

# Nano Phase Characterization by Transmission Electron Microscopy: Experimental and Simulation

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Received 4 August 2015; accepted 3 November 2015; published 6 November 2015

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## Abstract

This paper introduces a methodology of characterization of nanostructured systems in which transmission electron microscopy is used as a central element of the study. Experimental studies of HREM are performed in parallel with studies in the Simula TEM program to stimulate high-resolution images and diffraction patterns. To confirm the accuracy of the results, studies of X-ray diffraction (XRD) were performed. In order to illustrate the methodology, bismuth oxide Bi<sub>2</sub>O<sub>3</sub> nanoparticles are synthesized by a method of biosynthesis because this sample is rich in structural information.

## Keywords

Transmission Electron Microscopy, Nanoparticles, Bismuth Oxide Bi<sub>2</sub>O<sub>3</sub>

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## 1. Introduction

Transmission electron microscopy (TEM) is a powerful technique that allows us to form images and diffraction patterns from diverse nanomaterials. These images can be used to determine the morphological and structural features of the samples under study. However, what in practice is needed is a full structural characterization of the samples. For this task, techniques such as X-ray diffraction (XRD), high resolution TEM (HRTEM), optical spectroscopy, Raman spectroscopy, infrared spectroscopy (IR) and fluorescence analysis must be used. All these

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in addition to the physical and chemical information are already available.

In this work, we describe a structural characterization of nanoparticles based on high resolution TEM images using our own software as well as commercial programs. To achieve this goal we study the synthesis of bismuth oxide particles through a biosynthesis method, using tannic acid as reducing agent, since these samples are very rich in structural details. Nowadays several research groups work on the synthesis of nanoparticles with technological applications using novel preparation methods, preferably those that are cheap and environmentally friendly. One of the interesting materials is bismuth oxide  $\text{Bi}_2\text{O}_3$ , which has many applications including medical ones since the  $\alpha\text{-Bi}_2\text{O}_3$  phase does show fungicidal activity against *Candida Albicans* [1] and also selectivity detection of NO as gas sensor [2], etc. In its most stable phase,  $\alpha\text{-Bi}_2\text{O}_3$  is a p-type semiconductor [3] that has been synthesized by several methods such as: hydrothermal [4], sol-gel [5], laser ablation [6] [7], Bismuth oxidation [8], microwaves [9], micro emulsion [10], PEG Precipitation [11].

## 2. Sample Preparation

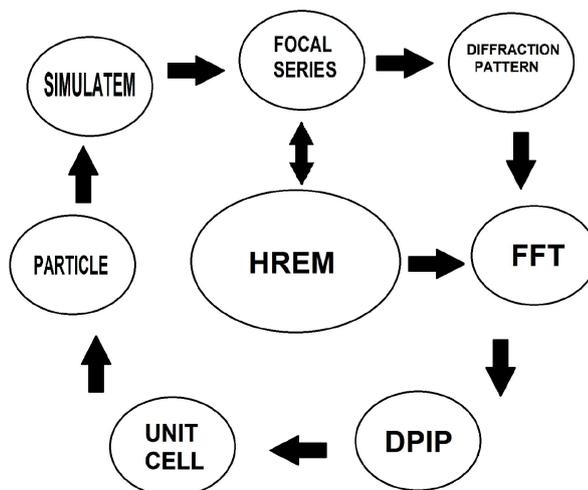
In order to prepare our samples, we use a small variation of the method of synthesis previously published [12]. In this method we used tannic acid ( $\text{C}_{76}\text{H}_{52}\text{O}_{46}$ ) and bismuth nitrate pentahydrate  $\text{Bi}(\text{NO}_3)_3 \cdot 5\text{H}_2\text{O}$ , the pH value was changed with NaOH and stabilized in  $\text{pH} = 11$  in order to obtain a more alkaline environment in the synthesis to continue the process of lyophilization [13]. Yellow-brown powder was obtained from which the samples for both HRTEM and XRD were prepared.

The microscopy characterization was done with a JEOL JEM-2010F FasTem microscope operating at 200 kV with a spherical aberration coefficient  $C_s = 0.5$  mm and fitted with analytical facilities. The X-ray measurements were carried out with a D8 Advance Bruker AXS diffractometer with  $\text{CuK}_\alpha$  radiation. The X-ray Diffraction Pattern was measured in the  $2\theta$  range from  $4^\circ$  to  $130^\circ$  with a step  $0.019^\circ$ .

For image processing and indexing of the nanoparticles, the computer programs Digital Micrograph and Diffraction Pattern Indexing Program (DPIP) [14] were used. Simulation of the nanoparticle morphology, TEM images and electron diffraction patterns was done with SimulaTEM [15], Materials Studio Version 2.1.5 and CaRiNe version 4.0 software.

## Procedure

The procedure followed is shown in a schematic way in **Figure 1**. The starting point is a high resolution image obtained from the Transmission Electron Microscope, and then the digital Fast Fourier transform (FFT) of the image (or of a desired part thereof) was obtained with the help of the commercial *Digital Micrograph* software. From this diffractogram we select at least two different spots and the  $(x,y)$  coordinates (with respect to a given rectangular coordinate system) are obtained. The center of the pattern is taken as the origin  $(0,0)$  of the reference frame.



**Figure 1.** Sketch of the proposed analysis scheme.

In the next stage we use our own tool *DPIP* to which we feed the relevant diffraction data from the powder diffraction files (such as  $h,k,l$  reflections and intensities, lattice parameters of the candidate structures, etc). We also input the  $(x,y)$  coordinates of the spots from the diffractogram and we select tolerance limits  $\Delta angle$  and  $\Delta distance$  (the difference between measured and calculated values).

*DPIP* provides the zone axis and the Miller indexes of the lattice planes considered that best match the measured spots. The program considers as many structures as needed (each represented by its x-ray table) but takes into account only solutions within the established error limits ( $\Delta angle$  and  $\Delta distance$ ).

The next step is to calculate the coordinates of all the atoms in a cluster of the same size as the actual cluster in the original image. For this, we use data from the literature and sometimes we are assisted by *Materials Studio*. The structure calculated is based on the identification provided by *DPIP* software.

After this, we feed the structure to *SimulaTEM* with which we can simulate images and diffraction patterns using the multislice method [16]. The input in this case consists of the coordinates  $(x,y,z)$  and atomic number of each atom together with the operating conditions of the microscope (accelerating voltage, spherical aberration etc.).

Once the data are introduced, the particle is oriented along the desired zone axes. Then focal series are calculated in a neighborhood of the Scherzer defocus condition. The procedure is repeated as many times as desired depending on how many zone axes and structure solutions are given by *DPIP* software. Finally the calculated and observed images are compared. Once the best matches are obtained we calculate the corresponding diffraction patterns for comparison with the diffractograms. The *CaRiNe* 4.0 software can be used to verify that the indexing is consistent and in agreement with the geometry (space group) of the sample.

### 3. Results

Here a full example of the procedure is shown outlined above where we want to identify a phase present in a particle starting with a HREM image (obtained with a JEOL JEM-2010F microscope).

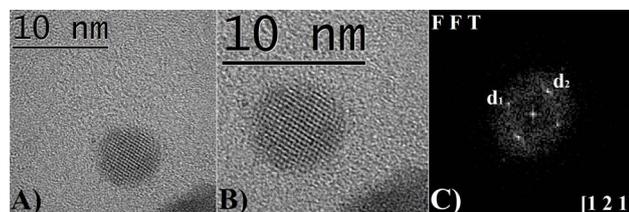
**Figure 2(A)** shows the experimental image; **Figure 2(B)** presents an enlarged view of the selected particle, and finally **Figure 2(C)** displays the corresponding FFT (diffractogram). As described before, the images **Figure 2(B)** and **Figure 2(C)** were obtained with the help of the *Digital Micrograph* software.

For this example we selected the spots encircled in the figure. With *Digital Micrograph* the positions  $(x,y)$  of the spots are measured. ((0,0) is assigned to the center of the diffractogram).

Given the preparation procedure, the nanoparticle is expected to be one of the possible bismuth oxides such as BiO [17], Bi<sub>2</sub>O<sub>3</sub> [18], Bi<sub>2</sub>O<sub>4</sub> [19], among others, but the most interesting is Bi<sub>2</sub>O<sub>3</sub> due the polymorphs that this oxide presents, and their possible applications.

We considered the Bi<sub>2</sub>O<sub>3</sub> polymorphs  $\alpha$ -Bi<sub>2</sub>O<sub>3</sub> (Monoclinic,) [20],  $\beta$ -Bi<sub>2</sub>O<sub>3</sub> (Tetragonal) [21],  $\gamma$ -Bi<sub>2</sub>O<sub>3</sub> (BCC) [22],  $\delta$ -Bi<sub>2</sub>O<sub>3</sub> (FCC) [23] and H-Bi<sub>2</sub>O<sub>3</sub> (hexagonal) [24] respectively. The crystallographic information for each of these is taken from the Powder Diffraction Files. PCPDFWIN x-ray card (version 2.2, 2003). **Table 1** shows these data.

With the positions of the spots and the known crystallographic data of the candidate structures we index the diffractograms using an error bound of  $\Delta angle$  and  $\Delta distance$  less than 1.1 degrees and 0.5 Å. After running *DPIP* for each of the polymorphs described above and for pure Bi (Monoclinic) [25]. We find that the smallest error of  $\Delta angle$  corresponds to the  $\delta$ -Bi<sub>2</sub>O<sub>3</sub> phase (77-0374). However, this phase present a  $\Delta distance$  out of the error limits that we set; so that this solution was not taken. In the same way, the error limit in  $\Delta angle$  was higher than the permitted error for phases such as Bi monoclinic (65-6203), Bi rhombohedral (05-0519) and H-Bi<sub>2</sub>O<sub>3</sub> (51-1161). At this stage, the remained possibilities are  $\alpha$ -Bi<sub>2</sub>O<sub>3</sub> and  $\beta$ -Bi<sub>2</sub>O<sub>3</sub>, so the analysis is now limited to



**Figure 2.** (A) HREM image of the particle under study; (B) Enlarged view; and (C) Corresponding FFT.

**Table 1.** DPIP solutions for the  $\beta$ -Bi<sub>2</sub>O<sub>3</sub> phase.

Phase	Angle	$\Delta$ angle	$h_1$	$k_1$	$l_1$	$\Delta d_1$	$h_2$	$k_2$	$l_2$	$\Delta d_2$	Zone Axis		
											X	Y	Z
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(2 -1 0)			0.227	(0 1 -2)			0.575	[1 2 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(2 -1 0)			0.227	(0 1 2)			0.575	[-1 -2 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(-2 -1 0)			0.227	(0 1 2)			0.575	[1 -2 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(2 1 0)			0.227	(0 -1 2)			0.575	[-1 2 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(-2 1 0)			0.227	(0 -1 2)			0.575	[1 2 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(2 -1 0)			0.227	(0 1 -2)			0.575	[1 2 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(-2 -1 0)			0.227	(0 1 -2)			0.575	[-1 2 1]		
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$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(-1 2 0)			0.227	(1 0 -2)			0.575	[2 1 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(1 2 0)			0.227	(-1 0 2)			0.575	[2 -1 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(1 2 0)			0.227	(-1 0 -2)			0.575	[-2 1 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(-1 2 0)			0.227	(1 0 2)			0.575	[-2 -1 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(1 -2 0)			0.227	(-1 0 -2)			0.575	[2 1 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(1 -2 0)			0.227	(-1 0 -2)			0.575	[-2 -1 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(-1 -2 0)			0.227	(1 0 2)			0.575	[-2 -1 1]		
$\beta$ -Bi <sub>2</sub> O <sub>3</sub>	98.79	1.09	(-1 -2 0)			0.227	(1 0 -2)			0.575	[2 -1 1]		

only two phases. X-Ray diffraction results pointed out that the predominant bismuth oxide in the sample correspond to the  $\beta$ -Bi<sub>2</sub>O<sub>3</sub>. Therefore, the use of complementary information allowed to discern between those proposed solutions. Several studies on bismuth oxide polymorphs have been reported and it is known that in bulk,  $\beta$ -Bi<sub>2</sub>O<sub>3</sub> is metastable; however, this phase has been observed at the nanoscale level [26]-[28].

Once the phase has been determined we see, **Table 1**, that there are two possible zone axes: [121] and [211].

To compare this result HRTEM images were simulated by using *Simula TEM* software. In **Figure 3(A)** starting with the unit cell for  $\beta$ -Bi<sub>2</sub>O<sub>3</sub> [29], we construct a super cell (**Figure 3(B)**) and finally larger nanoparticle with the help of Materials Studio till we get a cuboctahedral shape with 24425 atoms and 10.86 nm width, as shown in **Figure 3(C)**.

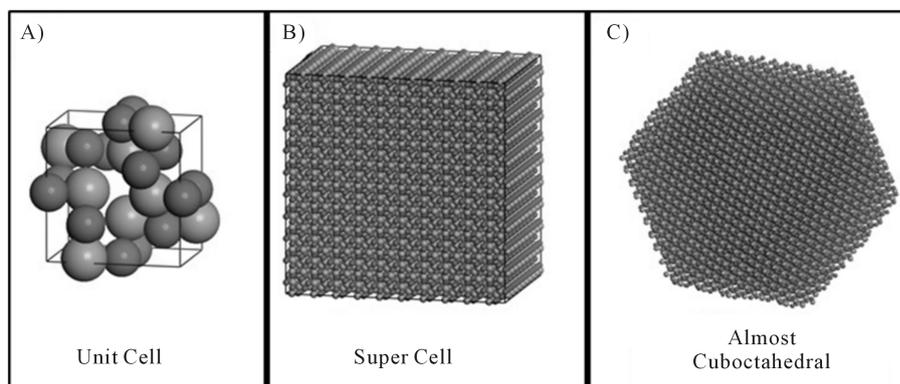
Once the structure is obtained, the cluster is rotated to any desired zone axis; given that the positions ( $x,y,z$ ) and atomic numbers of all the atoms are known SimulaTEM can be used with the parameters describing the actual microscope operation. The experimental image is shown in **Figure 2** and the microscope parameters are en-listed in **Table 2**. The starting point for the focal series was taken to be the Scherzer defocus condition.

The focal series can be seen in **Figures 4(A)-(C)** for [121]. **Figures 4(D)-(F)** focal series for [211] in comparison with **Figure 2** shows that the best visual fit is to a [121] zone axis orientation.

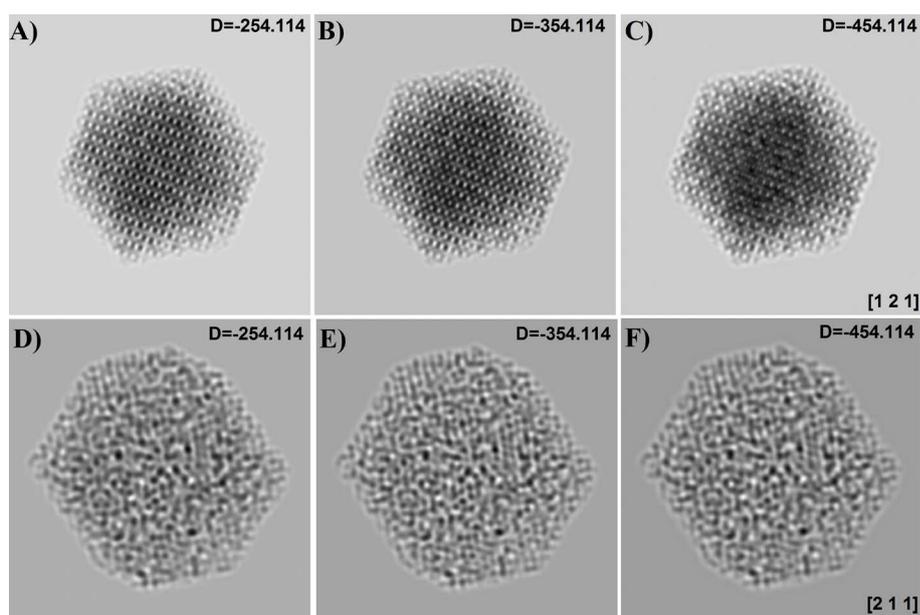
In **Figure 5(A)**, the experimental HREM is shown together with the simulated images **Figure 5(B)** and its simulated diffraction pattern, **Figure 5(C)**.

So far the phase and the zone axis have been determined and it only remains to complete the indexing of the points in the diffractogram. CaRiNe software was employed for comparison.

The final result is shown in **Figure 6**, where we display the indexed diffraction pattern for a  $\beta$ -Bi<sub>2</sub>O<sub>3</sub> (Tetragonal) structure. The points  $d_1$  and  $d_2$  from the diffractogram correspond to the planes (-2 1 0) and (0 -1 2) respectively. In **Figure 7**, the X-ray diffraction pattern confirms the presence of  $\beta$ -Bi<sub>2</sub>O<sub>3</sub> which corresponds to ICDD:PDF-2 card 00-0027-0050. In addition to this phase NaNO<sub>3</sub> (Nitratine) is detected (PDF-2 card 00-036-1474). The characterization of the particle has been completed.



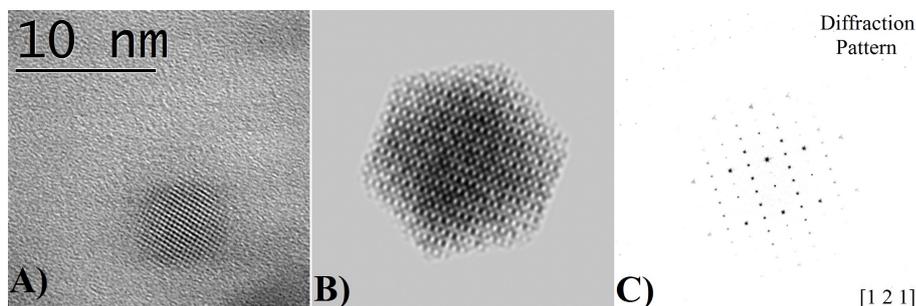
**Figure 3.** (A) Unit cell of  $\beta$ - $\text{Bi}_2\text{O}_3$ ; (B) Super cell; (C) The cluster thus generated.



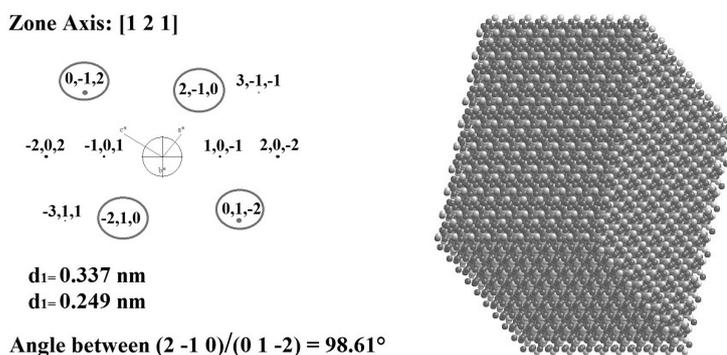
**Figure 4.** (A)-(C) Simulated focal series for the [121]; (D)-(F) [211] zone axes around the Scherzer condition (central images ((B) and (E))).

**Table 2.** Parameters used with SimulaTEM for both [121] and [211] zone axes, F2 and F5 corresponds to the Scherzer condition for [121] and [211] respectively.

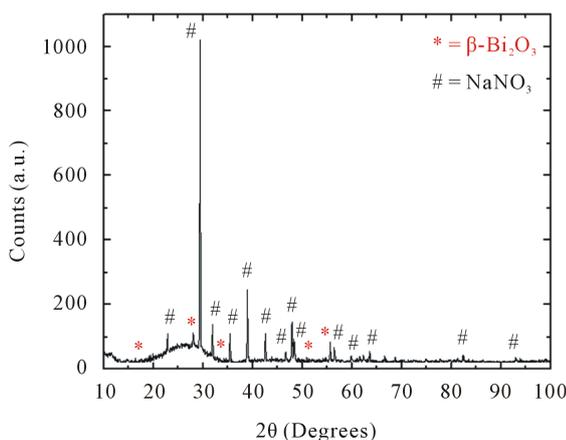
Microscope 2010F	F1	F2	F3	F4	F5	F6
Voltage (kV)	200	200	200	200	200	200
Cs. Spherical aberration (mm)	0.5	0.5	0.5	0.5	0.5	0.5
Defocus spread ( $\text{\AA}$ )	199	199	199	199	199	199
Beam spread ( $\text{\AA}$ )	0.1	0.1	0.1	0.1	0.1	0.1
Defocus ( $\text{\AA}$ )	-254	-354	-454	-254	-354	-454
Astigmatism ( $\text{\AA}$ )	0	0	0	0	0	0
Astigmatism azimuth (degrees)	30	30	30	30	30	30
Image width ( $\text{\AA}$ )	173.5	173.5	173.5	173.5	173.5	173.5
Slice width ( $\text{\AA}$ )	2	2	2	2	2	2
Number of slices	49	49	49	49	49	49



**Figure 5.** (A) The HREM image; (B) The simulated image (Scherzer condition); and (C) The calculated diffraction pattern.



**Figure 6.** The geometry of the diffraction pattern (left) and of the structure.



**Figure 7.** X-ray diffraction spectrum. The presence of  $\beta\text{-Bi}_2\text{O}_3$  is confirmed. In the sample besides  $\beta\text{-Bi}_2\text{O}_3$  we see Nitratine, this phase is due to the NaOH used to vary the pH.

#### 4. Conclusions

A protocol for structural characterization of nanoparticles based in high resolution TEM images was described. High resolution images must be Fourier-transformed to obtain reciprocal space information, in general a direct electron diffraction pattern is difficult (but not impossible) to obtain for particles in this size range. These diffractograms together with x-ray spectra (necessarily from large samples) represent an excellent option for the identification of the phase. The images provide information on the shape (habit) of the nanoparticles, indicates whether they are single crystals or twins or if there are structural defects such as stacking faults or dislocations. Working with many particles provides size distributions. Greater certainty is provided from the comparison between actual and simulated images and diffraction patterns.

Although the X-ray spectrum indicates the presence of  $\beta$ -Bi<sub>2</sub>O<sub>3</sub> only the detailed analysis we have presented confirms that a given particle is (or is not)  $\beta$ -Bi<sub>2</sub>O<sub>3</sub>. **Figure 1** summarizes the analysis procedure that we propose, the message being that both actual measurements and simulations complement each other.

## Acknowledgements

Our gratitude to Roberto Hernández Reyes for his aid with the Electron Microscope, Antonio Morales for X-Ray measurements at IFUNAM and to Dr. José Guadalupe Pérez for allowing us to use his licensed copy of CaRIne. The financial support from DGAPA (grant PAPIIT IN108915) is also acknowledged. Francisco M. Ascencio Aguirre thanks to CONACyT for the Ph.D. scholar fellowship.

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