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Flood Resilient Cities: A Syntactic and Metric Novel on Measuring the Resilience of Cities against Flooding, Gothenburg, Sweden

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Abstract

Flooding is one of the most destructive natural disasters which have rapidly been growing in frequency and intensity all over the world. In this view, assessment of the resilience of the city against such disturbances is of high necessity in order to significantly mitigate the disaster effects of flooding on the city structures and the human lives. The aim of this paper is to develop a method to assess the resilience of a river city (the city of Gothenburg in Sweden), which is prone to flood Hazard, against such disturbances. By simulating flood inundation with different return periods, in the first step, the areas of impact are determined. To assess the resilience, two different methods are followed. One is a syntactic method grounded in the foreground network in space syntax theory and the other is based on measuring accessibility to the essential amenities in the city. In the first method, similarity and sameness parameters are defined to quantitatively measure the syntactic resilience in the city. In the next step, accessibility to amenities and the minimum distance to amenities before and after each disturbance is measured. The results, in general, show that such disturbances affect the city structure and the resilience of the city differently. For instance, the city is more resilient after flooding according to accessibility measures. This clearly means that the answer to the question of resilience is mainly dependent on "resilience of what and for what."

Keywords

Flooding, Resilience, GIS, Space Syntax, Accessibility

1. Introduction

Flooding as a natural disaster has great impacts on both individuals and communities and causes social, economic and environmental consequences is flooding. Flood is defined as a great overflow of water which especially submerges normally dry lands. Given the broad and intensive impacts on human loss, damaging of transportation, power plants and waste water systems, crops and farming and many other subsequences, people during the history put lots of effort to develop solutions to reduce flood impacts [1]. However, given the aberrant human interference in ecological system, urban sprawling, climate change, besides natural factors such as topography, geology of basins, land cover, amount of rainfall and etc. [2] [3], the frequency and intensity of flooding is increasing [4] [5] [6]. Based on statistics from the Centre for Research on the Epidemiology of Disasters [7] in the period 1994-2013 floods were the most frequent type of disasters, accounted 43 percent of all disasters and affected 55 percent of total population of the world during the past two decades. The report also emphasizes that floods had the most economical damage (US\$ 636 billion) after the storms and earthquakes during this period. Flood forecasting and flood warning, as European Union notices, is a "prerequisite for successful mitigation of flood damage" [8]. One of the frequently occurring flooding is river flooding which occurs when a river excesses the capacity of its canal because of rainfall, flash flooding, snowmelt and etc. and overflows its banks and the surrounding areas called flood plain. When the flood plain includes the urbanized areas, such flooding has great impacts on both population and infrastructures. Therefore, flood risk management in urban areas plays an essential role in preventing or reducing the impacts of flooding [9]. Flood simulation has a long history and from two centuries ago hydrologist and engineers have attempted to develop and improve prediction models of water flow in canals and watersheds [10]. The state-of-the-art in flood modelling is using GIS capability as a platform which enables researchers to combine physical and hydrological measurements with social and urban infrastructure data and estimate urban flood damage and flood vulnerability [11] [12] [13] [14].

Demir and Kisi [12], in a study on the Mert River in Turkey, integrated GIS and hydraulic model to represent a flood risk map. Creating a digital elevation model (DEM) of the study area and taking advantage of HEC-RAS¹ software, they simulate flood flows of different return periods in a range of 5 to 10000 years. The result showed that the area in the downstream of the Mert River affected by a flood with a return period of 10-years was 30 percent which was comparable with the impacts of an occurred flood in 2012 in the same area. In another study in the central part of Gothenburg, Sweden, Filipova and collogues [15] using MIKE 21 as hydrologic simulation software developed a 2-dimensional simulation model of flooding. Data used in this research was DEM, tem—

¹Hydrologic Engineering Centers River Analysis System(HEC-RAS) is one of the most applicable software in flood modelling released by USACE (United States Army Corps of Engineers, http://www.hec.usace.army.mil/).

poral precipitation data and land use values. The result showed that different part of the city including streets, canals and residential area can be affected by flood flow in case of intense precipitation and overloading the drainage system. Some researchers go steps further and not only simulate flooding but try to also measure the vulnerability of a city to flooding and make a city more resilient against flood. In this way, Lhomme and collogues [1], developing a Web-GIS for resistance capacity, absorption capacity and recovery capacity of different networks, tried to propose a framework to improve urban resilience in facing to flooding. In their research, the stress was on the urban networks and how the efficiency of such networks plays an important role in economic activity and other public facilities and infrastructures. Gil and Steinbach [16] used objective properties of the road network such as connectivity, closeness and between ness to show the indirect effect of flood Hazard on transport and socio-economic situations in London. In their paper, areas of impact were assessed based on two parameters, the level of separation from the rest of the city and the degree of accessibility to the rest of the city. The term resilience was coined in ecology by Holling [17, P.14] and defined as "a measure of the persistence of systems and of their ability to absorb change and disturbance and still maintain the same relationships between populations or state variables". Given the enhancing use of the term in many different fields such as economy, sociology, networking and engineering the definition and concept of resilience can vary and sometimes is malleable as it can be in contrast to its definition in other disciplines. The main difficulties occur when efforts are devoted to form the concept in order to take the term out of a purely abstract and general form and advance it toward a specific characteristic in a measurable and functional form [18] [4] [19]. However, there are common definitions of resilience in urban planning and disaster management. Wilbanks [20] defined urban resilience as "capability to prepare for, respond to, and recover from significant multi-hazard threats with minimum damage to public safety and health, the economy, and security" and Lhomme et al. [21] defined it as "the ability of a city to operate in a degraded mode (absorption capacity) and to recover its functions, despite the fact that some urban components are disrupted". UNSIDR [22] defined resilience in disaster management as "the ability of a system, community or society exposed to hazards to resist, absorb, accommodate to and recover from the effects of a hazard in a timely and efficient manner, including through the preservation and restoration of its essential basic structures and functions." In this view, as Carpenter et al. [23] noticed the main questions are resilience of what or resilience to what rather than the terminology itself. In contrast to flood modeling and flood simulation with a long history, urban resilience against flood Hazard is still under development due to the complexity of the urban systems and urban drainage systems [24]. It has been proven that urban forms and urbanization patterns are in close relationships and interaction with natural phenomena and the balance between them might break or disrupt with changing or damaging the physical structure of the cities [25] [26] [27] [28] [29]. Flood Hazard and urban flooding

thus as physical phenomena are influenced by the form of the cities and thus the magnitude of their impacts on urban infrastructures and human lives can be intensified by urban infrastructures such as street networks and buildings [24]. The aim of this research is to measure the resilience of a city against flooding according to the impacts of flooding on the street networks using two different methods; a syntactic measurement of the street networks discussed in space syntax research [27] [30], as its combination with resilience has recently proposed different approaches in assessing resilience, covering a range of possibilities from theory to practice at different scales of built environment from building to urban scale [18] [31] [32] [33]; and a metric measurement of accessibility of the street networks to amenities. In this view, comparing the syntactic properties of the street networks before and after flooding as well as exploring changes in the accessibility of the street networks after flooding are the ways conducted in this research in order to investigate the degree of resilience and vulnerability of the city against flooding.

The rest of this paper is organized as follows: in the next section, the study area and data used in this research are explained. The method to simulate flooding is briefly discussed and mostly referred to the work of the other researchers, since they are not central to this paper. Then, syntactic properties of the street networks are introduced and the way to calculate syntactic parameters of resilience is explained. Taking advantage of spatial analyses and statistics, the results of different analyses are illustrated and discussed in the result and discussion section. The paper ends up with the conclusions.

2. Study Area and Dataset

2.1. Study Area

Gothenburg with a population of 544285 is the second largest city in Sweden after the capital Stockholm (SCB, 2016, www.scb.se). The city is located on the west coast, in southwestern Sweden and the average elevation of the city is about 12 meters from the sea level. Göta River originates from the Vanern Lake and after over a distance of 93 km and passing through the city of Gothenburg empties into the Kattegat sea area in Baltic Sea. Göta River is Sweden's largest and richest rivers and represents, for example, the water source for drinking water to approximately 700,000 people. The river is used for many different interests. Göta River is also of great importance for agriculture and absolutely necessary to industries and other businesses to function. With an average water discharge of 563 m³/s Göta River as a natural resource not only influences the flora and fauna around itself but it also has a great impact on the community and the city streaming in [34]. Figure 1 shows the city and the flow of Göta River.

The city of Gothenburg is located in the estuary of Göta River along the coast of Kattegat, placing the city at high risk of rising water level of both the sea and the river, causing flooding in the city. Following a global trend, the rate of flooding in Gothenburg is increasing in recent years [15] [35]. Thus, measuring and estimating the flood risk, mapping and assessing potential damage and eco-

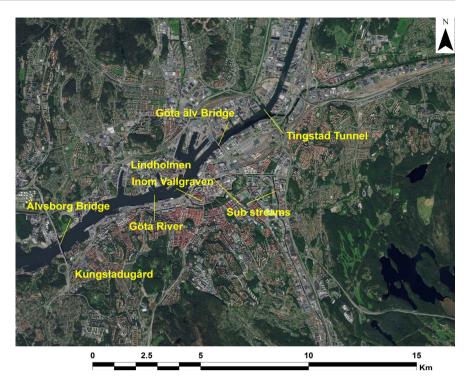


Figure 1. Position of Göta River in the city of Gothenburg.

nomical loss are not only of interest for researchers but are critical for city planners and other societies of the city dealing with flood Hazard and city infrastructures [34].

This paper aims at estimating flood in the city with different return periods in order to map the area at high risk and from that assess the resilience of the city against different simulated floods. The study area, in this research, is limited to that part of the river streaming in the city (municipality border) and flood simulation and its potential impacts on the structure of the city are investigated in such area.

2.2. Dataset

Data required for this paper are obtained from the following sources:

- Digital elevation model (DEM) with a resolution of 2 meters which covers the whole study area. The data source used for DEM production is LAS dataset which is an industry-standard binary format for storing airborne LIDAR data, provided by the Lantmäteriet (Swedish National Land Survey:

<u>http://www.lantmateriet.se/</u>) with an average spacing of 0.6 meter. All the analyses and converting LAS dataset to raster were done in ArcGIS and using LAS dataset toolbar embedded in this software.

It should be noted that in order for accuracy of the flooded area, in this research, both digital train model and digital surface model are produced. In this view, the real height of objects such as street networks and bridges can be determined, helping find out if the flooded area inundates such objects.

- Urban road network or road center line of Gothenburg derived from open

street map (OSM, downloaded from https://www.geofabrik.de/).

- Urban infra structures including the location of amenities (**Figure 2**) collected from a project called "Dela[d] Stad" [36] funded by Boverket/MISTRA Urban Futures (**Table 1**).
- Hydrological data and measurements of the river flows for a period of 15 years collected from the Swedish Meteorological and Hydrological Institute (SMHI)

(http://vattenwebb.smhi.se/modelarea/).

The normal editing on street networks and other data are done to make them GIS-ready and usable for the next analyses.

Due to completely different but relative analyses done for this research, the methodology is divided into three parts. In the first part, the methods to simulate flood flow explained. In the second part, the method used for defining and measuring the resilience in the city based on syntactic properties is discussed

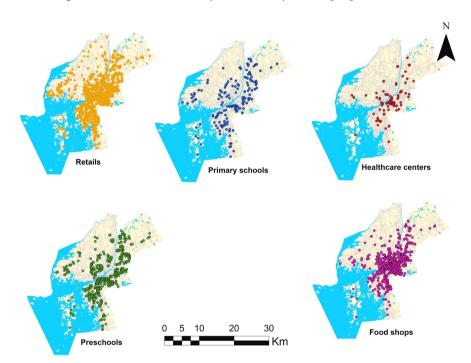


Figure 2. Distribution of different amenities in the cities.

Table 1. Different amenities used in this study.

Amenities	Number	
Retails	2471	
Pre-Schools	566	
Primary schools	180	
Healthcare centers	147	
Food shops	1237	
Total	4601	

and in the last part with introducing accessibility and the way measuring this value is illustrated. Having a better view of the methodology applied in this research each part is supported by a flowchart showing the implementation process in steps.

3. Methodology

3.1. Flood Simulation

River flooding with frequent occurrence can have great impacts in short time on the city and the life style of human. Gothenburg as a river and coastal city shows a higher potential to be exposed by flooding. Mapping the areas drowned by flooding will prepare useful information which can be used in the analysis of resilience.

Among different methods and tools used by different researchers, according to the data availability, level of desired accuracy, time and cost consuming. the method represented here is grounded in a GIS platform using tools developed by ESRI and HEC-RAS to model a flood simulation. Flowchart illustrated in Figure 3 shows the implementation process in steps.

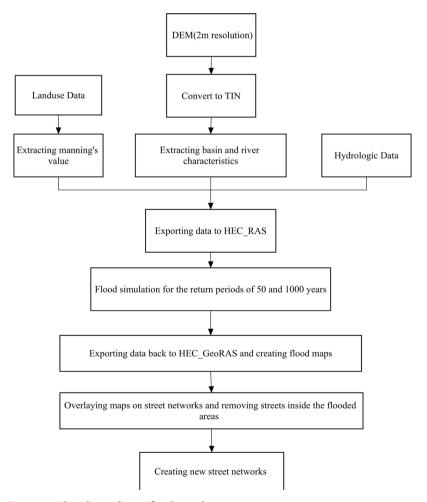


Figure 3. Flowchart of river flood simulation.

It is worth mentioning that due to some simplifications applied on such simulation, it should not be used by city planners as a high accurate result in their decision, but generally suggests a reliable method to analyze and measure the impact of flood Hazard on the city in order to assess the resilience and vulnerability of the city against such disturbances. Furthermore, the main part of this research is on measuring the city resilience in presence of flood Hazard, finding out how a city interacts with disasters causing changes in the structure of the city.

The first step is the preparation of DEM model of the study area obtained in a resolution of 2 meters from Lantmäteriet (https://www.lantmateriet.se). In the second step the maximum annual instant flows for the study area are obtained from SMHI. Then, using HEC-GeoRAS as a module embedded in ArcGIS software, the delineation of the watershed and stream network and geometric data including cross sections, flow direction, bank areas and Manning coefficient using the satellite image and based on the type of land use map are prepared and used as inputs to HEC-RAS to simulate potential water flow or flooding according to different return periods of 50 and 1000 years. In the end, the result is converted to the GIS platform to prepare the flood map (see [3] [12] [37]).

3.2. How to Measure Resilience

The main part of the methodology is devoted to measuring the resilience of the city against flood Hazard. The basis of resilience discussed in this research is on measuring Space Syntax properties including normalized angular integration value (NAIN) and normalized angular choice value (NACH) (cf. to [38] [39]). Integration is defined as the degree to which each segment, forming the street networks, is accessible from all others in a system. In this view, integration is comparable to closeness centrality [40]. Choice value is comparable to betweenness [41] in graph theory and is defined as the number of shortest paths that passes through each segment of all shortest paths between all pairs of segments in a system. A segment is a straight part of the street which lies between two consecutive intersections [39]. In line with this visualization, foreground network as a rudimentary concept is defined and applied to the street networks. Foreground network is part of the network which links the city centers together in different scales and normally includes longer and straighter segments of the network. To apply this concept to the street networks, according to the definition of NAIN and NACH, in this research, foreground network is considered as the number of segments with the top 10 percent of NACH and NAIN values [27] [18]. Now, similarity and sameness as the two measures to evaluate the degree of resilience of the city are introduced. Similarity measures the degree to which the size of foreground network has changed after a disturbance. This change can be calculated based on Equation (1),

$$\Delta x = \left| \left(A - B \right) \right| / A \tag{1}$$

where Δx is the change in the size of the foreground network, and A and B are

the size of the foreground network before and after a disturbance. In this view, the city structure is more similar, if Δx tends toward zero. Sameness measures the degree to which the segments forming foreground network before a disturbance also remain the same after that disturbance. In this view, a comparison of geometry of segments forming foreground networks before and after a disturbance can reveal the percentage of the segments remaining the same after disturbance. Sameness differs from zero to one, meaning that a higher percentage of sameness points out to relatively a higher resilience in the structure of the city and vice versa (refer to [18] for details). **Figure 4** shows a flowchart illustrating the process of extracting these two measures.

Another subject, proposed in this research to evaluate the resilience of the city is accessibility which can be defined and measured as the ease with which amenities can be reached from an origin through street networks in a city. In this view, accessibility can be affected and confined by flooding according to nearness or farness of an amenity to the flooded areas. In this research, accessibility is calculated based on the metric distance measured on street networks and illustrated as the number of amenities located within specific distances from street networks (Figure 5). Comparing accessibility measures before and after each disturbance will show the street networks of which their accessibility has changed after flooding. The impact of such disturbances is illustrated in the number and the intensity of changes in the accessibility of the street networks to different amenities.

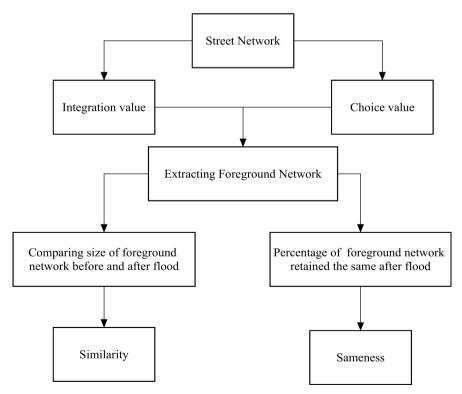


Figure 4. Flowchart of measuring the resilience of street networks based on foreground network.

Summarizing this section and better understanding of what analyses are going to be done in this research, Table 2 shows the list of all analyses conducted in

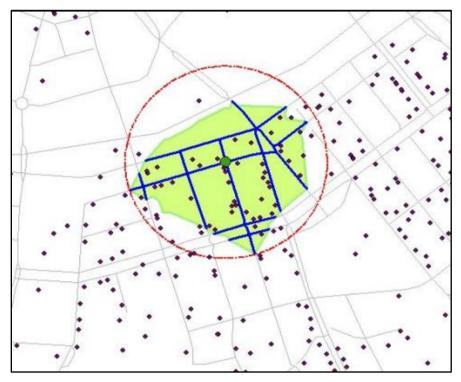


Figure 5. Accessible amenities within 100 meters from an origin (green point). It can be seen that the number of amenities fallen in the red circle (buffer around the origin) is different with the number of amenities fallen in the green polygon (accessibility on the street network).

Table 2. List of analyses conducted on street networks.

Syntactic Properties	Geometric Distance (Degree)	Compared to original situation for	
Normalized Angular Integration (NAIN)	180, 270, 360, 450, 900, 1200, 1800, 3600, 4500	Flood L & Flood H	
Normalized Angular Choice (NACH)	180, 270, 360, 450, 900, 1200, 1800, 3600, 4500	Flood L & Flood H	
Accessibility	Metric Distance (Km)	Compared to original situation for	
Retail	3	Flood L & Flood H	
Healthcare	3	Flood L & Flood H	
Preschool	3	Flood L & Flood H	
Primary school	3	Flood L & Flood H	
Food shop	3	Flood L & Flood H	
Minimum Distance	Metric Distance (m)	Compared to original situation only for	
Retail	In Meter	Flood H	
Healthcare	In Meter	Flood H	
Preschool	In Meter	Flood H	
Primary school	In Meter	Flood H	
Food shop	In Meter	Flood H	

this research. As seen, the main analyses are syntactic properties of the street networks based on NAIN and NACH properties, accessibility analysis of the street networks to the different amenities and analysis of the minimum distance of the street networks to amenities. It is worth mentioning that the results of all 3 analyses are illustrated and discussed in a comparison manner to realize the effect of flooding on the street networks.

4. Results and Discussions

The results are illustrated in a comparative manner, meaning that the same analyses are conducted on street networks before (in the steady state of the city without any disturbance) and after the disturbances when the streets inundated by flooding are removed from the network. Comparing these two situations can realize the degree to which the city keeps its resilience against flooding. The section starts with the comparison between syntactic properties (NACH and NAIN) of the city to show how such values changes before and after flood inundations. It should be noted that flood simulation calculated for the two return periods of 50 and 1000 years, hereafter called Flood L (low flooding) and Flood H (high flooding) respectively. In the main part of this section, the city resilience based on similarity and sameness measures and accessibility of street networks to different amenities is examined before and after flooding in order to figure out how the city is resilient to such disturbances. Table 2 shows the list of different analyses done for this research.

4.1. Syntactic Properties

Figure 6 shows the segments and the areas inundated (directly affected) by flooding with two different return periods. Table 3 includes number of segments and amenities located in the area inundated by flooding. What should be noticed in this research, is that the terms inundated and affected are used to address to different concepts. In this view, the term *inundated* points to segments and amenities drowned by water, while the term *affected* points to all other segments and amenities located outside the flooded areas and indirectly affected by flooding. The focus of this research is on affected parts and puts away inundated parts from the analyses. As an expected trend, the number of segments and amenities inundated by Flood H is more than Flood L.

Figure 7 shows NACH and NAIN values at global scale (angular analysis in 4500 degrees is considered as global) in different situations. As an interesting point, it can be seen that after Flood L and Flood H, the maximum NACH values increase, compared to the original situation. Additionally, segments with the high values (colored in black) are slightly moved back from the center and around the river, a spatial trend seen more in Flood H and less in Flood L respectively. For NAIN values, the maximum values vividly reduce after all disturbances (more in Flood H and less in Flood L respectively) and segments with the high values are intensely disappeared from the city center and around the river compared to the original situation.

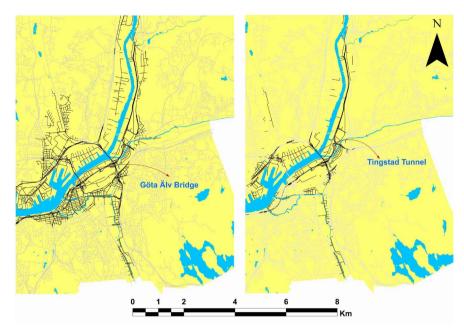


Figure 6. Street segments inundated (black) by Flood L (right) and Flood H (left), removed from the network for a comparative analysis.

Table 3. Number of segments and amenities directly affected (inundated) by flooding.

Disturbances	Total	Inundated by Flood L	Inundated by Flood H
Segments	100,556	2188	6680
Retail	4612	176	1329
Healthcare	147	5	28
Preschool	566	0	18
Primary school	180	0	6
Food shops	1237	95	443

Table 4 shows mean and maximum NACH and NAIN values extracted from street networks in different angular distances from local scales (180 - 450 degrees) to mid scales (900 - 1800 degrees) and global scales (3600 and 4500 degrees) before and after disturbances. As an expected trend in all situations and for both mean and maximum values, NACH and NAIN values reduce as they move from local to global scales. As an example, NACH property at the local scale (180 degrees) for original situation is 1.207, while it reduces to 0.911 at the global scale of 4500 degrees. Understanding how flooding changes the syntactic properties of the street networks, a comparison on the values before and after disturbances are conducted and the differences to original situation at each scale are illustrated in diagrams (Figure 8 and Figure 9).

To be consistent with the results, in all cases the values of original situation is subtracted from the disturbed situations (flood inundations). As a general trend, the differences in the mean value for all situations and for both NACH and NAIN values are positive or zero, meaning that the mean values decrease or re-

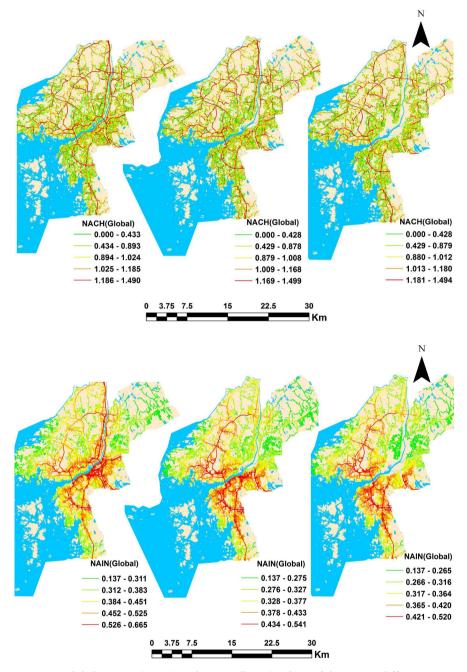


Figure 7. Global NACH (upper) and NAIN (lower) values of the city in different situations.

main unchanged after disturbances. The other trend which is also more or less the same is that the differences increase as the scale of angular analyses increase toward the global level. Having this in detail, **Figure 8** shows the differences for mean NACH and NAIN values on diagrams. As seen, for NACH (upper diagram), despite the generally increasing pattern, differences at the middle scales (900 and 1200 degrees) slightly reduce and rise again with moving to global scale. Such pattern is not seen for NAIN (lower diagram), as it shows steady increase in the differences, while increasing the scale. Based on **Figure 8**, flood

Table 4. NACH and NAIN properties of the street network calculated in different radii (O: original situation, L: Flood L and H: Flood H).

-						
NACH (degree)	O_mean	L_mean	H_mean	O_maximum	$L_{\rm maximum}$	H_maximum
180 (Local)	1.207	1.203	1.203	2.372	2.372	2.372
270	1.132	1.127	1.127	1.827	1.827	1.827
360	1.086	1.082	1.081	1.603	1.603	1.603
450	1.055	1.051	1.050	1.541	1.541	1.541
900	0.976	0.974	0.972	1.421	1.422	1.445
1200	0.950	0.949	0.947	1.436	1.436	1.447
1800	0.924	0.921	0.919	1.426	1.421	1.419
3600	0.910	0.895	0.889	1.485	1.483	1.473
4500 (Global)	0.911	0.893	0.886	1.490	1.499	1.494
NAIN(degree)	O_mean	L_mean	H_mean	O_maximum	L_maximum	$H_{maximum}$
NAIN(degree) 180 (Local)	O_mean 1.720	L_mean 1.717	H_mean 1.715	O_maximum 4.187	L_maximum 4.187	H_maximum 4.199
, 0	_	_	_	_	_	_
180 (Local)	1.720	1.717	1.715	4.187	4.187	4.199
180 (Local) 270	1.720 1.259	1.717 1.254	1.715 1.249	4.187 2.505	4.187 2.504	4.199
180 (Local) 270 360	1.720 1.259 1.027	1.717 1.254 1.020	1.715 1.249 1.013	4.187 2.505 1.596	4.187 2.504 1.596	4.199 2.504 1.599
180 (Local) 270 360 450	1.720 1.259 1.027 0.887	1.717 1.254 1.020 0.878	1.715 1.249 1.013 0.871	4.187 2.505 1.596 1.4	4.187 2.504 1.596 1.404	4.199 2.504 1.599 1.402
180 (Local) 270 360 450 900	1.720 1.259 1.027 0.887 0.613	1.717 1.254 1.020 0.878 0.597	1.715 1.249 1.013 0.871 0.587	4.187 2.505 1.596 1.4 1.018	4.187 2.504 1.596 1.404 1.001	4.199 2.504 1.599 1.402 0.992
180 (Local) 270 360 450 900 1200	1.720 1.259 1.027 0.887 0.613 0.548	1.717 1.254 1.020 0.878 0.597 0.527	1.715 1.249 1.013 0.871 0.587 0.516	4.187 2.505 1.596 1.4 1.018 0.902	4.187 2.504 1.596 1.404 1.001 0.880	4.199 2.504 1.599 1.402 0.992 0.866
180 (Local) 270 360 450 900 1200 1800	1.720 1.259 1.027 0.887 0.613 0.548 0.486	1.717 1.254 1.020 0.878 0.597 0.527 0.454	1.715 1.249 1.013 0.871 0.587 0.516 0.442	4.187 2.505 1.596 1.4 1.018 0.902 0.772	4.187 2.504 1.596 1.404 1.001 0.880 0.723	4.199 2.504 1.599 1.402 0.992 0.866 0.709

inundations show the higher differences and such differences increase as the analyses move toward the global scales. In this view, the maximum difference for NACH value is seen in 4500 degrees for flood (H) which is equal to 0.025 followed by 0.018 for flood (L) respectively. The maximum difference in NAIN value is also seen in 4500 degrees for flood (H) which is equal to 0.084 and followed by 0.068 and 0.50 for flood (L) accordingly.

Additionally, the results show that NAIN values compared to NACH values are more affected by disturbances. **Figure 9** shows differences for the maximum values on diagrams. As seen, differences in NACH values (upper diagram) follow different trend as that in the mean values. In this case, differences are zero at the local scales (180, 270, 360 and 450 degrees) for all situations, while taking negative values at the mid scales (900 and 1200 degrees) for Flood H. However, at the global scales (3600 and 4500 degrees) both Flood H and Flood L show positive values in 3600 degrees and negative values in 4500 degrees. For NAIN values, the maximum difference is seen in 4500 degrees for all situations and it is 0.145 for flood (H), 0.124 for flood (L). As a conclusion for this part, it can be stated that disturbances such as flood inundations influence syntactic properties

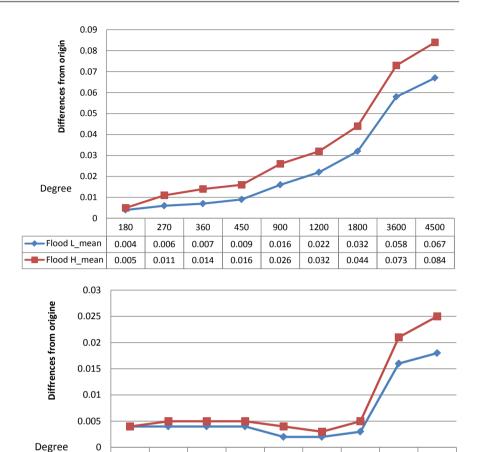


Figure 8. Differences in NACH (upper) and NAIN (lower) properties from local to global for different disturbances.

450

0.004

0.005

900

0.002

0.004

1200

0.002

0.003

1800

0.003

0.005

3600

0.016

0.021

4500

0.018

0.025

of the city structure by generally decreasing the values for NAIN and NACH properties less at local scales and more at global scales. The only exception is maximum NACH values that follow a nuanced trend at local and global scales for different situations.

4.2. Similarity

← Flood L_mean

Flood H_mean

As explained in the previous section, the basis for measuring similarity and sameness is foreground network. Figure 10 shows the foreground network based on NAIN and NACH values before and after the disturbances. It should be noted that the foreground network for all situations considers the segments which have the top 10 percent values of NAIN and NACH measures of angular segment analysis at a global scale (4500 degrees). As seen in Figure 10, foreground network (NAIN derivation) in the original situation is expanded to the both sides of the river and follows the river direction specifically in the northern part. The number of segments forming the foreground network is equal to 1580 based on Table 5. In Figure 10 (mid upper), foreground network after Flood L

180

0.004

0.004

270

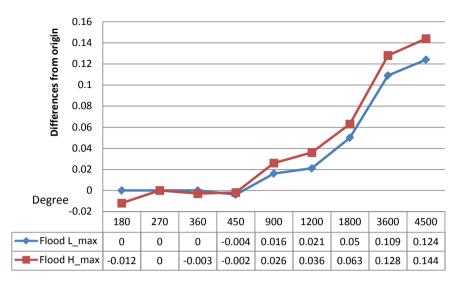
0.004

0.005

360

0.004

0.005



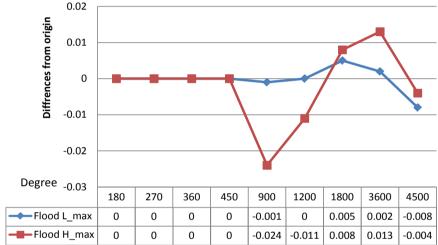


Figure 9. Differences in Maximum NACH (upper) and maximum NAIN (lower) properties from local to global for different disturbances

Table 5. Size of foreground network and similarity measured based on NACH and NAIN values in different situations.

Number of segments in Foreground network				Similari	ty to origin
Situations	Original	Flood L	Flood H	Flood L	Flood H
NACH	2035	1073	1165	0.473	0.428
NAIN	1580	1515	1549	0.041	0.02

shows that the upper part of original foreground network is removed and only the lower part remains. To compensate the effect of disturbance, the expansion of foreground network is perpendicular to the river direction. In this case, the number of segments forming foreground network is 1515 and the size of change is 0.041 based on **Table 5**. The situation after Flood H, based on **Figure 10** (upper right), follows closely the same situation as Flood L, except that the number of segments forming the foreground network is 1549 which is higher than Flood

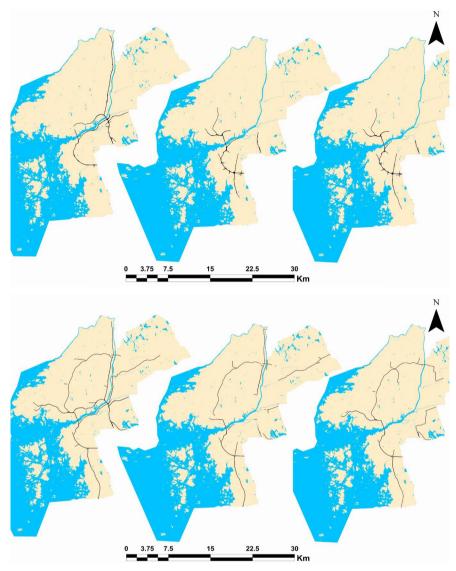


Figure 10. Foreground network of the street segments in different situations: NAIN derivation (upper) and NACH derivation (lower). From left to right: original, After Flood L and After Flood H

L, consequently resulted in the smaller size of change (0.020) and indeed higher similarity. The situation is different for NACH values. Figure 10 (lower left) shows that foreground network (NACH), in the original situation is expanded around the river on the both sides and follows the direction of river and its main tributaries. The number of segments forming the foreground network is 2035 based on Table 5. As a similar occurrence in both situations (Flood L and Flood H) and for both properties (NAIN and NACH), the tunnel is removed from the foreground network and the foreground network, no longer follows the river stream.

Figure 10 (mid lower) shows that the foreground network after Flood L is moved from the center of the city in the both sides of the river and forms only the outer parts. The tunnel is removed and the upper bridge loses some of its

connection in the northern part. Based on **Table 5** the number of segments and the size of change in foreground network are 1073 and 0.473 accordingly. Finally, in **Figure 10** (lower right), foreground network after Flood H is removed completely from the center of the city. The tunnel is removed but the bridge retains its connections and new connections are also added to the bridge in the north part. In this view, the number of segments and the size of changes in foreground network are 1165 and 0.428 respectively (**Table 5**). This makes the size of foreground network after Flood H more similar to original foreground network.

4.3. Sameness

As discussed in methodology, the number of such segments compared with the total number of segments forming the foreground network defines sameness measure which is a factor to show how resilient the city is against disturbances. In this view, the greater number of unchanged segments conveys the higher resilient in the street networks. Figure 11 shows the segments of foreground network remained unchanged after disturbances. As a similar trend in both Flood L and Flood H, it can be seen that the impact of flooding on the riparian areas causes that the same segments are located far from the river. Figure 11 also shows that the connection of the two riverbanks, inside the city area, is limited to a bridge (Älvsborg Bridge) in the south and both Göta Älv Bridge and Tingstad Tunnel in the middle and the north of the city are removed from the city transport system.

Table 6 shows the results of sameness in different situations for the city of Gothenburg. Flood L has the lowest sameness for NACH (0.408) and Flood H has the lowest sameness for NAIN (0.301).

Flood H also shows the higher sameness than Flood L for NACH values which literally points out to relatively a higher resilience. According to Figure 10 and Figure 11 and Table 5 and Table 6, it can be seen that Flood H shows higher resilient in the foreground network compared to Flood L, although the number of segments inundated by Flood H is much more than by Flood L. It seems that in the case of Flood H, by removing more segments from the original network, the city restore itself by making new connections around the original foreground network while in the situation of Flood L, the observed compensation lacks such connections.

4.4. Accessibility

Accessibility analysis as defined in the methodology part is conducted on the city network in different situations before and after disturbances to show how flood inundations influence accessibility to different amenities in the city. In this section accessibility is measured based on metric distance (3000 meters as a basis) on city network before flooding and then it is compared to the same measure after flooding. As an agreement in this paper, without considering the direction of

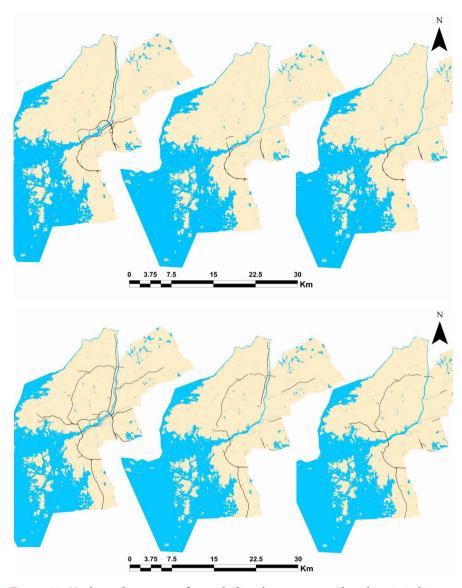


Figure 11. Unchanged segments after each disturbance compared to the original situation: NAIN (upper) and NACH (lower) derivations. From left to right: original, After Flood L and After Flood H.

Table 6. Sameness measured based on NACH and NAIN in different situations.

	Number of same s	segments to origin	Degree o	f Sameness
Situations	Flood L	Flood L	Flood L	Flood H
NACH	831	864	0.408	0.425
NAIN	523	476	0.331	0.301

the river, the left part of the river is determined as the northern part and the right part of the river as the southern part.

4.4.1. Accessibility to Retails

In Figure 12, the degree of accessibility difference between original situation

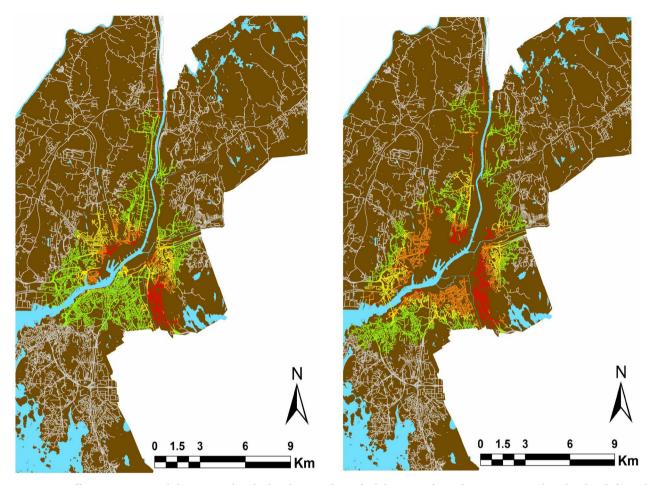


Figure 12. Differences in accessibility to retails calculated in a radius of 3 kilometers from the street networks: Flood L (left) and Flood H (right). Differences are increased from green to red.

and flood situations is shown in different colors from green color showing the low differences to red color showing the high differences. As seen, the area of differences for Flood L is distributed asymmetrically to the both sides of river, but with a high change in the middle of the river city. As an interesting point, the riparian areas in the southern side are less affected by Flood L compared to the northern side. The most affected areas in the southern side occur along the sub stream river. Figure 12 (right) shows a different situation for Flood H and the areas of impact are expanded. In this view, the riparian areas in the both sides are highly affected and the total number of segments affected by Flood H (23603) is increased compared to Flood L (20780) based on Table 7. However, the asymmetrical distribution of accessibility differentiation is yet seen and same as Flood L, the area along the sub stream river is highly affected and further extended to the both sides of the sub stream.

4.4.2. Accessibility to Healthcare Centers

In Figure 13, the difference in accessibility to healthcare centers for Flood L and Flood H is illustrated. In Flood L situation, same as accessibility to retails, the influenced areas are not distributed equally to the both sides, as it is more ex-

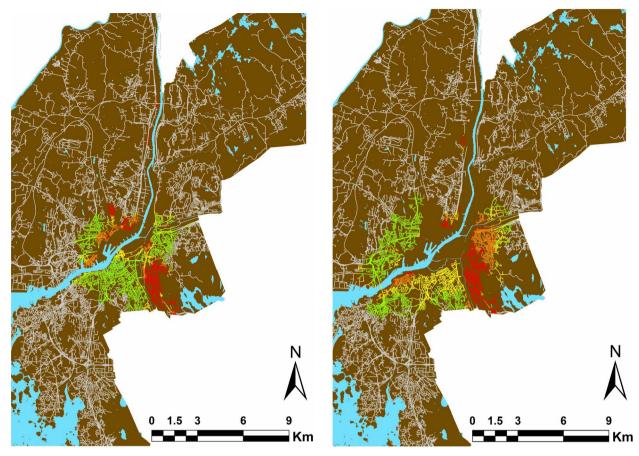


Figure 13. Differences in accessibility to healthcare centers calculated in a radius of 3 kilometers from the street networks: Flood L (left) and Flood H (right). Differences are increased from green to red.

Table 7. Number of segments of which accessibility and minimum distance are affected by Flood L and Flood H for different amenities separately.

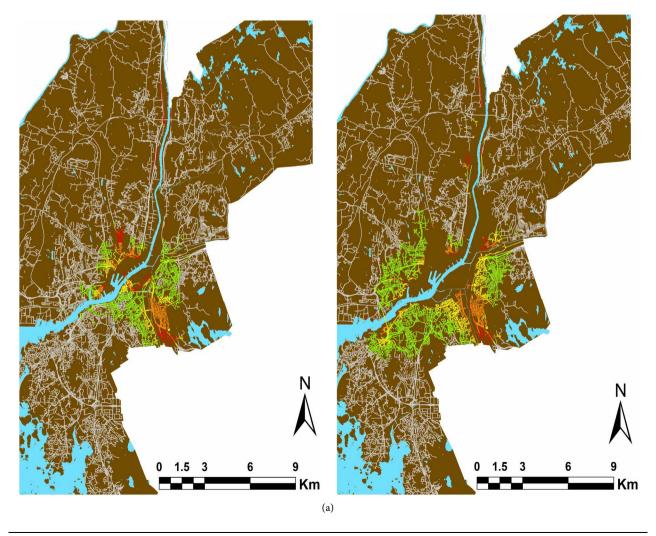
	Floo	d-L	Fl	ood-H
Amenities	Accessibility	Minimum distance	Accessibility	Minimum distance
Retails	20,780	737	23,603	547
Healthcare	12,060	2748	14,994	3788
Preschool	9391	1776	14,453	818
Primary school	7465	1442	10,336	1205
Foods shops	22,030	734	21265	1773

tended in the southern part of the river alongside the sub stream. Additionally, as seen in **Figure 13**, the eastern part of the sub stream is also more affected compared to the western part, while the western part is more expanded. The situation in the northern part of the river shows that riparian areas spatially in the middle part are more influenced by Flood L. Looking at **Figure 13** for Flood H (right), three different distributions are recognized. A more affected but less distributed area is located in the eastern part of the sub stream, a low to mid af-

fected but more distributed in the western part of the sub stream and a low affected and less distributed area located in the northern part of the main river. Riparian areas in the southern side of the river are generally more affected than areas in the northern side of the river. Table 7 shows the number of segments which their accessibility reduces after flood events. Based on Table 7, the number of affected segments for healthcare centers is less than for retails, stating a higher impact of flooding on retails.

4.4.3. Accessibility to Preschools and Primary Schools

In **Figure 14(a)** and **Figure 14(b)**, the differences in accessibility to preschools and primary schools after disturbances are investigated. Despite following a similar trend to the other amenities, there are yet differences in their distributions. For Flood L, the southern part and the area along the sub stream is intensively affected for both preschools and primary schools. In the northern part, the marginal area along the river shows higher impact. However, as seen in **Figure 14(a)** preschools are more affected by Flood L rather than primary schools. This can be found by both broader distributions of affected areas and the number of segments with the higher impact (orange and red colors) in preschools compared to



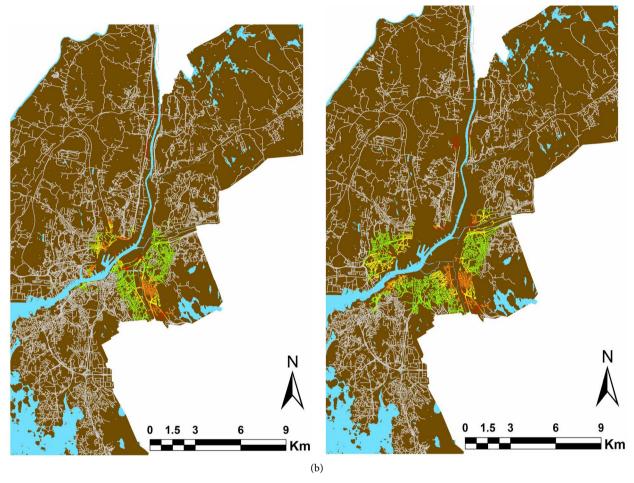


Figure 14. (a) Differences in accessibility to preschools calculated in a radius of 3 kilometers from the street networks. Flood L (left) and Flood H (right). Differences are increased from green to red; (b) differences in accessibility to primary school calculated in a radius of 3 kilometers from the street networks. Flood L (left) and Flood H (right). Differences are increased from green to red.

primary schools. For Flood H, the affected areas for preschools are more distributed compared to primary schools. This can be seen on both sides of the river. Additionally, Flood H, same as Flood L, has a higher impact on the accessibility to preschools than to primary schools, represented by more areas highlighted in red for preschools. **Table 7** also shows that the number of segments with a reduced accessibility for preschools (14,453) is higher than for primary schools (10,336). However, the number of segments affected by flooding for schools is by far less than for healthcare centers and retails.

4.4.4. Accessibility to Food Shops

By comparing the influenced areas for Flood L and Flood H in **Figure 15**, it can be seen that the general trend of both flooding is similar and the differences is in the degree of impact which is obviously higher for Flood H. Same as the other amenities, the affected areas are more distributed in the southern part of the river spatially around the sub stream. For Flood L, this distribution to some extent follows the river stream, a trend also seen in retails but not seen in schools and healthcare centers. The reason might be in the higher distribution of such amen-

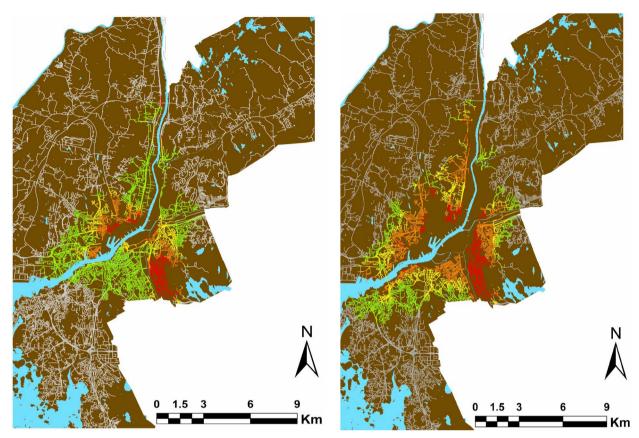
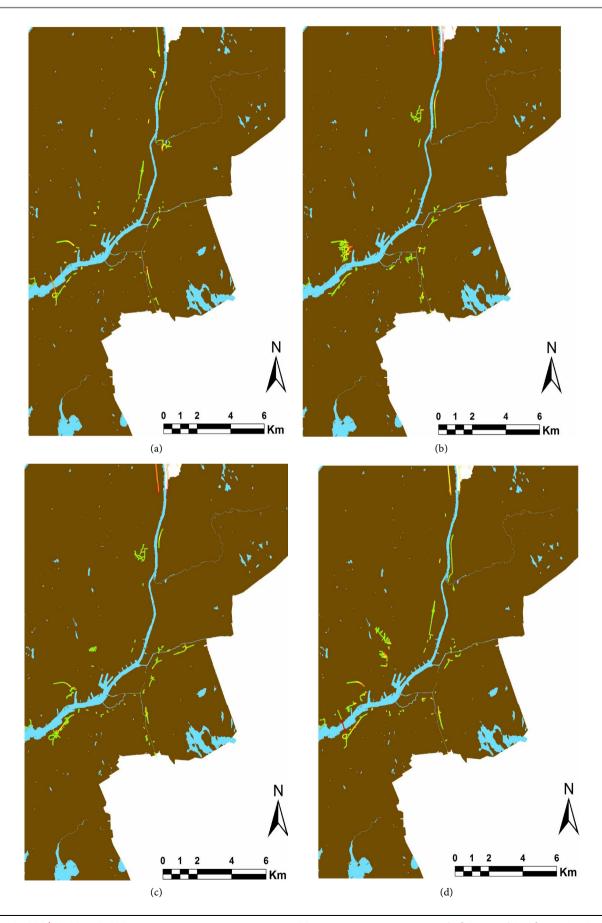


Figure 15. Differences in accessibility to food shops calculated in a radius of 3 kilometers from the street networks. From left to right: Flood L and Flood H. Differences are increased from green to red.

ities around the river stream (**Figure 2**). For Flood H, although the degree of impact is higher than Flood L, as an interesting point, the number of affected segments is less than Flood L this can be found by **Table 7** in which the number of affected segments for Flood L is 22030 while it is 21265 for Flood H. This is because, as previously mentioned, in this research the focus is on the segments affected by flooding not inundated by that. In this view, by considering the number of segment directly affected (inundated) by flooding obtained in **Table 2**, it can be seen that 6680 segments are inundated by Flood H which is much bigger than 2188 segments inundated by Flood L.

4.4.5. Minimum Distance to Different Amenities

One of the important parameters representing the impact of flood events on the city structure is changes in the minimum distance to amenities. In this view, areas with a higher impact usually show an increase in the distance to the closest amenity. In the last part of this paper the analysis of the minimum distance to the different amenities is done. Thanks to slight changes in the minimum distance to the amenities specifically after Flood L, in this section the result is illustrated only for Flood H, but Table 7 contains the results for both situations. As a general trend in all maps in Figures 16(a)-(e), the effect of Flood H on the minimum distance to amenities is low and mostly limited to few segments in the



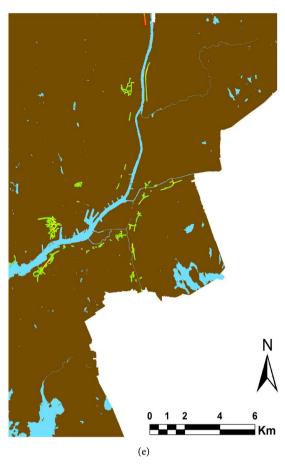


Figure 16. Segments of which the minimum distance to different amenities are increased after Flood H. (a) retails; (b) primary school; (c) preschool; (d) food shops and (e) healthcare centers. Green (low changes) and red (high changes).

riparian areas of the main river, while their distributions are not symmetric and do not follow the direction of main river. It can be seen that the most affected amenity by minimum distance is healthcare centers (3788 segments). As such, retails are the least affected amenities (547) among all. This is because of the differences in the distributions (Figure 2) and in the number of different amenities (Table 1), causing one amenity (healthcare here) more and another (retails here) less vulnerable to flooding. Additionally, as a difference between the preschools and primary schools' tendencies, it can be seen that the minimum distance for primary schools is more affected by Flood H spatially on the northern side of the river. As an interesting point, it can be seen that Älvsborg Bridge in retails and healthcare centers is also affected and its minimum distance to these amenities is increased. In this view, the degree of impact for healthcare centers is bigger since the bridge is highlighted in red while for retails it is seen in orange. It should be noted again that the results illustrated here focus on the segments and amenities outside of the inundated areas and tries to illustrate the effect of flooding on the rest of the city. This, therefore, means that the segments and amenities affected directly (inundated) by such disturbances are locked up from the entire analyses in this research. Table 3 gives a summary of the segments and amenities removed from the analyses.

5. Conclusions

Flooding as natural disasters with rapid increase of their occurrences has great impact on the structure of cities and the city networks. Thus, investigating the impact of such disasters, and determining sensitive and high-risk areas of the city are essential in order to manage and reduce the risk of such disasters. In this paper, the resilience of the city of Gothenburg against river flooding is investigated. Two different methods are conducted on the street networks; syntactic resilience and accessibility assessment. In the syntactic resilience, two factor similarity and sameness are applied on the foreground network of the city.

Similarity for NAIN and NACH properties shows that the city after Flood H is more similar to the original situation according to the size of foreground network. The result of sameness for NAIN shows that the city after Flood L has a higher degree of sameness, while sameness of the city after Flood H for NACH property is higher. In this view, the overall results of syntactic resilience state that the city after Flood H is more resilient than after Flood L. Again, it should be noticed that the analyses are focused on the remaining areas after flooding and the inundated areas are excluded from the analyses. The comparison of syntactic properties of the street networks in different angular radii before and after flooding shows that NAIN and NACH properties are affected by flooding, as in most cases the degree of changes (decrease or increase) at medium and global scales is higher. Additionally, in most cases, except for maximum NACH, syntactic values after flooding reduce in which the maximum reduction in most cases goes for the city after Flood H.

In accessibility analysis, two parameters are measured; accessibility of street networks to different amenities in the city and the minimum metric distance to amenities. As a general trend, Flood H influences the accessibility to amenities more than flood L and in this respect, it can be stated that the city is more resilient after Flood L. However, the results of accessibility are different according to different amenities. In this view, retails and food shops are more affected by flooding, while schools show the minimum impact of flooding. Additionally, the results show that the disturbances do not influence the minimum distance to amenities significantly and the number of affected segments are low, particularly compared with the affected segments in accessibility analysis. In this view, healthcare centers show the highest effect of minimum distance after Flooding, while food shops and retails are amenities with the lowest impact of flooding.

In conclusion, according to the results of different analyses, it can be stated that the city, in general, is more resilient specifically against Flood L and such disturbances do not affect the remaining part of the city significantly. However, it should be noticed that the resilience measured in this research is based on the indirect effect of flooding and, thus, it does not consider directly inundated areas. In this view, more analyses such as the assessment of human and financial

losses in the flooded areas are also needed in order to have a better estimation of the resilience of the city against such disturbances, stating that the resilience of a city should be investigated from different point of view and based on a bundle of different parameters and, thus, it should not be confined to one or two parameters

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