

# FDTD Simulation of Three Photon Absorption and Realization of NAND Gate with GaAs Wire Waveguide

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## ABSTRACT

GaAs has high three photon absorption (3PA) co-efficient at mid-infrared wavelength like 2.2  $\mu\text{m}$  and waveguides can be formed with this material like silicon nano-wires. It is shown that three-photon-absorption in GaAs wire waveguide can be utilized to form NAND gate. Three-photon-absorption is incorporated in one-dimensional Finite Difference Time Domain (FDTD) equations. The evolution of a probe pulse under the influence of a pump pulse through cross-absorption in a waveguide is investigated using FDTD simulation, where the dominant process is nonlinear three-photon-absorption. Output probe power dependence on input pump power shows that GaAs waveguide NAND gate has higher extinction ratio in comparison to NAND gate using two-photon-absorption in silicon waveguide.

**Keywords:** Three Photon Absorption; Fifth Order Nonlinearity; FDTD; Full Vector Finite Difference Method; Pump Beam and Probe Beam

## 1. Introduction

GaAs is an important material in the realm of nonlinear photonics. GaAs/AlGaAs multiple quantum well structures (MQW) exhibit high Kerr-type nonlinearity due to excitonic resonances near the band gap [1]. In a directional coupler with nonlinear core or cladding region, power exchanges between the guides cease when the input power is raised beyond a critical power [2-6]. This fact was used to design and implement power switching at relatively low powers using such MQW structures although large loss in the medium near the bandgap is an impediment [7,8].

On the other hand, composites of GaAs, like AlGaAs, InGaAs can be used to form semiconductor optical amplifiers (SOA). SOAs are low-cost optical amplifiers—a potential candidate to replace electronic devices in local distribution systems for faster applications. Many signal processing elements and logic gates [9-12] have been proposed and verified. However, the speed of these devices is also limited by the response time of the carriers.

After some pioneering works by M. Lipson *et al.*, silicon photonics [13] is a very active field of study for the realization of all optical logic gates. Kerr nonlinearity of silicon is not very high—it is about  $10^{-9}$  times higher than GaAs MQW structure. Integrated photonic circuits

were formed with micro-ring resonators using free carrier dispersion [14] and with slot waveguides using field switching in the middle cladding region [15]. Other nonlinear effects of silicon like Two Photon Absorption [16, 17], Raman Effect [18,19], Polarization Rotation [20], Fourwave Mixing [21,22] can also be used to realize all optical logic gates.

One of the major advantages of silicon is that waveguides can be formed with very small transverse dimensions—in the range of few nm, which are called silicon wires. GaAs is also compatible with silicon platform and GaAs wires can be formed with appreciable bending [23]. Other nonlinear effects of GaAs are also prominent and still not fully explored [24].

It is observed that silicon photonics can be used with higher efficiency in the mid infra-red region *i.e.* 2 - 10  $\mu\text{m}$  [25]. GaAs has some superior characteristics in this wavelength range and one can tap amplification also due to direct bandgap nature of this material [26].

T. K. Liang *et al.* [16] proposed ultrafast all optical NOR gates based on two photon absorption (2PA) in silicon. We have earlier shown that NAND gates can also be formed, in principle, using 2PA in silicon, but the extinction ratio is poor [27].

Between NOR and NAND gates based on absorption

or loss, NAND gate is preferable because it has only one low output state. In this paper, we show that using 3PA in GaAs, NAND gates can be formed with better extinction ratio. Silicon has low 3PA coefficient, so it can not be used that way.

In Section 2, we have incorporated 3PA loss in the Ampere's law of Maxwell's equations. The inclusion of this nonlinear term makes FDTD update equations [28-30] complicated. We show a procedure to simplify the FDTD update equations. FDTD update equations are set up with 3PA process included and for simultaneous evolution of pump and probe pulses through cross-absorption. In Section 3, we first determined the effective index and modal field of the GaAs wire waveguide using our indigenously-developed full vector finite difference method without and with Kerr nonlinearity which leads to simplification of the FDTD formulation to one-dimension. We also discussed the effects of Kerr nonlinearity on the temporal evolution of the pump pulse. Then we validated our FDTD equations reproducing the theoretical law of power attenuation during propagation along the waveguide. Next we determined the probe power output for various input pump powers for a fixed length of the waveguide. These studies form the basic of the NAND gate we design. The waveguide structure for this gate device and its working is also illustrated in this section.

## 2. Theory

The evolution of a single pump beam of intensity  $I_p$  in a medium with three-photon-absorption coefficient  $\gamma_{3PA}$  is given by

$$\frac{dI_p}{dz} = -\gamma_{3PA} I_p^3 \quad (1)$$

This can also be expressed in terms of the electric field  $E_p$  as

$$\frac{dE_p}{dz} = -\frac{\gamma_{3PA}}{2} \left( \frac{1}{2} \epsilon_0 c n_0 \right)^2 |E_p|^4 E_p \quad (2)$$

where  $\epsilon_0$  is the electric permittivity of free space,  $c$  the velocity of light in free space and  $n_0$  is the effective index of the waveguide. The above process involves a fifth order nonlinear interaction. The polarization related to this process

$$\mathbf{P}_{NL}^5 = \epsilon_0 \chi^5 \mathbf{E} \mathbf{E} \mathbf{E} \mathbf{E} \mathbf{E} \quad (3)$$

The imaginary part of  $\chi^5$  contributes to 3PA process. One can write

$$\mathbf{P}_{NL}^5 = \epsilon_0 \epsilon_{NL}^5 \mathbf{E} \quad (4)$$

where  $\epsilon_{NL}^5$  is the relative electric permittivity arising from fifth order nonlinearity. Then considering only 3PA

process

$$\begin{aligned} \epsilon_{NL}^5 &= \frac{i\gamma_{3PA}c}{2\omega} 2n_0 \left( \frac{1}{2} \epsilon_0 c n_0 \right)^2 |E|^4 \\ &= -\frac{\epsilon_0^2 n_0^3 c^3 \gamma_{3PA}}{4i\omega} |E|^4 \end{aligned} \quad (5)$$

So,

$$\mathbf{P}_{NL}^5 = -\frac{\epsilon_0^3 n_0^3 c^3 \gamma_{3PA}}{4i\omega} |E|^4 \mathbf{E} \quad (6)$$

Multiplying both sides of (6) by  $-i\omega$  and replacing it by  $\partial/\partial t$

$$\frac{\partial \mathbf{P}_{NL}^5}{\partial t} = \frac{\epsilon_0^3 n_0^3 c^3 \gamma_{3PA}}{4} |E|^4 \mathbf{E} \quad (7)$$

Maxwell's equation (Ampere's law) with linear and nonlinear polarization can be expressed as

$$\begin{aligned} \nabla \times \mathbf{H} &= \frac{\partial \mathbf{D}}{\partial t} \\ &= \frac{\partial(\epsilon_0 \mathbf{E})}{\partial t} + \frac{\partial \mathbf{P}_L}{\partial t} + \frac{\partial \mathbf{P}_{NL}}{\partial t} \\ &= \epsilon_0 \epsilon_r \frac{\partial \mathbf{E}}{\partial t} + \frac{\partial \mathbf{P}_{NL}}{\partial t} \end{aligned} \quad (8)$$

where  $\epsilon_r$  is the linear part of relative electric permittivity.

We consider only 3PA effect in the nonlinear polarization. Then putting (7) in (8)

$$\epsilon_0 \epsilon_r \frac{\partial \mathbf{E}}{\partial t} = -\frac{\epsilon_0^3 n_0^3 c^3 \gamma_{3PA}}{4} |E|^4 \mathbf{E} + \nabla \times \mathbf{H} \quad (9)$$

In our 1D FDTD, we take  $\epsilon_r = n_0^2$ , the effective index of the waveguide. Then writing  $\alpha_p = \frac{1}{4} \epsilon_0^2 c^3 n_0 \gamma_{3PA}$ , (9)

takes the form  $\frac{\partial E_y}{\partial t} = -\alpha_p E_y^5 + \frac{1}{\epsilon_0 n_0^2} \frac{\partial H_x}{\partial z}$

This leads to the following finite difference equation for electric field update

$$\begin{aligned} E_{yp}^{n+1}(i) - E_{yp}^n(i) \\ = -\alpha_p \Delta t \left\{ E_{yp}^{n+\frac{1}{2}}(i) \right\}^5 + \frac{F_c Z_0}{n_0^2} \left[ H_{xp}^{n+\frac{1}{2}}(i-1) - H_{xp}^{n+\frac{1}{2}}(i) \right] \end{aligned} \quad (10)$$

where  $F_c = c \Delta t / \Delta z$  is the Courant number. It is taken as unity.  $Z_0$  is the impedance of the vacuum.

$$Z_0 = \sqrt{\frac{\mu_0}{\epsilon_0}}$$

The other FDTD equation for magnetic field update keeps its usual form

$$H_{xp}^{n+\frac{1}{2}} \left( i + \frac{1}{2} \right) - H_{xp}^{n-\frac{1}{2}} \left( i + \frac{1}{2} \right) = \frac{F_c}{Z_0} \left[ E_{yp}^n(i+1) - E_{yp}^n(i) \right] \quad (11)$$

To simplify FDTD update Equation (10), one can make use of Taylor series expansion [31]

$$\begin{aligned} \left(E^{n+\frac{1}{2}}\right)^5 &= (E^n)^5 + \frac{\partial(E^n)^5}{\partial t} \cdot \frac{\Delta t}{2} \\ &= (E^n)^5 + 5 \cdot (E^n)^4 \cdot \frac{1}{2} [E^{n+1} - E^n] \\ &= \frac{5}{2} (E^n)^4 E^{n+1} - \frac{3}{2} (E^n)^5 \end{aligned}$$

Then Equation (10) takes the form

$$E_{yp}^{n+1}(i) = F_{1p}(i) E_{yp}^n(i) + F_{2p}(i) \left[ H_{xp}^{n+\frac{1}{2}}(i-1) - H_{xp}^{n+\frac{1}{2}}(i) \right] \quad (12)$$

where

$$F_{1p}(i) = \frac{1 + (3/2)\alpha_p \Delta t \{E_{yp}^n(i)\}^4}{1 + (5/2)\alpha_p \Delta t \{E_{yp}^n(i)\}^4} \quad (13a)$$

$$F_{2p}(i) = \frac{F_c Z_0}{n_0^2} \cdot \frac{1}{1 + (5/2)\alpha_p \Delta t \{E_{yp}^n(i)\}^4} \quad (13b)$$

When one pump beam and a probe beam of different frequencies are present, the change in intensity of the pump and probe beam can be obtained using (3),

$$\frac{dI_p}{dz} = -\gamma_p (I_p^3 + 6I_p^2 I_s + 3I_p I_s^2) \quad (14a)$$

$$\frac{dI_s}{dz} = -\gamma_s (I_s^3 + 6I_s^2 I_p + 3I_s I_p^2) \quad (14b)$$

$\gamma_p, \gamma_s$  are the 3PA coefficients of pump and probe waves respectively. The probe beam is much weaker than the pump beam. Keeping the dominant terms in (13),

$$\frac{dI_p}{dz} = -\gamma_p I_p^3 \quad (15a)$$

$$\frac{dI_s}{dz} = -\gamma_s (3I_s I_p^2) \quad (15b)$$

The update equation for the pump and probe electric fields has the same form as (12). Denoting the probe fields by  $E_{ys}$  and  $H_{xs}$ , in the update Equation (12), using (15b) the coefficients  $F_{1s}$  and  $F_{2s}$  are given by

$$F_{1s}(i) = \frac{1 - \frac{3}{2}\alpha_s \Delta t \{E_{yp}^n(i)\}^4}{1 + \frac{3}{2}\alpha_s \Delta t \{E_{yp}^n(i)\}^4} \quad (16a)$$

$$F_{2s}(i) = \frac{1}{1 + \frac{3}{2}\alpha_s \Delta t \{E_{yp}^n(i)\}^4} \quad (16b)$$

### 3. Results and Discussions

The structure of the GaAs wire [23] is shown in **Figure 1**. The GaAs wire waveguide having a square cross-sectional area of width  $W$  rests on a thick SiO<sub>2</sub> platform. The wavelength of the probe beam is taken to be 2.2  $\mu\text{m}$ ; the waveguide is single-moded at this wavelength. We have used Gaussian pulses of 0.5 ps width for the pump beam and continuous oscillatory field of wavelength 2.2  $\mu\text{m}$  for the probe beam.

The peak strength of the probe beam is taken to be  $10^{-2}$  times the pump strength. The centre wavelength of the pump beam is set at slightly different value to filter out the pump wave at the output where the probe is also present. The choice of the pump wavelength and width  $W$  of the waveguide depends on several factors which is discussed in the following.

The gates, we propose, works on the attenuation of optical power due to 3PA as it propagates along the waveguide. There is also another third order nonlinear process in this level—Kerr effect. This process changes the shape of the transverse modal field distribution and also the pulse shape in the time domain. So, it is important to look at the role of this effect while the power in the waveguide changes during propagation.

To estimate the effect of Kerr nonlinearity in the modal field distribution, we made a full vector finite difference method (FVFD) modal analysis of the waveguide taking Kerr effect into account. The FVFD we have developed on our own and coded in Matlab. It is very fast, works on the inverse iteration method [32]. We found the effective area  $A_{\text{eff}}$  of the waveguide given by [33]

$$A_{\text{eff}} = \frac{\left( \int \int_{-\infty}^{+\infty} |\Psi(x, y)|^2 dx dy \right)^2}{\int \int_{-\infty}^{+\infty} |\Psi(x, y)|^4 dx dy} \quad (17)$$

$\Psi(x, y)$  is the transverse field distribution, either  $E$ -field or  $H$ -field.

Nonlinearity is incorporated in this scheme through the modification in the refractive index profile and iteration [6]. The difference of effective index values and modal field distributions of the waveguide, with and without nonlinearity at the maximum power  $-2 \text{ GW/cm}^2$  we consider, is quite small; the change in the effective area is only 0.5%. So one can neglect the transverse distribution of the modal field and use one-dimensional FDTD to extract the power evolution along the waveguide. The refractive index of GaAs at 2.2  $\mu\text{m}$  wavelength is 3.3552 and that of SiO<sub>2</sub> is 1.4350. Then effective index of the wire waveguide  $n_0 = 1.542$  and the effective area is 0.23  $\mu\text{m}^2$ .

When one uses ultra-short pulses and high power to tap nonlinear absorption like 2PA or 3PA, dispersion and

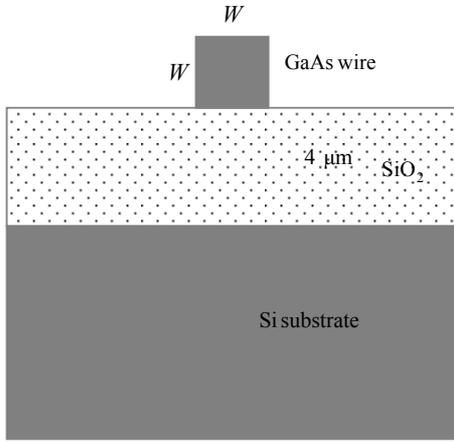


Figure 1. Schematic diagram of GaAs wire.

self-phase-modulation (SPM) effects must be investigated.

We have found group velocity dispersion (GVD) parameter  $\beta_2$  and third order dispersion (TOD) parameter  $\beta_3$  with our FVFDMM for a range of wavelengths. Material dispersion and waveguide dispersion both are considered simultaneously in the analysis. Variation of  $\beta_2$  with  $\lambda$  within the range of our interest (1.8 to 2.1  $\mu\text{m}$ ), is shown in **Figure 2** for three widths of the GaAs wire. Variation of  $\beta_3$  is shown in **Figure 3**.

It is observed that for 440  $\mu\text{m}^2$  cross-section,  $\beta_2$  is almost flat but the value is near  $-10 \text{ ps}^2/\text{m}$ . For ultra-short pulses, GVD must be very low to avoid pulse dispersion [33].

To set  $\beta_2$  at a low value near  $\lambda = 2 \mu\text{m}$ , 420  $\mu\text{m}^2$  is most suitable. Near zero dispersion wavelength, one must take care of Third Order Dispersion (TOD) or  $\beta_3$ . **Figure 3** shows  $\beta_3$  is low for 420  $\mu\text{m}^2$  cross-section near  $\lambda = 2 \mu\text{m}$ .

At 2.02  $\mu\text{m}$  wavelength, length associated with GVD,  $L_D = T_0^2 / |\beta_2| = 11.5 \text{ m}$ , length associated with TOD,  $L'_D = T_0^3 / |\beta_3| = 2.7 \text{ m}$ .

At 2  $\mu\text{m}$ ,  $L_D = 1.08 \text{ m}$  and  $L'_D = 3.5 \text{ m}$ .

So, around 2  $\mu\text{m}$  wavelength, dispersion wavelengths  $L_D$  and  $L'_D$  can be set to values large compared to the desired length of the waveguide, 0.5 cm.

Nonlinear Kerr coefficient of GaAs,  $n_2 = 1.3 \times 10^{-17} \text{ m}^2/\text{W}$  [34], is about thousand times higher compared to that in silica. So, it may give rise to appreciable SPM effects. SPM is appreciable in a waveguide when the length of propagation  $L$  is comparable to the nonlinear length  $L_{NL}$  defined by [33]

$$L_{NL} = \frac{1}{\gamma P_0}$$

where  $\gamma = k_0 n_2 / A_{eff}$  and  $P_0$  is the peak power of the pulse.

$A_{eff}$  is determined with FVFDMM; at  $\lambda = 2 \mu\text{m}$ , it is

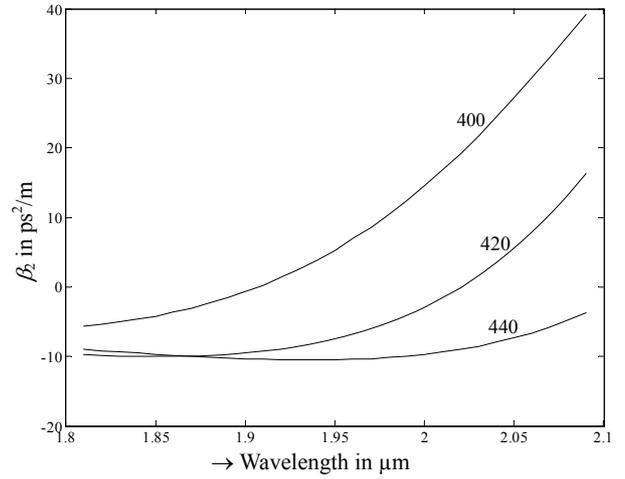


Figure 2. Variation of GVD ( $\beta_2$ ) with  $\lambda$ .

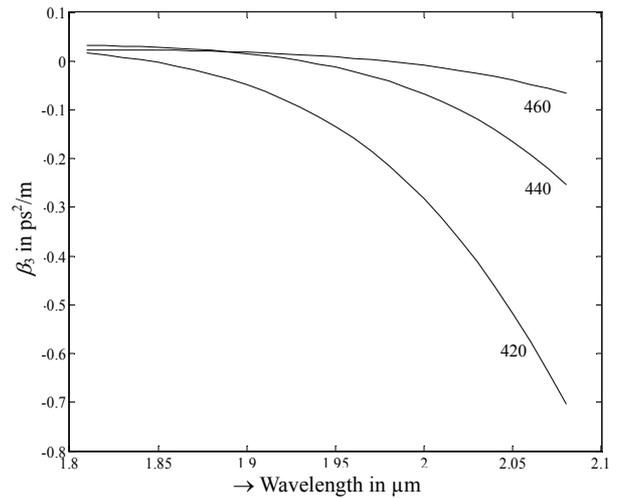


Figure 3. Variation of TOD ( $\beta_3$ ) with  $\lambda$ .

0.23  $\mu\text{m}^2$ . Maximum intensity of the pump pulse used here is around 2  $\text{GW}/\text{cm}^2$ . This gives  $P_0 \cong 2 \text{ Watt}$  and  $L_{NL} = 2.5 \text{ cm}$ . Since peak power falls due to 3PA during propagation,  $L_{NL}$  can be considered large compared to the waveguide length 0.5 cm; therefore SPM effects can be neglected. The value of  $\gamma_{3PA}$  is 0.32  $\text{cm}^3/\text{GW}^2$  [34], at the probe wavelength 2.2  $\mu\text{m}$ . At the wavelength of the pump beam – 2  $\mu\text{m}$ ,  $\gamma_{3PA}$  is 0.18  $\text{cm}^3/\text{GW}^2$ .

The NAND gate device that acts on the principle of three-photon cross absorption is shown in **Figure 4**. Two pump beams are fed into the waveguide through S-bends and the probe beam is injected straight at the center. At first, we have validated our FDTD formulas (11), (12) with co-efficients given by (13) and (16). **Figure 5** shows the attenuation of the pump and probe beams during propagation through a distance of 1 cm, as obtained with FDTD simulation and from the theoretical result—Equation (15). Pump and probe intensity variation obtained from FDTD simulation is shown with red line

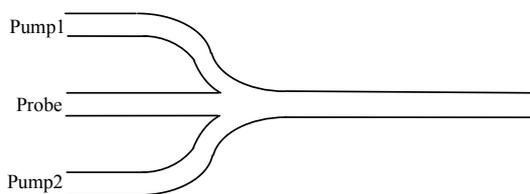


Figure 4. Structure of the NAND gate device.

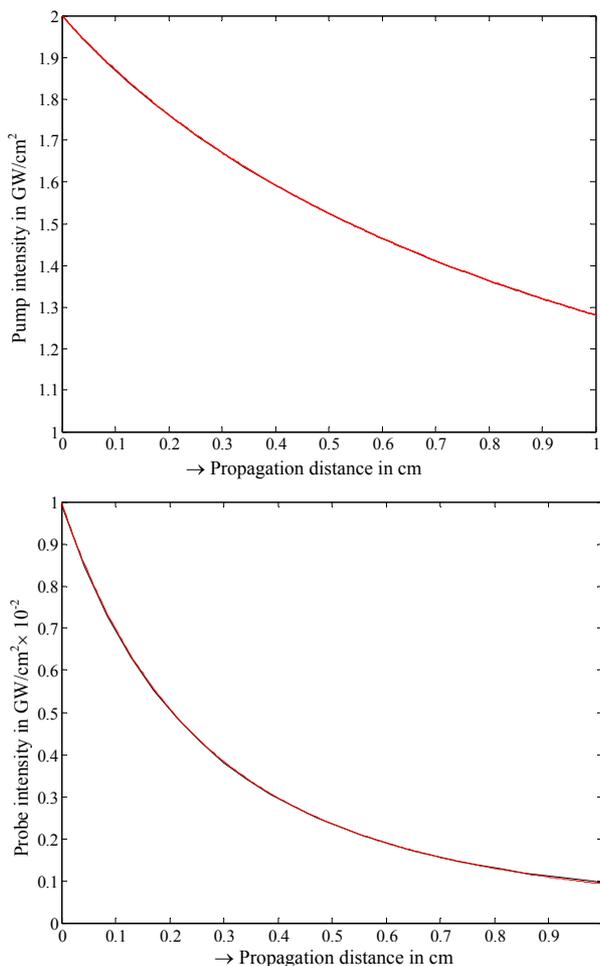


Figure 5. Attenuation of pump and probe intensity with propagation. Black line—FDTD; Red line—Equation (15).

curve and that from Equation (15) is shown with black line curve. The curves are almost coincident.

We have coded our FDTD program in MATLAB. The probe beam develops an inverted Gaussian pulse at the point of the pump beam. We have set up a program to get the envelope of the probe beam which shows the form of the dark pulse clearly. We have taken  $\Delta z = 4.28 \times 10^{-8}$   $\mu\text{m}$ ; it is observed that such a fine numerical grid is necessary for proper development of the probe pulse. We have taken numerical window size =  $10,000 \times \Delta z$  and PML layers of 10 cell width. After 15,420 time steps, as the fields reach the right edge, they are partially shifted to the left and the probe field is fed into the input at the

right phase. In this way, same numerical window can be used taking time update as long as one wants saving computational time enormously.

The evolution of the pump pulse and dark probe pulse are shown in Figure 6. One pump pulse and its corresponding probe pulse are shown near the input end; the shape of those pulses is also shown at the output end—after propagation through 1 cm length of the waveguide.

The minimum of the dark pulse after 0.5 cm propagation for a range of input pump intensity from 0 to 2  $\text{GW}/\text{cm}^2$ , is shown in Figure 7. It shows that for 0.9  $\text{GW}/\text{cm}^2$  pump input intensity, the output probe intensity is down by about 70% and when the input intensity is 1.8  $\text{GW}/\text{cm}^2$ , the output is down by about 36%. If 50% intensity level is used as threshold, the switching of the output from high to low as the input intensity is changed from 0.9 to 1.8  $\text{GW}/\text{cm}^2$  can be used to form a NAND gate with the gate structure of Figure 4 as shown in Table 1.

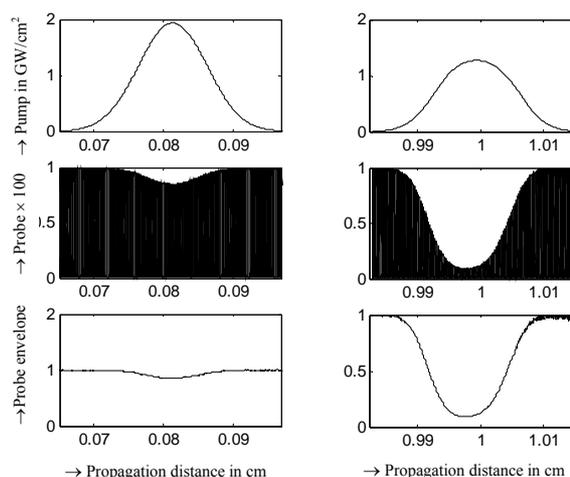


Figure 6. Pump pulse and dark pulse formation in the probe beam.

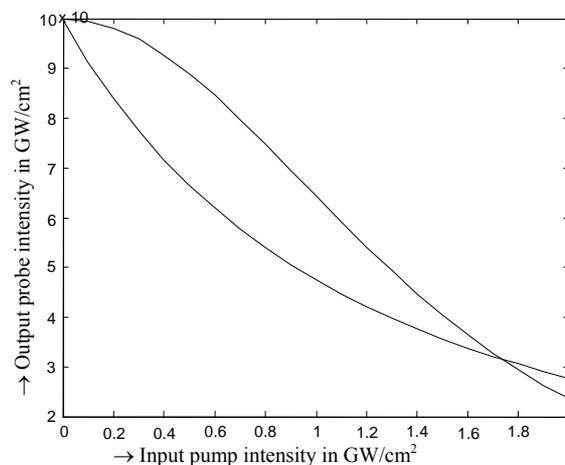


Figure 7. Variation of probe intensity with pump intensity for 0.5 cm guide length.

**Table 1. Realization of NAND gate.**

Probe in Unit: $10^{-2}$ GW/cm <sup>2</sup>	Pump 1 Unit: GW/cm <sup>2</sup>	Pump 2 Unit: GW/cm <sup>2</sup>	Probe out Unit: $10^{-2}$ GW/cm <sup>2</sup>	Output logic
1	0	0	100%	1
1	0.9	0	70%	1
1	0	0.9	70%	1
1	1.8	1.8	36%	0

In **Figure 7**, the dotted line is the corresponding probe intensity variation in silicon wire waveguide based on two photon absorption (wavelength  $1.55 \mu\text{m}$ ,  $\beta_{2PA} = 0.9 \text{ cm/GW}$ ).

The curve for Si-wire waveguide in **Figure 7** shows that NAND switching can be obtained for  $0.5 \text{ cm}$  guide length. Without any pump input, probe intensity gets out undiminished. When pump 1 or pump 2 is present and equal to  $0.9 \text{ GW/cm}^2$ , the probe output is 51%. When both pump 1 and pump 2 are present, the output is attenuated down to 34%. If 40% probe power is taken as threshold, the output is low only when both pump 1 and pump 2 are present; NAND switching can be realized with the Si-wire waveguide structure shown in **Figure 4**. However, GaAs waveguide has higher extinction ratio and higher difference between high and low states.

#### 4. Conclusion

GaAs has some superior nonlinear behavior than silicon and its potentiality is not yet fully explored. We have considered a GaAs wire waveguide and determined its effective index with a full vector finite difference method with and without Kerr nonlinearity. The small difference of the effective index values when Kerr nonlinearity is taken into account prompted us to simulate the evolution of pump and probe field along the same waveguide through cross-absorption using one-dimensional FDTD. In this paper, we have incorporated three-photon-absorption in one-dimensional FDTD update equations. GaAs has significant three-photon-absorption co-efficient. We have considered a GaAs wire waveguide structure (**Figure 4**) that takes in two pump beams and one probe beam, puts them into a single waveguide. We have shown that one can realize NAND gate with this structure where the intensity of the input pump beams is the input states and the output probe intensity is the output state. Similar gate structure can be formed if GaAs is replaced with Si-wire waveguide but that has lower extinction ratio.

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