

# Voltage Sag Characterization in a Distribution Systems: A Case Study

Suresh Kamble<sup>1</sup>, Chandrashekhar Thorat<sup>2</sup>

<sup>1</sup>Electrical Department, Government Polytechnic, Aurangabad, Maharashtra, India

<sup>2</sup>Principal Government Polytechnic, Aurangabad, Maharashtra, India

Email: [stkamble14@gmail.com](mailto:stkamble14@gmail.com), [csthorat@yahoo.com](mailto:csthorat@yahoo.com)

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## Abstract

Voltage sags caused by the short-circuit faults in transmission and distribution lines have become one of the most important power quality problems facing industrial customers and utilities. Voltage sags are normally described by characteristics of both magnitude and duration, but phase-angle jump should be taken into account in identifying sag phenomena and finding their solutions. In this paper, voltage sags due to power system faults such as single phase-to-ground, phase-to-phase, and two-phase-to-ground faults are characterized by using symmetrical component analysis and their effect on the magnitude variation and phase-angle jumps for each phase are examined. A simple and practical method is proposed for voltage sag detection, by calculating RMS voltage over a window of one-half cycle. The industrial distribution system at Bajaj hospital is taken as a case study. Simulation studies have been performed by using MATLAB/SIMULINK and the results are presented at various magnitudes, duration and phase-angle jumps.

## Keywords

Power Quality; Voltage Sags; Characterization

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## 1. Introduction

According to IEEE standard 1159-1995, a voltage sag is defined as a decrease in rms voltage down to 90% to 10% of nominal voltage for a time greater than 0.5 cycles of the power frequency but less than or equal to one minute [1]. Voltage sags have always been present in power systems, but only during the past decades have customers become more aware of the inconvenience caused by them [2].

Voltage sag may be caused by switching operations associated with a temporary disconnection of supply, the flow of inrush currents associated with the starting of motor loads, or the flow of fault currents. These events may emanate from the customers system or from the public network. Lighting strikes can cause momentary voltage sags [3].

The interests in the voltage sags are increasing because they cause the detrimental effects on the several sensitive equipments such as adjustable-speed drives, process-control equipments, programmable logic controllers, robotics, computers and diagnostic systems, is sensitive to voltage sags. Malfunctioning or failure of this equipment can cause by voltage sags leading to work or production stops with significant associated cost [4] [5].

In the conventional method to assess these effects, voltage sags are characterized by its magnitude and duration. The magnitude is defined as the percentage of the remaining voltage during the sag and the duration is defined as the time between the sag commencement and clearing [5]. However, balanced and unbalanced faults not only cause a drop in the voltage magnitude but also cause change in the phase angle of the voltage. Therefore, power–electronics converter that uses phase angle information for their firing instants may be affected by the phase angle jump [6] [7]. In order to find any solutions for voltage sag problems due to faults, it is necessary to identify characteristics of magnitude, duration and phase angle variations.

RMS (voltage or current) is a quantity commonly used in power systems as an easy way of accessing and describing power system phenomena. The rms value can be computed each time a new sample is obtained but generally these values are updated each cycle or half cycle. If the rms values are updated every time a new sample is obtained, then the calculated rms series is called continuous. If the updating of rms is done with a certain time interval, then the obtained rms is called discrete [7]. The analysis of different voltage sag characteristics of different disturbances, a method using rms voltage to detect the voltage sag is proposed in this paper. The correctness of the method is proved by simulations.

In this paper, a comprehensive study is presented in order to show the proposed characterization of voltage sags for the three types of faults, SLG, LL, and LLG. The algorithms for voltage sag detection and results by using MATLAB/SIMULINK software.

## 2. Voltage Sag Characteristics

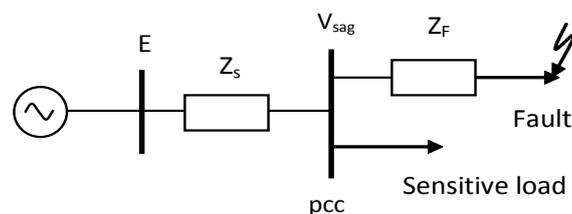
Voltage sag is defined as a decrease in rms voltage at the power frequency for durations of 0.5 cycles to 1 minute. This definition specifies two important parameters for voltage sag: the rms voltage and duration. The standard also notes that to give a numerical value to a sag, the recommended usage is a sag 70%, which means that the voltage is reduced down to 70% of the normal value, thus a remaining voltage of 30%. Sag magnitude is defined as the remaining voltage during the event. The power systems faults not only cause a drop in voltage magnitude but also cause change in the phase-angle of the voltage. The parameters used to characterize voltage sag are magnitude, duration and phase angle jump.

### 2.1. Voltage Sag Magnitude

The magnitude of voltage sag can determine in a number of ways. The most common approach to obtain the sag magnitude is to use rms voltage. There are other alternatives, e.g. fundamental rms voltage and peak voltage. Hence the magnitude of the sag is considered as the residual voltage or remaining voltage during the event.

In the case of a three-phase system, voltage sag can also be characterized by the minimum RMS-voltage during the sag. If the sag is symmetrical *i.e.* equally deep in all three phases, the lowest remaining voltage in any of the phases can be used to characterize the sag. If the sag is unsymmetrical, *i.e.* the sag is not equally deep in all three phases, the phase with the lowest remaining voltage is used to characterize the sag [8].

The magnitude of voltage sags at a certain point in the system depends mainly on the type and the resistance of the fault, the distance to the fault and the system configuration. The calculation of the sag magnitude for a fault somewhere within a radial distribution system requires the point of common coupling (pcc) between the fault and the load to be found. **Figure 1** shows the voltage divider model. Where  $Z_s$  is the source impedance at the pcc and  $Z_F$  is the impedance between the pcc and the fault. In the voltage divider model, the load current before as well as during the fault is neglected. There is no voltage drop between the load and the pcc. The voltage sag at the pcc equals the voltage at the equipment terminals, the voltage sag can be found from the Equation (1).



**Figure 1.** Voltage divider model.

$$V_{sag} = \frac{Z_F}{Z_S + Z_F} E \quad (1)$$

We will assume that the pre-event voltage is exactly 1 pu, thus  $E = 1$ . This result in the following expression for the sag magnitude

$$V_{sag} = \frac{Z_F}{Z_S + Z_F} \quad (2)$$

For fault closer to the pcc the sag becomes deeper (small  $Z_F$ ). The sag becomes deeper for weaker supplies (larger  $Z_S$ ) [6].

## 2.2. Voltage Sag Duration

The duration of voltage sag is mainly determined by the fault-clearing time. The duration of a voltage sag is the amount of time during which the voltage magnitude is below threshold is typically chosen as 90% of the nominal voltage magnitude. For measurements in the three-phases systems the three rms voltages have to be considered to determine duration of the sag. The voltage sag starts when at least one of the rms voltages drops below the sag-starting threshold. The sag ends when all three voltages have recovered above the sag-ending threshold [9].

## 2.3. Phase Angle Jump

To obtain the phase-angle jump of a measured sag, the phase-angle of the voltage during the sag must be compared with the phase-angle of the voltage before the sag. The phase-angle of the voltage can be obtained from the voltage zero-crossing or from the phase of the fundamental component of the voltage. The complex fundamental voltage can be obtained by doing a Fourier transform on the signal. This enables the use of Fast-Fourier Transform (FFT) algorithms. To explain an alternative method, consider the following voltage signal:

$$v(t) = X \cos(\omega_0 t) - Y \sin(\omega_0 t)$$

$$v(t) = \text{Re}\{(X + jY)e^{j\omega_0 t}\} \quad (3)$$

with  $\omega_0$  the fundamental (angular) frequency. Two new signals are obtained from this signal, as follows:

$$v_d(t) = 2v(t) \times \cos(2\omega_0 t) \quad (4)$$

$$v_q(t) = 2v(t) \times \sin(2\omega_0 t) \quad (5)$$

which we can write as

$$v_d(t) = X + X \cos(2\omega_0 t) + Y \sin(2\omega_0 t) \quad (6)$$

$$v_q(t) = -Y + Y \cos(2\omega_0 t) + X \sin(2\omega_0 t) \quad (7)$$

Averaging the two result signals over one-half cycle of the fundamental frequency gives the required fundamental voltage.

$$X + jY = \bar{v}_d(t) - j\bar{v}_q(t) \quad (8)$$

Knowing the values of X and Y, the sag magnitude can be calculated as  $\sqrt{X^2 + Y^2}$  and the phase-angle jump as  $\arctan \frac{Y}{X}$ . This algorithm has been applied to detect the phase-angle jump. The effect of averaging  $v_d(t)$  and  $v_q(t)$  over one full cycle of the fundamental frequency is shown in **Figure 3(c)** for the phase-angle jump. The effect of a larger window is that the transition is slower, but the overshoot in phase angle is less. Which window length needs to be chosen depends on the application.

To understand the origin of phase-angle jump associated with voltage sags, the voltage divider model of **Figure 1** can be used again, with the difference that  $Z_s$  and  $Z_f$  are complex quantities which we will denote as  $\bar{Z}_s$  and  $\bar{Z}_f$ . This gives for the voltage at the pcc.

$$\bar{V}_{sag} = \frac{\bar{Z}_F}{\bar{Z}_S + \bar{Z}_F} \quad (9)$$

Let  $\bar{Z}_S = R_S + jX_S$  and  $\bar{Z}_F = R_F + jX_F$ . The argument of  $\bar{V}_{sag}$ , thus the phase-angle jump in the voltage, is given by the following expression:

$$\Delta\phi = \arg(\bar{V}_{sag}) = \arctan\left(\frac{X_F}{R_F}\right) - \arctan\left(\frac{X_S + X_F}{R_S + R_F}\right) \quad (10)$$

If  $\frac{X_S}{R_S} = \frac{X_F}{R_F}$ , expression (10) is zero and there is no phase-angle jump. The phase-angle jump will thus be present if the X/R ratios of the source and the feeder are different [6] [10].

### 3. Simulation Study

#### Fault System Model

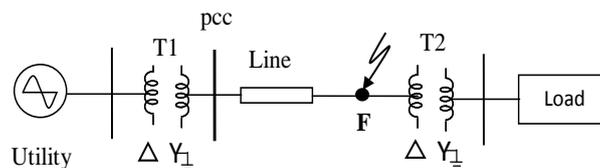
**Figure 2** shows the single line diagram of the express feeder for Bajaj hospital under study. It is fed from 33/11 kv distribution substation of Maharashtra State Distribution Company Limited (MSEDCL), Railway station, Industrial area, Aurangabad, India has been consider for voltage sag analysis. The system is modeled using the simulink and Simpower System utilities of MATLAB. **Table 1** shows system parameters used in the simulation.

The performance study of sample system is carried out for detection and characterization of voltage due to power system faults. It is assumed that a fault has occurred at position F, on the primary side of distribution transformer T2, and the fault lasted for 4 cycles from  $t = 0.045$  to  $0.125$  seconds. The monitoring equipment is installed at the pcc.

### 4. Simulation Results

#### 4.1. Single Phase-to-Ground Fault

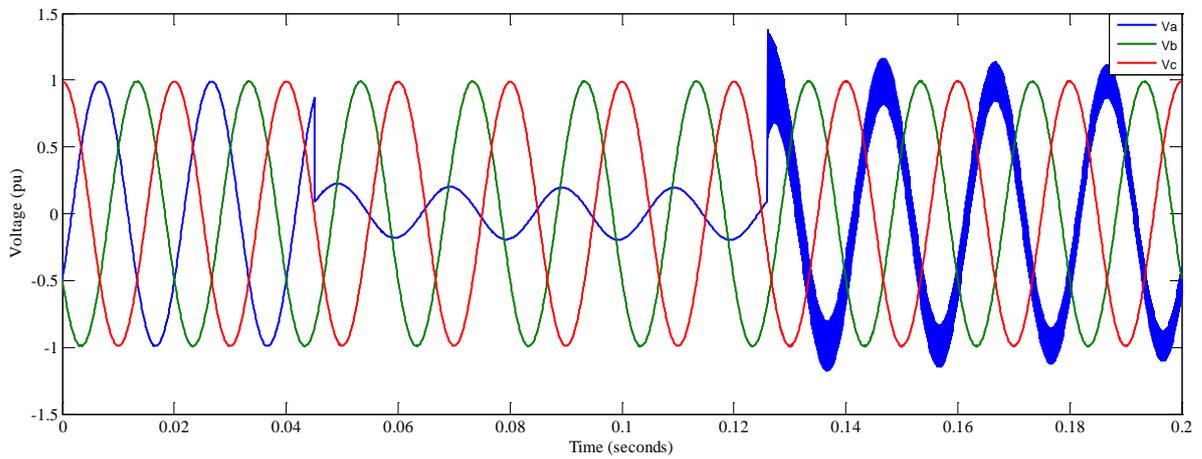
For simulation it is assumed that a single phase fault has appeared on phase A at position F. Phase voltages waveform, rms voltages, and their phase angles are shown in **Figure 3**. The waveform shown in **Figure 3(a)** shows an overvoltage at the end of the sag in faulted phase A. This overvoltage is almost certainly related to the cause of the fault. The voltage of phase A drops nearly zero is up to 0.2 pu, while phases B and C voltages normally remains at pre-fault levels as shown in **Figure 3(b)**. During the sag the voltage in the faulted phase Va is suppressed with a large phase-angle jump ( $-48.92$ ) degree, whereas the phase-angle jump in the other two non-faulted phases is almost not affected. The duration of voltage sag in this case is 88 ms.



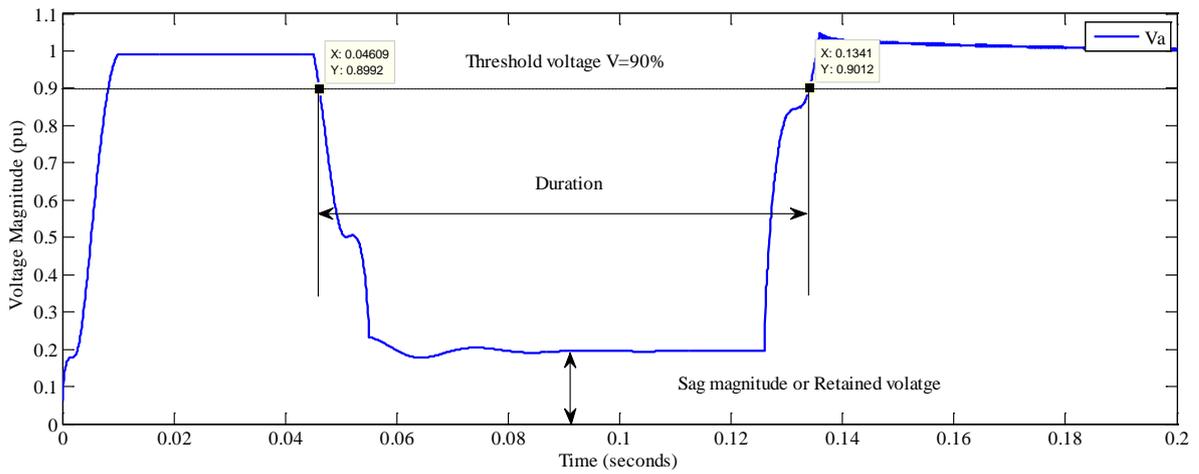
**Figure 2.** Single line diagram of distribution system for simulation.

**Table 1.** Distribution system parameters.

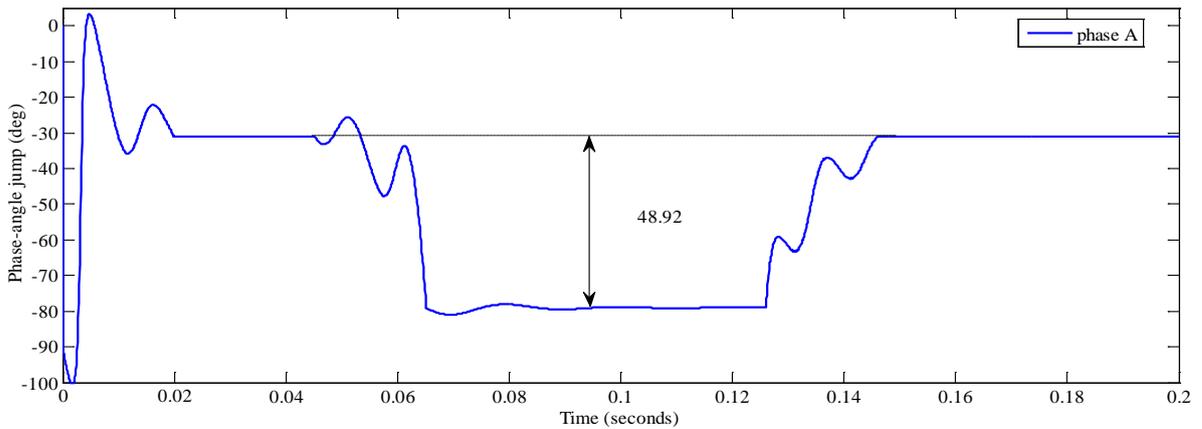
Sr. No	Component	Details
1	Source	10 MVA, 33 kv, X/R = 10
2	Transformer T1	5 MVA, 33/11 kv, %Z = 7.15, X/R = 10, DYn11
3	Transformer T2	750 KVA, 11/0.433 kv, %Z = 5, X/R = 6, DYn11
4	Line	0.6748 + j0.372/km, 2 km
5	Load	208 KW and 130 KVAR
6	Frequency	50 Hz



(a)



(b)

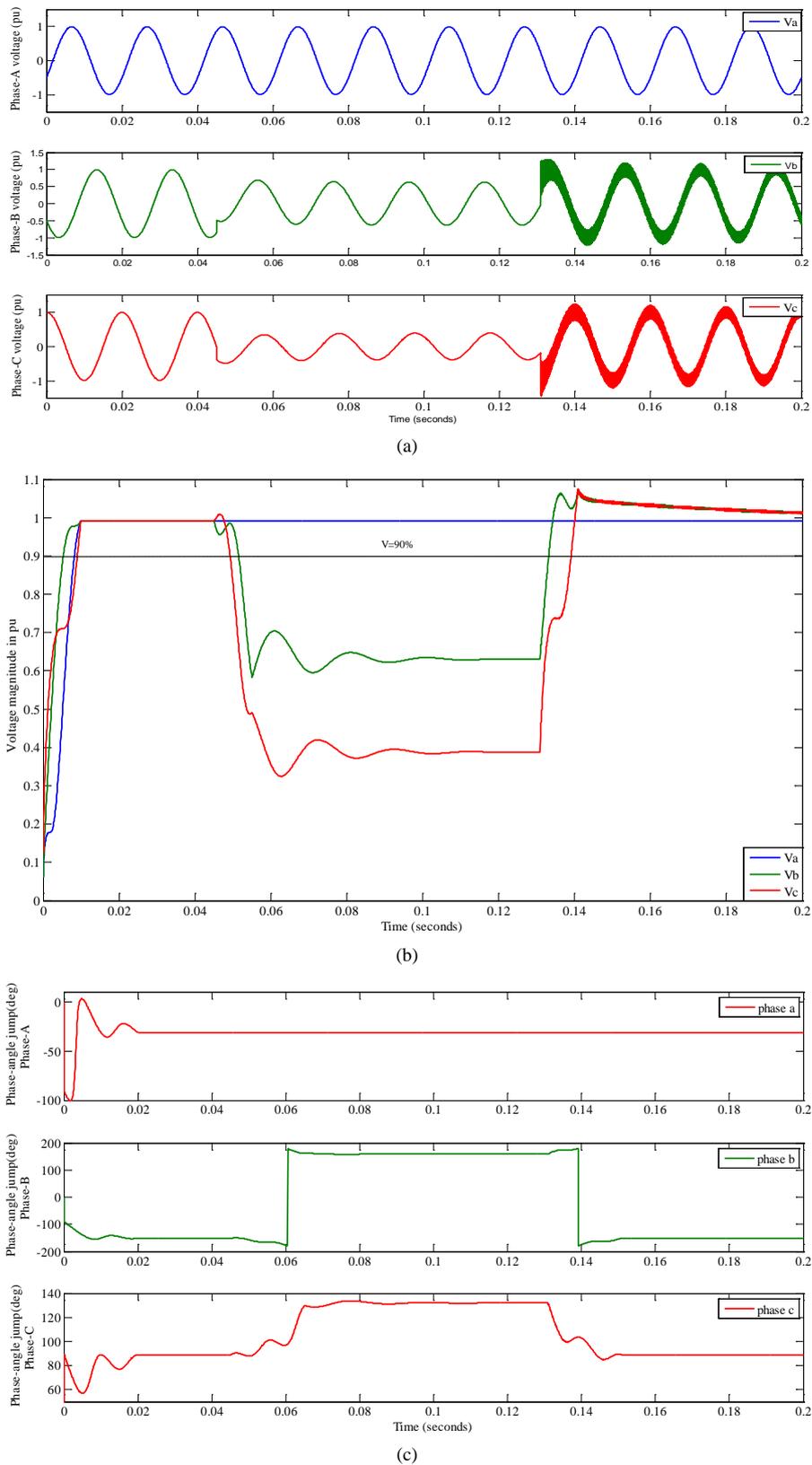


(c)

**Figure 3.** Single-phase-to-ground fault (a) voltage waveform; (b) rms voltage sag magnitude; (c) phase-angle jump.

### 4.2. Phase-to-Phase Fault

In addition to single phase-to-ground faults, the phase-to-phase faults also cause voltage sag. However, characteristics for magnitude changes and phase-angle jump are not similar to those of SLG faults. **Figure 4** shows the

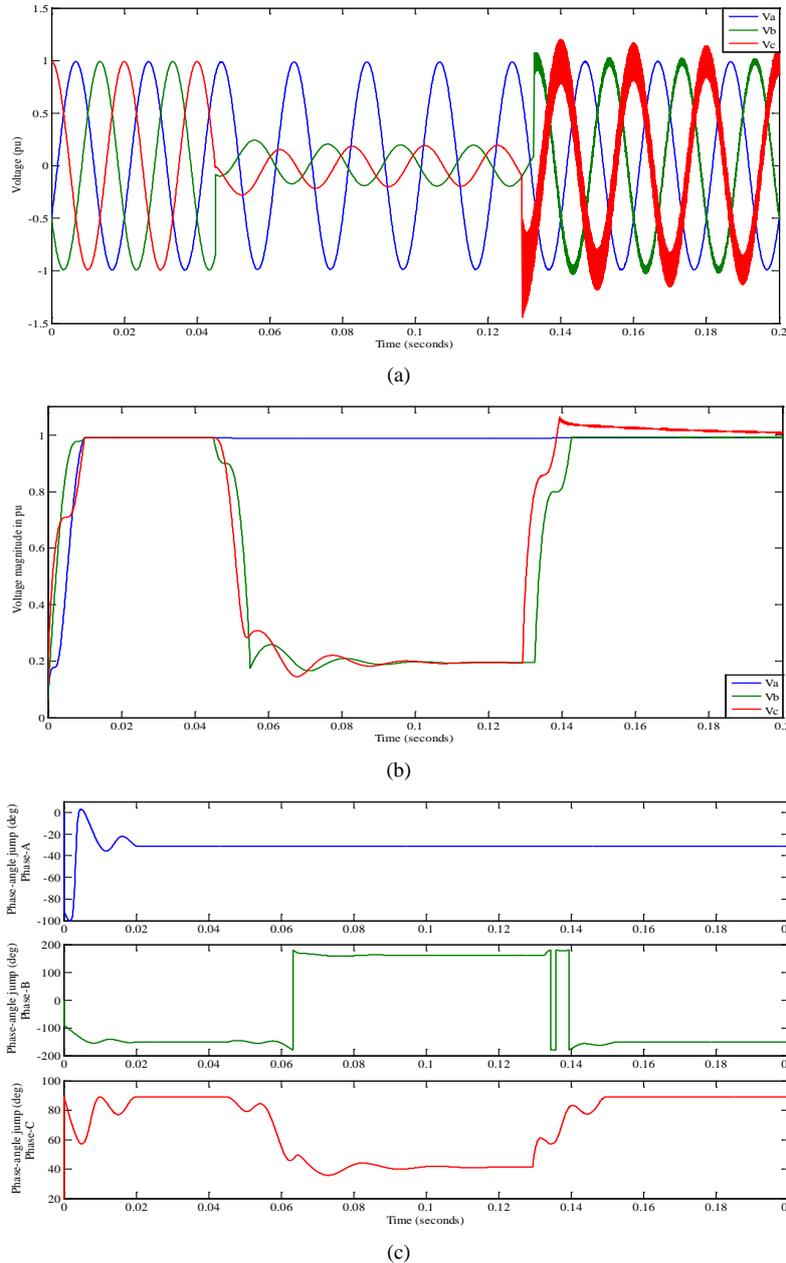


**Figure 4.** Phase-to-phase fault (a) Three-phase voltage waveform; (b) rms voltage sag magnitude for phase A, B and C; (c) Phase-angle jumps for phase A, B and C.

voltage waveform, rms voltage and phase-angle jump characteristics for phase voltages due to phase-to-phase fault between phases B and C. In **Figures 4(b)** and **(c)**, magnitudes and phase angles of phases B and C, with a large voltage drop in the two phases  $V_b$  and  $V_c$  but phase voltage  $V_a$  remains unchanged. The phase voltages drop in magnitude  $V_b = 0.63$  and  $V_c = 0.39$  pu, The duration of voltage sag phases B = 80.72 ms, and C = 89.88 ms, and the phase-angle jumps are (+159) degree, and (+42) degree respectively.

### 4.3. Two Phase-to-Ground Fault

A voltage sags due to a two-phase-to-ground fault between phases B, C and ground. The voltage waveform, rms voltages and phase-angle jump are recorded at the pcc as shown in **Figure 5**. This shows a significantly large



**Figure 5.** Two-Phase-to-ground fault (a) Three-phase voltage waveform; (b) rms voltage sag magnitude for phase A, B and C; (c) Phase-angle jumps for phase A, B and C.

drop in rms voltage in the faulted phases B and C, but no change in phase A. The phase voltages drop in magnitude  $V_b = 0.2$  and  $V_c = 0.2$  pu, the duration of voltage sag phases B = 92.2 ms, and C = 88.9 ms, and the phase-angle jumps are +160, and -41.7 degree respectively.

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