

Focal Region Field of a Two Dimensional Gregorian System Coated with Isotropic Chiral Medium

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ABSTRACT

Focal region field of a two dimensional Gregorian system coated with chiral medium is analyzed at high frequency. Maslov's method is used because the Geometrical Optics approximation fails at focal points. Maslov's method combines the simplicity of ray theory and the generality of Fourier transform. Fields patterns are calculated numerically and the results are plotted. The effects of thickness of chiral layer, chirality parameter of the chiral medium and permittivity of the medium are analyzed. The problem of simple dielectric layer is discussed as a special case of this problem.

Keywords: Chiral Medium, Maslov, Smethod, Gregorian System, Focal Region Field

1. Introduction

The knowledge of focal region field of focusing systems is useful for synthesizing feed arrays in imaging and design of multiple beam antennas in communication systems. The focusing of electromagnetic waves into material media is also a subject of considerable current interest due to applications in hyperthermia, microscopy, and optical data storage. Geometrical optics (GO) approximation is one of the well known method for evaluating high frequency field. It has been widely used to study various kinds of problems in different areas of electromagnetics, acoustics and seismology [1-3]. GO approximation for wave solution is important in electromagnetics because it provide insight into the behavior of wave front. GO is used only for high frequency approximation of a wave, provided the ray tube does not vanish. However, at caustic regions the ray tube shrinks to zero and GO show singularity at these regions. These regions are of great importance in all practical problems e.g. parabolic, paraboloidal and circular reflectors etc. To avoid these singularities Maslov proposed a method based on Maslov's theory [4,5]. Maslov's method has been used to find the field at caustic regions [6-20]. The idea in Maslov's method provides a systematic procedure for predicting the field in the caustic region by combining the simplicity of ray theory and generality of the transform method. High frequency field expressions has been derived around feed point of a two dimensional Gregorian system using the Maslov's method in [19]. The same focussing system has been coated with isotropic and homogeneous chiral medium and field expressions are obtained. In Section 2 the plane wave reflection from a chiral slab backed by perfect electric conducting (PEC) plane is considered. In Section 3 high frequency expression for the field of a chiral coated Gregorian system excited by plane wave is derived. Numerical results and discussion are presented in Section 4 and the paper is concluded in Section 5.

2. Reflection of Plane Waves From a Chiral Slab Backed by Conductor

In this paper we want to find the reflected field around the focal region of a two dimensional Gregorian's main parabolic reflector coated with chiral medium. To achieve this the reflection of plane waves from a chiral slab backed by perfect electric conducting (PEC) plane is discussed as in [15,21]. As shown in **Figure 1** the region $z \le 0$ is occupied by free space defined by following equations

$$D = \varepsilon_{\scriptscriptstyle 0} E$$

$$B = \mu_{o}H$$

and the region $0 \le z \le d$ is occupied by the chiral medium defined by Drude-Born-Fadorov (DBF) constitutive

relations [21] as follows

$$D = \varepsilon (E + \beta \nabla \times E)$$

$$B = \mu(H + \beta \nabla \times H)$$

The PEC is placed at z = d as shown in **Figure 1**. The reflection coefficients for the parallel and perpendicular components of polarization is calculated in [11]

$$\begin{bmatrix} B_{\perp}B_{\parallel} \end{bmatrix} = \left(\begin{bmatrix} r \end{bmatrix} + \begin{bmatrix} T \end{bmatrix} \left(\begin{bmatrix} \Delta \end{bmatrix} \begin{bmatrix} R_{3} \end{bmatrix} \Delta \right) - \begin{bmatrix} R \end{bmatrix} \right)^{-1} \begin{bmatrix} t \end{bmatrix} \left(A_{\perp}A_{\parallel} \right)$$
 (1)

In the above equation, A_{\perp} , A_{\parallel} and B_{\perp} , B_{\parallel} are the parallel and perpendicular components of polarization of the incident and reflected fields respectively. [r], [T], [R] and [t] are 2×2 matrices. Elements of the matrices, which are Fresnel coefficients, are given in [15]. Δ and R_{3} are also 2×2 matrices and are given in [15]. Using these reflection coefficients, the focal region fields of a two dimensional Gregorian's system are derived.

3. Focal Region Field of Two Dimensional Gregorian Reflector

Gregorian system consists of two reflectors, one is parabolic main reflector and another is hyperbolic sub-reflector as shown in **Figure 2**. This system has several advantages over a single parabolic reflector. In this paper we want to study the caustic region field of a two dimensional Gregorian system when the main reflector is coated with chiral medium using GO and Maslov's method. The equations of each reflector are given as follows

$$\zeta_{1} = \frac{\xi_{1}^{2}}{4f} - f + c, \ \zeta_{2} = a \left[\frac{1 - \xi_{2}^{2}}{b^{2}} \right]^{\frac{1}{2}} c^{2} = a^{2} + b^{2}$$

$$aR_{2} = c\zeta_{2} - a^{2}, \qquad aR_{1} = c\zeta_{2} + a^{2}$$
(2)

In the above relations (ξ_1, ζ_1) and (ξ_2, ζ_2) are the Cartesian coordinates of the point on the parabolic and elliptical reflectors, respectively. The Incident wave traveling along the negative z-axis is given by

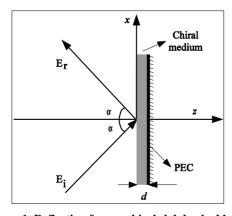


Figure 1. Reflection from a chiral slab backed by PEC

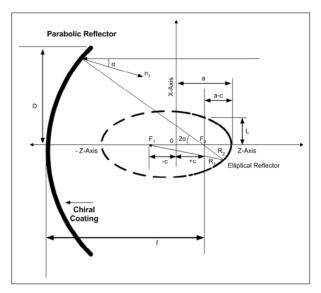


Figure 2. Gregorian antenna coated with chiral medium

$$E^{i} = (A_{x}i_{y} + A_{x}i_{x}) \exp(jkz)$$
 (3)

where, A_y , A_x are the components along y-axis and x-axis of the initial amplitude of the incident field respectively. The wave reflected from the hyperboloidal surface is given by

$$E^{r} = [B_{\perp}i_{y} + B_{\parallel}\{-\sin(2\alpha - 2\psi)i_{x} - \cos(2\alpha - 2\psi)i_{z}\}]$$

$$\times \exp[-jkz\{\sin(2\alpha - 2\psi)i_{x} + \cos(2\alpha - 2\psi)i_{z}\}]$$
(4)

The wave vector of the wave reflected by the parabolic reflector is given by

$$p_i^r = -\sin 2\alpha i_i + \cos 2\alpha i_i \tag{5}$$

and the wave vector of the wave reflected by the hyperbolic reflector is

$$p_{\alpha}^{r} = -\sin(2\alpha - 2\psi)i_{\alpha} - \cos(2\alpha - 2\psi)i_{\alpha}$$
 (6)

where, the angle α and angle ψ are given by the relation

$$\sin \alpha = \frac{\xi_1}{\sqrt{\xi_1^2 + 4f^2}}, \cos \alpha = \frac{2f}{\sqrt{\xi_1^2 + 4f^2}}$$

$$\sin \psi = -\frac{1}{\sqrt{R_1 R_2}} \frac{a}{b} \, \xi_2, \cos \psi = \frac{1}{\sqrt{R_1 R_2}} \frac{b}{a} \, \zeta_2$$

In the above equations R_1 and R_2 are the distances from the point (ξ_2, ζ_2) to the focal points z=-c and z=c, respectively. The unit normal vectors to the parabolic and hyperbolic surfaces are given by n_1 and n_2 respectively. These normals can be written as

$$n_1 = -\sin \alpha i_1 + \cos \alpha i_2, n_2 = -\sin \psi i_1 + \cos \psi i_2$$

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The general form of the geometrical optics solution for the wave is given by [19]

$$E(r) = E_{0} \left\{ \frac{D(\tau)}{D(0)} \right\}^{\frac{1}{2}} \exp\{-jk_{0}(S_{0} + \tau)$$
 (7)

The Jacobian associated with the wave reflected by the parabolic reflector is given by [19]

$$J(\tau) = \frac{D(\tau)}{D(0)} = 1 - \frac{\cos^2 \alpha}{f} \tau \tag{8}$$

The Cartesian coordinates of the ray reflected by the hyperbolic surface is given by

$$x = \xi_2 + p_{x2}\tau = \xi_1 + p_{x1}\tau_1 + p_{x2}\tau \tag{9}$$

$$z = \zeta_2 + p_{zz}\tau = \zeta_1 + p_{z1}\tau_1 + p_{zz}\tau \tag{10}$$

where, $\tau_1 = \sqrt{(\xi_1 - \xi_2)^2 + (\zeta_1 - \zeta_2)^2}$. In the above equation (p_{x_1}, p_{z_1}) and (p_{x_2}, p_{z_2}) are the rectangular components of reflected wave vectors p_r^1 and p_r^2 , respectively. Now we consider the field after the reflection from the hyperbolic cylinder. The transformation from the Cartesian coordinates (x, z) to the ray coordinates (ξ_1, τ) is given by [19]

$$D(\tau) = \frac{\cos^2 \alpha}{f} R_2 \left[1 - \frac{\tau}{R_1} \right] \tag{11}$$

Thus the geometrical ray expression of each component of the reflected wave is

$$E_{x}' = -\cos(2\alpha - 2\psi)B_{\parallel}\left[1 - \frac{\tau}{R_{\perp}}\right]^{-\frac{1}{2}} \exp\left[-jk\left(S_{0} + \tau_{1} + \tau\right)\right]$$

(12)

$$E_{y}' = B_{\perp} \left[1 - \frac{\tau}{R_{1}} \right]^{\frac{1}{2}} \exp \left[-jk \left(S_{0} + \tau_{1} + \tau \right) \right]$$
 (13)

$$E_{z}^{r} = -\sin(2\alpha - 2\psi)B_{\parallel} \left[1 - \frac{\tau}{R_{\perp}}\right]^{\frac{1}{2}} \exp\left[-jk(S_{0} + \tau_{1} + \tau)\right]$$
(14)

where, E_0^r is the amplitude of the incident wave at the reflection point on the parabolic surface and

$$S_{_{0}} = -\zeta_{_{1}} = 2f \frac{\cos 2\alpha}{1 + \cos 2\alpha} - c \tag{15}$$

$$\tau_{1} = \sqrt{(\xi_{2} - \xi_{1})^{2} + (\zeta_{2} - \zeta_{1})^{2}}$$
 (16)

$$\tau = \sqrt{(x - \xi_2)^2 + (z - \zeta_2)^2}$$
 (17)

As indicated by (7), E(r) will become infinite for

 $\frac{D(\tau)}{D(0)} = 0$ i.e. at the caustic points. The expression

which is valid at the focal point according to Maslov's method is given by [19]

$$E(r) = \sqrt{\frac{k_0}{j2\pi}} \int_{-\infty}^{\infty} A_0(\xi) \left[J(\tau) \frac{\partial p_z}{\partial z} \right]$$

$$\times \exp\{-jk_0[S_0 + \tau - (x, p_z)p_z + zp_z]\}$$
(18)

The amplitude term $\left[J(\tau)\frac{\partial p_{zz}}{\partial z}\right]^{\frac{1}{2}}$ in the above equation is given by [19]

$$\left[J(\tau)\frac{\partial p_{zz}}{\partial z}\right]^{\frac{1}{2}} = \frac{\sqrt{R_{i}}}{\sin(2\alpha - 2\psi)}$$
 (19)

The phase function is given by

$$S = S_0 + \tau_1 + \tau - z(x, p_n)p_n + p_n z \tag{20}$$

where, $S_0 + \tau_1$ is given by (15). The extra term is given by

$$S_{xx} = \tau - z(x, p_{z_2})p_{z_2} + p_{z_2}z$$

$$= \tau - (\zeta_2 + p_{z_2}\tau)p_{z_2} + p_{z_2}$$

$$= (p_{x_2})^2 \tau + (z - \zeta_2)p_{z_2}$$

$$= p_{x_2}(x - \xi_2) + (z - \zeta_2)p_{z_2}$$

$$= -\rho \cos(2\alpha - 2\psi - \phi)$$

$$+ \left[\sin(2\alpha - 2\psi)\xi_1 + \cos(2\alpha - 2\psi)\xi_2\right]$$

We substitute (19)-(20) into (18) and taking $A_{\circ}(\xi) = 1$, we can find the finite field around the caustic as given below

$$E_{x}^{r} = \sqrt{\frac{k}{j2\pi}} \left[\int_{A_{1}}^{A_{2}} + \int_{-A_{2}}^{-A_{1}} \left| \cos(2\alpha - 2\psi) B_{\parallel} \sqrt{R_{1}} \right| \right] \times \exp\left[-jk(S_{0} + \tau_{1} + S_{\alpha}) d(2\alpha)$$
(21)

$$E_{y}^{r} = \sqrt{\frac{k}{j2\pi}} \left[\int_{A_{1}}^{A_{2}} + \int_{-A_{2}}^{-A_{1}} B_{\perp} \sqrt{R_{1}} \right] \times \exp\left[-jk(S_{0} + \tau_{1} + S_{-}) d(2\alpha) \right]$$
(22)

$$E_{z}^{r} = \sqrt{\frac{k}{j2\pi}} \left[\int_{A_{1}}^{A_{2}} + \int_{-A_{2}}^{-A_{1}} \sin(2\alpha - 2\psi) B_{1} \sqrt{R_{1}} \right] \times \exp\left[-jk(S_{0} + \tau_{1} + S_{m}) d(2\alpha) \right]$$
(23)

In the above equation, R_1 , S_0 , τ_1 and S_{ex} are expressed in terms of α and A_1 and A_2 are the subtention angles 2α at the edges of the parabolic and hyperbolic surfaces. The limit of integration are calculated by the expression

$$A_1 = 2 \arctan\left(\frac{D}{2f}\right), A_2 = \arctan\left(\frac{L}{2c}\right)$$

4. Result and Discussion

Field pattern around the caustic region of a Gregorian system are determined using (21-23) by performing the integration numerically. The line plots of the field around the focal region located between the two reflectors, that point \mathbf{F}_2 in **Figure 2**. Simulation were done for $A_1 = \pi/4.1$, $A_2 = \pi/6.5$, $k_0 = 1$, f = 100, $\mu = \mu_0$ and different values of $\varepsilon = \varepsilon/\varepsilon_0$, d, and β . We have considered two types of polarization for incident wave. One is $(A_x = 0, A_y = 1)$ and the other is $(A_x = 1, A_y = 0)$. The results are plotted in **Figures 3-20**. In all figures horizontal axis is z-axis and vertical axis corresponds to the absolute value of reflected field component. All plots are taken at x = 0. We have studied the effects of thickness of the the coated layer (d), the chirality parameter (β) and the relative permittivity of the me-

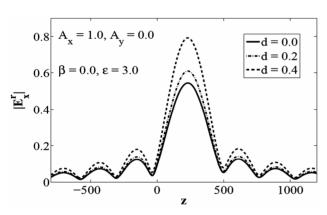


Figure 3. Plot of $/E_x^r/$, when parabolic reflector is coated with dielectric layer of varying thickness d

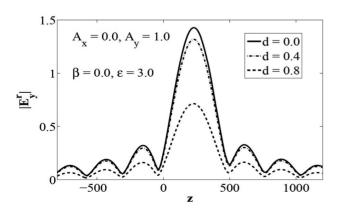


Figure 4. Plot of $\mid E_y^r \mid$, when parabolic reflector is coated with dielectric layer of varying thickness d

dium (ε) on the focal region field. **Figures 3-5** show the effect of increase in the value of d keeping $\beta = 0$ and $\varepsilon = 3$, that is ordinary dielectric case. We have shown in **Figure 3** and 5the $|E_i^r|$ and $|E_i^r|$ for $(A_{x} = 1, A_{y} = 0)$. These figures show that increase in thickness of the coated layer (d) results an increase in $|E^r|$ and $|E^r|$. **Figure 4** shows the plot of $|E^r|$ for $(A_{x} = 0, A_{y} = 1)$. This figure shows decrease in field strength as d increases. Figures 6-11 show the effect of d while keeping $\beta = 0.5$ and $\varepsilon = 1$ for both types of polarization. Figures 7 and 11 show increase in the field strength of $|E_i|$ and $|E_i|$ for $(A_{\omega} = 1, A_{\omega} = 0)$, respectively. **Figure 6** and **10** show the cross polarization effect due to chiral medium for polarization $(A_{i} = 0, A_{i} = 1)$, which also increases with increase in d. For d = 0, cross polarization effect vanishes and field strength increases with increase in d. **Figure 8** shows the plot of $|E_y'|$ for $(A_x = 0, A_y = 1)$, which decreases with increase in d, and Figure 9

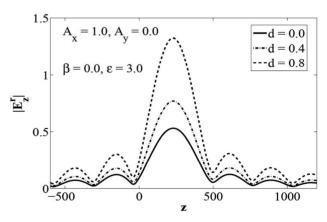


Figure 5. Plot of $|E_{\varepsilon}^r|$, when parabolic reflector is coated with dielectric layer of varying thickness d

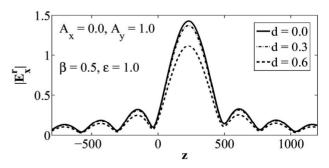


Figure 6. Plot of $|E_x'|$, when the thickness of the coated layer d is varying. The impedance of chiral medium is equal to that of free space

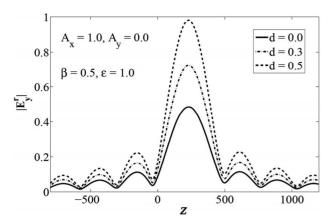


Figure 7. Plot of $|E_x^r|$, when the thickness of the coated layer d is varying. The impedance of chiral medium is equal to that of free space

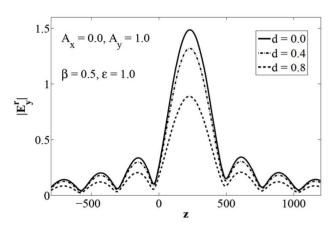


Figure 8. Plot of $|E_y'|$, when the thickness of the coated layer d is varying. The impedance of chiral medium is equal to that of free space

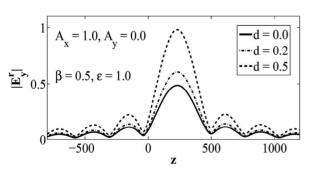


Figure 9. Plot of $|E_y^r|$, when the thickness of the coated layer d is varying. The impedance of chiral medium is equal to that of free space

shows the plot for $(A_x = 1, A_y = 0)$. This figure shows that cross polarization effect are zero for d = 0, but increases with increase in layer thickness d.

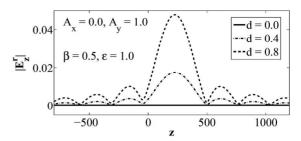


Figure 10. Plot of $|E_z^r|$, when the thickness of the coated layer d is varying. The impedance of chiral medium is equal to that of free space

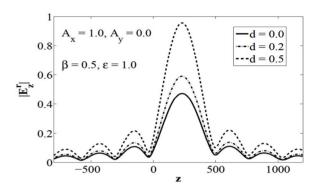


Figure 11. Plot of $|E_z^r|$, when the thickness of the coated layer d is varying. The impedance of chiral medium is equal to that of free space

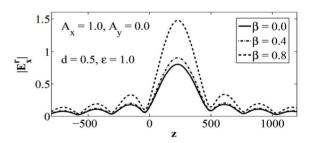


Figure 12. Plot of $|E_x^r|$ showing the effect of chirality parameter β . The impedance of chiral medium is equal to that of free space

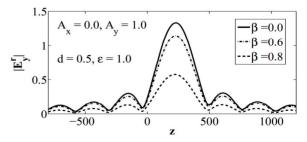


Figure 13. Plot of $|E_y^r|$ showing the effect of chirality parameter β . The impedance of chiral medium is equal to that of free space

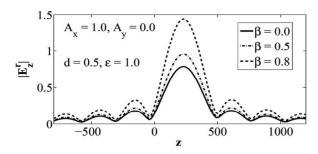


Figure 14. Plot of $|E_z^r|$ showing the effect of chirality parameter β . The impedance of chiral medium is equal to that of free space

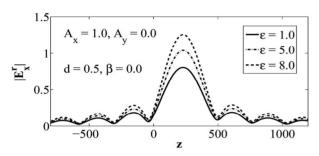


Figure 15. Plot of $|E'_x|$ showing the effect of relative permittivity ε of dielectric layer

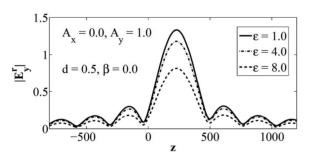


Figure 16. Plot of $|E_y^r|$ showing the effect of relative permittivity ε of dielectric layer

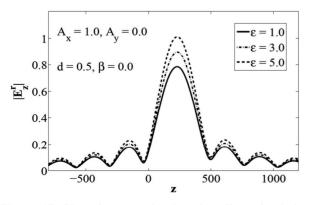


Figure 17. Plot of $|E'_z|$ showing the effect of relative permittivity ε of dielectric layer

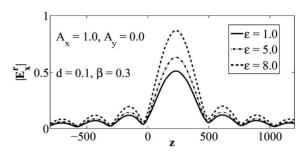


Figure 18. Plot of $|E'_x|$ showing the effect of relative permittivity ε of chiral layer

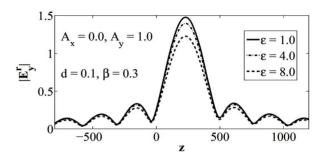


Figure 19. Plot of $|E'_j|$ showing the effect of relative permittivity ε of chiral layer

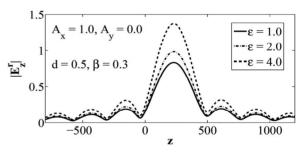


Figure 20. Plot of $|E_z^r|$ showing the effect of relative permittivity ε of chiral layer

Figures 12 and **14** show the effect of chirality parameter β on field components while keeping $\varepsilon=1$ and d=0.5. **Figures 12** and **14** show the plots of $|E_x^r|$ and $|E_z^r|$ for $(A_x=1,A_y=0)$ respectively. These figures show that field strength increases with increase in chirality parameter β . **Figure 13** shows that $|E_y^r|$ decreases with increase in β . Cross polarization effects have not been shown because they have same trends as discussed above. **Figures 15-17** show the effect of ε while keeping d=0.5 and $\beta=0$, that is for ordinary dielectric case. **Figures 15** and **17** show the plot of $|E_x^r|$ and $|E_z^r|$ for polarization $(A_x=1,A_y=0)$ respectively and show the increase in the field strength if

we increase the relative permittivity of dielectric medium coated on the surface of reflector. **Figure 16** shows that $|E_y^r|$ decreases with increase in ε for polarization $(A_x = 0, A_y = 1)$. **Figures 18-20**, which are for chiral coating, show the same trends as in **Figures 15-17**.

5. Conclusions

Focal region fields of a two dimensional Gregorian reflector is analyzed using GO and Maslov's method. Two types of polarization are discussed. The reflected field components are analyzed numerically and the results are given in the focal plane. It is concluded that increase in chirality parameter (β), increase in thickness (d) and relative permittivity (ε), results in increase in of $|E_x^r|$ and $|E_z^r|$ for $(A_x=1,A_y=0)$. While $|E_y^r|$ decreases for $(A_x=0,A_y=1)$. Cross polarized fields exist when $k\beta \neq 0$ and increase with increase in value of d.

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