

Performance Research on Magnetotactic Bacteria Optimization Algorithm with the Best Individual-Guided Differential Interaction Energy

Hongwei Mo, Lili Liu, Jiao Zhao

Automation College, Harbin Engineering University, Harbin, China

Email: honwei2004@126.com, liulilikaoyan@163.com, zhaojiaoyouxiang@163.com

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Abstract

Magnetotactic bacteria optimization algorithm (MBOA) is a new optimization algorithm inspired by the characteristics of magnetotactic bacteria, which is a kind of polyphyletic group of prokaryotes with the characteristics of magnetotaxis that make them orient and swim along geomagnetic field lines. The original Magnetotactic Bacteria Optimization Algorithm (MBOA) and several new variants of MBOA mimics the interaction energy between magnetosomes chains to obtain moments for solving problems. In this paper, Magnetotactic Bacteria Optimization Algorithm with the Best Individual-guided Differential Interaction Energy (MBOA-BIDE) is proposed. We improved interaction energy calculation by using the best individual-guided differential interaction energy formation. We focus on analyzing the performance of different parameters settings. The experiment results show that the proposed algorithm is sensitive to parameters settings on some functions.

Keywords

Magnetotactic Bacteria, Nature Inspired Computing, Differential Interaction Energy, Parameters Settings

1. Introduction

The research of algorithms have been conducted many years, the field of algorithm is very mature now. Evolutionary algorithm (EA) is a very popular research field. The common evolutionary algorithms are genetic algorithm (GA), Differential Evolution (DE) [1], Particle Swarm Optimization (PSO) [2] and Bacterial Foraging Optimization algorithm (BFOA) [3] and so on.

Magnetotactic Bacteria Optimization Algorithm (MBOA) [4] [5] which is introduced by Mo is one of the modern heuristic algorithms and inspired by the magnetotactic bacteria. In nature, magnetotactic bacteria (MTBs) is a special kind of bacteria which have many micro magnetic particles named magnetosome in their bodies.

These magnetic particles can generate moments to guide the bacteria to swim along geomagnetic field lines of the earth [6] [7]. In recent years, several improved MBOA, such as BMMBOA [8], MBOA-BR [9], MBOA-BT [10], PSMBA [11], MBMMA [12], have been proposed to modify the performance of MBOA. In the Moments of the Best Individual-based Magnetotactic Bacteria Optimization Algorithm (BMMBOA), similar to DE/best/1, the problem solutions are generated by moments mechanisms based on interaction energy among solutions [8]. In the Magnetotactic Bacteria Optimization Algorithm Based On Best-R and Scheme (MBOA-BR), similar to DE/best/r and scheme, it regulates the moments based on the information exchange between best individual's moments and some randomly one [9]. In the Magnetotactic Bacteria Optimization Algorithm based on Best-Target (MBOA-BT), similar to DE/best/target scheme, some cells will receive MTS information from the interaction between the local best one and the target one to balance the local search and global search [10]. In the Power Spectrum-Based Magnetotactic Bacteria Algorithm (PSMBA), it is based on the models of power spectra of the magnetic field noise produced by Brownian rotation of nonmotile bacteria in zero magnetic field [11]. In the Magnetotactic Bacteria Moment Migration Algorithm (MBMMA), the moments of relative good solutions can migrate each other to enhance the diversity of the MBMMA [12].

In this paper, we proposed a Magnetotactic Bacteria Optimization Algorithm with the Best Individual-guided Differential Interaction Energy (MBOA-BIDE) in order to overcome the shortcomings of complicated interaction energy calculation of the original MBOA and several new variants of MBOA and focus on the study of the effect of different parameters settings.

2. Magnetotactic Bacteria Optimization Algorithm with the Best Individual-Guided Differential Interaction Energy (MBOA-BIDE)

In the following, we briefly describe the basic operators and the main steps of MBOA-BIDE. MBOA-BIDE mainly has three steps and three main operators including moment generation, moment regulation, moment replacement.

2.1. Interaction Distance

First, in the algorithm, each solution is looked as a cell containing a magnetosome chain. At first we define X_{best} stands for the best cell of the population in the current generation t . The distance of the cell X_i and the best cell X_{best} , $D_i^t = (d_{i1}^t, d_{i2}^t, \dots, d_{in}^t)$, is calculated as follows: .

$$D_i^t = X_{best}^t - X_i^t \tag{1}$$

After that, we can get a distance matrix $D^t = (D_1^t, D_2^t, \dots, D_i^t, \dots, D_N^t)^t = \begin{bmatrix} d_{11}^t & d_{12}^t & \dots & d_{1n}^t \\ d_{21}^t & d_{22}^t & \dots & d_{2n}^t \\ \vdots & \vdots & \dots & \vdots \\ d_{N1}^t & d_{N2}^t & \dots & d_{Nn}^t \end{bmatrix}$. N is the size of

cell population, n stands for dimension of every cell.

2.2. Moments Generation

Based on the distances among cells, the interaction energy $E_i^t = (e_{i1}^t, e_{i2}^t, \dots, e_{ij}^t, \dots, e_{in}^t)$ is defined as

$$e_{ij}^t = c_1 * d_{ij}^t + c_2 * d_{pq}^t \tag{2}$$

where the settings of c_1 and c_2 will be discussed in the next section. d_{pq}^t stands for randomly selected variables from D^t . $p \in [1, N]$, $q \in [1, n]$.

After obtaining interaction energy, the moments M_i^t are generated as follows:

$$M_i^t = \frac{E_i^t}{B} \tag{3}$$

where the settings of B will be discussed in the next section.

Suppose $M_i^t = (m_{i1}^t, m_{i2}^t, \dots, m_{ij}^t, \dots, m_{in}^t)$, we can obtain a moment vector matrix $M^t = (M_1^t, M_2^t, \dots, M_i^t, \dots, M_N^t)^t$

$$= \begin{bmatrix} m'_{11} & m'_{12} & \cdots & m'_{1n} \\ m'_{21} & m'_{22} & \cdots & m'_{2n} \\ \vdots & \vdots & \cdots & \vdots \\ m'_{N1} & m'_{N2} & \cdots & m'_{Nn} \end{bmatrix}.$$

Then the total moments of a cell is regulated as follows:

$$v'_{ij} = x'_{ij} + m'_{is} \times rand \quad (4)$$

where m'_{is} stands for the moment of a randomly selected MTS from M^l . $l \in [1, N]$, $s \in [1, n]$.

2.3. Moments Regulation

After moments generation, the moments regulation is realized as follows:

If $rand > 0.5$, the moments in the cell are regulated as follows:

$$u'_{ij} = v'_{cbestj} + (v'_{cbestj} - v'_{ij}) \times rand \quad (5)$$

Otherwise, they are regulated as follows:

$$u'_{ij} = v'_{ij} + (v'_{cbestj} - v'_{ij}) \times rand \quad (6)$$

where v'_{cbestj} stands for the j th dimension of current best cell V'_{cbest} in the current generation.

2.4. Moments Replacement

After the moments regulation, we set a replacement probability 0.5, some cells with worse fitness are replaced as follows:

if $rand > 0.5$,

$$x'^{t+1}_{ij} = m'_{l'j} \times rand \quad (7)$$

where l' is a random number between 1 and N . $m'_{l'j}$ stands for the moment of a randomly selected MTS from $M'_{l'}$.

3. Parameters Settings

To evaluate the performance of MBOA-BIDE, the experiments are carried out on 10 benchmark functions. In this section, the benchmark functions are presented firstly. Secondly, the simulation results obtained from different parameter settings are analyzed and discussed.

In all experiments, during each run, a maximum fitness evaluation of 200000 generations is used. To reduce statistical errors, each test is repeated 30 times independently and the mean results are used in the comparisons.

3.1. Benchmark functions

The ten basic benchmark problems summarised in **Table 1**, can be classified into two groups. The first five functions $f_1 - f_5$ are unimodal functions. The unimodal functions here are used to test if MBOA-BIDE can maintain the fast-converging feature compared with the other methods. The next five functions $f_6 - f_{10}$ are multimodal functions with many local optima. These functions can be used to test the global search ability of the algorithm in avoiding premature convergence.

3.2. The effect of population size N

We set MBOA-BIDE with different population size ($N = 10, 40, 50, 100, 150$ and 200). The results of different population size are presented in **Table 2**. From **Table 2**, we can see that population size N with 40 is providing the best results in eight of the ten selected functions.

In this study, MBOA-BIDE with different population size N are ranked based on their mean performances. They are ranked according to their performances using a standard competition ranking scheme. In competition ranking, algorithms receive the same rank if their performances are same. The next performing algorithm is

Table 1. Benchmark functions.

| Function | Range | D | Formulation |
|------------------------------|-------------------|----|---|
| f_1 : Sphere | [-100, 100] | 30 | $f(x) = \sum_{i=1}^n x_i^2$ |
| f_2 : Schwefel 2.22 | [-10, 10] | 30 | $f(x) = \sum_{i=1}^n x_i + \prod_{i=1}^n x_i $ |
| f_3 : Schwefel 1.2 | [-100, 100] | 30 | $f(x) = \sum_{i=1}^n (\sum_{j=1}^i x_j)^2$ |
| f_4 : Quartic Noise | [-1.28, 1.28] | 30 | $f(x) = \sum_{i=1}^n ix_i^4 + random[0,1]$ |
| f_5 : Rosenbrock | [-30, 30] | 30 | $f(x) = \sum_{i=1}^{n-1} [100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2]$ |
| f_6 : Rastrigin | [-5.12, 5.12] | 30 | $f(x) = \sum_{i=1}^n [x_i^2 - 10 \cos(2\pi x_i) + 10]$ |
| f_7 : Generalized Schwefel | [-500, 500] | 30 | $f(x) = \sum_{i=1}^n -x_i \sin(\sqrt{ x_i })$ |
| f_8 : Foxholes | [-65.536, 65.536] | 2 | $f(x) = \left[\frac{1}{500} + \sum_{j=1}^{25} \frac{1}{j + \sum_{i=1}^2 (x_i - a_{ij})^6} \right]^{-1}$ |
| f_9 : Sixhump | [-5, 5] | 2 | $f(x) = 4x_1^2 - 2.1x_1^4 + \frac{1}{3}x_1^6 + x_1x_2 - 4x_2^2 + 4x_2^4$ |
| f_{10} : Goldstein price | [-2, 2] | 2 | $f(x) = \begin{bmatrix} 1 + (x_1 + x_2 + 1)^2 \\ (19 - 14x_1 + 3x_1^2 - 14x_2 + 6x_1x_2 + 3x_2^2) \\ 30 + (2x_1 - 3x_2)^2 \\ 18 - 32x_1 + 12x_1^2 + 48x_2 - 36x_1x_2 + 27x_2^2 \end{bmatrix}$ |

assigned a rank with a gap (gap is determined based on the number of equally performing algorithms). **Table 3** provides the ranks of the different population size and the average rank for all the functions based on mean performances. Based on the average ranking, the order of performance obtained is $N = 40$ followed by $N = 50$, $N = 10$, $N = 100$, $N = 150$ and $N = 200$ respectively.

Figure 1 presents the histograms that indicate the number of times each population size N have achieved the ranks in the range of 1 to 6. It can be seen that $N = 40$ achieves the top rank as compared to the other different population size.

3.3. The effect of magnetic field B

To study the effects of B in MBOA-BIDE, we use f_5 , f_7 and f_8 for testing the performance of MBOA-BIDE. Firstly we suppose B is constant ($B = 1, 3, 5, 7, 10$), and study the effect of B on test functions. Secondly, we also study the effect of B varying with generation increases as follows:

- B is linearly increases from 1 to 10 ($B = 1 - 10$ LINER).
- B is exponentially increases from 1 to 10 ($B = 1 - 10$ EXP)
- B is linearly increases from 1 to 100 ($B = 1 - 100$ LINER)
- B is exponentially increases from 1 to 100 ($B = 1 - 100$ EXP).

The results are shown in **Table 4**. From **Table 4**, for f_5 , we can see that when B is constant, $B = 10$, the method can achieve better performance, when $B = 1 - 100$ LINER can achieve better performance on f_5 . For f_7 , when $B = 3$ and $B = 1 - 100$ EXP, the method can achieve better performance. For f_8 , we can see that when $B = 1$ and $B = 1 - 10$ LINER can achieve better performance.

Figure 2 Presents the line chart and histograms that indicate the mean, best and median values each B have achieved for f_7 , respectively. From **Figure 2**, we can see when $B = 1 - 100$ EXP, MBOA-BIDE achieve the

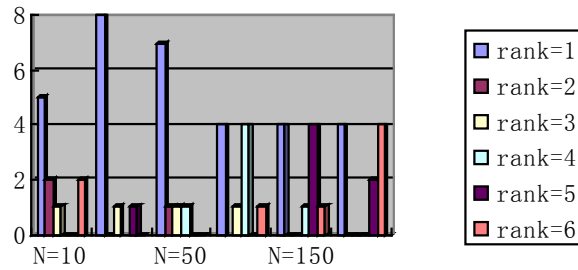


Figure 1. Histogram of individual mean ranks.

Table 2. Statistical results obtained by MBOA-BIDE with different population size N .

| Func. | | $N = 10$ | $N = 40$ | $N = 50$ | $N = 100$ | $N = 150$ | $N = 200$ |
|----------|------|---------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| f_1 | Mean | 0 | 0 | 0 | 0 | 2.5201e-254 | 4.5896e-181 |
| | Dev | 0 | 0 | 0 | 0 | 0 | 0 |
| | Rank | 1 | 1 | 1 | 1 | 5 | 6 |
| f_2 | Mean | 0 | 0 | 0 | 4.3137e-209 | 3.3968e-129 | 5.5820e-91 |
| | Dev | 0 | 0 | 0 | 0 | 6.3405e-129 | 1.2236e-90 |
| | Rank | 1 | 1 | 1 | 4 | 5 | 6 |
| f_3 | Mean | 0 | 0 | 0 | 3.0876e-312 | 5.5975e-182 | 1.0773e-124 |
| | Dev | 0 | 0 | 0 | 0 | 0 | 3.8100e-124 |
| | Rank | 1 | 1 | 1 | 4 | 5 | 6 |
| f_4 | Mean | 1.4263e-05 | 2.2258e-05 | 1.1082e-05 | 2.7951e-05 | 2.2837e-05 | 2.7755e-05 |
| | Dev | 1.0928e-05 | 1.7502e-05 | 1.1717e-05 | 2.8866e-05 | 1.5794e-05 | 3.4894e-05 |
| | Rank | 2 | 3 | 1 | 6 | 4 | 5 |
| f_5 | Mean | 21.4943 | 21.3003 | 22.1453 | 23.6719 | 24.2513 | 24.6209 |
| | Dev | 0.7394 | 0.4264 | 0.3933 | 0.2229 | 0.2143 | 0.1610 |
| | Rank | 2 | 1 | 3 | 4 | 5 | 6 |
| f_6 | Mean | 0 | 0 | 0 | 0 | 0 | 0 |
| | Dev | 0 | 0 | 0 | 0 | 0 | 0 |
| | Rank | 1 | 1 | 1 | 1 | 1 | 1 |
| f_7 | Mean | -1.1199e+04 | -1.1808e+04 | -1.1535e+04 | -1.0843e+04 | -1.0664e+04 | -1.0807e+04 |
| | Dev | 1.0496e+03 | 1.0526e+03 | 1.5453e+03 | 1.9108e+03 | 1.7327e+03 | 1.5578e+03 |
| | Rank | 3 | 1 | 2 | 4 | 6 | 5 |
| f_8 | Mean | 7.8914 | 2.5827 | 2.4521 | 1.1949 | 0.9980 | 0.9980 |
| | Dev | 4.0483 | 3.3070 | 3.6346 | 1.0783 | 4.1884e-12 | 5.8272e-12 |
| | Rank | 6 | 5 | 4 | 3 | 1 | 1 |
| f_9 | Mean | -1.03162842 | -1.03162845 | -1.03162845 | -1.03162845 | -1.03162845 | -1.03162845 |
| | Dev | 3.2639e-08 | 6.5144e-10 | 9.0922e-10 | 3.3173e-10 | 4.8852e-10 | 7.3936e-10 |
| | Rank | 6 | 1 | 1 | 1 | 1 | 1 |
| f_{10} | Mean | 3.0000 | 3.00000 | 3.0000 | 3.00000 | 3.00000 | 3.00000 |
| | Dev | 3.7073e-07 | 5.7118e-08 | 3.7689e-08 | 5.3505e-08 | 2.3598e-08 | 3.1246e-08 |
| | Rank | 1 | 1 | 1 | 1 | 1 | 1 |

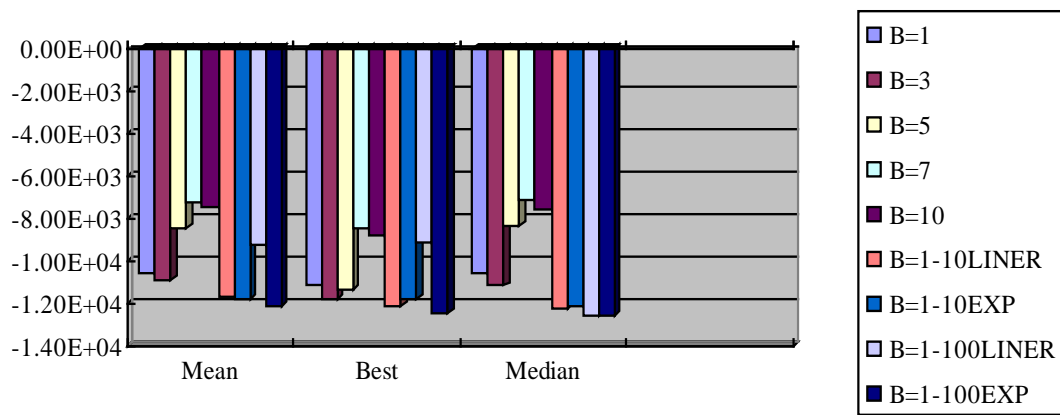


Figure 2. Histogram of statistical results of MBOA-BIDE with different B values

Table 3. Rank table for the mean values.

| Fun | N = 10 | N = 40 | N = 50 | N = 100 | N = 150 | N = 200 |
|-----------|--------|--------|--------|---------|---------|---------|
| f_1 | 1 | 1 | 1 | 1 | 5 | 6 |
| f_2 | 1 | 1 | 1 | 4 | 5 | 6 |
| f_3 | 1 | 1 | 1 | 4 | 5 | 6 |
| f_4 | 2 | 3 | 1 | 6 | 4 | 5 |
| f_5 | 2 | 1 | 3 | 4 | 5 | 6 |
| f_6 | 1 | 1 | 1 | 1 | 1 | 1 |
| f_7 | 3 | 1 | 2 | 4 | 6 | 5 |
| f_8 | 6 | 5 | 4 | 3 | 1 | 1 |
| f_9 | 6 | 1 | 1 | 1 | 1 | 1 |
| f_{10} | 1 | 1 | 1 | 1 | 1 | 1 |
| Avg. rank | 2.4 | 1.6 | 1.6 | 2.9 | 3.4 | 3.8 |

Table 4. Statistical results obtained by MBOA-BIDE with different B values.

| Fun | Mean | Median | Dev | Best | Worst |
|---------------------|---------|---------|--------|---------|---------|
| $B = 1$ | 26.9030 | 26.9095 | 0.1675 | 26.5374 | 27.2250 |
| $B = 3$ | 21.6974 | 21.8007 | 0.4795 | 20.6532 | 22.7105 |
| $B = 5$ | 21.2422 | 21.2866 | 0.4115 | 19.8061 | 21.8931 |
| $B = 7$ | 21.1473 | 21.2003 | 0.4291 | 19.7336 | 22.0915 |
| f_5 $B = 10$ | 20.9895 | 21.0589 | 0.3426 | 19.8434 | 21.5301 |
| $B = 1 - 10$ LINER | 21.2495 | 21.3203 | 0.4827 | 20.4088 | 22.3778 |
| $B = 1 - 10$ EXP | 20.3502 | 20.3270 | 0.9573 | 18.1462 | 21.9417 |
| $B = 1 - 100$ LINER | 19.3093 | 19.3314 | 0.1863 | 18.7989 | 19.6055 |
| $B = 1 - 100$ EXP | 21.0213 | 21.0466 | 0.3493 | 20.1838 | 21.4598 |

Continued

| | | | | | | |
|-------|---------------------|-------------|-------------|------------|-------------|-------------|
| | $B = 1$ | -1.0623e+04 | -1.0600e+04 | 247.5844 | -1.1137e+04 | -1.0214e+04 |
| | $B = 3$ | -1.0880e+04 | -1.1211e+04 | 1.0098e+03 | -1.1755e+04 | -8.3927e+03 |
| | $B = 5$ | -8.4505e+03 | -8.3105e+03 | 1.2271e+03 | -1.1428e+04 | -6.8399e+03 |
| | $B = 7$ | -7.2628e+03 | -7.1560e+03 | 548.8644 | -8.4595e+03 | -6.3355e+03 |
| f_7 | $B = 10$ | -7.4822e+03 | -7.5949e+03 | 647.8553 | -8.8086e+03 | -6.0637e+03 |
| | $B = 1 - 10$ LINER | -1.1722e+04 | -1.2147e+04 | 1.3761e+03 | -1.2320e+04 | -6.9487e+03 |
| | $B = 1 - 10$ EXP | -1.1799e+04 | -1.1768e+04 | 134.5198 | -1.2219e+04 | -1.1609e+04 |
| | $B = 1 - 100$ LINER | -9.1931e+03 | -9.1373e+03 | 1.3684e+03 | -1.2563e+04 | -6.5952e+03 |
| | $B = 1 - 100$ EXP | -1.2099e+04 | -1.2530e+04 | 1.3411e+03 | -1.2553e+04 | -7.2080e+03 |
| | $B = 1$ | 3.3981 | 0.9980 | 4.1130 | 0.9980 | 12.6705 |
| | $B = 3$ | 5.6198 | 4.5408 | 3.8717 | 0.9980 | 12.6705 |
| | $B = 5$ | 7.1337 | 8.2029 | 4.7696 | 0.9980 | 12.6705 |
| | $B = 7$ | 5.8563 | 3.9683 | 4.4765 | 0.9980 | 12.6705 |
| f_8 | $B = 10$ | 6.3849 | 6.1614 | 3.6604 | 0.9980 | 12.6705 |
| | $B = 1 - 10$ LINER | 1.8220 | 0.9980 | 2.4891 | 0.9980 | 12.6705 |
| | $B = 1 - 10$ EXP | 2.8240 | 0.9980 | 3.8456 | 0.9980 | 12.6705 |
| | $B = 1 - 100$ LINER | 2.7863 | 0.9980 | 3.8309 | 0.9980 | 12.6705 |
| | $B = 1 - 100$ EXP | 2.2053 | 0.9980 | 3.0987 | 0.9980 | 12.6705 |

performance on f_7 .

3.4. The Effect of c_1 and c_2

Firstly we suppose that c_1 and c_2 is constant, and study the effect of c_1 and c_2 on three test functions. We set $c_1 + c_2 = 1$, and c_1 with different values (0.1, 0.3, 0.5, 0.7, 0.9). Secondly, we also study the effect of c_1 and c_2 varying with generation increases. The parameter settings are as follows:

- $c_1 = 0 - 1$ L: c_1 is linearly increases from 0 to 1, $c_2 = 1 - c_1$;
- $c_2 = 0 - 1$ L: c_2 is linearly increases from 0 to 1, $c_1 = 1 - c_2$;
- $c_1 = 0.1 - 1$ E: c_1 is exponentially increases from 0.1 to 1, $c_2 = 1 - c_1$;
- $c_2 = 0.1 - 1$ E: c_2 is exponentially increases from 0.1 to 1, $c_1 = 1 - c_2$;
- $c_1 = 0 - 2$ L: c_1 is linearly increases from 0 to 2, $c_2 = 2 - c_1$;
- $c_2 = 0 - 2$ L: c_2 is linearly increases from 0 to 2, $c_1 = 2 - c_2$;

The statistical results are shown in **Table 5**.

From **Table 5** and **Table 6**, we can see that for f_5 , $c_2 = 0.1 - 1$ E obtain the best performance. For f_7 and f_8 , $c_1 = 0 - 2$ L obtain the best performance. and based on the average ranking, the order of performance obtained is $c_2 = 0 - 1$ L followed by $c_1 = 0 - 2$ L, $c_1 = 0 - 1$ L, $c_2 = 0 - 2$ L, $c_1 = 0.3$, $c_1 = 0.1$, $c_1 = 0.1 - 1$ E, $c_1 = 0.9$, $c_1 = 0.7$, $c_2 = 0.1 - 1$ E and $c_1 = 0.5$, respectively.

4. Conclusion

In this paper, by analyzing the performance of different parameters settings of MBOA-BIDE, we can see that when $N = 40 - 50$, B is exponentially increases from 1 to 100, c_2 is linearly increases from 0 to 1. $c_1 = 1 - c_2$, MBOA-BIDE obtain the better performance. The experiment results show that the proposed algorithm is

Table 5. Statistical results obtained by MBOA-BIDE with different C_1 and C_2 values.

| Fun | | Mean | Median | Dev | Best | Worst | Rank |
|---------------|-----------------|--------------------|----------------|---------------|-------------|----------------|----------|
| f_5 | $c_1 = 0.1$ | 21.3901 | 21.4491 | 0.2710 | 20.6426 | 21.8700 | 9 |
| | $c_1 = 0.3$ | 21.0181 | 21.0926 | 0.3837 | 20.1813 | 21.6728 | 6 |
| | $c_1 = 0.5$ | 21.0303 | 21.0385 | 0.3369 | 20.2972 | 21.7053 | 7 |
| | $c_1 = 0.7$ | 20.9564 | 20.9955 | 0.3636 | 20.0590 | 21.5185 | 5 |
| | $c_1 = 0.9$ | 21.3102 | 21.3443 | 0.2975 | 20.4737 | 21.8988 | 8 |
| | $c_1 = 0-1$ L | 21.0213 | 21.0466 | 0.3493 | 20.1838 | 21.4598 | 3 |
| | $c_2 = 0-1$ L | 21.0500 | 21.0776 | 0.4023 | 20.2052 | 21.7740 | 4 |
| | $c_1 = 0.1-1$ E | 20.8318 | 20.8450 | 0.3135 | 20.2436 | 21.6018 | 2 |
| | $c_2 = 0.1-1$ E | 20.7453 | 20.7975 | 0.3485 | 19.8905 | 21.3564 | 1 |
| | $c_1 = 0-2$ L | 21.8727 | 22.0773 | 0.6619 | 19.7414 | 22.8133 | 11 |
| $c_2 = 0-2$ L | 21.7704 | 21.9754 | 0.5780 | 20.3235 | 22.8893 | 10 | |
| f_7 | $c_1 = 0.1$ | -1.2352e+04 | -1.2532e+04 | 985.4425 | -1.2549e+04 | -7.1345e+03 | 4 |
| | $c_1 = 0.3$ | -1.2406e+04 | -1.2533e+04 | 690.3886 | -1.2547e+04 | -8.7509e+03 | 3 |
| | $c_1 = 0.5$ | -1.2295e+04 | -1.2536e+04 | 912.3674 | -1.2548e+04 | -8.8768e+03 | 6 |
| | $c_1 = 0.7$ | -1.2170e+04 | -1.2535e+04 | 1.1179e+03 | -1.2556e+04 | -8.6381e+03 | 7 |
| | $c_1 = 0.9$ | -1.2105e+04 | -1.2529e+04 | 1.3193e+03 | -1.2548e+04 | -7.3420e+03 | 8 |
| | $c_1 = 0-1$ L | -1.2099e+04 | -1.2530e+04 | 1.3411e+03 | -1.2553e+04 | -7.2080e+03 | 9 |
| | $c_2 = 0-1$ L | -1.2417e+04 | -1.2535e+04 | 646.0001 | -1.2552e+04 | -8.9972e+03 | 2 |
| | $c_1 = 0.1-1$ E | -1.2091e+04 | -1.2534e+04 | 1.3939e+03 | -1.2548e+04 | -6.6607e+03 | 10 |
| | $c_2 = 0.1-1$ E | -1.1775e+04 | -1.2533e+04 | 1.7649e+03 | -1.2547e+04 | -6.7527e+03 | 11 |
| | $c_1 = 0-2$ L | -1.2430e+04 | -1.2436e+04 | 34.6550 | -1.2488e+04 | -1.2349e+04 | 1 |
| $c_2 = 0-2$ L | -1.2297e+04 | -1.2434e+04 | 763.0817 | -1.2498e+04 | -8.2595e+03 | 5 | |
| f_8 | $c_1 = 0.1$ | 2.2362 | 0.9980 | 3.3244 | 0.9980 | 12.6705 | 4 |
| | $c_1 = 0.3$ | 2.7849 | 0.9980 | 3.7353 | 0.9980 | 12.6705 | 8 |
| | $c_1 = 0.5$ | 4.2983 | 0.9980 | 4.6656 | 0.9980 | 12.6705 | 11 |
| | $c_1 = 0.7$ | 2.9363 | 0.9980 | 3.7453 | 0.9980 | 12.6705 | 9 |
| | $c_1 = 0.9$ | 2.4267 | 0.9980 | 3.7530 | 0.9980 | 12.6705 | 6 |
| | $c_1 = 0-1$ L | 2.2053 | 0.9980 | 3.0987 | 0.9980 | 12.6705 | 3 |
| | $c_2 = 0-1$ L | 2.3454 | 0.9980 | 3.5817 | 0.9980 | 12.6705 | 5 |
| | $c_1 = 0.1-1$ E | 2.7436 | 0.9980 | 3.6848 | 0.9980 | 12.6705 | 7 |
| | $c_2 = 0.1-1$ E | 3.1675 | 0.9980 | 4.0601 | 0.9980 | 12.6705 | 10 |
| | $c_1 = 0-2$ L | 1.0102 | 0.9980 | 0.0563 | 0.9980 | 1.2898 | 1 |
| $c_2 = 0-2$ L | 1.5118 | 0.9980 | 2.0119 | 0.9980 | 12.6705 | 2 | |

Table 6. Rank table for the mean values.

| c_1, c_2 | Individual ranking of benchmark functions | | | Avg. RANK (R) |
|-------------------|---|-------|-------|---------------|
| | f_5 | f_7 | f_8 | |
| $c_1 = 0.1$ | 9 | 4 | 4 | 5.67 |
| $c_1 = 0.3$ | 6 | 3 | 8 | 5.67 |
| $c_1 = 0.5$ | 7 | 6 | 11 | 8 |
| $c_1 = 0.7$ | 5 | 7 | 9 | 7 |
| $c_1 = 0.9$ | 8 | 8 | 6 | 6.67 |
| $c_1 = 0 - 1 L$ | 3 | 9 | 3 | 5 |
| $c_2 = 0 - 1 L$ | 4 | 2 | 5 | 3.67 |
| $c_1 = 0.1 - 1 E$ | 2 | 10 | 7 | 6.33 |
| $c_2 = 0.1 - 1 E$ | 1 | 11 | 10 | 7.33 |
| $c_1 = 0 - 2 L$ | 11 | 1 | 1 | 4.33 |
| $c_2 = 0 - 2 L$ | 10 | 5 | 2 | 5.67 |

sensitive to parameters settings on some functions.

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