

Likelihood Parameterization of Bicycle Crash Injury Severities

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ABSTRACT

This paper evaluates different factors and parameters contributing to likelihood of bicycle crash injury severity levels. Multinomial Logit (MNL) model was used to analyze impact of different roadway features, traffic characteristics and environmental conditions associated with bicycle crash injury severities. The multinomial model was used due to its flexibility in quantifying the effect of the independent variables for each injury severity categories. Model results showed that, severity of bicycle crashes increases with increase in vehicles per lane, number of lanes, bicyclist alcohol or drug use, routes with 35 - 45 mph posted speed limits, riding along curved or sloped road sections, when bicyclists approach or cross a signalized intersection, and at driveways. In addition, routes with a high percentage of trucks, roadway sections with curb and gutter, cloudy or foggy weather and obstructed vision were found to have high probability of severe injury. Segments with wider lanes, wide median and wide shoulders were found to have low likelihood of severe bicycle injury severities. Limited lighting locations was found to be associated with incapacitating injury and fatal crashes, indicating that insufficient visibility can potentially lead to severe crashes. Other findings are also presented in the paper.

Keywords: Bicycle Crash; Injury Severity; Multinomial Logit

1. Introduction

The average annual number of bicycle fatal crashes from 1998 to 2008 in United States was 721. In 2008, 716 pedalcyclists were killed and an additional 52,000 bicyclists were injured in traffic crashes. Pedalcyclist deaths accounted for 2 percent of all traffic fatalities, and made up 2 percent of all the people injured in traffic crashes in 2008 (NHTSA, 2008 [1]). The same report highlights that pedalcyclist fatalities occurred more frequently in urban areas (69%), at non-intersection locations (64%), between 5 p.m. and 9 p.m. (28%), and during the months of June (9%) and September (12%). This paper evaluates factors influencing bicycle crash injury severities.

Bicycle crashes have been studied by several researchers for the past decade. Cheryl *et al.* [2] developed a bicycle route safety rating model based on injury severity. The model development was conducted using a logistic transformation of bicycle crash data from Jersey City, New Jersey, for the period 1997 to 2000. The resulting model met 90% confidence level by using various operational and physical factors like traffic volume, lane width, population density, highway classification, and presence of vertical grades, one-way streets, and truck

routes to predict the severity of an injury that would result from a motor vehicle crash that occurred at a specific location. In another study, Jeremy and Asad [3] examined the effect of roadway and environmental factors on injury severity in bicycle-motor vehicle collisions. An ordered probit model for injury severity was estimated using the Highway Safety Information System (HSIS) data set for two-lane roadways. The model parameters and the marginal effects of significant variables were used to examine the influence of roadway and crash characteristics on injury severity of cyclists. In this study, speed limit, straight and curved grades, fog and unlighted darkness were found to increase injury severity, while average annual daily traffic, an interaction of the shoulderwidth and speed-limit variables, and street lighting were found to be associated with decreased injury severity.

Karl and Lei [4] found that bicyclists are more likely to be attentive than motorists, and slightly less likely to be associated with misjudgment or alcohol or drug use than motorists. The same study found that bicyclists are much more likely to disregard traffic controls or go the wrong way on a street just before becoming involved in a collision than motorists. Motorists are more likely to fail to yield, to engage in improper overtaking, or to follow too closely before becoming involved in a collision than

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bicyclists. Shankar and Mannering [5] found that riding without a helmet, and under the influence of alcohol increased the likelihood of a disabling injury or fatality. The same study found that the use of alcohol, overspeeding, and older motorcyclists were associated with higher likelihood of severe injury.

Quddus et al. [6] used ordered probit model to study how various factors, including specific characteristics of the roadway and the riders, can lead to different levels of injury and damage severity. The rationale for using the ordered probit model was due to its capability to model categorical dependent variables. The authors dismissed the use of unordered multinomial, nested logit, or probit models because they do not account for the ordinal nature of the injury categories and the association of independence of irrelevant alternatives (IIA) in the multinomial logit (MNL) models. The ordered probit models are known to have weakness in classification of injury severity. However they are useful when the coefficient for each variable in the model is required to classify injury severities category. On the other hand, unordered multinomial model is appropriate for evaluating the effect of the variables to each injury severity category. Shankar and Mannering (1996) [5] used the multinomial logit model to examine factors affecting injury severities. Their findings revealed that the multinomial logit formulation was a potential approach to determine significant factors affecting severity. The main disadvantage of using the multinomial logit model was that the error term follows a generalized extreme value (GEV) distribution, which leads to the issue of IIA.

A review of these previous studies however indicated plenty of methodologies in evaluating bicycle crashes. In view of the methodologies used in previous studies and their recommendations for further research, this paper examines the use of the multinomial logit (MNL) model in analyzing bicycle crash severity. Ordered models are not used herewith due to their limited independent variables effect outcome probabilities, Washington *et al.* [7].

Based on the bicycle related statistics presented above, it is therefore warranted to examine the factors contributing to these types of crashes. This study complements the desire of many all any transportation related agencies and jurisdiction in ensuring the safe use of bicycle as the mode of transportation. Understanding the factors contributing to the levels of injury severity is an important step towards making bicycle one of the safe and more attractive modes. Furthermore, differentiating the contributing factors may help establish safer bicycle mode of transportation.

2. Methods

The MNL have been used widely on injury severity studies. As an extension from the Logit model, MNL is used for dependent variable with more than 2 categories or indicators, Quddus et al. [5] and Mouskos, et al. [8]. The MNL model is built based on the assumption that the choice between any pair of alternatives of the response variable is independent of the availability of other alternatives. It implies that the random part of utility function is independent among the alternatives. The multivariate response variable can be distinguished depending whether the variable has an ordered or unordered category. When categories in the response variable are not ordered, MNL regression becomes appropriate compared to other type of regressions, Shankar and Mannering [4]. Suppose there are J categories of the injury severity as the response variable, then there will be J - 1 equations for MNL as a binary logistic regression comparing a group with the reference (base) category or comparison group. Using the maximum likelihood, MNL simultaneously estimates the J-1 logit functions. The probabilities of other members in other categories are compared to the probability of membership in the reference category. Suppose the utility function is denoted as, Washington et al. [7]:

$$U_{ki} = X_k \beta_i + \varepsilon_{ki} \tag{1}$$

where X_k is the independent variable, β_i is the coefficient associated with each independent variable, and ε_{ki} is the error term. Suppose the response variable q_k , is subjected to different categories of severity, $0, \, \cdots, \, i$, then

$$q_k = j$$
, if $U_{ki} \ge U_{ki}$ for $j \ne i$.

In this study, i=0, 1, 2 and 3 where U_{k0} represent non-injury crash, U_{k1} represent possible injury or non-incapacitating crash, U_{k2} represent incapacitating injury and U_{k3} representing fatal crash. From the four injury categories, three equations are formed, one for each category in relation to the reference or base category, in this case is U_{k0} . The general logistic equation is given as, Washington, *et al.* [6], Shankar and Mannering [4];

$$P(q_k = j) = \frac{e^{X_k \beta_j}}{1 + \sum_{i=1}^{J} e^{(X_k \beta_i)}}$$
(2)

The odds ratio (P_{kj}/P_{ki}) will depend log-linearly on x_k , *i.e.*,

$$\log\left(\frac{P_{kj}}{P_{ki}}\right) = x_n' \left(\beta_j - \beta_i\right) \tag{3}$$

The interpretation of the effects of explanatory variables to the responses is based on comparing the coefficient of variable in the category modeled to the reference (base) category. Possible or non-incapacitating injury, incapacitating injury and fatal crash model results are interpreted in relation to base category which is non-

injury crash. The marginal effect of an independent variable x_k on the choice probability for alternative j can be expressed as:

$$\frac{\partial P(q=j\mid x)}{\partial x_{k}} = P_{j}(\beta_{jk} - \overline{\beta}_{k}) \tag{4}$$

Equation (4) depends not only on the parameter β_{jk} but also on the mean of all other alternatives

$$\overline{\beta}_k = \left(\sum_{i=1}^J \beta_{jk}\right)^{-1} \tag{5}$$

Direct interpretation of the parameter estimates can be done using the log of odds ratio:

$$\frac{\partial \log \left(P_{j} / P_{i} \right)}{\partial x_{i}} = \beta_{jk} - \beta_{ik} \tag{6}$$

This is reduced to,
$$\frac{\partial \log(P_j/P_i)}{\partial x_k} = \beta_{jk}$$
 for compari-

sons with the reference category i if the coefficients associated with the base category are set to zeros. A positive coefficient to the variable will mean the relative probability of injury severity \mathbf{J} increases relative to the probability of the same variable in the base category. The estimation can be performed by using the maximum likelihood (ML) method in which the log likelihood function is given as

$$\log L = \sum_{k=1}^{K} \sum_{j=1}^{J} q_{kj} \log(P_{kj})$$
 (7)

with $q_{kj}=1$ if the crash record k falls into severity category j and $q_{kj}=0$ if otherwise.

3. Study Data

The study utilized crashes involving bicycles which occurred on Florida State maintained highways from 2004 to 2008. A total of 10,708 bicycle related crashes were screened, among them, 11% none injury, 28% possible injury, 42% non-incapacitating injury, 16% incapacitating injury, and 3% fatal crashes. The study combined the severity into three main groups. The first group coded as "0" (none-injury), representing bicycle crashes that resulted in no injury. The second group is possible injury and non-incapacitating injury combined together and coded as "1" (moderate injury) representing bicycle crashes that resulted in minor injuries. The third group is incapacitating injury and fatal coded as "2" (severe injury) representing all bicycle crashes resulted into body disability or death occurring within 30 days after the crash. The three categories were used in MNL model where category 0 is pivoted as a base.

The analysis used both continuous and categorical variables in the model. The summary of continuous variables is included in **Table 1**. Categorical variables used

Table 1. Variables summary statistics.

| | Mean | Std. Dev | Min. | Max. |
|-------------------------------------|--------|----------|------|---------|
| Average Annual Daily Traffic (AADT) | 35,725 | 16,099 | 1000 | 161,000 |
| Vehicle per Day per Lane | 7206 | 2762 | 250 | 26,833 |
| Number of Lanes | 5 | 1 | 2 | 8 |
| Lane Width | 29 | 8 | 8 | 84 |
| Shoulder Width | 3 | 2 | 0 | 25 |
| Medium Width | 19 | 16 | 0 | 800 |
| Percentage of Trucks | 5 | 3 | 0 | 42 |
| Age | 35 | 21 | 15 | 100 |
| Speed Limit | 42 | 6 | 15 | 55 |

are listed in **Table 2**. Most of these categorical variables were coded as binary (taking on values of 1 or 0).

Analysis showed that 25% of all crashes analyzed resulted from the vehicle or bicycle making a right turn, 2% when changing lane, 9% when making left turn and 3% when slowing. For contributing causes failed to yield right of way comprised of approximately 36% of all crashes. With respect to land use, 24% of the bicycle crashes occurred in residential areas while 76% occurred in commercial or business areas. Signalized intersections and intersection influenced crashes contributed to about 75% of the bicycle crashes. At intersection crashes are those which are within 50 ft from the intersection or ramp. The influenced areas are those within 250 ft from an intersection or ramp. Alcohol and drug related bicycle crashes comprised of about 10% of total crashes. For the crashes that resulted from Driving under the Influence (DUI) of alcohol, 15% resulted in fatality. General statistics of some numerical variables analyzed are summarized in Table 1.

4. Results

None-injury crash category (e.g. category 0) was kept as a base in MNL model. The models developed compared the coefficient magnitudes and signs of the independent variables in relation to the base category. The MNL results are presented in **Table 3**. The model result parameters are interpreted in relation to the base category as indicated. It should be noted that some independent variables were significant in one injury category but insignificant in other.

4.1. Curved Sections

The coefficient of the curved sections in the model is positive in both categories. The magnitude of the coefficients increases steadily from category 1 to category 2, indicating that crashes occurring in curved areas will have strong probability of resulting into severe injury

Table 2. Coding of categorical variables.

| Categorical variable | Coding |
|--|-------------------------------|
| Presence or absence of sloped roadway sections | Coded as 1 and 0 respectively |
| Roadway section without or with shoulder | Coded as 1 and 0 respectively |
| At intersection and influenced or not intersection | Coded as 1 and 0 respectively |
| Driveways or non-driveway | Coded as 1 and 0 respectively |
| Dusk, night, no light or daylight | Coded as 1 and 0 respectively |
| Cloudy, rain, fog or clear | Coded as 1 and 0 respectively |
| Curved roadway sections or straight | Coded as 1 and 0 respectively |
| Special speed zone control or non-speed zone | Coded as 1 and 0 respectively |
| Signal control or no control | Coded as 1 and 0 respectively |
| Stop sign control or not | Coded as 1 and 0 respectively |
| Vision obstructed or not | Coded as 1 and 0 respectively |
| Urban areas or other areas | Coded as 1 and 0 respectively |
| 30 mph or less speed limit or higher speed | Coded as 1 and 0 respectively |
| 35 - 45 mph speed Limit or lower speed | Coded as 1 and 0 respectively |
| Drug or alcohol use or none | Coded as 1 and 0 respectively |

Table 3. Injury severity modeling results.

| Multinomial logistic regression Likelihood ratio chi ² = 7363.23 Log likelihood = -8082.3266 | Number of observ $Prob > chi^2 = 0.00$ $Pseudo R^2 = 0.31$ | | |
|---|--|------------|---------|
| Possible or non-incapacitating injury severity | Coefficient | Std. error | Z-value |
| Vehicle per day per lane | 9.0E-07 | 7.5E-08 | 12.03 |
| Number of lanes | 0.1530 | 0.061 | 2.49 |
| Median width | -0.0031 | -0.002 | 1.82 |
| Lane width | -0.0287 | -0.011 | 2.65 |
| Shoulder width | -0.0088 | -0.005 | 1.74 |
| Bicyclist age | 0.0079 | 0.001 | 8.28 |
| Percentage trucks | 0.0089 | 0.006 | 1.42 |
| Sloped roadway sections | 0.0104 | 0.005 | 2.13 |
| No shoulder | 0.0468 | 0.004 | 10.83 |
| At intersection of influenced | 0.2249 | 0.064 | 3.49 |
| Driveways | 0.3101 | 0.071 | 4.37 |
| Dusk, night, no light | 0.1010 | 0.048 | 2.1 |
| Cloudy, rain, fog | 0.1308 | 0.051 | 2.58 |
| Curved roadway sections | 0.2221 | 0.146 | 1.52 |
| Special speed zone control | 0.1607 | 0.071 | 2.26 |
| Signal control | 0.0685 | 0.031 | 2.22 |
| Stop sign control | 0.1083 | 0.057 | 1.9 |
| Vision obstructed | 0.1497 | 0.062 | 2.4 |
| Urban areas | 0.2106 | 0.130 | 1.62 |
| 30 mph or less speed limit | -0.2057 | 0.103 | -1.99 |
| 35 - 45 mph speed limit | 0.1085 | 0.043 | 2.5 |
| Drug or alcohol use | 0.3130 | 0.077 | 4.05 |

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Continued

| Incapacitating injury or fatal | | | |
|--------------------------------|----------|---------|-------|
| Vehicle per day per lane | -2.3E-05 | 1.1E-05 | -1.98 |
| Number of lanes | 0.4170 | 0.217 | 1.92 |
| Median width | -0.0020 | 0.001 | -2.42 |
| Lane width | -0.0423 | 0.014 | -3.11 |
| Shoulder width | -0.0842 | 0.033 | -2.55 |
| Bicyclist age | 0.0248 | 0.003 | 8.56 |
| Percentage trucks | 0.0206 | 0.011 | 1.89 |
| Sloped roadway sections | 0.0499 | 0.022 | 2.22 |
| No shoulder | 0.3371 | 0.167 | 2.02 |
| At intersection of influenced | 1.1469 | 0.147 | 7.79 |
| Driveways | 1.9544 | 0.253 | 7.74 |
| Dusk, night, no light | 0.8689 | 0.128 | 6.81 |
| Cloudy, rain, fog | 0.1854 | 0.080 | 2.31 |
| Curved roadway sections | 0.4855 | 0.196 | 2.48 |
| Special speed zone control | 0.4816 | 0.153 | 3.15 |
| Signal control | -0.0916 | 0.173 | -0.53 |
| Stop sign control | 0.8683 | 0.248 | 3.5 |
| Vision obstructed | 0.1384 | 0.085 | 1.62 |
| Urban areas | 0.8300 | 0.253 | 3.28 |
| 30 mph or less speed limit | -1.3688 | 0.319 | -4.29 |
| 35 - 45 mph speed Limit | 0.8890 | 0.160 | 5.55 |
| Drug or alcohol use | 1.7918 | 0.138 | 13.01 |

compared to light injury. The finding coincides with previous study which found that higher crash rates can be expected on curves than tangents, with rates ranging from two to four times higher than tangents, Jeremy and Asad [3].

4.2. Posted Speed Limit

Speed limit is a function of several roadway parameters, sight distance and roadway condition. The study grouped the speed limit into three, from 15 - 30 mph were coded as "1" representing low speed, 35 - 45 mph coded as "2" and 50 mph or above representing higher speed coded as "0". As it was found in curved sections, the coefficient of high speed is positive in both models (**Table 3**). The likelihood of severe injury is high at high speed compared to low speed. The finding is consistent with the previous researches which found speeding to be associated with severe injury, Jeremy and Asad [3].

4.3. Lighting

Lighting conditions is categorized in Florida crash form into daylight, dusk, dawn, dark with street light and dark without traffic light. These categories were grouped into two, one coded "0" representing day light and the other

coded as "1" for limited lighting conditions, dusk, dawn and dark which represent "limited lighting" resulted with positive coefficient in both severe injury and fatal crash models. Based on the results, severe injury or fatal bicycle crashes will be expected at locations with limited lighting conditions compared to locations with adequate lighting.

4.4. Traffic Volume per Lane and Percentage of Trucks

Percentage of trucks is the average proportions of trucks to the total number of vehicles at that particular section. The variable has positive coefficient in the model (**Table 3**). The safety problem between trucks and bicycles can lie on the visibility of the truck drivers and smallness of the bicycle itself. Traffic volume have strong positive coefficient in less severe (possible or non-incapacitating) but negative coefficient for incapacitating/fatal model indicating crashes occurring in the congested areas will have less severe injuries. The result related with AADT might be different if crash frequency was the subject, some previous studies has found increase in crash frequency with increase in traffic volumes, Mouskos *et al.* [8].

4.5. Location

Crash location refers to location on the roadway where the crash occurred. The location can be at the intersection, driveways, ramps, railroad, bridges, parking lots, toll booth and public bus stops. In modeling, the factors were grouped into 3 categories with code "0" representing non-intersection related crashes, "1" representing at intersection or intersection influenced crashes, "2" for driveways and "3" representing other remaining location categories. Result shows bicycle crashes occurring at driveways and intersections are likely to result in either non-incapacitating, incapacitating injury, or fatal (**Table 3**).

4.6. Age

Older bicyclists seem to be more vulnerable to fatal injury than younger ones. The models show positive, significant coefficient in the fatal injury category in both models (**Table 3**). This finding is consistent with the previous research which found increase in age to be associated with likelihood of severe injury crash (Shankar and Mannering [5]).

4.7. Number of Lanes, Lane Width, Shoulder Width and Median Width

As expected, number of lanes showed positive coefficients to injury severity, the finding which is consistent with findings from previous studies that evaluated crashes involving bicycle and all other vehicle types, Theodore et al., Miao and Lump, Miao, Garber and Ehrhart [9-12]. In multilane segments, as the number of vehicles per lane increases, there become fewer gaps to allow lane changing, turning movements, or merging, which eventually increases the likelihood of crashes. Median width is significant with a negative coefficient, indicating likelihood of bicycle crash injuries severity level decreases as median width increases. This is consistent with many previous studies, Milton and Mannering, Abdel-Aty and Radwan and Lee and Mannering [13-15]. The results show that wider lanes reduce the probability of severe injury. Wider lanes can be used by a bicyclist as a room for correcting errors in the situation of near crash occurrence. Wider shoulders have negative coefficient showing its important role in reducing bicycle crash injury severities. From a highway safety point of view, a shoulder can be used by a bicyclist to stop in case of an emergency or during an incident, and drivers can take advantage of wider shoulders to avoid hitting roadside objects. In addition, bicyclists can veer to wider shoulders to avoid a crash.

5. Conclusion

The model results indicate that there are significant fac-

tors that influence bicycle injury severities on the highways. Significance of these factors to the occurrence of crashes varies depending on human judgment, contributing causes, environmental conditions, traffic characteristics, geometrics and location on highways. The multinomial Logit (MNL) model was used for analysis as it allows the use of one injury severity as a reference category while analyzing others. The results showed that, increase in number of lanes, alcohol and drug use, high posted speed limit links, curved areas, turning movements, intersection and driveways, and driving with no adequate daylight have strong significance effects on intensifying injury severity. In addition, the higher the percentage of trucks and the older the bicyclist means the more severe the injury. Regarding traffic volumes, the study found that under congestion condition few severe incidents occur though higher crash frequencies can be expected. Limited lighting locations was found to be associated with incapacitating injury and fatal crashes, indicating that insufficient visibility can potentially lead to severe crashes.

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