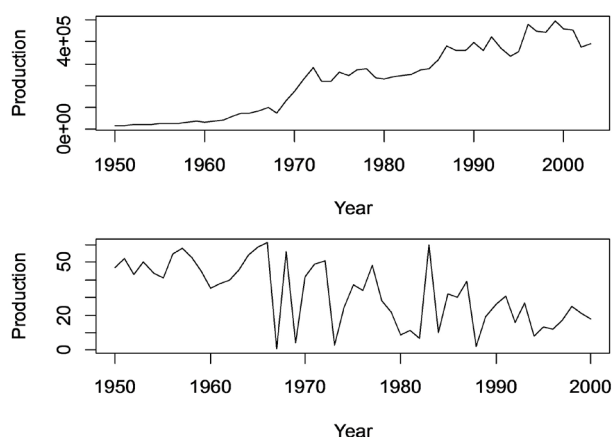


Figure 1. Time series plot of fishery landings from Ghanaian waters: top—total production (TFL), bottom—*S. maderensis* (SML).

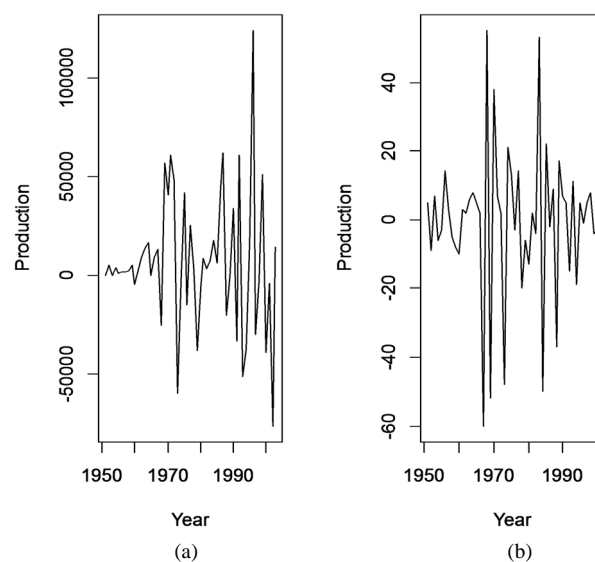


Figure 2. Time series plot of the differenced series: (a) TFL; (b) SML.

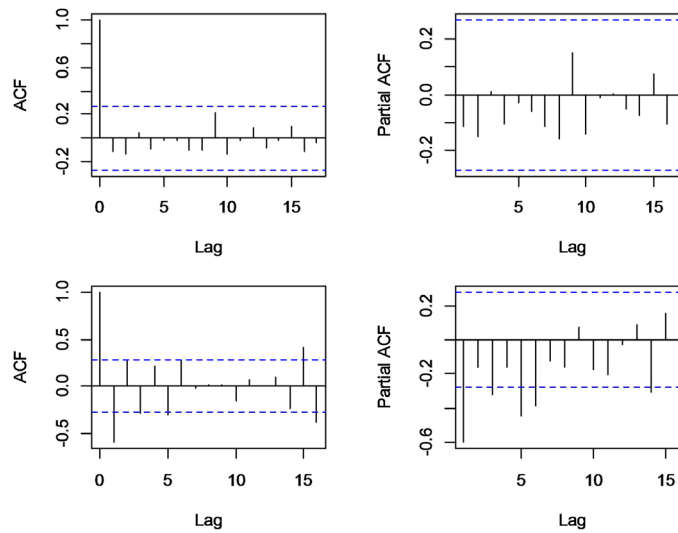


Figure 3. Correlogram (ACF and PACF) of differenced series for fishery landings: Top panel—TFL, Bottom panel—SML.

Table 1. Tentative models employed for forecasting fishery landings.

Technique		Total fishery landings (TFL)			<i>S. maderensis</i> landings (SML)			
	Model	AIC	AICC	BIC	Model	AIC	AICC	BIC
Exponential Smoothing	NN	1320.55	1320.79	1324.53	NN	481.77	482.02	485.64*
	AN	1308.01	1308.83	1315.97	AN	478.01*	478.88*	485.73
	MN	1307.13	1307.95	1315.09*	MN	496.06	496.93	503.79
	A _d N	1310.62	1311.87	1320.57	A _d N	485.11	486.44	494.77
	M _d N	1306.28*	1307.53*	1316.22	M _d N	481.40	482.73	491.06
		Total fishery landings (TFL)			<i>S. maderensis</i> landings (SML)			
	Model	AIC	AICC	BIC	Model	AIC	AICC	BIC
ARIMA Method	(0, 1, 0)	1260.28	1260.36	1262.25	(0, 1, 1)	422.07	422.32	425.89
	(0, 1, 1)	1261.99	1262.23	1265.93	(1, 1, 1)	423.03	423.55	428.77
	(1, 1, 0)	1262.03	1262.27	1265.97	-	-	-	-
	<i>Model with drift</i>				<i>Model with drift</i>			
	(0, 1, 0)	1236.31*	1236.55*	1240.25*	(1, 1, 0)	425.26	425.78	430.99
	(0, 1, 1)	1237.38	1237.87	1243.29	(0, 1, 1)	408.53*	409.05*	414.27*
	(1, 1, 0)	1237.63	1238.12	1243.54	(1, 1, 1)	409.10	409.98	416.74
	-	-	-	-	(2, 1, 1)	411.02	412.38	420.58

*Means best model based on selection criterion.

These different model structures were then compared to the automatically estimated NNAR(1) and NNAR(7) feed-forward networks for total and *S. maderensis* landings respectively. The results presented in **Table 2** indicate that all the parsimonious models chosen are adequate in accordance with the Ljung-Box (except only ARIMA for SML) and Box-Pierce tests. The homoscedasticity of model residuals were confirmed by the ARCH-LM test which failed to reject the null hypothesis of ARCH effects for the different structural models (**Table 2**).

3.2. Model Comparisons

As mentioned in the previous section, it should be noted that the naïve model was employed to compare forecast improvements made by the other methods. Forecast plots of the various models selected compared to the test set revealed that the ARIMA model clearly fitted the trend wrongly for total landings (Figure 4). The forecast accuracies of the various models developed for total fishery production are presented in Table 3. The results again show that the ARIMA model over-fits performing well on the training set and poorly on the test set. With none of the two over fitting the data set, both ANN and naïve models performed well as they recorded low forecast

Table 2. Diagnostic tests on residuals of various structural models.

Landing/Method		df	Box-Pierce test		Ljung-Box test		ARCH-LM test	
			χ^2	<i>P</i> -value	χ^2	<i>P</i> -value	χ^2	<i>P</i> -value
TFL	Naïve	10	6.517	0.770	7.761	0.652	14.765	0.141
	ETS (MN)	10	6.719	0.752	7.817	0.647	6.234	0.795
	ARIMA	10	6.640	0.759	7.880	0.641	12.461	0.255
	ANN	10	4.683	0.911	5.644	0.844	6.337	0.786
SML	Naïve	10	38.269	3.407e−05	42.276	6.696e−06	13.690	0.188
	ETS (NN)	10	13.992	0.173	16.382	0.089	2.993	0.982
	ARIMA	10	18.033	0.0544	20.866	0.022	6.259	0.793
	ANN	10	7.636	0.664	9.410	0.494	10.500	0.398

Table 3. Accuracy measures of the different forecasting structural models.

Model Approach		RMSE	MAE	MPE	MAPE	MASE
Total Fishery Landings (TFL)						
Training set	Naïve	34,601.240	23,756.570	4.802	11.386	1.000
	ETS (MN)	38,555.670	26,070.540	−3.900	11.910	1.097
	ARIMA	33,552.200	23,103.790	−3.643	12.606	0.973
	ANN	31,787.550	21,790.550	−3.072	11.222	0.917
Test set	Naïve	33,516.810	27,312.900	−5.423	7.694	1.150
	ETS (MN)	43,310.440	35,583.770	−8.817	10.051	1.498
	ARIMA	69,589.190	60,919.700	−16.053	16.998	2.564
	ANN	35,431.410	28,760.270	−6.190	8.121	1.211
Sardinella Madrensis Landings (SML)						
Training set	Naïve	21.800	14.540	−222.036	259.513	1.000
	ETS (NN)	15.725	11.596	−190.238	208.178	0.798
	ARIMA	14.003	10.671	−145.741	171.006	0.734
	ANN	4.000	2.990	−33.284	41.305	0.206
Test set	Naïve	15.994	12.200	−27.503	74.212	0.839
	ETS (NN)	15.266	11.800	−45.206	82.238	0.812
	ARIMA	20.763	14.824	34.703	51.093	1.020
	ANN	16.796	12.460	−13.516	67.634	0.857

error values compared to the others (*i.e.* “ETS” and ARIMA). With regards to *S. maderensis*, the ANN model over-fits performing well on the training set and poorly on the test set for most error metrics (Table 3). An examination of Figure 5 however reveals that the ARIMA model underestimates compared to the others. Here, the exponential smoothing approach was superior to the other methods based on all forecast accuracy measures except MAPE.

In order to reliably select an appropriate model, a cross-validation test was further performed and the results presented in Figure 6 and Figure 7. It is observable that ANNs outperform all other models at every forecast

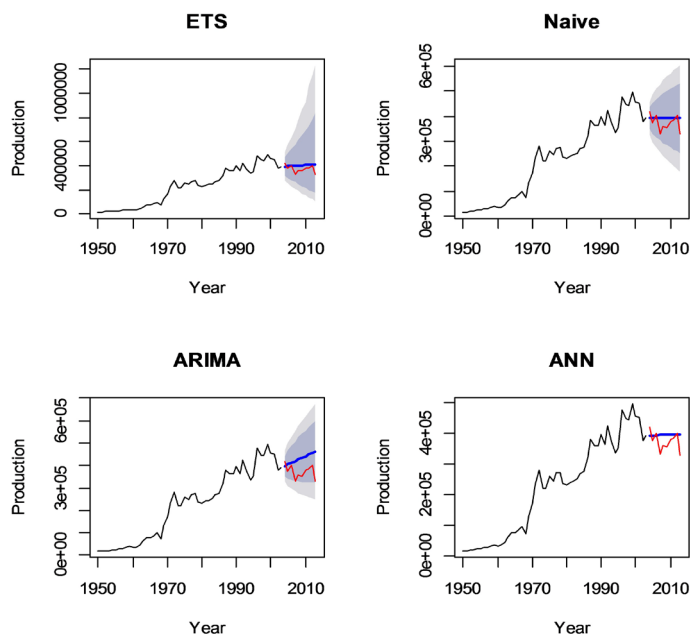


Figure 4. Comparison of forecast plot (blue line) generated by various forecasting models to the test set (red line)—TFL.

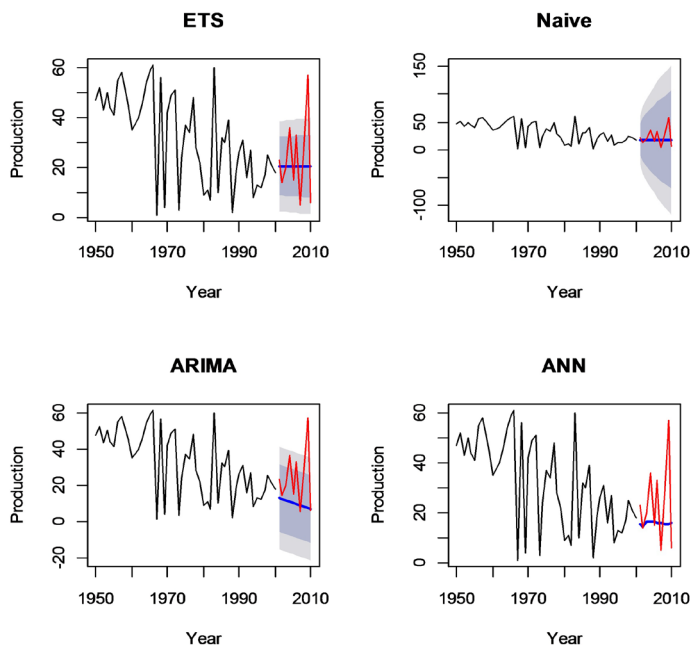


Figure 5. Comparison of forecast plot (blue line) generated by various forecasting models to the test set (red line)—SML.

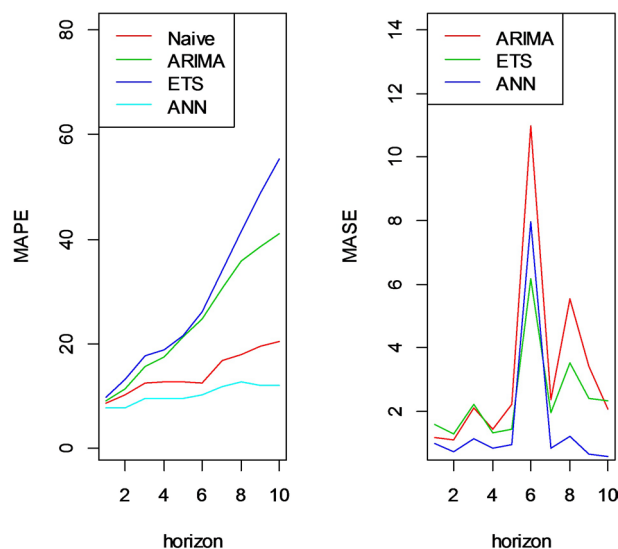


Figure 6. “Cross-validation” of the different structural models—TFL.

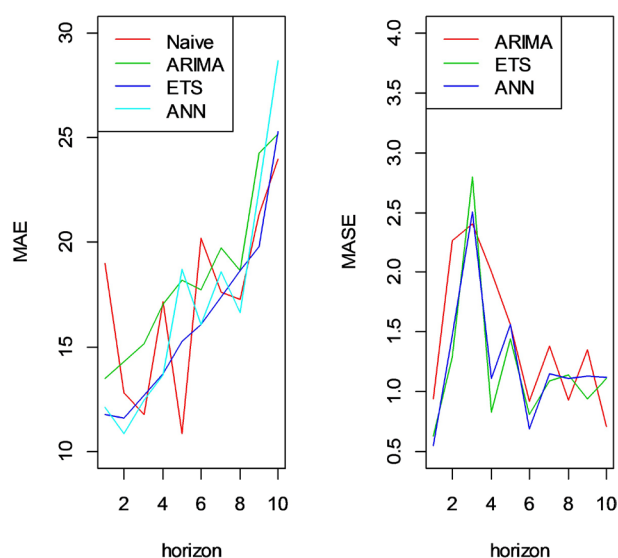


Figure 7. “Cross-validation” of the different structural models—SML.

horizon for total fishery landings (ETS was second best using MASE). However, the exponential smoothing technique was much more appropriate for modeling *S. maderensis* landings compared to the others (ANN was second best using MASE). Generally, the ARIMA technique performed poorly for both *S. maderensis* and total fishery landing forecasts.

4. Discussion

When investigating long term variation in fishery production, it is crucial to consider seasonal patterns of landings. However, such monthly time series data may not always be available in some situations. In spite of this, early recognition of production shortfalls based on available data (*i.e.* yearly landings) is significantly vital in averting depletion of fisheries stocks amidst threats of climate change and other associated pressures. Thus, in this paper, the main interest is to investigate and evaluate the effectiveness of various time series methods in forecasting annual fishery production.

In principle and practice (*i.e.* methods and results), the differences in the statistical models employed have been briefly demonstrated in the previous sections. Exponential smoothing methods are widely popular because they are robust and relatively easier to compute and apply. Also, the ability of the ARIMA model to capture historical information through AR and MA processes makes it very attractive to researchers especially after the advent of the Box-Jenkins methodology. One comparative advantage of ANNs over the two other methods used is that it can extract non-linear relationships within time series data. This is important since fishery stocks (*i.e.* abundance, distribution, etc.) may be affected by several factors such as anthropogenic and or climatic variables among others. This major advantage may have accounted for the good performance of ANNs on most forecast error metrics for total fishery landings (e.g. MASE, MAE, MAPE). The findings of this study (both TFL and SML) are also corroborated by other researches which revealed that ARIMA models perform poorly compared to ANNs [31] [32].

However, it is necessary that the limitations encountered be acknowledged. Firstly, this comparative study only applied three different forecasting techniques among the numerous approaches that exist in literature. For instance, Generalized Autoregressive Conditional Heteroscedasticity (GARCH) models have been proposed to handle various deficiencies in the ARIMA. Also, the feed forward neural network and more specifically the neural network autoregression model is one of several types of artificial intelligence approaches that can be used in time series analysis. However, these three forecasting approaches are employed herein because they are the most typically used by researchers.

As indicated by [33] and confirmed herein (*i.e.* exponential smoothing vs. ARIMA or ANN—e.g. SML), complex methods do not necessarily yield better forecast accuracies than simple ones. Also, though diagnostic tests revealed that all developed models were adequate, they produced varying forecast results. For instance, while the ARIMA model wrongly predicted the trend in fishery landings (e.g. increased TFL), the other approaches predicted otherwise. Thus, fishery resources will be impacted negatively (*i.e.* lead to overexploitation) if the ARIMA TFL model which forecasted a false steep rise in landings is considered in the management of the resource. This will in the long run have consequent effects on livelihoods and the economy as a whole. Hence, for efficient making and implementation of management decisions, it is vital that researchers and policy makers examine various time series approaches before applying an appropriate one to time series data.

5. Conclusion

Conclusively, research efforts on predicting fishery landings should be taxonomical (e.g. family, species, etc.) and/or resource specific (e.g. inland; marine—pelagic/demersal) in order to specifically target and ensure efficient management of the fisheries resource base to avoid overexploitation (and its resultant effects on fishery stocks).

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