Mechanical response of uterine tissue under the influence of hemostatic clips: A non-linear finite-element approach

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ABSTRACT

A modeling strategy to predict the ability of surgical clips to achieve mechanical hemostasis when applied to the cut edge of a thick and muscular tissue is presented in this work. Although such a model may have broad utility in the design of hemostatic clips and other surgical and wound closure applications, our particular focus was on uterine closure following a Cesarean delivery. Mechanical closure of a blood vessel, which is the first step in the hemostatic process, is established when the compressive forces on the outer surface of a blood vessel are sufficient to overcome the local blood pressure and collapse the vessel. For thick tissue, forces applied to the tissue surface set up a stress distribution within the tissue that, if sufficient to mechanically close all vessels, will lead to cessation of local blood flow. The focus of the current work was on utilization of a planar and nonlinear finite element model to predict the pressure distribution within uterine tissue under the influence of hemostatic clips. After experimental model validation with a polymer tissue phantom, design curves were numerically developed, which consisted of the clip force necessary to achieve hemostasis for a given thickness tissue as well as the resulting deformed tissue thickness. Such curves could form the basis for a preliminary clip design, which would provide initial design guidance before more expensive experimental studies were reauired.

Keywords: Medical Device Design; Hemostasis; Finite Element Modeling; Tissue Modeling; Myometrial Tissue

1. INTRODUCTION

Computer simulations are routinely used to aid in the

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design and development of engineered products. Typical computational models consider stress analysis to predict material failure, fluid dynamics to predict fluid shear stress imposed on structures, or heat transfer to predict temperature distributions. Application of simulations to medical device design is complicated by many factors, such as uncertainty in tissue material properties and geometry due to physiological variation [1], nonlinear constitutive models [2], and the presence of non-traditional or multi-physics effects (e.g., muscle contraction, blood flow within tissue, and fluid-structure interaction). The focus of the current work is to model via a nonlinear finite element formulation the mechanical interaction between hemostatic clips and uterine tissue in closure applications during cesarean delivery, furnishing useful indications for clip design.

During cesarean deliveries, which account for approximately 32% of births in the United States [3], the baby is delivered through incisions in the uterus and abdomen rather than vaginally. Once the baby and placenta have been delivered, the surgeon sutures the incisions closed, starting with the uterine wall and working outward towards the body surface. There are both short-term and long-term risks associated with cesarean delivery, including hemorrhage, injury to urogenital and gastrointestinal organs, and uterine complications affecting subsequent pregnancies. In addition, the formation of adhesions, common after pelvic surgery, is considered to be a leading cause of infertility [4]. A surgical closure device that reduces these risks would be of great value.

Hemostatic clips are an alternative to sutures for surgical closure, such as the Raney clip used on the scalp. Mechanically, clips and sutures both apply compressive forces to the tissue to occlude transected vessels and stop blood flow; they differ in that clips which do not penetrate the tissue, but rather apply a force to the surface of the tissue and rely on internal compressive stress within the tissue for vessel closure. This lack of penetration of



clips rela- tive to sutures may decrease tissue damage by applying a smaller, more uniform stress to the tissue surface. In ad- dition, with the development of a specialized application tool, clips may be faster to apply than sutures, thereby limiting blood loss.

A key design constraint in developing such clips is that the force applied to the tissue surface generates sufficient internal pressure throughout the tissue thickness to maintain vessel closure throughout the tissue. This is particularly challenging for thick tissue, such as myometrium, which can be as thick as 1.5 cm at the time of delivery [5]. The focus of the current work is to model via a nonlinear finite element formulation the mechanical interaction between hemostatic clips and uterine tissue in closure applications during caesarean delivery, furnishing useful indications for clip design.

2. MATERIALS AND METHODS

2.1. Geometric Model

To apply the hemostatic clip, the cut edges of the tissue (tissue shown in grey in **Figure 1**) would be drawn together and everted, and the clip placed on the exterior surface of the organ. Contact between the clip and the tissue is depicted two-dimensionally in **Figure 1**. The two portions of the clip that come in contact with the tissue are labeled "indenters." Tissue thickness is given by t and indenter width by t. The indenters come in contact with the tissue at a distance t from the edge and apply a load compressing the tissue between them. The distance t was set at 1 cm, which is based on the dimensions of the simulated clip. Simulations were run for indenter widths of 2 mm and 5 mm, and tissue thicknesses of 1.5 cm and 2 cm.

2.2. Theoretical Background

To predict whether a given stress distribution would be

sufficient for hemostasis, recall that the components of the traction vector t_i (force per unit area) on a surface within a material are given by:

$$t_i = \sigma_{ii} n_i, \tag{1}$$

where σ_{ii} are the components of the Cauchy stress, n_i are the components of the unit outward normal of the surface, and summation over repeated indices is implied. Our working assumption is that if the compressive traction on the surface of a blood vessel exceeds the internal pressure (i.e., local blood pressure), the vessel will collapse. In this work, the pressure to induce collapse was set at 200 mmHg. This assumption ignores two important effects—pressure drop within a vessel due to blood flow and the presence of passive or active elastic tension within the wall of the vessel [6]. Either effect, however, would serve to decrease the external pressure required for vessel occlusion. Pressure drop due to flow would reduce the internal pressure while muscle tension would be in the same direction as external pressure and thus work towards vessel occlusion. Thus, estimates based on this model will be conservative, which is appropriate from the perspective of design (i.e., the model creates an additional safety factor).

From elementary solid mechanics (e.g., [7]), the three principal stresses at a point (denoted σ_1 , σ_2 and σ_3) contain the maximum and minimum values for any coordinate system passing through the point. This implies that the minimum principal stress (*i.e.*, negative stress with largest magnitude) is a coordinate-independent measure of compressive stress within the tissue.

2.3. Finite Element Simulations

Abaqus finite element software (Simulia, Providence, RI) was used to create a two-dimensional (plane strain) finite element model based on the geometry described previously. Bilinear quadrilateral elements were used, and

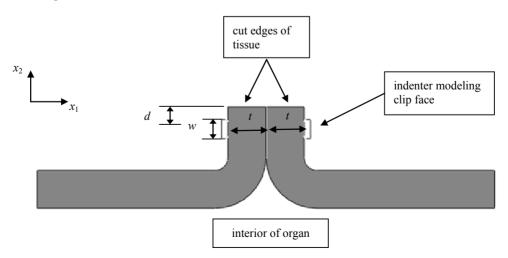


Figure 1. Axisymmetric geometry used to model the clamping of uterine tissue.

large deformation effects were included to account for the compliant nature of muscle tissue. A Newton-Rhapson method was used to solve the nonlinear equations. The far ends of each piece of tissue, which represent the continuing uterine tissue, were fixed in all directions. The indenters were constrained to only move in the x_1 direction, and they were also prevented from rotating in the $x_1 - x_2$ plane. Boundary conditions depicted in **Figure 2** were applied to the model.

Contact was established between each indenter and its respective piece of tissue, as well as between the two pieces of tissue. Because the interface between the two pieces of tissue would be moist and well lubricated, this contact was defined as frictionless. The contact between the indenters and tissue was given a coefficient of friction of 0.9. Although the actual coefficient of friction between these parts is not known and depends on the geometry of the indenter face, a sensitivity study showed a variation of less than 1% over a range of 0.3 to 0.9 (data not shown).

The force applied by the clips to the tissue was simulated by applying a concentrated force at the center of each indenter (**Figure 2**). Because of the 2D plane-strain approximation, this force corresponds to the force per

unit depth of the clip (depth refers to the dimension running into the page). In other words, the area of the clip contacting the tissue would be equal to depth \times width.

2.4. Material Model for Myometrial Tissue

Uterine tissue was treated as an isotropic, incompressible, hyperelastic material. Uterine tissue is generally isotropic, with muscle fibers oriented in the circumferential, longitudinal, and diagonal directions. Since our loading is perpendicular to these fiber directions, an isotropic model is a reasonable approximation. In addition, although muscle often displays viscoelastic characteristics [8], the current study focused on the steady-state stress distribution, so viscous effects were not included. Given that compression was the primary loading mechanism for the clips under consideration, a constitutive model for uterine tissue was developed based on data in the literature describing primarily the compressive mechanical properties of human myometrium [9]. That study showed a large variability in stress-strain behavior between samples. To account for this variability, three representative curves were created and used for analysis-high, medium, and low stiffness (Figure 3). Each loading case was run for all three material models.

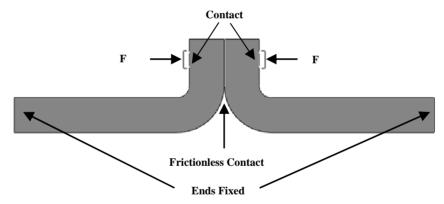


Figure 2. Boundary and loading conditions for finite element simulation.

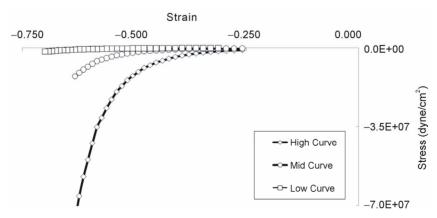


Figure 3. Three different stress-strain curves used to model the nonlinear elasticity of uterine tissue in this study. Data taken from [9].

Each stress-strain curve was fit to a 3rd order Ogden hyperelastic model within Abaqus, and these models were used throughout the simulations. The formulation of the Ogden strain energy function that was used is given by,

$$U = \sum_{i=1}^{3} \frac{2\mu_{i}}{\alpha_{i}^{2}} \left(\overline{\lambda}_{1}^{\alpha_{i}} + \overline{\lambda}_{2}^{\alpha_{i}} + \overline{\lambda}_{3}^{\alpha_{i}} - 3 \right) + \sum_{i=1}^{3} \frac{1}{D_{i}} \left(J^{el} - 1 \right)^{2i}$$
 (2)

where $\overline{\lambda}_i = J^{-1/3} \lambda_i$ are the deviatoric principal stretches, J is the determinant of the deformation gradient tensor, J^{el} is the elastic volume ratio (equal to J for isothermal problems such as assumed in the current work) and α_i , μ_i , D_i are material parameters. Values for these coefficients are provided below in **Table 1**.

Although muscle tissue is essentially incompressible [10], this constraint is difficult to enforce exactly in a plane strain setting. Numerically, incompressibility is usually implemented by including a volume dilatation term with a large but finite bulk modulus in the strain energy function [the last term in Equation (2), above]. In the current work, the material parameter governing compressibility, D_i is parameterized in terms of the Poisson ratio, v (a Poisson ratio tending to 0.5 corresponds to incompressibility). The relationship among the Ogden material properties and the Poisson ratio is given by [11],

$$v = \frac{3(K/\mu_i) - 2}{6(K/\mu_i) + 2} \tag{3}$$

where $\mu_i = \mu_1 + \mu_2 + \mu_3$ and *K* is the bulk modulus.

A sensitivity study showed that running our simulation for values of v between 0.495 and 0.4995 led to a coefficient of variation of less than 1% in the minimum compressive stress (data not shown). A value of v=0.499 was used in all simulations. Finally, the indenters were modeled as rigid bodies, so no material properties were associated with them.

2.5. Simulations

The simulation focused on the effects of two variables on internal tissue pressure: the width of the indenter face (2 mm and 5 mm) and tissue thickness (1.5 cm and 2 cm).

Table 1. Material parameters for Ogden material model fit from Reference [9]. μ_i have dimensions of dynes/cm², α_i are unitless.

	High	Mid	Low
μ_1	-3,135,789	13,814	-52,338
μ_2	3,064,710	80,456	145,693
μ_3	193,610	12.3	-38,515
$lpha_{ m l}$	6.10	2.84	4.33
α_2	6.39	9.23	8.22
α_3	-4.28	-12.56	-4.60

The load applied to the indenter was incremented from 1 N to 20 N for each case. In addition, the variability in uterine material properties was accounted for by running three simulations for each combination of indenter height and tissue thickness. Each simulation represented a different set of uterine material properties (high, middle, and low stiffness) as in **Figure 3**.

2.6. Data Analysis

As mentioned previously (Theoretical Background section), the most negative value among the three principal stresses (i.e., the minimum principal stress) at a point in the tissue corresponds to the maximum compressive stress at that location (of course, it is possible in general to have a case in which all three principal stresses are positive, such as tri-axial stretching, but that was not the case in this simulation). Minimum principal stress data were collected within the band of elements between the indenters, as this is where compressive loads would be felt. The location which corresponds to the smallest magnitude of these minimum principal stresses would be experiencing the lowest compressive load, and thus apply the smallest compressive load to close blood vessels in the area. This value will be referred to as the minimum compressive stress. When the minimum compressive stress exceeds local blood pressure, it is predicted that hemostasis will be achieved through the thickness of the

From these data, a series of design curves were generated relating the minimum compressive stress to the range of tissue material properties, indenter width, and tissue thickness as a function of the load applied to the indenter. In addition, the final distance between the indenter faces was quantified; this distance is a measure of the deformed tissue thickness, and is valuable for design purposes.

2.7. Model Validation

To validate the numerical model, an experiment was set up mimicking the physical system (**Figure 4**). Sylgard 527 dielectric gel (Dow Corning, Midland, MI), cast into a disc (12 cm radius, 2 cm thickness), was used as a tissue analog [12]. The gel disc was placed on a lubricated, rigid base. A stainless steel indenter was custom-fabric-cated (2 inch diameter with 0.25 inch radius rounded edge) and attached in series with a 300-lb load cell (Omega Engineering, Stamford, CT) to a screw-driven load frame via a custom-made carriage. Force-sensitive resistors (Tekscan, Inc, Boston, MA) were used to measure contact pressure between the bottom of the gel disc and the rigid support. One sensor was placed directly under the indenter and another at 2 cm away from the indenter. All sensors were calibrated before each trial. In

a given trial, a given displacement was applied to the carriage while the indenter force and contact pressure were measured. Both pressure sensor and load cell data were collected using a digital data acquisition system (National Instruments, Austin, TX).

Prior to the indentation tests, an unconfined compression test was performed on smaller gel discs (4.5 cm diameter) to quantify the material properties of the gel. In these experiments, the indenter was replaced with a lubricated flat metal plate. The gel material was fit to a Neo-Hookean material model (μ = 78,192 dynes/cm², ν = 0.499). Note that although the material model is slightly different from the one used for the tissue, the one-parameter Ogden model is equivalent to a Neo-Hookean model.

An axisymmetric finite element mesh was created of the gel and indenter (**Figure 5**). The same element formulation and solution method as described for the myometrial tissue model was used in this model. A displacement boundary condition was applied to the indenter and frictionless contact was enforced at the boundary between the gel and the rigid base. The reaction force of the indenter and the base contact pressure were computed and compared to experimental values for the same indenter displacement. Accurate prediction of the base contact pressure for the tissue-like material will be used as verification of the prediction of compressive stresses within simulated myometrial tissue.

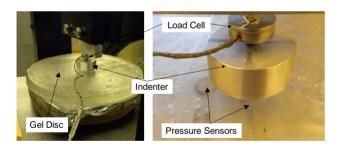


Figure 4. Experimental apparatus used for validation of computer model.

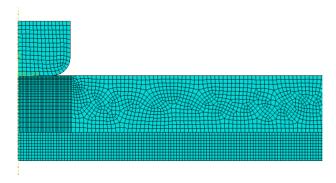


Figure 5. Axisymmetric finite element mesh of gel and indenter used for validation.

3. RESULTS

3.1. Validation Model

Before considering the myometrial tissue model, the validation model was first studied. For both indenter force and surface pressure, comparison between experimental results and simulations of the gel disc was excellent (**Figures 6** and **7**).

3.2. Myometrial Model

In general, the simulated uterine tissue showed a characteristic stress distribution during compression by the indenters, as shown in **Figure 8** for 1.5 cm thickness tissue, a 2 mm indenter face. As expected, the deformation was significant, given the very compliant nature of muscle tissue. The minimum principal stress (*i.e.*, largest compressive stress) was centered between the indenters; stress decreased in magnitude towards the indenter edge, where the tissue is in tension as it wraps around the curved portion of the indenter.

Based on the full set of simulation results, design curves were created relating indenter force to the minimum compressive tissue stress between the indenters. A representative set of curves is shown in **Figure 9** for a tissue thickness of 2 cm, an indenter width of 5 mm, and all three myometrial material models. **Table 2** summarizes the results of the force data. The third column shows the range of forces required per cm of clip width to achieve hemostasis accounting for both high and low stress-strain curves.

The deformed tissue thickness at the hemostatic load for each condition is shown in **Table 3**. The range of values for each thickness and width represents the thickness at the load required for hemostasis for low and high

Table 2. Force per unit depth of clip required to achieve hemostasis. The values corresponding to low and high tissue stiffness tissue are presented.

Tissue Thickness (cm)	Indenter Width (mm)	Force Range Required for Hemostasis (N/cm)
1.5	2	2.8 - 3.5
1.5	5	3 - 4
2	2	3.8 - 5
2	5	4 - 5.4

Table 3. Deformed tissue thickness of each sample at hemostatic load. The values corresponding to low and high tissue stiffness tissue are presented.

Tissue Thickness (cm)	Indenter Width (mm)	Tissue thickness at hemostatic load (cm)
1.5	2	0.50 - 1.17
1.3	5	0.54 - 1.19
2	2	0.63 - 1.54
2	5	0.69 - 1.57

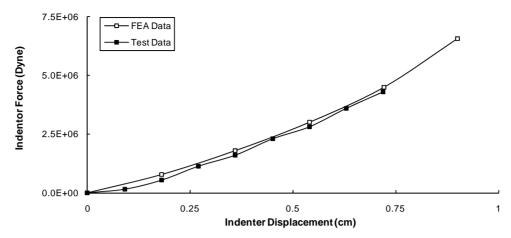


Figure 6. Comparison of indenter force vs. displacement curve for simulation and experiment, showing excellent agreement.

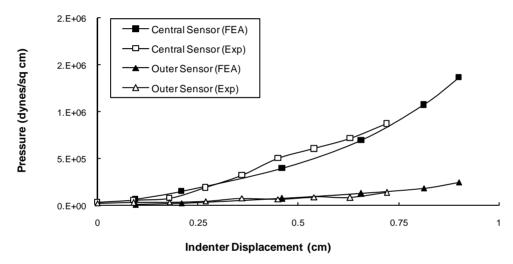


Figure 7. Comparison of contact pressure for simulation and experiment, showing excellent agreement. The central sensor was located directly under the indenter and the outer sensor was 2 cm out from center of the indenter.

stiffness curves at each tissue width and indenter width. Note that the large range in strains, due to the non-linear stiffness of the tissue. For example, for the 1.5 cm tissue and 2 mm indenter face, tissue compressed to 33% of its original thickness for the high compliance tissue while only deforming to 80% of the original thickness for the low-compliance curve.

4. DISCUSSION

The goal of this work was to develop, validate, and apply a framework to utilize finite element modeling in the design of hemostatic clips for surgical closure applications. Surgical closure techniques aim to mechanically facilitate apposition of cut edges of tissue to promote wound healing, while stopping blood flow to allow hemostasis to occur. The central issue addressed in this work was the ability of a hemostatic clip applied at the surface of a thick and muscular organ to provide suffi-

cient internal pressure to achieve mechanical hemostasis throughout the tissue. Although the particular focus was on uterine tissue at full-term pregnancy, the work is broadly applicable to surgical closure of other thickwalled organs.

The guiding principle underlying the analysis is that if the compressive stress acting on a blood vessel within a tissue exceeds local blood pressure, the vessel will collapse and blood flow will be halted in that particular vessel. If the compressive stress throughout the entire thickness of the tissue exceeds local blood pressure, then bleeding should be stopped, allowing the clotting process to begin.

To predict the distribution of compressive stress within the tissue, we utilized the finite element method. The finite element method breaks the domain into small elements, over which the equations of mechanics are solved, yielding the stress distribution over the entire domain.

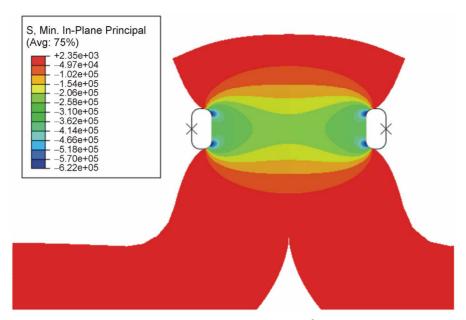


Figure 8. Distribution of minimum principal stress (dynes/cm²) for representative load case (1.5 cm tissue thickness; 2 mm indenter, mid-level material model).

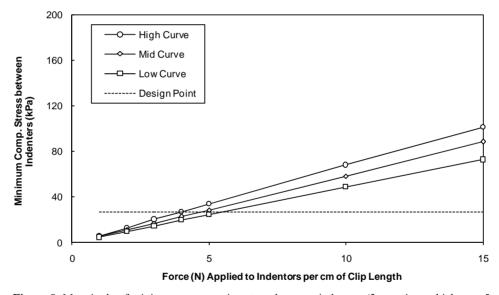


Figure 9. Magnitude of minimum compressive stress between indenters (2 mm tissue thickness; 5 mm indenter width).

From basic continuum mechanics, the state of stress can be represented in a coordinate-invariant manner through the three principal stresses, which are the eigenvalues of the stress tensor. Furthermore, the minimum value of the principal stress components represents the maximum compressive stress at a point in the tissue. The condition for hemostasis was that the maximum compressive stress must exceed the local blood pressure through the entire tissue thickness (*i.e.*, the *minimum value of the maximum compressive stress* exceeding local blood pressure throughout the tissue). Based on the considerations above, design curves were developed which related tis-

sue thickness, tissue material properties, and applied load to achieve hemostasis.

The design curves were intended to aid in clip design by estimating whether a given clip design would achieve hemostasis in advance of any physical testing. To illustrate one possible scenario, it should consider a candidate clip design that utilized elastic deformation to provide clamping force, such as in a spring-loaded clamp. In such a case, the clip would first be opened, allowing it to be placed on the tissue. The tissue would in turn deform under the pressure applied by the clip, and the system would come to a state of equilibrium. The magnitude of

the clamping force applied by the clip in this equilibrium state would depend upon the final deformed thickness of the tissue. Knowledge of the force-deflection characteristics of the tissue (*i.e.*, the final deformed tissue thickness in response to a given clip force) would provide valuable information in designing the clip. This clamping force would then be compared to the force required for hemostasis to see if the design is viable.

One of the challenges in utilizing computational modeling as a design tool for medical devices is the inherent uncertainty in physiological systems, both with respect to tissue constitutive models as well as geometry. In general, mechanical property data for human subjects are often scarce and may show considerable variations among individuals (see Figure 3). In addition, geometric parameters such as tissue thickness may vary between individuals, or even within an individual for different parts of the organ or for different times. This is particularly relevant in the current application, cesarean delivery, due to the rapid post-delivery changes in uterine thickness and geometry. Our approach was to estimate upper and lower bounds for both thickness and material properties. Simulations were carried out between these bounds, and ranges for hemostatic force were provided, rather than a single value.

Several simplifications were utilized in this work that could potentially impact the results. The geometric model utilized was strictly two-dimensional, which necessitated neglecting three-dimensional effects. One such three-dimensional effect relates to the use of multiple clips to close an incision. Even if interlocking clips were used, the pressure between clips may fall below the hemostatic limit even if the pressure directly under the clip is sufficient. This issue can be handled with tightlyspaced clips and a reasonable factor of safety. Another three-dimensional effect relates to the clip-face geometry. In this work, the faces of each clip were modeled as smooth, whereas they will most likely be textured or serrated to grip the tissue without slipping. The complex stress distribution associated with such a face will be a local effect and will not affect the overall stress distribution away from the clip, according to St. Venant's Principle [7]. Finally, uterine tissue was modeled to be isotropic, while muscle tissue is known to be anisotropic. However, in this case, the load is applied perpendicular to the fiber direction (normal to the surface), so it is reasonable to ignore anisotropy.

This work focused specifically on closure of a fullterm pregnant uterus; the development of hemostatic clips as an alternative to sutures for closure as a part of cesarean delivery has the potential to improve patient outcomes. However, the general methodology is applicable to a number of thick-walled organs, and has demonstrated that computational modeling can provide valuable information to aid in implant design, potentially improving the efficiency of the design process.

5. ACKNOWLEDGEMENTS

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