

ASTROSAT/UVIT Near and Far Ultraviolet Properties of the M31 Bulge

Denis Leahy, Cole Morgan, Joseph Postma, Megan Buick

Department of Physics and Astronomy, University of Calgary, Calgary, Canada Email: leahy@ucalgary.ca

How to cite this paper: Leahy, D., Morgan, C., Postma, J. and Buick, M. (2021) ASTROSAT/UVIT Near and Far Ultraviolet Properties of the M31 Bulge. *International Journal of Astronomy and Astrophysics*, **11**, 151-174.

https://doi.org/10.4236/ijaa.2021.112009

Received: April 12, 2021 **Accepted:** May 24, 2021 **Published:** May 27, 2021

Copyright © 2021 by author(s) and Scientific Research Publishing Inc. This work is licensed under the Creative Commons Attribution International License (CC BY 4.0).

http://creativecommons.org/licenses/by/4.0/

Abstract

AstroSat has surveyed M31 with the UVIT telescope from 2017 to 2019. The central bulge of M31 was observed in 2750 - 2850 A, 2000 - 2400 A, 1600 -1850 A, 1450 - 1750 A, and 1200 - 1800 A filters. A radial profile analysis, averaged along elliptical contours which approximate the bulge shape, was carried out in each filter. The profiles follow a Sersic function with an excess for the inner ~8" in all filters, or can be fitted with two Sersic functions (including the excess). The ultraviolet colours of the bulge are found to change systematically with radius, with the center of the bulge bluer (hotter). We fit the UVIT spectral energy distributions (SEDs) for the whole bulge and for 10 elliptical annuli with single stellar population (SSP) models. A combination of two SSPs fits the UVIT SEDs much better than one SSP, and three SSPs fit the data best. The properties of the three SSPs are age, metallicity (Z) and mass of each SSP. The best fit model is a dominant old, metal-poor (10^{10} yr, $\log(Z/Z_{\odot}) = -2$, with Z_{\odot} the solar metallicity) population plus a 15% contribution from an intermediate (10^{9.5} yr, $\log(Z/Z_{\odot}) = -2$) population plus a small contribution (~2%) from a young high-metallicity (108.5 yr, $\log(Z/Z_{\odot}) = -0.5$) population. The results are consistent with previous studies of M31 in optical: both reveal an active merger history for M31.

Keywords

UV Astronomy, Galaxies: M31

1. Introduction

The spiral galaxy Andromeda, also known as M31, is the nearest such galaxy to our own. Our external vantage point makes it feasible to study aspects of M31 that are difficult to study in our own galaxy. Interstellar extinction is not as major a factor when studying M31 as it is studying the Milky Way, owing to the former's inclination that allows observation of the whole disk of the galaxy. Studies of large numbers of stars have been done in great detail for the Milky Way, but distances often possess high uncertainty, due in part to extinction. An advantage of studying objects in M31 is that it is at a well-known distance (785 \pm 25 kpc) [1]. The intrinsic brightness of many objects can therefore be more precisely measured than galactic sources. M31 has been observed in optical on numerous occasions. The highest resolution observations were carried out with the Hubble Space Telescope (HST), including the Pan-chromatic Hubble Andromeda Treasury (PHAT) survey [2]. In near and far ultraviolet (NUV and FUV), the GALEX instrument has surveyed M31 [3].

The AstroSat mission, launched on September 28th, 2015, has carried out a survey of M31 in near and far UV. AstroSat is an orbiting observatory equipped with five instruments: the UV Imaging Telescope (UVIT) for visible and Ultra-Violet (UV); the Soft X-ray Telescope (SXT), Large Area Proportional Counters (LAXPC) and Cadmium-Zinc-Telluride Imager (CZTI) instruments for soft through hard X-rays; and the Scanning Sky Monitor (SSM), an X-ray survey instrument [4].

Analysis of the M31 UVIT survey observations has been presented in part by [5] [6] [7] [8] [9]. These papers have dealt with resolved stellar objects, including analysis of UV brightest stars in the bulge, the M31 UVIT point source catalog, matching UVIT point sources with Chandra sources in M31, improvements in astrometry and photometry for the M31 survey, first results from matching UVIT sources with HST/PHAT sources in the NE spiral arms of M31, and a study of FUV variable sources in M31 using a new second epoch observation of the central field of M31. The UVIT observations for the M31 survey are described in the M31 UVIT point source catalog paper [8]. 19 UVIT fields of 28 arcmin diameter were required to cover the M31 area (Figure 2 of [8]).

The current analysis is primarily concerned with the unresolved ultraviolet sources in M31's central bulge. The bulge of a galaxy is the central concentrated set of stars which is ellipsoidal in shape, smoothly distributed and consists of a substantial fraction of the galaxy's stars. UVIT's multiple filters within the NUV and FUV bands allow for an in-depth look at the UV colours of the bulge. In Sections 2 and 3, the observations and data analysis methods are described. The results are reviewed in Section 4 including radial profile analysis and UV colour change of the bulge with radius. In Section 5, synthetic colour magnitude diagrams (CMDs) are used to model the colour change of the bulge with radius and constrain the stellar populations in the bulge. We close with a brief summary.

2. Observations

The UVIT instrument onboard AstroSat has high spatial resolution (~1 arcsec), a 28 arcminute field of view, and was capable of observing in a variety of FUV and NUV filters [10]. However, partway through observations of M31, the NUV detector of UVIT failed, resulting in partial coverage of M31 in NUV. The entire galaxy has been observed in the FUV, and the central bulge is included in the portion with NUV data. The central bulge of M31 is entirely contained within Field 1 of the UVIT Andromeda survey. The bulge of M31 was observed by UVIT in 2017 [5] and at a second epoch in 2019. New in-orbit calibrations of the UVIT instrument have been carried out by [11] and are applied here to the 2017 and 2019 observations.

The basic data processing was carried out using CCDLab [12], with updated astrometry calibration from [13], and updated photometry as described in [6] and [9]. M31 Field 1 (the bulge field) was observed by the UVIT instrument in 5 FUV and NUV filters. From longest to shortest wavelength, these are: N279N, N219M, F172M, F169M, and F148W, where the label contains the central wavelength (in nm) of each filter and band¹.

The images were taken across two epochs, labelled A for the 2017 observation and B for the 2019 observation. The first set of observations included N279N, N219M, F172M, and F148W images, while the second set included F172M, F169M and F148W images. Merged images, here labelled "M", were produced for filters F172M and F148W which had data from both A and B epochs. The merged images were created by adding the counts images for A and B, adding the exposure maps for A and B, then dividing the counts images by the exposure images to create a count/s image from which fluxes can be extracted using the UVIT calibrations (updated in [11]).

The full 3-colour image of Field 1 made from the 2017 epoch N279N, N219M and F148W images is shown in [5]. The image includes the bright central bulge, which is likely dominated by unresolved FUV and NUV emission from large numbers of low-luminosity stars in the bulge. Field 1 contains other prominent features, including resolved and unresolved emission from numerous stars in the inner spiral arms of M31, dust lanes which are visible as dark lanes, and several foreground stars, which can be identified using either Gaia parallax [7] or co-lour-magnitude diagram analysis [8].

The central part of Field 1 is the area that contains the central bulge of M31, here defined as the inner ~7 arcminute diameter part of the 28-arcminute diameter full area of Field 1. The area studied here is shown in **Figure 1**, with the images of the bulge shown for the five different NUV and FUV filters.

Due to the low inclination of M31, a few dust lanes are visible, e.g. NW of the bulge by \sim 80 arcmin. The amount of area covered by the dust lanes is not large, so we did not correct for the reduction in flux caused by these dust lanes in our analysis. However, we did test an analysis which accounts for the bright point sources in the images. We masked the bright point sources and replaced them with the average values of surrounding pixels. We compared the brightness profiles derived with and without the point sources and found there was no significant difference. Thus, we decided to leave the point sources in the images for the final analysis.

¹*N* is for NUV, F is for FUV. The filter transmission curves are given in [10].



Figure 1. The five processed images used in this analysis. Top Left: N279N_A, top right: N219M_A, middle left: F148W_M, middle right: F169M_B, bottom: F172M_M. The A, B and M refer to epoch A, epoch B and merged images, respectively. The images are 410" by 410" across, and centred on 00 h 42 m 44.34 s ra., +41 d 16'08.44" dec.

3. Data Analysis

3.1. Elliptical Brightness Profile Extraction

Figure 2 illustrates the ellipticity of the central bulge of M31 at the longest NUV and shortest FUV wavelengths. Shape changes of the bulge across different wavelengths are investigated here by fitting elliptical Gaussian functions to the images using CCDLab for a set of square bounding boxes of different sizes all centred on the bulge. The centre of the bulge was chosen as the brightest pixel in the



Figure 2. The bulge of M31 in N279N (top) and F148W (bottom) with contours drawn in green using the ds9 image viewer, and a subset, drawn in white, selected from the 240 ellipses used to create the elliptical profiles. The images are 370"E-W by 330"N-S.

core in the majority of filters. Figure 3 shows the ellipticity (a/b) and inclination (ϕ) as a function of major axis (a). Inclination is measured in radians clockwise from the EW axis. Data from bounding boxes < 40 pixels half-width are not shown. This corresponds to a cutoff of 4.2" the small central part of the bulge, which has a complex structure (e.g. [14]).

To measure the brightness and UV colours of the bulge we measured average flux per pixel as a function of semi-major axis, extracted using elliptical annuli. This method was chosen over radial profiles using circular annuli because the images are not circularly symmetric, and thus the brightness changes significantly with azimuthal angle for circular annuli. The brightness profiles using elliptical annuli account for the elliptical shape of the bulge projected on the sky.

Pixels (coordinates x, y) were counted within a given ellipse annulus if they satisfied:

$$2a - 0.5 < \sqrt{\left(x - F1x\right)^2 + \left(y - F1y\right)^2} + \sqrt{\left(x - F2x\right)^2 + \left(y - F2y\right)^2} \le 2a + 0.5$$

Here (F1x, F1y) and (F2x, F2y) are the positions of the focii of the given ellipse:



Figure 3. Top: Ellipticity, (semi-major axis a)/(semi-minor axis b), of the bulge as a function of semi-major axis in pixel units, derived from Gaussian fits. Bottom: Inclination (radians, CW from W) of the bulge as a function of semi-major axis in pixel units. 1 pixel is 0.4168".

$$F1x = Cx + \cos(p) * \sqrt{a^2 - b^2}$$

$$F1y = Cy + \sin(p) * \sqrt{a^2 - b^2}$$

$$F2x = Cx - \cos(p) * \sqrt{a^2 - b^2}$$

$$F2y = Cy - \sin(p) * \sqrt{a^2 - b^2}$$

(Cx, Cy) is the (x, y) position of the centre of the bulge on the image, *a* is the semi-major axis desired, in pixels, *b* the corresponding semi-minor axis, and *p* the inclination of the major axis from the image's horizontal, in radians. The av-

erage flux per pixel is calculated by summing the counts/sec in each pixel within a thin elliptical annulus, dividing by the number of pixels in the annulus, then using the UVIT calibration to convert count rate per pixel to flux per pixel.

To extract flux measurements for the same elliptical annuli of the bulge for all filters, we used the ellipse parameters vs. semi-major axis from the N279N_A image analysis. As a test, the analysis was repeated using ellipse parameters derived from the F148W_M image. However, there was little difference in the resulting elliptical profiles, so the analysis presented here was carried out using the N279N_A ellipse parameters. Average flux per pixel was extracted for 240 elliptical annuli, from the centre out to 400 pixels (167") along the major axis. Examples of these ellipses are drawn in **Figure 2**. One ellipse was used for each of the first 200 pixels along the major axis, and then one ellipse for every 5 pixels for the remaining 200 pixels.

3.2. UV Colour-Colour Diagram

To study the colour change in the bulge, we produced a colour-colour diagram using the elliptical profiles of flux per pixel from the above analysis. The colours chosen were ratio of flux per pixel of F148W to N219M and ratio of N219M to N279N. The standard deviation of values of the fluxes from the different pixels in each annulus was used as estimate of the flux errors, and propagation of errors was used to calculate the errors in the colours.

4. Results

4.1. Elliptical Brightness Profile Analysis

Analytic functions were fit to the elliptical surface brightness profiles of the bulge to quantify the shape in a simple manner. The fits were carried out using χ^2 minimization. For these fits the fractional error for each semi-major axis value was taken as $1/\sqrt{N}$ with *N* the number of counts at the semi-major axis².

Initially, we fit a Sersic function, f(a), to the observed surface brightness vs. semi-major axis, *a*. Sersic functions are commonly used to approximate stellar distributions in elliptical galaxies and spiral bulges:

$$f(a) = I0 \times \exp\left(-k \times a^{1/n}\right)$$

with *I*0 the central surface brightness, *n* the Sersic index, and *k* the e-folding constant for decrease of surface brightness. This is equivalent to the original form of the Sersic function given by [15], $f(r) = \sum_{e} \exp\left(-b(n) \times \left[(r/R_e)^{1/n} - 1 \right] \right)$ with $\sum_{e} = I0 \times \exp\left(-b(n)\right)$ and $R_e = (b(n)/k)^n$. For our data, in units of flux per pixel (erg·cm⁻²·s⁻¹·A⁻¹·pixel⁻¹), we use units of pixels for *a*.

The elliptical profiles generally follow a Sersic shape, with an excess in the center in all filters. The top panel of **Figure 4** shows the F148W profile. The

²*N*The systematic errors in converting counts/s to flux or magnitude ([11] and [10]) are small compared to the $1/\sqrt{N}$ statistical errors for these narrow (1 pixel wide) elliptical areas. $f(r) = \sum_{e} \times \exp\left(-b(n) \times \left[(r/R_{e})^{1/n} - 1 \right] \right)$ with $\sum_{e} = I0 \times \exp\left(-b(n)\right)$ and $R_{e} = (b(n)/k)^{n}$. For our data, in units of flux per pixel (erg·cm⁻²·s⁻¹·A⁻¹·pixel⁻¹), we use units of pixels for *a*.



Figure 4. Top: Elliptical proles of the bulge (flux per pixel) vs. semi-major axis for the five UVIT filter bands. The bulge shows a sharp increase in surface brightness toward the centre. Bottom: Sersic fits (black dash line) to the F148W elliptical profile (orange solid line), with added Point Source Functions (PSFs, red dash lines). 400 pixels is 167".

Sersic function (black dashed line) fits very well the majority of the bulge (from semi-major axis of \sim 8" to 167"). The excess is not consistent with a point source at the centre of the bulge, as shown by the red dashed lines in **Figure 4**, which

include Sersic plus the radial profile of a point source (the UVIT point-spreadfunction or PSF [10]). The shape of the excess is too broad and flat compared to the PSF. Higher resolutions are required to study the inner \sim 2", as was done by [14] at optical wavelengths.

Table 1 shows the results of single Sersic function fit to the bulge, including and omitting the inner 10 pixels (~4") of the bulge. Comparing the two cases shows that omitting the inner ~4" results in a significant reduction in χ^2 . Using the fit with the inner 4" omitted, the Sersic index, n, varies with wavelength, with n increasing from 2.3 to 5.7 for decreasing wavelengths 279 nm \Rightarrow 219 nm \Rightarrow 172 nm,

Single Sersic Fit ^b	N279N	N219M	F172M	F169M	F148W
<i>I</i> 0	2.01E-17	4.69E-17	1.84E-15	4.28E-16	1.84E-16
k	0.278	1.26	4.15	2.79	2.01
n	2.54	4.74	9.07	6.79	5.55
χ^2	104	74	124	151	190
DOF ^c	236				
Single Sersic Fit ^d	N279N	N219M	F172M	F169M	F148W
<i>I</i> O	1.70E-17	2.17E-17	1.34E-16	8.05E-17	5.16E-17
k	0.213	0.736	1.90	1.45	1.07
п	2.33	3.71	5.69	4.78	4.07
χ^2	71	50	80	99	918
DOF ^c	226				
Sersic + Gaussian Fit ^b	N279N	N219M	F172M	F169M	F148W
ЛО	1.67E-17	2.13E-17	1.29E-16	7.17E-17	4.86E-17
k	0.206	0.723	1.87	1.37	1.03
п	2.30	3.68	5.64	4.64	4.00
Ig	1.37E-17	1.9902E-17	1.30E-17	1.20E-17	1.24E-17
σ	4.47	3.97	4.09	4.49	4.33
χ^2	71	51	81	98	914
DOF ^c	234				
Double Sersic Fit ^b	N279N	N219M	F172M	F169M	F148W
I O ₁	1.62E-17	1.46E-17	8.29E-17	4.81E-17	3.15E-17
k_1	0.195	0.509	1.53	1.10	0.762
n_1	2.27	3.20	5.09	4.18	3.51
102	2.06E-17	2.59E-17	2.21E-17	2.06E-17	2.86E-18
k	0.172	0.560	0.244	0.263	0.403
n_2	0.848	1.39	0.948	1.02	1.20
χ^2	69	47	79	94	770
DOF ^c	233				

Table 1. Best-fit bulge profile parameters^a.

"The uncertainties in all parameters are ~5%. ^bThe fits include data for semi-major axis of 1 to 400 pixels. ^cDOF stands for degrees-of-freedom. ^dThe fits included data for semi-major axis of 10 to 400 pixels. then decreasing from 5.7 to 4.1 for 172 nm \rightarrow 169 nm \rightarrow 148 nm. The fits are acceptable (χ^2 < degrees-of-freedom or DOF) except for the F148W data, which has the highest signal-to-noise of the five filters.

To better fit the F148W data, and to see if the inner part of the bulge could be fit, we carried out fits to the full data (1 to 400 pixels) with double-Sersic functions, and Sersic + Gaussian functions. The Gaussian function is:

$$g(a) = Ig \times \exp\left(-\frac{a^2}{2\sigma^2}\right)$$

Results are given in **Table 1**. For F148W, the Sersic plus Gaussian is significantly better than a single Sersic (χ^2 of 914 vs. 1900), and the double Sersic better than Sersic plus Gaussian (χ^2 of 770 vs. 914).

Figure 5 shows the double Sersic fits to measured surface brightness for all filters, illustrating that the central bulge (≤ 10 ") and rest of the bulge (~ 10 to 167") are well fit. The N219M filter observed surface brightness looks different than the other filters: it is faintest in the inner bulge and approximately matches the shorter wavelength profiles for the outer bulge³.



Figure 5. Double Sersic fits (dashed lines) compared to the data (solid lines). The fits include data from 1 pixels to 400 pixels (167"). Data errors range from a minimum 1.3% to 1.8% for F148W to a maximum of 2.5% to 4.5% for N279N. Errors for the other filters range between 1.7% to 3.1%. A \pm 5% error bar is shown on the N219M curve for illustration. The errors are similar to the differences between the data points and the fit curves.

³The conversion between counts and flux is not the cause for this difference, because the conversion was well-calibrated [10] [11]. The intrinsic mean stellar emission spectrum decreases with decreasing wavelength and would yield N219M fainter than N279N but brighter than the FUV filters. However, N219M it is at the peak of the UV extinction curve at 220 nm (Figure 3 of [16]). At 220 nm A_{λ}/A_{ν} is larger than for larger or smaller wavelengths by a factor of ~1.6, so moderate extinction can make the N219M surface brightness smaller than the FUV surface brightnesses.

4.2. Simple Models for UV Colours of the M31 Bulge

The UV colour change of the bulge is shown in **Figure 6**. The semi-major axis, *a*, is encoded in a standard RGB colour scheme, with bluest for a = 0 gradually changing to green at $a \approx 50^{\circ}$, green changing to orange at $a \approx 100^{\circ}$ and orange changing to red at the outermost analyzed ellipse, with $a = 167^{\circ}$.



Figure 6. Top: UV colour-colour diagram of the bulge of M31, for elliptical annuli of different semi-major axes, from 0 to 400 pixels (0 to 167"). Semi-major axis is encoded by RGB colour, as shown by the panel on the bottom (the color scale is compressed for semi-major axes between 200 and 400 pixels because the NUV and FUV colours change slowly for semi-major axes > 200). The dashed lines show the UV colours for black-bodies and Castelli & Kurucz stellar atmosphere models of varying temperature along the line, with different extinction values for each line.

The larger errors and higher spread for the innermost ellipses (upper points in the diagram) are caused by the fewer pixels per annulus for annuli of small semi-major axis. The colour-colour diagram shows a significant change in the ultraviolet colour of M31's bulge. Points nearest the centre have a greater ratio of F148W flux to N219M flux than those further out, while having a similar ratio of N219M to N279N. Thus, the FUV-NUV colour (vertical axis) of the bulge becomes "bluer" towards the core. Most of the colour change occurs between the centre and half-way out the analyzed region, from semi-major axis of 0 to ~83 arcsec.

Colours for blackbody models and Castelli-Kurucz stellar atmosphere models [17] (from the STScI website <u>https://www.stsci.edu/</u>) are plotted for comparison. For the stellar atmospheres, surface gravities were taken as the recommended values for each temperature, and solar metallicity was used. Model colours are calculated as the ratio of filter fluxes determined from a given model spectrum multiplied by the applicable UVIT filter response curve. Interstellar extinction is calculated using equations from [16] which include the wavelength dependence for optical and UV. The extinction is parametrized by A_V , given in magnitudes for the V band, and includes internal extinction within the bulge of M31 plus foreground extinction in the Milky Way along the line-of-sight toward M31.

The data are consistent with blackbodies between 9500 and 11,000 K, with extinction values, A_{V_3} between 0.4 and 0.7. The stellar atmosphere models suggest a lower temperature range, 8500 to 9000 K, and a higher extinction, between 0.7 and 1.1. The stellar models are more realistic if the emission is from stellar atmospheres, particularly if the UV emission primarily comes from a population of unresolved hot stars. This change in model temperature can be interpreted as a rise in the average temperature stars towards the centre. Leahy *et al.* (2018) [5] found evidence for a young hot stellar population in M31's bulge, and this combined with other evolved stars are possible causes of the colour changes.

4.3. Stellar Population Models for UV Magnitudes of the M31 Bulge

To construct more realistic models for the FUV and NUV flux from the M31 bulge, which consists of large numbers of unresolved stars, it is necessary to consider stellar population models. The basic models are simple stellar populations (SSPs) which consist of a set of stars of a single age and metallicity but with a range of initial masses. More complex models can then be constructed by combinations of these SSPs.

Here, we use the SSPs using the Padova stellar models, calculated using the CMD 3.4 online tool at <u>http://stev.oapd.inaf.it/cgi-bin/cmd</u>. In CMD 3.4, we used the recommended options: PARSEC evolutionary tracks [18], version 1.2S, for pre-main sequence to first thermal pulsation or carbon ignition, and COLIBRI [19] for thermal pulsation-asymptotic giant branch evolution, ending at total loss of the envelope. Circumstellar dust properties were used for M stars and for C stars from [20], long-period variability along the red giant branch and

asymptotic giant branch phases was taken from [21], and the initial mass function of [22] was used. For our application, synthetic photometry was calculated in AB magnitudes for the UVIT filter bands.

For comparison to the M31 bulge we calculated models for 8 ages, *T*, with $\log(T) = 6.5, 7, 7.5, 8, 8.5, 9, 9.5$ and 10. For each age, we calculated models for metallicities, Z, with $\log(Z/Z_{\odot}) = -2, -1.5, -1, -0.5, 0$ and 0.5. For age $\log(T) = 10$ we added $\log(Z/Z_{\odot}) = -2.5$ to our grid of models. The UVIT F148W, F169M, F172M, N219M and N279N AB magnitudes for each star in the population were obtained, then we combined these to obtain the AB magnitudes for each SSP.

We add extinction, with parameter A_V , using the extinction curve of [16]. The resulting SSP UVIT colours are compared to the colours of the M31 bulge in **Figure 7**. It is seen that the inner bulge colours (blue points) are similar to SSPs with $A_V \sim 0.4 - 0.6$ and a range of ages or metallicities. The middle bulge colours (orange points) are similar to SSPs with $A_V \sim 0.2$ and low age (log(*T*) ~ 6.5 to 7 and low metallicities (~-1.5 to -2).

The above comparison of SSPs with colours is incomplete, so we carry out fitting of the M31 bulge FUV-NUV spectral energy distribution (SED) to multiple stellar populations. This has the advantages of including data from all five UVIT



Figure 7. UV colour-colour diagram of the bulge of M31, for elliptical annuli of different semi-major axis. The dashed, dash-dot, and dotted lines show the colours calculated from stellar population synthesis models (see text), with different extinction for each set of 5 lines. Stellar metallicity varies along each line, from $\log(Z/Z_{\odot}) = -2.0$ to +0.5 (left end to right end), and population age, with T in years, is different for each line according to colour.

filters, instead of three, and preserves the normalization which is required to obtain the size of the stellar populations. We extracted the FUV and NUV magnitudes for the whole bulge, here taken as an outermost ellipse with semi-major axis of 450 pixels (188"). This large ellipse was divided into 10 annuli of ~equal-area to examine spatial variations. The semi-minor axis, b, to semi-major axis, a, ratios (b/a) were taken from the above analysis. For the whole and 10 annuli regions, systematic errors in conversion from counts/s to flux and magnitude are comparable to the $1/\sqrt{N}$ statistical errors, so were included.

Table 2 shows the parameters of the elliptical annuli. For each area the UVIT magnitudes were fit by minimizing χ^2 with either 1, 2 or 3 SSPs. The fitting was

2 SSP fit ^a							
Region	$a^{\scriptscriptstyle b}_{\scriptscriptstyle in}$	a_{out}^{b}	χ^2	M1 ^c	M2 ^c	A_v	
Whole	0	187.6	4.58	1.59E9	9.41E7	0.456	
Ann 1	0	58.4	8.77	3.13E8	3.39E7	0.483	
Ann 2	58.4	83.4	7.17	2.24E8	1.74E7	0.467	
Ann 3	83.4	104.2	5.92	1.86E8	1.44E7	0.456	
Ann 4	104.2	116.7	4.54	1.13E8	8.63E6	0.449	
Ann 5	116.7	133.4	4.47	1.51E8	1.10E7	0.438	
Ann 6	133.4	145.9	3.85	1.29E8	8.32E6	0.434	
Ann 7	145.9	158.4	4.34	1.10E8	7.99E6	0.420	
Ann 8	158.4	166.7	4.03	7.14E7	5.30E6	0.423	
Ann 9	166.7	179.2	5.16	1.08E8	7.80E6	0.416	
Ann 10	179.2	187.6	4.94	6.81E7	5.14E6	0.405	
$3SSP \ fit^d$	$a^{\scriptscriptstyle b}_{\scriptscriptstyle in}$	a_{out}^{b}	χ^2	M1 ^c	M2 ^c	M3 ^c	A_v
Whole	0	187.6	1.01	1.59E9	2.73E8	4.76E6	0.466
Ann 1	0	58.4	1.11	3.13E8	2.73E7	1.32E6	0.457
Ann 2	58.4	83.4	1.15	2.24E8	2.12E7	7.17E5	0.472
Ann 3	83.4	104.2	1.14	1.86E8	2.48E7	5.84E5	0.469
Ann 4	104.2	116.7	0.84	1.20E8	1.77E7	3.44E5	0.467
Ann 5	116.7	133.4	0.96	1.52E8	2.73E7	4.30E5	0.460
Ann 6	133.4	145.9	0.75	1.35E8	2.38E7	3.18E5	0.461
Ann 7	145.9	158.4	0.93	1.10E8	2.51E7	3.03E5	0.453
Ann 8	158.4	166.7	0.77	8.57E7	1.77E7	1.99E5	0.457
Ann 9	166.7	179.2	1.05	1.15E8	2.95E7	2.86E5	0.457
Ann 10	179.2	187.6	0.82	8.59E7	2.07E7	1.66E5	0.449

Table 2. M31 bulge stellar population fits.

^aThe other best-fit parameters were $\log(T1) = 10$, $\log(Z1/Z_{\odot}) = -2$, $\log(T2) = 9$, $\log(Z2/Z_{\odot}) = -1.5$ for Ann 1 to Ann 10; for Whole the best-fit parameters were the same except for $\log(Z2/Z_{\odot}) = -2$. ^b a_{in} and a_{out} are the inner and outer semi-major axes for each annulus. ^cMasses are given in units of M_{\odot} . ^dThe other best-fit parameters were $\log(T1) = 10$, $\log(Z3/Z_{\odot}) = -2$, $\log(T2) = 9.5$, $\log(Z2/Z_{\odot}) = -2$, $\log(T3) = 8.5$, $\log(Z3/Z_{\odot}) = -0.5$, for all regions. carried out for each SSP in the grid of log(*T*) and log(Z/Z_{\odot}). For each SSP the free parameters were mass of the SSP and A_V . For the case of 2 or 3 SSP fits, the extinction was taken to be the same for both (or three) SSPs. The best-fit was chosen to be the SSP with the lowest χ^2 of all SSPs in the grid. For the case of 2 SSPs and 3 SSPs the grids were 4 and 6 dimensional, resp. None of the single SSP models are able to fit the data. The top panel of **Figure 8** shows a few of the single SSPs compared to the data for the Whole region (black line labelled M31 Bulge). The data errors are comparable to the symbol sizes. The SSP normalization was chosen so that the calculated magnitudes of the SSP did not exceed the data. It is seen that young SSPs (log(*T*) < 9) are too faint for the longer wavelength data (by ~2 magnitudes) and that old SSPs are too faint for the shorter wavelength data.



Figure 8. Top panel: Single stellar population (SSP) models compared to the data (black line) for the Whole Bulge region (0 to 188" in semi-major axis, see **Table 2**) of M31. T is the age in years and Z is the metallicity of the population. None of the SSPs can fit the data. Bottom panel: data for the Whole Bulge region (black symbols and line) and for the innermost annulus (0 to 58" in semi-major axis, blue symbols and line); model of 3 combined SSPs for the Whole Bulge region (red symbols and dashed line); model of 2 combined SSPs for the innermost annulus (magenta symbols and dashed line).

Including a second SSP improves the fit significantly. The bottom panel of **Figure 8** shows the best-fit 2 SSP model (magenta line) for the innermost annulus/ellipse (data shown by blue symbols and solid line). Adding a third SSP further improves the fit. The Whole region data (top, black symbols and solid line) and the best-fit 3 SSP model (red symbols and dashed line) are shown. The best-fit masses and extinction (A_V) for the 2 and 3 SSP models are listed in **Table 2**.

For the 1 SSP model there are 4 parameters (2 grid parameters and 2 continuous parameters) and 5 data points. Best-fit χ^2 values are between 1000 to 2000 for the 10 annuli and whole regions and rule out single SSP models. For the 2 SSP models there are 7 parameters (4 grid, 3 continuous), more than the number of data points, thus a statistically good fit should have $\chi^2 \sim 1$. The χ^2 values are between 4 and 9, indicating a large improvement over the 1 SSP model. The 3 SSP models have 10 parameters (6 grid, 4 continuous) and $\chi^2 \sim 1$ as expected for good fits. The 3 SSP models show significantly better fits than the 2 SSP models, but they have the disadvantage of having more parameters than the number of data points in the SED.

5. Discussion

M31's bulge, analyzed here out to ~170", is elliptical. The ellipticity is different in the different NUV and FUV filters (**Figure 3**) with a smaller ellipticity found in the longer wavelength filters (e.g. at semi-major axis of 25", $a/b \approx 1.17$ in NUVN2 vs. 1.27 in F148W). The ellipticity is lowest near the centre: $a/b \approx 1.14$: this is apparent on the contour plots (**Figure 2**). It increases outward, peaking at ~17" major axis in the NUV, and at ~25" in the FUV. Further from the centre the ellipticity decreases outward, to a minimum near ~55", then increases outward to the maximum semi-major axis analyzed here (~95").

Outside of 17", the ellipticity increases with decreasing wavelength (top panel of **Figure 3**). Inside of 17" the ellipticity decreases with decreasing wavelength, *i.e.* it is approximately reversed, likely indicating a different physical component, or different mix of stellar populations, in the central part of the bulge.

The bulge's inclination changes smoothly with increasing semi-major axis, increasing from $\simeq 23^{\circ}$ reaching a peak of $\simeq 48^{\circ}$ in all filters at $\sim 25^{\circ}$. It then slowly decreases outwards to $\simeq 33^{\circ}$, implying a clockwise rotation from centre to semi-major axis of 17^o, followed by a gradual counterclockwise rotation from there outward to the maximum semi-major axis of 95^o. This small amount of rotation (25°) is in the contour plots (**Figure 2**) but it is not easy to discern. The bulge is significantly more circular very near the centre.

The brightness profile of the bulge vs. semi-major axis was extracted using 1 pixel wide elliptical annuli. There is a sharp increase of brightness towards the centre. The profile was fit with a Sersic function, showing an excess at the centre which is more extended (\simeq 2") than a point source (bottom panel of **Figure 4**).

Thus, we fit the bulge with the sum of a Sersic and a Gaussian and the sum of

two Sersic functions. The double Sersic functions yield the best fit, although the decrease in χ^2 is highly significant only for the F148W data. We conclude that the profile is more complex than can be fit with simple analytic functions, such as we have used. For no galaxy other than M31 do we have such good photometry in NUV and FUV. Thus, simple analytic fits to a galaxy bulge profile have not tested to this level previously.

The next step of analysis of the bulge considered spectral changes vs. semi-major axis distance. We analysed the colour-colour diagram using flux ratio of F148W to N219M (equivalent to N219M magnitude minus F148W magnitude) vs. flux ratio of N219M to N279N (equivalent to N279N magnitude minus N219M magnitude). In this diagram, hotter (brighter at shorter wavelengths) objects are higher in the diagram, and objects with more extinction are further left. The latter is a result of the peak of the UV extinction curve at \approx 220 nm, matching the N219M filter.

From the colour-colour diagram (**Figure 6**), the centre of the bulge is seen to be hotter (blackbody temperature \approx 11500 K, or Castelli-Kurucz stellar atmosphere temperature \approx 8800 K) than the outer parts of the bulge (blackbody temperature \approx 9750 K, or Castelli-Kurucz stellar atmosphere temperature \approx 8450 K). The extinction of the bulge is between $A_V = 0.4$ and 0.7 for blackbodies, or between $A_V = 0.7$ and 1.1 for stellar atmospheres. The data errors are such that the outer bulge has distinctly lower extinction than the middle bulge, but the central bulge has extinction consistent with either middle or outer bulge.

Because the bulge NUV and FUV emission is from a large number (of order ~10⁹) of stars, we compare the colour-colour diagram to the colours calculated for single stellar populations (SSPs). SSPs with different ages and metallicities are shown. Figure 7 shows that comparison. The apparent trend is that the outer bulge (red points) is more consistent with a young (~10^{6.5-7} yr) metal poor ($\log(Z/Z_{\odot}) \sim -2$) SSP, the middle bulge (green points) is more consistent with slightly less young (~10^{7-7.5} yr), less metal poor ($\log(Z/Z_{\odot}) \sim -1$ SSP, and the inner bulge (blue points) is more consistent with older (~10^{8.5} yr), metal poor ($\log(Z/Z_{\odot}) \sim -1.5$) SSP.

We carried out fits to the bulge spectral energy distribution (SED) using all five UVIT filters. No single SSP is a good fit (**Figure 8**). This shows that the colour-colour diagram does not contain enough information to properly constrain stellar populations. A mixture of two SSPs or three SSPs was able to fit the SED of the M31 bulge. The three SSP fit is significantly better than the two SSP fit.

The SEDs were extracted for 10 elliptical annuli in the bulge each with $\simeq 10\%$ of the whole bulge area, with outer semi-major axis of each annulus ranging from ~60" to ~190". For each annulus two SSP and three SSP fits were carried out. The results are shown in **Figure 9** for extinction, and **Figure 10** for masses of the SSPs. There is a mixture of at least two and probably three different SSPs, based on χ^2 of the fits in **Table 2**. This holds for all 10 annuli, *i.e.*, throughout the M31 bulge.



Figure 9. Best-fit extinction (A_V) vs. outer semi-major axis (a_{out}) of each annulus from the 2 SSP fits (red points) and from the 3 SSP fits (black points). **Table 2** gives the inner and outer semi-major axes of each annulus, a_{in} and a_{out} . The two points for largest a_{out} are for the outer-most annulus (lower point) and the Whole Bulge region (upper point). Linear functions are fit to A_V vs. a_{out} for all annuli for the 2 SSP model and fit to all but the innermost annulus for the 3 SSP model.

The extinction is variable, decreasing from centre (<60") to outer part of the bulge (180 to 190") in a nearly linear manner. The slope from the two SSP fit is steeper than for the three SSP fit, but the extinction falls in a narrow range (A_V = 0.4 to 0.5) for both models. The three SSP fits show evidence for a decrease in extinction for the centre.

The two SSP fit has an old (10¹⁰ yr) metal poor ($\log(Z/Z_{\odot}) = -2$) population plus an intermediate age (10⁹ yr) less metal poor ($\log(Z/Z_{\odot}) = -1.5$) population for the whole bulge and for all of the individual annuli. The masses of the old and intermediate age populations vary with distance from center but the ratio of intermediate SSP mass to old SSP mass is typically ≈ 0.1 . Both populations mass vs. distance from centre are well fit by exponential functions, with scale lengths of 65" for the intermediate age SSP and 110" for the old SSP. The higher concentration of the younger hotter population toward the centre can explain the trend seen in the colour-colour diagram.

The three SSP fit has an old (10¹⁰ yr) metal poor ($\log(Z/Z_{\odot}) = -2$) population plus an intermediate age (10^{9.5} yr) metal poor ($\log(Z/Z_{\odot}) = -2$) population and a young (10^{8.5} yr) higher metallicity ($\log(Z/Z_{\odot}) = -0.5$) population. The masses of the three populations vary with distance from center. The ratio of intermediate SSP mass to old SSP mass is typically ~0.15. The ratio of young SSP mass to old SSP mass is typically ~0.02. The SSP masses vs. distance from centre are well fit by exponential functions, with scale lengths of 75" for young SSP, ~450" for the intermediate SSP and 110" for the old SSP.



Figure 10. Top panel: Best-fit SSP masses vs. outer semi-major axis (a_{out}) of each annulus from the 2 SSP fits, with red points for the older metal-poor population and blue points for the younger metal-rich population. **Table 2** gives the inner and outer semi-major axes, a_{in} and a_{oub} of the 10 annuli and of the Whole bulge region. Bottom panel: Best-fit SSP masses vs. outer semi-major axis (a_{out}) of each annulus from the 3 SSP fits, with red points for the oldest metal-poor population, cyan points for the younger metal-rich population, and blue points for the intermediate age and metallicity population. For each set, there are two points at largest a_{out} the lower mass is for the outermost annulus and the higher mass is for the Whole Bulge region. Exponential functions are fit to A_V vs. a_{out} for all annuli for the 2 SSP and 3 SSP models.

The dominant old metal poor population has the same scale height and normalization from the two SSP and three SSP fits. The three SSP fit (with significantly improved χ^2) effectively replaces the 10° yr component of the two SSP fit with two separate SSPs of ages 10^{9.5} yr and 10^{8.5} yr. The scale-heights of the latter two populations are very different: the 10^{9.5} yr SSP has scale-height 450" vs. 75" for the youngest SSP. The different scale-heights of the 3 SSPs explains the observed colour change of the bulge: it is hotter near centre where the youngest SSP has the largest fractional contribution.

Hammer *et al.* (2018) [23] carried out hydrodynamical simulations of mergers with M31 and compared the simulations to several sets of observations of M31, including parameters of the Giant Stream, the M31 disc age-dispersion relation, the long-lived 10 kpc ring, the recent and long-lived star formation event, and the slope of the halo profile. They found that a 4:1 major merger where the nuclei merged 2 - 3 Gyr ago, with first passage 7 - 10 Gyr ago, could explain many of the observed features of M31. McConnachie *et al.* (2018) [24] analyzed data from the Pan-Andromeda Archaeological Survey of M31 to summarize the substructures in the stellar halo of M31. Their analysis shows the most distinctive substructures were produced by at least 5 different accretion events in the past 3 - 4 Gyr.

The minimum of 5 accretion events [24] can be consistent with merger with a single major galaxy [23] because there were a few passages between first passage and final merger of the nuclei. The passage would have created major streams of stars and gas which would cause accretion events at several different times and with different orbital parameters.

Our SSP fits to the bulge measure star formation in the bulge and are consistent with the above results. This star formation is caused by accretion of gas or disturbance of ambient gas to induce star formation⁴, thus related to merger and accretion events. The 10^{9.5} yr population comprises 17%, and the 10^{8.5} yr population comprises 0.3% of the mass of the old population (**Table 2**). If there are more than 3 SSPs in the bulge, the current analysis is unable to detect them given the data errors.

There have been previous studies of the stellar populations in the bulge of M31 ([25] [26] [27] and references therein). Our results are consistent with theirs, in that the bulk of the mass of stars are old (age ~10 Gyr), but not consistent in that they find that the old bulge population is metal rich, with [Fe/H] ~0.3 dex. The main difference between the previous studies and this study is that previous studies have used optical observations (optical HST photometry, or Lick indices), while we use FUV and NUV band photometry. One possibility is that the current set of SSP models are not accurate enough in the FUV to determine metallicity reliably. We plan to update the current study when SSP models which are better verified in the FUV become available.

The spatial structure of the M31 bulge has been studied by [28], with primary analysis of the Spitzer IRAC 3.6 micron observations of M31. That study fitted the bulge ignoring the inner few arcseconds containing the nucleus of M31. The fits used a Sersic profile for radial profiles along the major and minor axes or

⁴This is less likely for the bulge than for the disc.

azimuthally averaged radially profiles. They used two fitting methods: non-linear least squares and Monte Carlo Markov Chain. The results (their **Table 2**) were a Sersic index, *n*, between 1.7 and 2.4 and an effective radius, R_{e} between 0.5 and 1.1 kpc. Both n and R_e had typical errors of 10%. In comparison, they fit the 2-D image using the GALFIT software [29] and obtained similar results: n between 1.9 and 2.0 and R_e between 0.9 and 1.0 kpc. Our longest wavelength is 279 nm, far shorter than the 3.6 micron data analyzed by [28]. For 279 nm we find n values of 2.33, 2.30 and 2.27 for single Sersic, Sersic plus Gaussian or double Sersic fits, respectively (second, third and fourth sections of Table 1). These values are only slightly higher than those from [28]. For the shorter NUV 219 nm and the three FUV bands, we find significantly higher Sersic indices (3.2 to 5.6). The fact that the Sersic indices are quite different for NUV and FUV should not be too surprising, given that the shorter wavelengths are highly sensitive to the rare young and hot stars. These we have shown are more concentrated in the centre of the bulge (most clearly shown here in Figure 10).

6. Conclusions

We have carried out observation of the bulge of the Andromeda Galaxy in NUV and FUV wavelengths using the UVIT instrument on the AstroSat Observatory. M31's bulge is elliptical in shape with small but distinctive changes in ellipticity and position angle with distance from the nucleus of M31.

The bulge is centrally concentrated in UV, and approximately follows a Sersic profile. The nucleus (in the innermost 4") is complex, as known from optical studies [14]. For the brightness profiles in all filters but F148W, the bulge is well fit by Sersic plus Gaussian or double Sersic functions. For F148W, with its high signal-to-noise, none of the attempted functions gave statistically good fits, but the double Sersic had the best-fit, and gave no systematic residuals vs. radius, which may indicate that the bulge has small scale structure or clumps which are not fit by any smooth function.

The UV colour-colour diagram shows that the bulge becomes significantly bluer towards the centre. We carried out an analysis of the FUV-NUV SEDs using SSPs for the whole bulge and the bulge subdivided into 10 elliptical annuli. Our best fit model has three SSPs at each radius and yields the same best-fit ages and metallicities vs. radius for these SSPs. There is a dominant old SSP $(10^{10} \text{ yr}, \log(Z/Z_{\odot}) = -2)$, an intermediate-mass, intermediate-age SSP $(10^{9.5} \text{ yr}, \log(Z/Z_{\odot}) = -2)$ and a young low-mass SSP $(10^{8.5} \text{ yr}, \log(Z/Z_{\odot}) = -0.5)$. The different SSPs have exponential mass profiles vs. radius with different scale-heights for each SSP. The ages and masses of the SSPs are consistent with an active merger history for M31, as known from studies of M31 using optical data.

The FUV and NUV data from UVIT/AstroSat are useful to measure the young stellar populations which emit at these wavelengths. Future studies of regions beyond the bulge promise to turn up more important properties of the ages and spatial distributions of stellar populations in M31.

Acknowledgements

This project is undertaken with the financial support of the Canadian Space Agency and of the Natural Sciences and Engineering Research Council of Canada. This publication uses data from the AstroSat mission of the Indian Space Research Institute (ISRO), archived at the Indian Space Science Data Center (ISSDC).

Conflicts of Interest

The authors declare no conflicts of interest regarding the publication of this paper.

References

- McConnachie, A.W., Irwin, M.J., Ferguson, A.M.N., *et al.* (2005) Distances and Metallicities for 17 Local Group Galaxies. *Monthly Notices of the Royal Astronomical Society*, 356, 979-997. <u>https://doi.org/10.1111/j.1365-2966.2004.08514.x</u>
- [2] Williams, B.F., Lang, D., Dalcanton, J.J., et al. (2014) The Panchromatic Hubble Andromeda Treasury. X. Ultraviolet to Infrared Photometry of 117 Million Equidistant Stars. The Astrophysical Journal Supplement Series, 215, 9-43. https://doi.org/10.1088/0067-0049/215/1/9
- [3] Martin, D.C., Fanson, J., Schiminovich, D., et al. (2005) The Galaxy Evolution Explorer: A Space Ultraviolet Survey Mission. The Astrophysical Journal Letters, 619, L1-L6. <u>https://doi.org/10.1086/426387</u>
- [4] Singh, K.P., Tandon, S.N., Agrawal, P.C., et al. (2014) ASTROSAT Mission. Proceedings of the SPIE, 9144E, 1S.
- [5] Leahy, D.A., Bianchi, L. and Postma, J.E. (2018) ASTROSAT/UVIT Survey of M31, First Results: UV-Bright Stars in the Bulge. *The Astronomical Journal*, **156**, 269-281. <u>https://doi.org/10.3847/1538-3881/aae9e8</u>
- [6] Leahy, D.A., Postma, J., Buick, M., et al. (2020) New Results from the UVIT Survey of the Andromeda Galaxy. <u>https://arxiv.org/abs/2012.02727</u>
- [7] Leahy, D.A. and Chen, Y. (2020) AstroSat UVIT Detections of Chandra X-Ray Sources in M31. The Astrophysical Journal Supplement Series, 250, 23-37. https://doi.org/10.3847/1538-4365/abadfb
- [8] Leahy, D.A., Postma, J., Chen, Y. and Buick, M. (2020) AstroSat UVIT Survey of M31: Point-Source Catalog. *The Astrophysical Journal Supplement Series*, 247, 47-63. <u>https://doi.org/10.3847/1538-4365/ab77a9</u>
- [9] Leahy, D., Buick, M., Postma, J. and Morgan, C. (2021) Far-Ultraviolet Variable Sources in M31. *The Astronomical Journal*, 161, 215-229. <u>https://doi.org/10.3847/1538-3881/abe9b3</u>
- [10] Tandon, S.N., Subramaniam, A., Girish, V., et al. (2017) In-Orbit Calibrations of the Ultraviolet Imaging Telescope. The Astronomical Journal, 154, 128-142. <u>https://doi.org/10.3847/1538-3881/aa8451</u>
- Tandon, S.N., Postma, J., Joseph, P., *et al.* (2020) Additional Calibration of the Ultraviolet Imaging Telescope on Board *AstroSat. The Astronomical Journal*, **159**, 158-169. <u>https://doi.org/10.3847/1538-3881/ab72a3</u>
- [12] Postma, J.E. and Leahy, D. (2017) CCDLAB: A Graphical User Interface FITS Image Data Reducer, Viewer, and Canadian UVIT Data Pipeline. *Publications of the As-*

tronomical Society of the Pacific, **129**, 115002. <u>https://doi.org/10.1088/1538-3873/aa8800</u>

- [13] Postma, J.E. and Leahy, D. (2020) An Algorithm for Coordinate Matching in World Coordinate Solutions. *Publications of the Astronomical Society of the Pacific*, **132**, 054503. <u>https://doi.org/10.1088/1538-3873/ab7ee8</u>
- [14] Lockhart, K.E. (2017) A High Resolution View of Galactic Centers: Arp 220 and M31. Ph.D. Thesis, University of Hawai'i, Manoa.
- [15] Sersic, J.L. (1968) Atlas de Galaxias Australes. Observatorio Astronomico, Cordoba.
- [16] Fitzpatrick, E.L. and Massa, D. (2007) An Analysis of the Shapes of Interstellar Extinction Curves. V. The IR-through-UV Curve Morphology. *The Astrophysical Journal*, 663, 320-341. <u>https://doi.org/10.1086/518158</u>
- [17] Castelli, F. and Kurucz, R.L. (2003) New Grids of ATLAS9 Model Atmospheres. Modelling of Stellar Atmospheres. *Proceedings of the* 210*th Symposium of the IAU*, Uppsala, 17-21 June 2002, A20.
- [18] Bressan, A., Marigo, P., Girardi, L., *et al.* (2012) PARSEC: Stellar Tracks and Isochrones with the PAdova and TRieste Stellar Evolution Code. *Monthly Notices of the Royal Astronomical Society*, **427**, 127-145. https://doi.org/10.1111/j.1365-2966.2012.21948.x
- [19] Pastorelli, G., Marigo, P., Girardi, L., *et al.* (2020) Constraining the Thermally Pulsing Asymptotic Giant Branch Phase with Resolved Stellar Populations in the Large Magellanic Cloud. *Monthly Notices of the Royal Astronomical Society*, **498**, 3283-3301. <u>https://doi.org/10.1093/mnras/staa2565</u>
- [20] Groenewegen, M.A.T. (2006) The Mid- and Far-Infrared Colours of AGB and Post-AGB Stars. Astronomy & Astrophysics, 448, 181-187. https://doi.org/10.1051/0004-6361:20054163
- [21] Trabucchi, M., Wood, P.R., Montalbán, J., et al. (2019) Modelling Long-Period Variables—I. A New Grid of O-Rich and C-Rich Pulsation Models. Monthly Notices of the Royal Astronomical Society, 482, 929-949. https://doi.org/10.1093/mnras/sty2745
- [22] Kroupa, P. (2001) On the Variation of the Initial Mass Function. *Monthly Notices of the Royal Astronomical Society*, **322**, 231-246. https://doi.org/10.1046/j.1365-8711.2001.04022.x
- [23] Hammer, F., Yang, Y.B., Wang, J.L., et al. (2018) A 2-3 Billion Year Old Major Merger Paradigm for the Andromeda Galaxy and its Outskirts. *Monthly Notices of* the Royal Astronomical Society, 475, 2754-2767. https://doi.org/10.1093/mnras/stx3343
- [24] McConnachie, A.W., Ibata, R., Martin, N., *et al.* (2018) The Large-Scale Structure of the Halo of the Andromeda Galaxy. II. Hierarchical Structure in the Pan-Andromeda Archaeological Survey. *The Astrophysical Journal*, 868, 55-91. <u>https://doi.org/10.3847/1538-4357/aae8e7</u>
- [25] Dong, H., Olsen, K., Lauer, T., *et al.* (2018) The Star Formation History in the M31 Bulge. *Monthly Notices of the Royal Astronomical Society*, **478**, 5379-5403. <u>https://doi.org/10.1093/mnras/sty1381</u>
- [26] Saglia, R.P., Opitsch, M., Fabricius, M.H., et al. (2018) Stellar Populations of the Central Region of M 31. Astronomy & Astrophysics, 618, A156. <u>https://doi.org/10.1051/0004-6361/201732517</u>
- [27] Stephens, A.W., Frogel, J.A., DePoy, D.L., *et al.* (2003) The Stellar Content of the Bulge of M31. *The Astronomical Journal*, **125**, 2473-2493. <u>https://doi.org/10.1086/374570</u>

- [28] Courteau, S., Widrow, L.M., McDonald, M., *et al.* (2011) The Luminosity Profile and Structural Parameters of the Andromeda Galaxy. *The Astrophysical Journal*, 739, 20-36. <u>https://doi.org/10.1088/0004-637X/739/1/20</u>
- [29] Peng, C.Y., Ho, L.C., Impey, C.D. and Rix, H.-W. (2010) Detailed Decomposition of Galaxy Images. II. Beyond Axisymmetric Models. *The Astronomical Journal*, 139, 2097-2129. <u>https://doi.org/10.1088/0004-6256/139/6/2097</u>