

# Determination of Neutron Fluxes and Spectrum Shaping Factors in Irradiation Sites of Ghana's Miniature Neutron Source Reactor (mnsr) by Activation Method after Compensation of Loss of Excess Reactivty

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# Abstract

Accurate neutron flux values in irradiation channels of research reactors are very essential to their usage. The total neutron flux of the Ghana Research Reactor-1 (GHARR-1) was measured after a beryllium reflector was added to its shim to compensate for excess reactivity loss. The thermal, epithermal and fast neutron fluxes were determined by the method of foil activation. The experimental samples with and without a cadmium cover of 1-mm thickness were irradiated in the isotropic neutron field of the irradiation sites of Ghana Research Reactor-1 facility. The induced activities in the sample were measured by gamma ray spectrometry with a high purity germanium detector. The necessary correction for gamma attenuation, thermal neutrons and resonance neutron self-shielding effects were taken into account during the experimental analysis. By defining cadmium cutoff energy of 0.55 eV, Al-0.1% Au wires of negligible thickness were irradiated at 3 kW to determine the neutron fluxes of two irradiation channels, outer channel 7 and inner channel 2 whose Neutron Shaping Factor ( $\alpha$ ) were found to be (0.037 ± 0.001) and (-0.961 ± 0.034). The neutron flux ratios at the inner irradiation site 2 were found to be,  $(25.308 \pm 3.201)$  for thermal to epithermal neutrons flux, (0.179) $\pm 0.021$ ) for epithermal to fast neutrons flux and (4.528  $\pm 0.524$ ) for thermal to fast neutrons flux, in the outer irradiation site 7, the neutron flux ratios were found to be,  $(40.865 \pm 3.622)$  for thermal to epithermal neutrons flux,  $(0.286 \pm 0.025)$  for epithermal to fast neutrons flux and  $(11.680 \pm 1.030)$  for thermal to fast neutrons flux.

Keywords: Fluence Rate, Foil Activation, Neutron Self-Shielding, Flux Ratio

# 1. Introduction

Neutrons are readily obtained by the action of alpha particles on some light elements, example, beryllium, boron, or lithium. Neutrons have high energies covering a wide range, example, from 1 MeV to 10 MeV or more. The sources are thus said to be polyenergetic [1].

Many of the techniques for production of homogeneous neutrons are also used in neutron energy measurement. The most important source of thermal neutrons is the nuclear reactor [2].

The inner irradiation sites in the research reactor are usually used to irradiate and analyze unknown samples, using the neutron activation technique through  $(n, \gamma)$ 

thermal neutron reactions. The inner irradiation site in the MNSR contains both the fast and the thermal neutron fluxes.

The Ghana Research Reactor-1 (GHARR-1) is specifically designed for use in neutron activation analysis (NAA) and isotope production; therefore there is need for a careful and complete characterization of the neutron flux parameters in the irradiation channels in order to optimize its utilization for NAA via relative, absolute and single comparator methods. Low-power research reactors such as the Canadian Slowpoke and the Chinese MNSR, which run on the same fuel loading for over ten years, are known to exhibit stable neutron flux characteristics.



Figure 1. MCNP plot of vertical cross section of GHARR-1 reactor (control rod in full withdrawn position) showing structural supports [3].

Design Considerations of Ghana Research Reactor-1 (GHARR-1)

The Ghana Research Reactor-1 (GHARR-1) which is a 30 kW tank-in-pool reactor, which uses 90.2% enriched uranium-Al alloy as fuel. Detail description of GHARR-1 can be found in Sogbadji *et al.*, 2010 [4].

## 2. Theory

The nuclei of certain naturally occurring isotopes can be transformed into radioactive ones by exposing the material to neutron radiation, and the activity of the radioactive products produced can be measured by means of appropriate counter system. In addition to the factors determined by the conditions of measurement, this activity is affected only by the neutron flux in the point of irradiation and by the activation cross section of the target material which in the present case is the neutron detector. Provided the activation cross section is known, the neutron flux can be determined by measurement of the activity of the sample irradiated [1].

Thermal neutron fluence rate determination

The equivalent 2200 m/s thermal fluence rate  $\phi_o$ , in which Au is irradiated and used as a monitor can be calculated as

$$\phi_o = \frac{Rs - F_{Cd}R_{s,Cd}}{g\sigma_o G_{th}} \tag{1}$$

where  $R_s$  and  $R_{s,Cd}$  are the reaction rate per atom of bare and Cd-covered isotope irradiation, g is the correction for departure from cross-section behavior,  $G_{th}$  the self- shielding factor for thermal neutrons,  $\sigma_o$  the thermal neutron cross-section, and  $F_{Cd}$  the cadmium correction factor [5];  $R_s$  and  $R_{s,Cd}$  are determined by the equation

$$R_{s} o \gamma R_{s,Cd} = \frac{\left(A_{sp} o \gamma A_{sp,e}\right) F_g M}{\theta N_A \gamma \varepsilon_p}$$
(2)

with

$$\left(A_{sp} \, o\gamma \, A_{sp,e}\right) = \frac{N_p \, / t_m}{w SDC} \tag{3}$$

where  $A_{sp}$ ,  $A_{sp,e}$  are the specific activities obtained after a bare and cadmium covered isotope irradiation,  $N_p$  the net number of counts under the full-energy peak collected during measuring time,  $t_m$ , w the weight of irradiated element,  $S = 1 - e^{-\lambda t} irr$  the saturation factor with  $\lambda$  being the decay constant,  $t_{irr}$  the irradiation time,  $D = e^{-\lambda t} d$  the decay factor with  $t_d$  being the decay time,

$$C = \left(1 - e^{-\lambda t} irr\right) / \lambda t_m$$

the measurement factor correcting for decay during the measuring time,  $t_m$ , M the atomic weight,  $\theta$ , the isotopic abundance,  $N_A$  the Avogadro's number,  $\gamma$  the absolute gamma-ray emission probability, p the full-energy peak detection efficiency, and  $F_g$  the correction factor for gamma-ray attenuation [5].

The correction factor for gamma-ray attenuation in the sample at a given gamma-ray energy at a fixed geometry for the case a cylinder, coaxially positioned with the detector, is given by

$$Fg = \frac{\mu x}{1 - e^{-\mu x}} \tag{4}$$

where  $\mu$  is the linear attenuation coefficient (cm<sup>-1</sup>),  $\mu/p$  is the total mass attenuation coefficient (cm<sup>2</sup>/g) for the compounds used.  $\rho$  is the density of sample (g/cm<sup>3</sup>) and x is the sample thickness (in cm) [5].

Epithermal neutron fluence rate determination.

In a mixed thermal and  $(1/E^{1+a})$  epithermal neutron field, the epithermal neutrons fluence rate per unit  $(E^{-a}/-a)1$  eV of neutron energy interval can be calculated by

$$\phi_e = \frac{\phi_o}{\left(R - F_{Cd}\right)} \cdot \frac{g\sigma_o}{I_o\left(\alpha\right)} \cdot \frac{G_{th}}{G_{epi}} \tag{5}$$

where *R* is the cadmium ratio defined by,  $R = A_{sp} / A_{sp,e}$ ,  $I_o \alpha$  the resonance integral cross-section, including contribution, characterized by epithermal neutron spectrum shaping factor, which is energy dependent, and  $G_{epi}$  the self-shielding factor for epithermal neutrons [5].

Fast neutron fluence rate determination

The fast neutron flux is usually defined by (IAEA, 1970) as

$$\phi_f = \int_{0.5}^{10} \phi(E) \mathrm{d}E \tag{6}$$

It is well known that the rate of change of radioactive atoms produced by the irradiation in the activation (production) rate minus the decay rate, as in Equation (4). The activation rate of fast neutron flux is given by the equation

$$A(t) = N_T \int_{05}^{10} \phi(E) \sigma_f(E) dE = N_T \overline{\sigma} \phi_f \qquad (7)$$

here

$$N_T = \frac{\theta \cdot w \cdot N_A}{M} \tag{8}$$

 $N_T$  is the total number of the nuclides of interest in the target [6]. By making  $\phi_f$  the subject in Equation (7) and replacing the activity by the activity Equation (3), the equation to determine the fast neutron was derived as follows;

$$\overline{\phi_f} = \frac{N_p \lambda M}{\left(1 - e^{-\lambda t_i}\right) e^{-\lambda t} d\left(1 - e^{-\lambda t_m}\right) N_A w \theta \varepsilon \gamma \overline{\sigma}_{n,x}}$$
(9)

where  $N_p$  is the net peak counts under gamma line of interest, *M* is the atomic mass of target nucleus,  $N_A$  is the Avogadro's number,  $\theta$  is the isotopic abundance of target nucleus,  $\gamma$  is the gamma-ray abundance of residual radionuclide,  $\lambda$  is the decay constant,  $t_i$  is the irradiation time,  $t_m$  is the measuring time,  $t_c$  is the cooling time,  $\varepsilon$  is the full energy peak efficiency, *w* is the mass of target isotope in sample,  $\overline{\sigma}_{n,x}$  is the threshold reaction fission spectrum averaged cross section of <sup>27</sup>Al(*n*, *p*)<sup>27</sup>Mg which is 4.00 mb [7] and  $\phi_f$  is the fast neutron flux [6].

Determination of Neutron Shaping Factor ( $\alpha$ )

For non-ideal reactor situation, the resonance integral, *Io*, needs to be modified with an  $\alpha$ -dependent term because the  $I_o$  values, which are valid only for ideal spectra, is not true for a deviating spectra [8].

For the non-ideal conditions  $I_o(\alpha)$  values ought to be used instead of  $I_o$ . The conversion of  $I_o$  to  $\alpha$ -dependent terms takes the form [9]:

$$I_o(\alpha) = \left(\frac{I_o - 0.429\sigma_o}{E_\gamma^{\alpha}} + \frac{0.429\sigma_o}{(2\alpha + 1)E_{Cd}^{\alpha}}\right) E_a^{\alpha} = \int_{ECd}^{\infty} \alpha(E) \frac{E_a^{\alpha}}{E^{1+\alpha}} dE$$

where  $E_{\gamma}^{\alpha} =$  effective resonance energy,  $E_{a}^{\alpha} = 1 \text{ eV}$ arbitrary energy,  $E_{Cd}^{\alpha} = 0.55 \text{ eV} -$  effective cadmium cut-off energy,  $\sigma_{o} = 2200 \text{ ms}^{-1} (n, \gamma)$  Cross section and  $\alpha =$  an experimentally determinable characteristics of the reactor channel. Although the epithermal neutrons represent only a small fraction of the total reactor neutrons, they are sometimes useful in NAA for several elements (e.g. Br, Kb, Sr, Mo, Ba, Ta and U) that have higher relative reaction rates for epithermal neutrons than for thermal neutrons. The technique of taking advantage of those  $(n, \gamma)$  reactions with high resonance integrals through the irradiation of samples under a cadmium cover to shield out the thermal neutrons is commonly known as Epithermal Neutron Activation Analysis (ENAA).

The large number of resonance peaks for most nuclides makes a calculation of effective cross sections for the epithermal neutrons slightly complicated. In order to avoid these resonances, a gold standard is used because the reaction <sup>197</sup>Au  $(n, \gamma)$  <sup>198</sup>Au has a single resonance (411 KeV) peak and it has been well investigated [10,11] and found to be 1550 barns. The activity ratio for an infinitely thin gold foil or alloy irradiated with and without cadmium covers (Cadmium ratio method) is used [12] for measuring epithermal flux-shaping factor and thermal to epithermal flux ratio. This method is also used as a calibration standard to measure the resonance integrals for  $(n, \gamma)$  reactions [9].

If the single comparator technique is adopted for routine NAA, the effect of the non-ideal epithermal spectrum should not be neglected. Thus, to be accurate in all relevant expressions,  $Q_o$  should be replaced by  $Q_o(\alpha)$ (where  $Q_o(\alpha)$  is the  $\alpha$ -corrected  $Q_o$  to take care of the non-ideality of the epithermal spectrum)

$$Q_o(\alpha) = \frac{I_o}{\sigma_{th}} = \left(\frac{Q_o - 0.429}{E_{\gamma}^{\alpha}} + \frac{0.429}{(2\alpha + 1)E_{Cd}^{\alpha}}\right)$$

where  $Q_o$  is the ratio of resonance is integral to thermal cross-section is given as  $Q_o = I_o / \sigma_{th}$  which is related to flux ratio, *f*, as  $f = (R_{Cd} - 1)Q_o$ 

Experimental determination of  $\alpha$ , using the cadmium ratio method involves irradiating two or more monitors (e.g. Au, Zr, Co) with and without cadmium alternately at the same irradiation channel [13].

When monitors such as <sup>197</sup>Au and <sup>94</sup>Zr are irradiated under uniform neutron flux, Equation (19) transforms to

$$(R_{Cd}-1)Q_o(\alpha)_1 = (R_{Cd}-1)Q_o(\alpha)_2$$

The epithermal deviation factor is obtained from Equation (21) using iteration method by using computer programming language such C++ or Fortran which produces more accurate results.

#### 3. Experimental

#### Flux Determination by the Activation Method

Two irradiation channels were chosen for the measurement, one outer channel, site 7, and one inner channel, site 2. These channels were chosen at random.

In the determination of the neutron fluxes at the outer and inner irradiation sites, 7 and 2 respectively, Al-0.1%Au alloy wires were used as the flux monitors. The samples (Al-0.1%Au alloy wires) to be activated were put in the polyethylene vials with 1 mm wall thickness and internal diameter of the tube is 15.0 mm. The polyethylene vials were stuffed with cotton to make it weighty and heat sealed. They were exposed to the neutrons in a fixed position in the irradiation channels of a larger volume compared to the sample volume via a pneumatic system. Therefore, the effect of thermal fluence depression at the irradiation site is neglected.

The irradiations of the samples were carried out within and without a cylindrical cadmium shield case at the outer and inner irradiation channels, 7 and 2 respectively. Since <sup>27</sup>Al isotope has low neutron absorption crosssection. Ten samples were irradiated in irradiation channels considered, four each for thermal neutrons and cadmium shielded for epithermal neutrons and the last two samples also cadmium covered for fast neutrons. The irradiation times of the  $(n, \gamma)$  reactions of the Al-0.1%Au wire were carefully chosen yielding enough activity to be measured in  $\gamma$ -ray counting system. The suitable waiting times were employed to minimize dead time losses.

The irradiation for thermal and epithermal neutron flux monitoring were performed for 1 hour, and 5 minutes for fast neutron flux in the inner irradiation channel 2. In the outer irradiation channel 7, the irradiation for thermal and epithermal neutron flux monitoring were performed for 1 hour, and 10 minutes for fast neutron flux.

The use of Al-0.1%Au foil for the irradiation under cadmium shield permits the monitoring of the fast neutron flux via the <sup>27</sup>Al (n, p) <sup>27</sup>Mg reaction and the epi-thermal neutron flux via the <sup>197</sup>Au  $(n, \gamma)$  <sup>198</sup>Au reaction simultaneously. The use of a bare Al-0.1%Au foil for the irradiation permits the monitoring of the thermal neutron flux via the <sup>197</sup>Au  $(n, \gamma)$  <sup>198</sup>Au reaction. All irradiations were performed at a thermal power level of 3kW, which corresponds to a thermal neutron flux value of 1.0  $\times$ 1011  $\text{cm}^{-2} \cdot \text{s}^{-1}$  preset on the control console. After the irradiation, induced radioactivity in detector foils were counted on a HPGe coaxial detector (ORTEC), which has a relative efficiency of 25% and energy resolution of 1.8 KeV at 1332.5 KeV gamma-ray of 60Co was used for the measurement [14]. The full-peak energy efficiency parameter of the detector has been determined by standard gamma ray sources by fitting the efficiency curve with a polynomial function using parameters determined earlier [14]. The gamma-ray acquisition system consists of MAESTRO Multi-Channel Analyzer (MCA) emulation software card, coupled to the detector via electronic modules.

In Equations (8), (12) and (16), the thermal, epithermal and fast neutron fluxes respectively are deduced relative to the spectrum averaged cross section data.

Determination of Neutron Shaping Factor ( $\alpha$ )

In the determination of the Neutron Shaping Factor ( $\alpha$ ) at the outer and inner irradiation sites, 7 and 2 respectively, Al-0.1%Au alloy wires and zirconium foils were used. The samples (Al-0.1%Au alloy wires and zirconium foils) to be activated were put in the polyethylene vials with 1 mm wall thickness and internal diameter of the tube is 15.0 mm. The polyethylene vials were stuffed with cotton to make it weighty and heat sealed. They are exposed to the neutrons in a fixed position in the irradiation channels of a larger volume compared to the sample volume. Therefore, the effect of thermal fluence depression at the irradiation site is neglected.

The irradiations of the samples were carried out within and without a cylindrical cadmium shield case at the outer and inner irradiation channels, 7 and 2 respectively. The irradiation times of the  $(n, \gamma)$  reactions of the Al-0.1Au wire and zirconium foils were carefully chosen yielding enough activity to be measured in  $\gamma$ -ray counting system. The suitable waiting times were employed to minimize dead time losses.

The irradiation was performed for 1hour at the entire irradiation channel (*i.e.* 7 and 2). The use of Al-0.1%Au foil for the irradiation under cadmium shield permits the monitoring of the cadmium ratio of gold via the reaction <sup>197</sup>Au  $(n, \gamma)$  <sup>198</sup>Au. The use of zirconium foil for the irradiation under cadmium shield permits the monitoring of the cadmium ratio of gold via the reaction <sup>95</sup>Zr  $(n, \gamma)$  <sup>96</sup>Zr. After the irradiation, induced radioactivity in detector foils were counted on the HPGe coaxial detector.

The Neutron Shaping Factor ( $\alpha$ ) at the outer and inner irradiation sites, 7 and 2, respectively were calculated using Equations (9) and (17) together with a computer program written in Fortran 90 to solve for the shaping factor ( $\alpha$ ) using Equation (9). The shaping factors ( $\alpha$ ) were deduced relative to the ratio of resonance to averaged cross section data, *Qo*.

## 4. Results and Discussion

The results of the measurements of the thermal, epithermal and fast neutron fluxes, and the Neutron Shaping Factor ( $\alpha$ ), carried out in this study and the ones reported earlier by other authors are presented and discussed below.

The determination of neutron fluxes in an irradiation channel is necessary to monitor the continuous stability of the nuclear reactor flux (required for neutron activation analysis), characterize a new channel and re-characterize an old channel [15] after refueling and/or core configuration change [16].

Experimental determination of thermal to epithermal flux is achieved via cadmium ratio or the bare monitor method [17]. The results obtained for this work and for similar work performed on the same reactor are presented in **Table 2**.

All neutron flux measurement was done at 3 kW, with the console recording a flux of  $1 \times 10^{11}$  cm<sup>-2</sup>·s<sup>-1</sup>, at 30 kW (full power) the reactor console records a neutron flux value of  $1 \times 10^{12}$  cm<sup>-2</sup>·s<sup>-1</sup>. This implies that the experimental flux values obtained at 3 kW could be estimated at 30 kW (full power) by multiplying the neutron fluxes at 3 kW with a factor of 10.

These estimated neutron flux values at 30 kW are shown in **Table 1** and the neutron flux ratios are shown in **Table 2**.

The results tabulated in **Table 2** show that at the inner channel 2 being considered, thermal fluxes were high, followed by the fast neutron flux neutrons and then the epithermal, but in the outer irradiation channel 7 the fast neutron flux is less than the epithermal in that channel, though thermal neutrons still exhibit the highest neutron



Figure 2. MCNP5 plot of GHARR-1 core configuration showing fuel region (reactor core), channels for irradiation, fission chamber, regulating rods, and annular beryllium reflector [3].

Table 1. Estimated neutron flux	values of the inner	2 and outer 7	irradiation of	channel at 30 kW
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CHANNELS	Thermal neutrons $\phi_o \times 10^{12} \left( n/\mathrm{cm}^2 \cdot s \right)$	Epithermal neutrons $\phi_e \times 10^{10} \left( n/\mathrm{cm}^2 \cdot s \right)$	Fast neutrons $\phi_f \times 10^{06} \left( n/\mathrm{cm}^2 \cdot s \right)$	
Inner Irradiation Channel 2	$0.9534 \pm 0.0011$	$3.7672 \pm 0.00421$	$1.7588 \pm 0.0168$	
Outer Irradiation Channel 7	$0.5605 \pm 0.0001$	$1.3716 \pm 0.0027$	0.5242 ± 0.0012	

Table 2. Measured neutron flux ratios of the inner 2 and outer 7 irradiation channel at 3kW

	Thermal-Epithermal Neutron	<b>Epithermal-Fast Neutron</b>	Thermal-Fast Neutron	
CHANNELS	Flux ratios	Flux ratios	Flux ratios	
	$f = \phi_o / \phi_e$	$f = \phi_e / \phi_f$	$f = \phi_o / \phi_f$	
Inner Irradiation	$25.308 \pm 0.001$	$0.179 \pm 0.021$	$4.528 \pm 0.524$	
Channel 2				
Outer Irradiation	$40.865 \pm 0.002$	$0.286 \pm 0.025$	$11680 \pm 1030$	
Channel 7	10.000 = 0.002	0.200 - 0.020	11000 - 1000	

flux in that channel. However, the flux ratios of the thermal to epithermal neutron fluxes in both outer and inner irradiation channels are comparable within error to flux ratios values obtained by Y. A. Ahmed *et al.* in 2006 on the same reactor [17]. The fast neutron flux measured at the outer irradiation channel 7 is very low as compared to the thermal flux at the same channel; this is due to neutron moderation by the annulus beryllium around the reactor core. At the inner irradiation channel 2 the fast neutron flux shows an appreciable amount which is in good agreement with WIMSD4 code measurement made by K. Khattab in 2005 [6]. This shows that there has not been any significant change to the neutron fluxes at the irradiation sites being considered since a beryllium plate was added to the top shim tray.

Neutron Shaping Factor ( $\alpha$ ) in the Irradiation Channels

Among the various experimental methods available for determining the Neutron Shaping Factor ( $\alpha$ ), the cadmium ratio method is known to yield the most accurate results. Determination of the shaping factor in this study was carried out using the cadmium ratio method.

In general, the neutron spectrum parameters  $\alpha$  obtained in this work for the irradiation channels of GHARR-1 being considered compares very well with the  $\alpha$  values obtained by Akaho *et al.* on the same reactor in 2002 [18].

The measured  $\alpha$  values for the outer irradiation channel of GHARR-1 used compares very well with the Nigeria Research Reactor-1 (NIRR-1) which is also an MNSR similar to GHARR-1, but  $\alpha$  values for the outer irradiation channel of GHARR-1 used deviates significantly when compared with that of NIRR-1. In order to ascertain the source of the deviation, the values of the cadmium ratios,  $R_{Cd}$ , of the isotopes used (<sup>94</sup>Zr and <sup>197</sup>Au) were considered since that of NIRR-1 could be found in other journals.

This was done because both reactors with similar fuel are believed to have identical neutron spectra. It was discovered that the difference may be due to the cadmium ratio value of <sup>197</sup>Au,  $R_{Cd}$  (Au), which is 2.36 determined in the work and is comparable to the work by Akaho *et al.* on the same reactor in 2002 [18] who had a cadmium ratio value of <sup>197</sup>Au,  $R_{Cd}$  (Au) for 2.36, which is not in good comparison with the result of 2.12 for NIRR-1 [7]. Even though these reactors are identical, this is possible due the fact that the two reactors have slightly different number of fuel pins, hence affecting the of fuel volume-moderator volume ratio.

#### 5. Conclusions

By using the Al-0.1%Au wire to measure the thermal,

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epithermal and fast neutron fluxes of the Ghana Research Reactor-1 (GHARR-1), the fluxes obtained in this work (as shown in **Tables 1** and **2**) are in good agreement with the neutron flux values obtained when the reactor was less than five (5) years old.

This shows that the miniature neutron source reactor, design by the Chinese, has good neutron flux stability over long periods of time since the GHARR-1 has been in operation for more than ten (10) years. This has also been confirmed by the Neutron Shaping Factor ( $\alpha$ ) obtained in this work since the shaping factor ( $\alpha$ ) of the irradiation channels considered in this work has not change significantly over the years.

In this thesis work, the shaping factor ( $\alpha$ ) was measured using the cadmium ratios of zirconium-95 and gold-198 coupled with an iterative computer program written in Fortran 90 for Equation (17), but this parameter, ( $\alpha$ ), could also be measured using the graphical method [22]. If this method is used in further researches, it will ascertain the results obtained in this work. I also recommend that other methods, such as the cadmium ratio method should be used to measure and confirm neutron flux ratios obtained at the irradiation channels used in this work.

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