Performance of Risk Measures in Portfolio Construction on Central and South-East European Emerging Markets

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Abstract

Aim of this paper is to characterize different risk measures in portfolio construction on seven Central and South-East European stock markets; Slovenia, Croatia, Hungary, Poland, Chez Republic, Romania and Turkey. Selected countries are members of EU, except Croatia and Turkey which have candidate status. Empirical part of this paper consists of three stages; at first descriptive statistics on stock returns was performed, afterwards different risk measures were employed in portfolio construction and in the last part, portfolios were tested in the out-of-sample period. Results indicate presence of extreme kurtosis and skewness in stock return series. Resulting portfolios incorporate stocks with extremely high kurtosis and stocks with negative skewness. Portfolio construction based only on risk and return results in major exposure to extreme returns and unsatisfactory portfolio out-of-sample results.

Keywords: Alternative Risk Measures, Central and South-East European Emerging Markets, Portfolio, Skewness, Kurtosis

1. Introduction

Transition economies in Central and South-Eastern Europe (CSEE) represent very attractive investment area for foreign investors. In the past few years these stock markets witnessed tremendous growth both in number of listed securities as well as in market capitalization. In 2007 stock market indices grew tremendously. In 2007 value of stock market index on Zagreb Stock Exchange rose 63.20%, Slovene stock market index rose 71.0%, while German stock market index rose 22.3%. Risk and illiquidity of stocks are the main problem on these markets especially in the recent period when the global economy was struck by financial crisis. Aim of this paper is to define characteristics of stock returns on CSEE equity markets. Portfolios of stocks will be formed on these markets using five risk measures: variance, semivariance, lower partial moment when target return is equal to 0, Mean Absolute Deviation and Conditional Value at Risk. Out-of-sample analysis of formed portfolios characterizes selected risk measures and their performance in presence of kurtosis and skewness.

Paper is organized as follows: Section 2 presents a brief review of previous researches. Risk measures employed in forming portfolios are presented in Section 3. Section 4 discusses data and methodology. Section 5 presents results of empirical analysis. Results include portfolio composition and their out-of-sample performance. In Section 6 main conclusions were drawn.

2. Previous Researches

The analysis of emerging capital markets has increased substantially in the recent years, however many studies had failed to take into account the characteristics of emerging markets in their analysis. The underlying assumption of the standard mean-variance model is that stock returns must be normally distributed, however this is in direct contradiction with the empirical evidence concerning the distribution of emerging markets returns. [1-5] concluded that Central and South-Eastern European equity markets have fat tails indicating presence of many extreme observations. According to [3] who examined the use of downside risk measures in construction of an optimal portfolio, the use of downside risk measures results in significant improvement in the out-of-sample performance of those portfolios. [6] examined benefits of diversification into three leading Central European equity markets using lower partial moment in the presence



of nonnormality of returns on those markets. Their study shows that investors could benefit diversifying into Central European equity markets. These results are supported by the relatively low short term correlations as well as the lack of cointegration between these markets and developed equity markets, their prospects for future economic growth and positive impact associated with their recent accession to the EU. Similar conclusion was brought in [7] where EU accession was highlighted as the key contributor to the reduction of risk on these markets. [8] indicates that South-Eastern Europe emerging markets are loosely related in periods of normal economic activity while in conditions of economic recession they exhibit strong interrelationship. [9] concluded that return distribution appears to be leptokurtic for all Euro stock markets. Investors are more exposed to the risk since the distribution of returns has a greater exposure to outlier events and bias to the downside.

3. Risk Measures

Many researches had their idea of the "best" risk measure to be applied in the portfolio selection; mean lower partial moment [10-12], Mean-absolute deviation (MAD) [13] and Conditional Value-at-Risk (CVaR) [14]. This study involves empirical analysis of most important risk measures proposed and compared in literature in construction of optimal portfolios on selected markets.

Variance which is by its definition measure of dispersion considers the positive and negative deviations from the mean as potential risk.

Variance of security is defined as:

$$\sigma_i^2 = E \left| x_i - E(x_i) \right|^2 \tag{1}$$

where σ_i^2 -variance of security *i*, x_i is random return on security *i*, and *E* is expectation operator.

In the case of variance, over-performance relative to the mean is penalized just as much as under-performance. In order to overcome this anomaly [10] proposed semivariance as risk measure. The natural extension of the semivariance [11,12] is the lower partial moment risk.

Semivariance is a statistical measure equal to sum of square deviations from the mean, taking into account only observations below the mean:

$$x_{i} = \begin{cases} x_{i} - E(x_{i}), & x_{i} < E(x_{i}) \\ 0, & x_{i} \ge E(x_{i}) \end{cases},$$
(2)

Semivariance =
$$E[(x_i)^2]$$
 (3)

Two alternative downside risk measures are examined in this paper. The first uses the mean as target rate, the mean semivariance, and the second uses a target rate of zero. These two risk measures are denoted as LPMM and LPM0. Both measures compute risk using only returns below the mean return or alternatively below a target return. In the presence of negative skewness in a return series downside returns will occur in larger magnitudes than upside returns, the opposite is true in the presence of positive skewness.

The absolute deviation of random variable is expected absolute value of difference between the random variable and its mean. [13] proved that minimizing Mean Absolute Deviation (MAD) is similar to minimizing variance if stock returns are multivariate normally distributed. Mean absolute deviation can be calculated using following expression:

$$MAD = E\left[\left|x_{i} - E\left(x_{i}\right)\right|\right]$$
(4)

The Conditional Value-at-Risk (CVaR) can be explained trough Value-at-Risk (VaR) [15]. Following equation defines conditional expectation in the lower tail of the distribution of returns and is equal to average of returns beyond VaR at level α :

$$CVaR_{\alpha}(x) = -E^{p}\left[x\middle|x \le -VaR(x)\right]$$
(5)

Unlike Value-at-Risk, the CVaR is coherent risk measure [16,17].

4. Data and Methodology

Analysis includes seven stock markets form CSEE region, five countries are members of EU: Poland, Czech Republic, Hungary and Romania, while two; Croatia and Turkey have candidate status. On every market ten stocks [18,19] from correspondent stock index were selected. Data series consists of 500 daily closing prices for each security in time period from November 2007 until the end of October 2009. Stocks were selected according to following criteria: stock was listed before 2007 and all stock prices were available in period from November 2007 until October 2009, selected stocks are members of national stock index which includes best stocks in the country irrelevant which sector they belong. Stocks which have the biggest share in construction of national index have advantage.

Series of daily logarithmic returns for each stock were calculated. In order to determine whether the stock returns follow the normal distribution in this paper are presented results of descriptive statistics (mean, standard deviation, skewness and kurtosis) and normality tests. Normality tests conducted in this paper are Shapiro Wilk (W test) and Kolmogorov-Smirnov (K-S) D test [20]. Using five risk measures for each stock market portfolios were estimated. Estimated portfolios were analyzed in the out-of-sample period from November 2008 until October 2009. For each estimated portfolio Cumulative Abnormal Returns (CAR-s) against German stock index DAX [6] were calculated. Standard event study methodology was used, abnormal daily returns of each portfolio against DAX index were calculated:

$$AR_{it} = r_{it} - r_{mt} \tag{6}$$

where r_{it} is daily return (t) for portfolio i and r_{mt} is the appropriate benchmark return.

The CAR from the beginning of the first day until the last day of trading is the summation of abnormal returns.

$$CAR_t = \sum_{t=1}^{s} AR_t \tag{7}$$

CARs were estimated assuming benchmark was the portfolios normal return.

5. Empirical Results

Selected markets could be divided in two groups dependently on risk level measured by standard deviation; countries with lower level of risk are: Poland, Turkey, Hungary and Slovenia while higher risks can be found in Romania, Chez Republic and Croatia. As expected the standard deviation indicates high level of risk in the CSEE markets. According to results of normality tests almost all 80 observed CSEE stocks do not pass normality test. Descriptive statistics indicates that all stocks have negative returns what is expected due presence of crisis, kurtosis is always greater than zero and statistically significant indicating fat tails and presence of many extreme observations. According to data from Table 2 and Table 5, stocks from Turkey and Poland have lowest kurtosis coefficients which do not exceed 2, while values of kurtosis coefficients from Table 1, Table 3, Table 4, Table 6 and Table 7 show that all stocks from Croatia, Romania, Slovenia, Chez Republic and Hungary have very high kurtosis coefficients. Similar conclusion can be drawn by observing results of normality tests; only two stocks from Poland pass W test and only one stock from Turkey passes KS normality test. Nonnormality, extreme returns and high kurtosis are rather rule than exception when observing stock returns in emerging CSEE markets. Correlation coefficients of all stocks are very high and positive indicating existence of crisis on capital markets giving little space for diversification. This situation is characteristic for all capital markets in the region.

Table 1. Results of descriptive statistics for stocks from Croatia and their portfolio weights.

Descriptive statistics	ADGR	ATPL	НТ	DLKV	IGHZ	ERNT	ULPL	PODR	INGR	KRAS
SKEWNESS	0.317*	-0.218	0.425*	1.043*	1.131*	-0.107	-0.701^{*}	-0.074	0.803*	0.216
KURTOSIS	5.064*	5.982*	6.462*	10.44*	8.604*	2.047^{*}	13.053*	3.451*	9.753*	2.69*
Resulting portfolios										
MV, LPMM, LPM0, CVaR, MAD	0.00%	0.00%	69.16%	0.00%	0.00%	0.00%	0.00%	30.84%	0.00%	0.00%

*Denotes statistical significance at 5% level.

Table 2. Results of descriptive statistics for stocks from Poland and their portfolio weights.

Descriptive statistics	TPSA	PKN	SOBK	GTC	PGN	KGHM	РКОВР	PBG	BZW	BAPE
SKEWNESS	0.244	-0.107	0.658*	0.152	0.007	-0.553^{*}	-0.116	-0.077	0.078	0.017
KURTOSIS	1.335*	1.358*	10.034*	1.752^{*}	0.775^{*}	7.307*	1.319*	0.188	1.681*	0.831*
Resulting portfolios										
MV	57.22%	0.00%	38.59%	0.00%	4.19%	0.00%	0.00%	0.00%	0.00%	0.00%
LPMM	55.72%	0.00%	41.22%	0.00%	3.06%	0.00%	0.00%	0.00%	0.00%	0.00%
LPM0	55.30%	0.00%	41.94%	0.00%	2.75%	0.00%	0.00%	0.00%	0.00%	0.00%
CVaR	56.65%	0.00%	39.60%	0.00%	3.76%	0.00%	0.00%	0.00%	0.00%	0.00%
MAD	51.63%	0.00%	48.37%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%

*Denotes statistical significance at 5% level.

Descriptive statistics	SNPP	BRDX	ROMP	AZOM	TSEL	BATR	ALRO	ATBE	SCDB	BCCA
SKEWNESS	-0.571*	-0.228	-0.475*	0.242	0.255	-11.15*	-0.467*	-0.563*	0.195	-0.414*
KURTOSIS	5.129*	3.797*	5.625*	1.341*	3.565*	153.136*	3.742*	4.94*	4.244*	5.979*
Resulting portfolios										
MV	0.00%	0.00%	0.00%	39.18%	0.00%	0.00%	22.26%	0.00%	0.00%	38.55%
LPMM	0.00%	0.00%	0.00%	39.65%	0.00%	0.00%	24.28%	0.00%	0.00%	36.07%
LPM0	0.00%	0.00%	0.00%	39.62%	0.00%	0.00%	24.15%	0.00%	0.00%	36.24%
CVaR	0.00%	0.00%	0.00%	40.06%	0.00%	0.00%	26.07%	0.00%	0.00%	33.87%
MAD	0.00%	0.00%	0.00%	34.03%	0.00%	0.00%	0.00%	0.00%	0.00%	65.97%

Table 3. Results of descriptive statistics for stocks from Romania and their portfolio weights.

*Denotes statistical significance at 5% level.

Table 4. Results of descriptive statistics for stocks from Slovenia and their portfolio weights.

Descriptive statistics	TLSG	SAVA	MELR	HDOG	PILR	ARPO	LKPG	GORE	KRKG	PETG
SKEWNESS	0.006	0.189	0.168	-0.16	-0.026	0.413*	0.154	-0.41*	-0.321*	0.528^{*}
KURTOSIS	2.79^{*}	3.311*	8.792^*	6.189*	3.363*	4.785*	2.827^{*}	1.637*	2.514^{*}	3.528^{*}
Resulting portfolios										
MV	0.77%	0.00%	15.33%	49.22%	15.71%	0.00%	0.00%	0.00%	18.97%	0.00%
LPMM	1.59%	0.00%	12.36%	50.19%	16.72%	0.00%	0.00%	0.00%	19.14%	0.00%
LPM0	2.55%	0.00%	12.06%	51.20%	16.40%	0.00%	0.00%	0.00%	17.79%	0.00%
CVaR	0.00%	0.00%	28.69%	47.30%	2.16%	0.00%	0.00%	0.00%	21.85%	0.00%
MAD	25.39%	0.00%	0.00%	74.61%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%

*Denotes statistical significance at 5% level.

Table 5	. Results c	of descriptive	e statistics fo	r stocks from	Turkey and	their portfoli	o weights
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Descriptive statistics	TCELL	GARAN	HALK	TUPRIS	AEFES	ISCTR	YKBNK	ERGEL	SAHOL	AKBNK
SKEWNESS	0.012	0.484^{*}	0.32*	-0.259	-0.126	0.316*	-0.079	0.376*	0.379*	0.479*
KURTOSIS	2.165*	1.337*	2.514*	1.285*	1.324*	2.308^{*}	2.104*	2.010^{*}	1.620*	2.921*
Resulting portfolios										
MV	16.40%	0.00%	0.00%	37.89%	36.81%	0.00%	0.00%	6.33%	2.57%	0.00%
LPMM	15.61%	0.00%	0.00%	35.94%	37.82%	0.00%	0.00%	7.63%	3.00%	0.00%
LPM0	15.30%	0.00%	0.00%	35.47%	38.28%	0.00%	0.00%	7.32%	3.63%	0.00%
CVaR	25.55%	0.00%	0.00%	6.35%	44.52%	2.32%	1.31%	18.02%	1.93%	0.00%
MAD	0.00%	0.00%	0.00%	69.30%	30.70%	0.00%	0.00%	0.00%	0.00%	0.00%

*Denotes statistical significance at 5% level.

Observed stock returns have asymmetric distribution. Skewness coefficients are quite different between countries generally, and between stocks within every stock market. Generally, skewness coefficients are statistically significant for major part of stocks but the sign of skewness coefficients is quite different. According to **Table 3** and **Table 6** most stocks from Romania and Chez Republic have statistically significant negative skewness. Table 1 and Table 5 show that most stocks from Croatia and Turkey have positive skewness coefficient. According to Table 2, Table 4 and Table 7 most stocks from Slovenia, Poland and Hungary do not have statistically significant skewness coefficient.

Using five different risk measures portfolios on every market were formed and their CARs were calculated. Results indicate that application of standard MV model

CEZ вком UNPE PGSN TABK CETV ECMP SPTT **Descriptive statistics** ORCO AAAA SKEWNESS -0.116 -0.614^{*} -0.713* 0.224 -1.314* -3.066* -0.303 -0.1030 2 5 2 0.357* KURTOSIS 7.073* 4.996* 7.483* 5.753* 10.762* 12.543* 6 184* 36.486* 8 274* 2.35^{*} **Resulting portfolios** MV, LPMM, LPM0, CVaR, 0.00% 0.00% 0.00% 0.00% 26.67% 0.00% 0.00% 73.33% 0.00% 0.00% MAD 0.00% 0.00% 0.00% 0.00% 0.00% 0.00% 0.00% 99.89% 0.00% 0.11%

Table 6. Results of descriptive statistics for stocks from Chez Republic and their portfolio weights.

*Denotes statistical significance at 5% level.

Table 7. Results of descriptive statistics for stocks from Hungary and their portfolio weights.

Descriptive statistics	GDRB	FHBK	FOTH	EMAS	EGIS	OTPB	PANP	RABA	MTEL	MOLB
SKEWNESS	-0.788^{*}	0.868^*	1.05*	-0.363*	-0.26	0.218	0.015	-0.493^{*}	0.061	-0.027
KURTOSIS	6.432^{*}	6.178^{*}	10.694^{*}	4.062^{*}	7.818^*	6.445*	3.433*	7.443*	6.406^{*}	7.033^{*}
Resulting portfolios										
MV	53.41%	0.00%	0.00%	19.65%	0.00%	0.00%	0.00%	0.00%	26.94%	0.00%
LPMM	50.65%	0.00%	0.00%	16.66%	0.00%	0.00%	0.00%	0.00%	32.69%	0.00%
LPM0	50.83%	0.00%	0.00%	16.84%	0.00%	0.00%	0.00%	0.00%	32.33%	0.00%
CVaR	51.02%	0.00%	0.00%	17.05%	0.00%	0.00%	0.00%	0.00%	31.93%	0.00%
MAD	35.35%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	64.65%	0.00%

*Denotes statistical significance at 5% level.

is questionable when CSEE emerging markets are observed. In order to overcome the nonnormality problem downside risk measures, LPMM and LPM0 were introduced. According to results from Tables 1 to 7, MV, LPMM and LMP0 portfolios have similar composition and similar stock weights and consequentially they have similar results in the out-of-sample period. These conclusions are compatible with [6]. MAD portfolios from all 7 markets share common characteristic; MAD portfolios are composed from smaller number of assets than other portfolios. CVaR portfolios are very hard to characterize because their composition is quite different than composition of other portfolios and their out-of-sample performance is different than performance of other portfolios. If MAD portfolios and CVaR portfolios are compared, CVaR portfolios are more stable while MAD portfolios have faster drops. These results are in accordance with results of previous researches [21,22]. This can be proved by examining volatility of CVaR and MAD portfolios in the out-of-sample period measured by standard deviation of portfolio returns in Table 8. Generally, comparison of CARs in the out-of-sample period does not give answer on the best risk measure. According to results from Table 8, application of standard MV model on these markets is quite questionable. Better results are possible what can be seen in case of Turkey, Slovenia, Romania and Poland were MAD or CVaR portfolios over-perform MV, LPMM and LPM0 portfolios. These results do not have continuity. CVaR portfolio over-performs in case of Romania and gives good results in case of Slovenia. MAD portfolios have better results in case of Poland, Slovenia and Turkey but these portfolio returns are always accompanied by higher volatility in the out-of-sample period. In case of Hungary best result is achieved by application of standard MV model.

6. Conclusions

In this paper behavior of risk measures in situation of nonnormality and their impact on portfolio composition were investigated. Employed statistical methods affirmed presence of nonormality and extreme kurtosis accompanied with skewness which is statistically significant for major part of stocks. The use of downside risk measures does not give significant improvement in the portfolio performance in the out-of-sample period. Employed risk measures are not able to recognize excess kurtosis and skewness in stock returns allowing highly risky securities to enter portfolio. CARs were calculated in order to follow the performance of resulting portfolios in the out-ofsample period. According to results, CVaR portfolios have slightly more stable returns in the out-of-sample period while MAD portfolios have highest volatility. LPMM, LPM0 and variance portfolios have similar composition, volatility and out-of-sample results. Natural

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Risk measure	Portfolios expected return (%)	Expected monthly return (%)	Standard deviation of portfolio return	CAR at the end of period (%)	
Croatia					
MV, LPMM, LPM0, CVaR, MAD	-0.0021	0.0005	2.2235	-0.5130	
Poland					
MV	-0.1698	-0.1242	2.2089	-26.9950	
LPMM	-0.1686	-0.1218	2.2119	-26.7923	
LPM0	-0.1683	-0.1211	2.2131	-26.7692	
CVaR	-0.1693	-0.1233	2.2098	-27.9404	
MAD	-0.1655	-0.1152	2.2297	-26.3223	
Romania					
MV	-0.1230	-0.1480	3.0093	-24.4724	
LPMM	-0.1182	-0.1458	3.0307	-23.5257	
LPM0	-0.1185	-0.1459	3.0292	-23.5895	
CVaR	-0.1140	-0.1438	3.0531	-22.6873	
MAD	-0.1755	-0.1731	3.0527	-34.9204	
Slovenia					
MV	0.0041	0.1809	2.9196	0.3880	
LPMM	0.0026	0.1781	2.9464	0.2446	
LPM0	0.0033	0.1801	2.9698	0.3111	
CVaR	0.0335	0.2319	2.8635	3.1472	
MAD	0.0448	0.2642	3.5960	4.2149	
Turkey					
MV	0.1276	0.1307	2.8488	31.5103	
LPMM	0.1262	0.1291	2.8428	31.1751	
LPM0	0.1262	0.1289	2.8409	31.1710	
CVaR	0.1079	0.1098	2.7865	26.6409	
MAD	0.1463	0.1504	3.1612	36.1460	
Chez Republic					
MV, LPMM, LPM, CVaR	-0.0451	-0.7725	2.2258	-9.8411	
MAD	-0.0777	-0.0200	2.5121	-16.9433	
Hungary					
MV	0.1322	0.1511	2.2899	28.2907	
LPMM	0.1292	0.1469	2.2857	27.6593	
LPM0	0.1294	0.1472	2.2858	27.6985	
CVaR	0.1296	0.1475	2.2859	27.7422	
MAD	0.1128	0.1238	2.4001	24.1482	

Table 8. Performance of resulting portfolios in the out-of-sample period.

extension of this paper would be presentation of risk measure which should take into account information on skewness and kurtosis of stock returns.

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