# Measuring Method of Radius of Curvature Based on Dual-Frequency Laser Interferometer 

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#### Abstract

In order to achieve high-accuracy measurement of radius of curvature of optical sphere, ultra-high accuracy radius of curvature testing device is developed by dual-frequency laser interferometer and Fizeau interferometer based on cat's eye and confocal method. Through analyzing the error source models of radius of curvature testing, optical configuration of the testing device has been optimized. Precise environment control and real-time monitoring system is also established to reduce the errors caused by environment. Through the above processes, the radius of curvature measurement relative accuracy is better than 2 ppm . One optical sphere, $\mathrm{R88.5} \mathbf{~ m m}$, test aperture 59 mm , has been tested. Testing result is $88499.465 \pm 0.176 \mu \mathrm{~m}$, meeting the design requirement. The method has high accuracy and practical advantages.


## Keywords

Radius of Curvature, Cat's Eye and Confocal Method, Dual-Frequency Laser Interferometer

## 1. Introduction

For high precision spherical optical elements are widely used in the fields of lithography, metrology, inertial confinement fusion, synchrotron radiation, etc., measurement accuracy requirements of radius of curvature of optical sphere continue to increase. High accuracy measuring technology of radius of curvature has important significance and application prospects [1] [2].

There are several methods of measuring radius of curvature, including spherometer, mechanical measurement by a Coordinate Measuring Machine (CMM), cat's eye and confocal method, laser tracker with laser interferometer method and so on. Spherometer has low relative accuracy about $3 \times 10^{-4}$ [3]-[4]. CMM has a relative accuracy about $4 \times 10^{-6}$, but there is the risk of scratches due to contact measurement. Laser tracker with laser interferometer method is always used in low accuracy and large radius of curvature measurement. Cat's eye and confocal method based on dual-frequency laser interferometer and Fizeau interferometer is suitable for high precision applications since it is non-contact and high accuracy [5]-[7].

[^0]High-accuracy testing device measuring radius of curvature based on cat's eye and confocal method is described in this paper. The testing device is developed based on dual-frequency laser interferometer and Fizeau interferometer. By analyzing the error source models of radius of curvature testing, optical configuration design of the testing device has been optimized. Precise environment control and real-time monitoring system is also established to reduce the errors caused by environment. Compared with other non-contact radius of curvature test methods, the method used in this paper has high accuracy and practical advantages.

## 2. Measuring Program of Radius of Curvature and Error Analysis

In this method, a figure measuring interferometer (a phase measuring interferometer, or PMI) is employed to identify the null positions at the center of curvature (confocal) and surface (cat's eye) of the test optical sphere. The power of the interferometric results is zero at those two positions. Move the test optic from cat's eye to confocal, called Z-direction. The dual-frequency laser interferometer (a displacement measuring interferometer, or DMI) is employed to identify the movement. The radius of curvature of the test optical sphere is equivalent to the Z-direction distance between cat's eye and confocal (Figure 1).

The main measuring error sources include: 1) cat's eye-confocal positional error, 2) test area error, 3) deadpath, 4) unsensed length, 5) cosine error, 6) DMI error, 7) PMI transmitted wavefront error, 8) error caused by the figure error and aperture variation.

### 2.1. Cat's Eye-Confocal Positional Error

Important characteristic of cat's eye-confocal positions is that the result of interferometric result defocus (Power) is zero. Environmental changes between interferometric cavity will reduce the test repeatability of defocus. Z-position of test optic is linear proportional to defocus around cat's eye and confocal. As in Equation (1),

$$
\begin{equation*}
\text { Power }=c_{0}+c_{1} \times Z_{\text {null }}+E_{\text {null }} \tag{1}
\end{equation*}
$$

where $c_{0}$ is the constant term, $c_{1}$ is the slope of defocus with Z-direction displacement., $Z_{\text {null }}$ is Z-position of test optic, $E_{\text {null }}$ is defocus variation caused by environmental changes. Cat's eye-confocal positional error could be represented as $\Delta Z_{\text {null }}$,

$$
\begin{equation*}
\Delta Z_{\text {null }}=E_{\text {null }} / c_{1} \tag{2}
\end{equation*}
$$

Due to cat's eye-confocal positional error varies when the environment changes, it could be achieved by statistical analysis. It is type A uncertainty. In this paper the measuring environment is well controlled, the cat's eye-confocal positional error is estimated about $0.120 \mu \mathrm{~m}$.

### 2.2. Test Area Error

Test area means the space between cat's eye and confocal positions. Environmental changes will cause the variation of refractive index of test area. Test area error is represented as Equation (3),


Figure 1. Schematic of cat's eye and confocal method for radius of curvature measurement.

$$
\begin{equation*}
\Delta L_{\text {Test }}=\Delta n \times R \tag{3}
\end{equation*}
$$

where $\Delta L_{\text {Test }}$ is test area error, $\Delta n$ is variation of air refractive index, $R$ is the length of test area. $\Delta n$ is calculated by Edlen formula [8] [9],

$$
\begin{equation*}
\Delta n=\sqrt{\left(2.7 \times 10^{-9} \Delta P\right)^{2}+\left(-9.3 \times 10^{-7} \Delta T\right)^{2}+\left(-1 \times 10^{-8} \Delta H\right)^{2}} \tag{4}
\end{equation*}
$$

where $\Delta P, \Delta T, \Delta H$ are the variation of barometric pressure, temperature and humidity. It is type A uncertainty. In this paper the test area error is estimated about $0.071 \mu \mathrm{~m}$.

### 2.3. Deadpath

Deadpath is the nearest Z-distance between test corner cube and reference corner cube. Deadpath error is caused by the variation of air refractive index.

$$
\begin{equation*}
\Delta L_{\text {dead }}=\Delta n \times L_{\text {dead }} \tag{5}
\end{equation*}
$$

where $\Delta L_{\text {dead }}$ is the deadpath error, $\Delta n$ is variation of air refractive index, $L_{\text {dead }}$ is the length of deadpath. In this paper environment is well controlled and monitored, what's more, the optical configuration is optimized to make the deadpath as short as possible. $L_{\text {dead }}$ is shorter than 200 mm . Deadpath error is estimated about $0.160 \mu \mathrm{~m}$. It is type A uncertainty.

### 2.4. Unsensed Length

The Z-distance between test optical sphere and test corner cube, and the Z-distance between reference corner cube and transmission sphere (TS lens) are unsensed length. The mechanism located in unsensed length will have a thermal expansion when temperature changes.

$$
\begin{equation*}
\Delta L_{\text {unsensed }}=\alpha L_{\text {unsensed }} \Delta T \tag{6}
\end{equation*}
$$

$\Delta L_{\text {unsensed }}$ is unsensed length error, $\alpha$ is the coefficient of thermal expansion, $L_{\text {unsensed }}$ is unsensed length, $\Delta T$ is variation of temperature. In this paper the optical configuration is optimized to make the unsensed length shorter than 50 mm , unsensed length error is estimated $0.024 \mu \mathrm{~m}$. It is type A uncertainty.

### 2.5. Cosine

If the laser beam is not exactly parallel with the direction of motion, a proportional difference increases with the measurement distance is established between the actual path length and the measured length. It is type B uncertainty.

$$
\begin{equation*}
\Delta L_{\text {cosine }}=\frac{R \theta^{2}}{2}=\frac{R}{2}\left(\left(\frac{\delta}{R}\right)^{2}+\theta_{P M I}^{2}+\theta_{\text {DMI }}{ }^{2}\right) \tag{7}
\end{equation*}
$$

where $\Delta L_{\text {cosine }}$ is cosine error, $R$ is radius of curvature of test optic, $\delta$ is straightness of motion mechanism, $\theta_{P M I}$ is the angle between PMI optical axis and the direction of movement of test optic, $\theta_{D M I}$ is the angle between DMI optical axis and the direction of movement of test optic. $\Delta L_{\text {cosine }}$ is estimated $0.024 \mu \mathrm{~m}$ in this paper.

### 2.6. DMI Error

In order to reduce DMI error, high precision dual-frequency laser interferometer should be used. DMI error includes type A and type B uncertainties. But type B uncertainty is major factor. According to the dual-frequency laser interferometer which is used, laser wavelength error ( $\pm 0.1 \mathrm{ppm}$ ) and wavelength stability ( $\pm 0.02 \mathrm{ppm}$ ), sub-divisional error ( 1.2 nm ) and DMI internal alignment error ( 2.2 nm ),

$$
\begin{equation*}
\Delta L_{D M I}=\left((0.1 \times 88.5)^{2}+(0.02 \times 88.5)^{2}+1.2^{2}+2.2^{2}\right)^{1 / 2} \tag{8}
\end{equation*}
$$

the DMI error $\Delta L_{D M I}$ is about $0.009 \mu \mathrm{~m}$.

### 2.7. PMI Transmitted Wavefront Error

This error exists, because the transmitted wavefront from PMI is not ideal.PMI transmitted wavefront error is
mainly from TS lens, whose transmitted wavefront is better than $0.5 \lambda \mathrm{PV}(\lambda=632.8 \mathrm{~nm})$ in this paper. Through analysis of test model in optical software Zemax, $\Delta L_{P M I}$ is less than $0.005 \mu \mathrm{~m}$ in this paper. It's system error belonging to type $B$ uncertainty.

### 2.8. Figure Error and Aperture Variation

Since the figure error of test surface, the PMI wavefront will not focus on the best fit sphere of test surface at cat's eye position. And when the test aperture changes, the radius of curvature of best fit sphere varies. The error $\Delta L_{\text {Arifact }}$ caused by figure error and aperture variation is estimated about $0.036 \mu \mathrm{~m}$.

### 2.9. Uncertainty Analysis of Radius of Curvature Testing Device

After analyzing the error source models from 2.1 to 2.8, the optical configuration design is optimized to reduce measurement errors. The testing device is developed as shown in Figure 2. There are two kinds of measurement errors, type A uncertainty and type B uncertainty. The type A uncertainty includes cat's eye-confocal positional error, test area error, deadpath, unsensed length. The type B uncertainty includes cosine error, DMI error, PMI transmitted wavefront error, error caused by the figure error and aperture variation. Abbe error is negligible.

$$
\begin{equation*}
E_{\text {A-type }}=\left(\Delta Z_{\text {null }}^{2}+\Delta L_{\text {Test }}^{2}+\Delta L_{\text {dead }}^{2}+\Delta L_{\text {unsensed }}^{2}\right)^{1 / 2} \tag{9}
\end{equation*}
$$

The type A uncertainty of the testing device is calculated by Equation (10) as $0.176 \mu \mathrm{~m}$.

$$
\begin{equation*}
E_{B-t y p e}=\left(\Delta L_{\text {cosine }}{ }^{2}+\Delta L_{D M I}{ }^{2}+\Delta L_{P M I}{ }^{2}+\Delta L_{\text {Artifact }}{ }^{2}\right)^{1 / 2} \tag{10}
\end{equation*}
$$

The type B uncertainty of the testing device is calculated by Equation (11) as $0.045 \mu \mathrm{~m}$.

$$
\begin{equation*}
E_{\text {Combined }}=\left(E_{\text {A-type }}{ }^{2}+E_{B-\text { type }}{ }^{2}\right)^{1 / 2} \tag{11}
\end{equation*}
$$

The combined uncertainty is $0.182 \mu \mathrm{~m}$ as Equation (12).
Hence, the testing device's combined uncertainty is $0.182 \mu \mathrm{~m}$ when measuring the test sphere ( R 88.5 mm , test aperture 59 mm ), relative accuracy is estimated as 2 ppm .

## 3. Experiment of Radius of Curvature Measurement

### 3.1. Measurement Procedure

- Adjust the direction of movement of the test optic, parallel with the PMI's and DMI's optical axis ( 0.5 mrad)
- Move the test optic to cat's eye position, then adjust TS to keep zero fringe pattern of PMI and set the three DMI zero.
- Move and adjust the test optical sphere to confocal position, keep zero fringe pattern of PMI, record the three DMI results and calculate average value. Average value is the nominal radius of curvature need to be tested.
- According to the barometric pressure, temperature and humidity value, get the real air refractive index. Then remove the error caused by variation of air refractive index, the real value of radius of curvature is achieved.


### 3.2. Experiment Result

Nine testing results of the radius of curvature of test optical sphere R88.5 is shown as follows (Table 1).
The type A uncertainty is $0.170 \mu \mathrm{~m}$ by statistical calculation. The testing result agrees with the analysis of error sources model in Chapter 2. Feasibility of optimizing optical configuration is verified. According to the analysis of type B uncertainty above, the combined uncertainty is shown as Table 2.

In summary, the testing result of the radius of test sphere R 88.5 mm is $88499.465 \pm 0.176 \mu \mathrm{~m}$, relative accuracy is 2 ppm (confidence level 95\%).

## 4. Conclusion

In order to achieve high accuracy radius of curvature measurement, cat's eye and confocal method based on dual-frequency laser interferometer is investigated. The radius of curvature testing device is developed, combining DMI, PMI and precise environment control and real-time monitoring system. The measurement error


Figure 2. Testing device for R88.5.
Table 1. Testing result of the radius of curvature of test sphere R88.5.

| No. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Average |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Testing result ( $\mu \mathrm{m}$ ) | 88,496.151 | 88,495.872 | 88,495.963 | 88,496.284 | 88,496.315 | 88,496.266 | 88,496.287 | 88,496.228 | 88,496.169 | 88,496.175 |
| Real value after correction ( $\mu \mathrm{m}$ ) | 88,499.641 | 88,499.352 | 88,499.453 | 88,499.524 | 88,499.465 | 88,499.436 | 88,499.447 | 88,499.498 | 88,499.389 | 88,499.465 |

Table 2. Analysis of the radius testing accuracy of test sphere.

| Type | $\mu \mathrm{m}$ |
| :---: | :---: |
| Type A uncertainty | 0.170 |
| Type B uncertainty | 0.045 |
| Combined uncertainty | 0.176 |

source models are established and analyzed to guide optimizing optical configuration. The radius of curvature of test sphere R88.5 mm, test aperture 59 mm is tested. The relative accuracy is 2 ppm , meeting the design requirement. In this paper, the core idea of the radius of curvature test method is to create all the test error source analysis models and to optimize testing device optical configuration for different test optics so that each source of error is minimized and ultra-high accuracy measurement of radius of curvature is achieved.

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