

Clustering-Inverse: A Generalized Model for Pattern-Based Time Series Segmentation*

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Received November 4th, 2010; revised January 5th, 2011; accepted January 19th, 2011

ABSTRACT

Patterned-based time series segmentation (PTSS) is an important task for many time series data mining applications. In this paper, according to the characteristics of PTSS, a generalized model is proposed for PTSS. First, a new interpretation for PTSS is given by comparing this problem with the prototype-based clustering (PC). Then, a novel model, called clustering-inverse model (CI-model), is presented. Finally, two algorithms are presented to implement this model. Our experimental results on artificial and real-world time series demonstrate that the proposed algorithms are quite effective.

Keywords: *Pattern-Based Time Series Segmentation, Clustering-Inverse, Dynamic Time Warping, Perceptually Important Points, Evolution Computation, Particle Swarm Optimization, Genetic Algorithm*

1. Introduction

With the large amounts of time series data arising from various fields in recent years, the time series data mining has emerged as an important research topic in the field of data mining [1-3]. Especially, as one of the most fundamental tasks in time series data mining, the time series segmentation has attracted extensive attention [4,5].

The conventional time series segmentation algorithms can be classified into the following two main categories [6]. The aim of the first category is to create a high level representation of the time series for indexing, clustering, and classification [7,8] and the aim of the second category is to identify switching dynamics in time series [9,10].

In addition to these two main categories of algorithms mentioned above, a kind of novel pattern-based time series segmentation algorithm (PTSS) in [11] and its improved versions [7,8] were developed to segment financial time series. The distinctive characteristic of PTSS is that a pattern time series set (*i.e.* a pattern template set) is given to control the segmentation. In the pattern time

series set, a pattern time series also represents a technique template, which indicates a representative time series segment in a time series. For different practical applications, the corresponding technique templates usually represent the special meaning. The aim of PTSS is to obtain the time series segments which are similar to a certain pattern template in the given pattern time series set. In this paper, we mainly focus on the study of PTSS.

In this study, by comparing PTSS with the prototype-based clustering (PC), we find that PTSS may be interpreted as an inverse problem of PC. According to this interpretation, a generalized model, called Clustering-Inverse model (CI-model), is proposed for PTSS. Then, the main components and processing operations of this model are discussed in detail. Furthermore, a detailed algorithm is presented to put this model into practice. As the matching measure of time series is of fundamental importance in segmentation, we also propose a new Perceptually Important Point (PIP) based Dynamic Time Warping (DTW) measure by integrating PIP identification mechanism [12] with DTW measure [13]. The advantage of the proposed measure is that it combines the merits of both PIP mechanism and DTW simultaneously. To investigate the performance of the proposed CI-model, we have applied the proposed algorithms to the real-world time series.

*This study was supported in part by the Hong Kong Polytechnic University under Grant Z-08R, by the National Natural Science Foundation of China under Grants 60773206, 60903100, 60975027 and 90820002, by the Natural Science Foundation of Jiangsu province under Grant BK2009067 and the Doctoral Foundation of Jiangnan University.

The contributions of this study can be summarized into the following four aspects:

- Give a new interpretation for PTSS;
- Propose a generalized CI-model for PTSS;
- Propose a PIP-based DTW measure;
- Present an algorithm based on the CI-model.

The paper is organized as follows. In section 2, a formal description and a new interpretation of PTSS are given. The proposed CI-model is introduced and its main components and processing operations are discussed in section 3. Section 4 presents a detailed algorithm to realize the proposed model. Experimental results are reported in Section 5. The conclusions and some prospects are given in section 6.

2. Description and New Interpretation about PTSS

2.1. Description about PTSS

First, we give a formal description of PTSS (Pattern based Time Series Segmentation). Given a time series $T = (t_1 t_2 \cdots t_n)$ and a set of pattern time series, or pattern templates, $D_p = \{P_i | P_i = (p_1 p_2 \cdots p_{m_i}), i = 1, 2, \dots, c\}$, where m_i, n denote the lengths of P_i and T , respectively. The aim of PTSS is to segment T into a set of k time series segments,

$$D_s = \{S_i | S_i = t_{b_i} t_{b_i+1} \cdots t_{e_i}, i = 1, \dots, k\}.$$

In the set D_s , each time series segment is similar to one of the pattern template in D_p , and meanwhile, the set D_s must satisfy the constraint: $T = S_1 S_2 \cdots S_k$, where b_i is the beginning position of S_i in T , $b_1 = 1$ and e_i is the ending position of S_i in T , $e_k = n$.

The obtained time series segments S_i from time series T by PTSS may have different lengths and can be classified into different subgroups, which are associated with the corresponding pattern templates. Therefore, D_s may be described as $D_s = D_{p_1} + D_{p_2} + \cdots + D_{p_c}$, where

$$D_{p_j} = \{S_i | \text{sim}(S_i, P_j) = \max_{h=1,2,\dots,c} \text{sim}(S_i, P_h)\};$$

$i = 1, 2, \dots, k$; $j = 1, 2, \dots, c$; $\text{sim}(\cdot)$ denotes a similarity measure between two time series.

2.2. New Interpretation about PTSS

In this subsection, we will discuss the relationship between PTSS and the prototype-based clustering (PC), and then give a new interpretation for PTSS. PC can be expressed as the following problem: Given a dataset D and the number c of its clusters, the aim of PC is to get c optimal prototypes V_i (e.g., cluster centers), $i = 1, \dots, c$. The sample points associated with the same prototype are as compact as possible while the sample

points associated with different prototypes are as scattered through the data space as possible. **Figure 1(a)** shows a simple illustration for PC. Correspondingly, we also give an illustration for PTSS in **Figure 1(b)**.

By comparing **Figure 1(a)** with **Figure 1(b)**, it is easy to find that the pattern template P_i in **Figure 1(b)** can be interpreted as a prototype V_i in **Figure 1(a)**. Meanwhile, the set of time series segments D_s in **Figure 1(b)** can be interpreted as the dataset D in **Figure 1(a)**. The essential difference between PC and PTSS lies in the fact that given the dataset D , the aim of PC is to get the optimal prototypes V_i in PC by optimization learning, while given the prototypes P_i , the aim of PTSS is to obtain the optimal dataset D_s . Hence, we can give the following interpretation: PTSS can be viewed as an inverse problem of PC and here we call it the clustering-inverse problem.

3. Clustering-Inverse: A Generalized Model for PTSS

3.1. The Framework of the Proposed Model: Clustering-Inverse

In terms of the interpretation in the above section, a generalized model, called clustering-inverse model (CI-model), is proposed for PTSS. The framework of the proposed model is shown in **Figure 2**.

In **Figure 2**, T denotes the time series to be segmented. The pattern time series set D_p is the pattern template set used as the constraints for the time series segmentation. The initialization operation is to present the initial segmentation point set which contains s segmentation points segmenting T into k time series segments with $k = s + 1$. The data processing operation in **Figure 2** is utilized to process the time series segment set D_s and the pattern time series set D_p . With a data processing operation, D_s and D_p can be transformed into the corresponding datasets D'_s and D'_p , which are usually more suitable for computing the matching measures between the pattern templates and the obtained

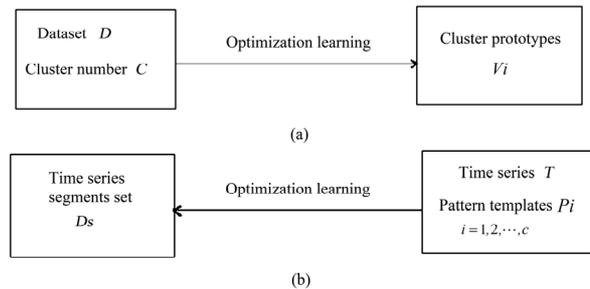


Figure 1. The illustrations of (a) the prototype-based clustering PC and (b) the pattern-based time series segmentation PTSS.

possible schemes to implement the proposed CI-model. Note here that the objective functions in (1), (2) and (6) are expected to achieve the minimum values, while the objective functions in (4) is expected to achieve the maximum value.

3.2.2. Optimization Method

In the proposed CI-model, the objective function is just the clustering objective function and the solution is the segmentation point set $D_{seg_point} = \{q_1, q_2, \dots, q_s\}$, which can be equivalently written as a vector

$\mathbf{q} = (q_1, q_2, \dots, q_s)$, where $q_{i-1} < q_i$ ($i = 1, 2, \dots, s-1$), $q_1 > 1$, $q_s < n$; and n is the length of time series T . Since the objective function usually can not be written as an analytic expression of the solution $\mathbf{q} = (q_1, q_2, \dots, q_s)$ directly, the traditional gradient optimization methods and some other commonly used derivative-based optimization methods are not suitable for this problem. Under these conditions, the following optimization methods can be considered.

1) Dynamic programming. It is the earliest technique utilized to solve the traditional time series segmentation problem [7]. A crucial step for dynamic programming methods is to transform the optimization problem into its corresponding dynamic programming equation. The weakness of this kind of method for time series segmentation is the high computational complexity. Meanwhile, it is not a trivial problem to transform the optimization process into its corresponding dynamic programming.

2) Random optimization. It is a simple method for the time series segmentation [17]. This method first gives an initial segmentation. Then, in the whole learning procedure, the following operation is repeated: a segmentation point is selected randomly to be replaced with an optimal point obtained by trying all other potential segmentation points. So the computational complexity is also quite high like the dynamic programming method.

3) Evolutionary optimization. Evolutionary optimization methods have been extensively studied and utilized in various fields in recent years and their applications in time series segmentation has been demonstrated in [11,12]. Compared with the above two optimization methods, the advantages of evolutionary optimization methods are their easy use and high intelligence. Due to the advantages of evolutionary optimization methods, in the following algorithms presented to implement the proposed CI-model, this kind of optimization methods is adopted.

3.2.3. Data Processing

Data processing is an important operation: 1) to transform the time series segments and pattern time series into easily processed data vectors; 2) to facilitate computing the matching measures between the obtained time series

segments and the pattern time series. For example, the transformation of the obtained time series segments and the pattern time series into the corresponding vectors with the same dimensional number will facilitate computing their matching measure using Euclidean distances; 3) to effectively reduce the computational complexity of matching measures. For example, the commonly used DTW measure for time series matching needs to solve a dynamic programming problem. With the increase of time series length, the computation time of DTW measure will become very burdensome. Thereby, the data processing is needed to improve the efficiency of DTW measure.

In this study, to realize the above functions we introduce the PIP (Perceptually Important Point) identification mechanism [11,12] as a data processing operation in CI. The PIP mechanism is to identify some perceptually important points in time series to represent the time series. Thus the computational complexity is greatly decreased because the number of PIPs is far smaller than the length of time series. Now we give a brief introduction to the PIP mechanism.

The idea of PIP identification is motivated by the fact that a time series can be usually characterized by a few important points. For example, the head-and-shoulder pattern time series consists of a head point, two shoulder points, and a pair of neck points. These points are perceptually important in the human visual identification process. Therefore, they can similarly be taken into account in the pattern matching process. Given a time series $X = (x_1, x_2, \dots, x_n)$, its m PIPs can be obtained by the following process. The first two PIPs that are found will be the first and last points of X . The next PIP will be the point in X with the maximum distance to the first two PIPs. The fourth PIP will then be the point in X with maximum distance to its two adjacent PIPs, either between the first and second PIPs or between the second and the last PIPs. The process of locating the PIPs continues until the number is equal to m . **Figure 3** shows the process of identifying 7 PIPs from the head-and-shoulder pattern time series with length $n = 60$.

3.2.4. Matching Measure

The matching measure of times series is of fundamental importance in time series data mining. The most commonly used measures are Euclidean distance and DTW measure [13]. In [11,12] the PIP-based Euclidean distance was proposed, which revealed much better performance in reducing the running time. Here, we first briefly introduce the three matching measures, and then propose a PIP-based DTW measure for time series matching. Our purpose is to present a measure which can

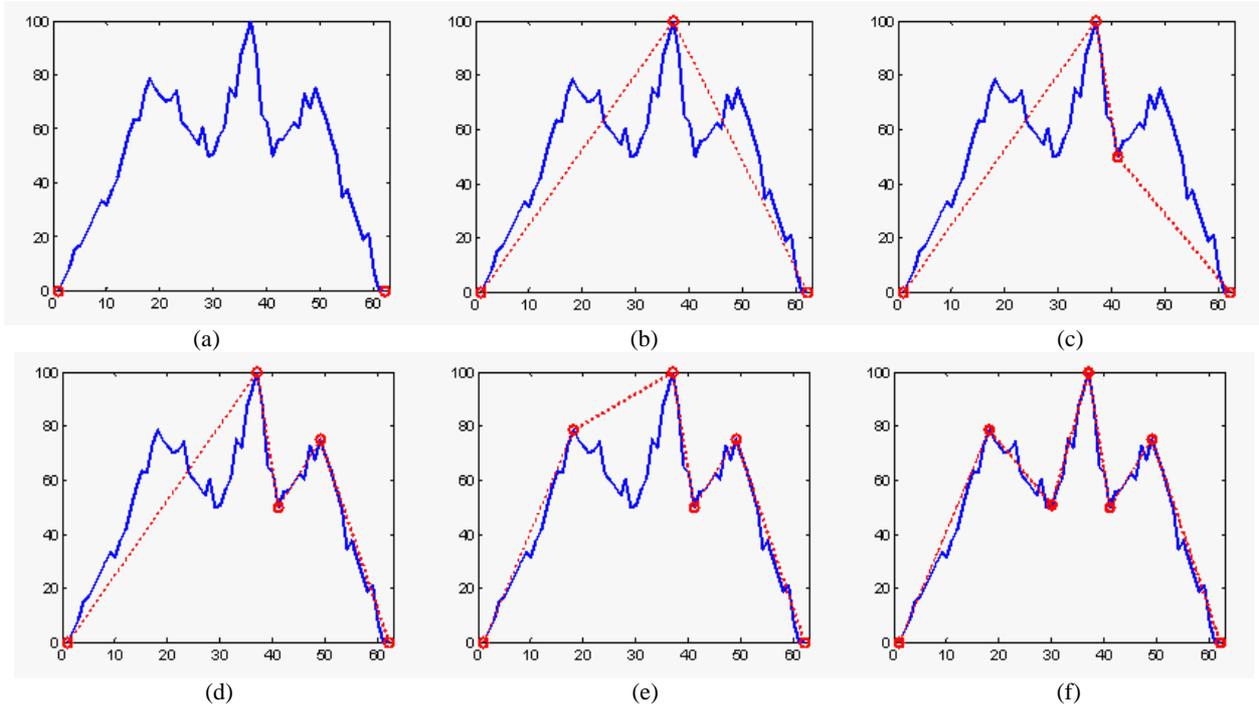


Figure 3. Identification of seven PIPs from the head-and-shoulder pattern time series.

simultaneously take advantage of these merits.

Euclidean distance: Given two time series $X = (x_1, x_2, \dots, x_n)$ and $Y = (y_1, y_2, \dots, y_n)$, which have the same length, the Euclidean distance of these two timeseries can be expressed as

$$D_2(X, Y) = \sqrt{\sum_{i=1}^n (x_i - y_i)^2} \quad (8)$$

The Euclidean distance measure has been extensively used in time series data mining. However, there is an increasing awareness that it is a much brittle measure in time series data mining [18].

DTW measure: To overcome the weakness of Euclidean distance, Berndt and Clifford introduced the Dynamic Time Warping (DTW) measure in the database community [13]. DTW measure enables matching similar time series with different lengths.

PIP-based Euclidean distance: A PIP-based Euclidean distance is presented in [11]. For two time series $X = (x_1, x_2, \dots, x_n)$, $Y = (y_1, y_2, \dots, y_m)$, assuming Y is a pattern time series, the PIP-based Euclidean distance between X and Y , D_{pip} , can be formulated as

$$D_{pip}(X, Y) = D_2(X_p, Y) = \sqrt{\sum_{h=1}^m (x_{p_h} - y_h)^2} \quad (9)$$

where $X_p = (x_{p_1}, \dots, x_{p_m})$ denotes the new time series containing m PIPs of time series X .

PIP-based DTW measure: Compared with Euclidean distance, the DTW measure has its distinctive advantages, such as robustness, elasticity. However, the DTW meas-

ure has an obvious weakness of high computational complexity. To reduce this weakness, a new modified DTW measure, named as PIP-based DTW measure, D_{pdt} , is introduced. This measure can be formulated as

$$D_{pdt}(X, Y) = D_{dtw}(X_p, Y_p) \quad (10)$$

where X_p and Y_p are two new time series which are composed of the obtained PIPs from X and Y , respectively. In this new measure, two adjustable parameters, r_1 and r_2 , are introduced to control the number of desired PIPs, where $m' = r_1 m$, $n' = r_2 m'$. Here, m, n are the lengths of X and Y , respectively; and m', n' are the lengths of X_p and Y_p respectively. The ranges of r_1 and r_2 are dependent on the time series to be segmented. For the time series that changes slowly, we can set much smaller values for r_1 and r_2 . When the time series changes quickly, the r_1 and r_2 should be much larger in order to maintain the segmentation performance.

In our experiments, we find that to set $0.5 \leq r_1 \leq 1$, $1 \leq r_2 \leq 1.5$ is appropriate in many cases.

3.2.5 Initialization

With different initializations, the obtained clustering prototypes in PC may be different. Likewise, the solutions of PTSS will be influenced by the initialization. Here two heuristic initialization strategies are proposed for the proposed CI-model.

- 1) Initialization for a desired solution with prior

knowledge. With his knowledge, the user can specify the approximate length $dlen$ of the desired times series segments. For example, given a stock index time series with length $l = 3000$ taken from the daily closing price, if the user wants to get the segments about a month period or three-month period, he sets $dlen = 30$ and $dlen = 90$, respectively. Correspondingly, $s = \lceil l/dlen \rceil - 1$ segmentation points can be initialized with the interval $dlen * r$, where $\lceil x \rceil$ denotes the minimal integer which is bigger than x and r is a random number to control the initial interval between the adjacent segmentation points. To set $r \in [0.75, 1.25]$ is appropriate for most cases.

2) Initialization evaluated by a specific performance index. In some cases, little information can be used to set $dlen$ for initializing the segmentation points. In this situation, we suggest to segment the time series by setting different values of $dlen$, such as setting $dlen = 100$, $dlen = 200$, and so on. Then, the appropriate initialization can be determined by a specific performance index as the criterion.

4. CI-Model Based PTSS Algorithm

4.1. General CI-Model Based PTSS Algorithm

In this subsection, the general CI-model based algorithm for PTSS is presented in **Table 1**. Evolutionary optimization methods have their distinctive advantages, such as much better global search ability. Among various evolutionary optimization methods, Particle Swarm Optimization (PSO) [20] is one of the most extensively studied methods. In the following subsection, we will present such a CI-model based PTSS algorithm using PSO.

4.2. PTSS Algorithm Based on CI-Model + SPSO

In this subsection, we introduce the PSO (Particle Swarm Optimization) for CI-model to implement the PTSS. The PSO is a population-based optimization method. The PSO is motivated by the behavior of organisms such as fishing schooling and bird flock. In a PSO system, each individual is taken as a particle and a particle is taken as a candidate solution to the problem at hand. Particles of the population fly around in a multi-dimensional search space, to find out an optimal or sub-optimal solution by competition as well as by cooperation among them.

For simplicity, here, we directly use the well-known Stand Particle Swarm Optimization (SPSO) as the optimization method for CI model. First, we describe the related important conceptions and search strategies of SPSO. Then, a PTSS algorithm based on CI-model + SPSO is presented.

4.2.1. Conceptions about SPSO

In SPSO, the population contains M particles and the

i th particle can be described by two state variables: the position vector $\mathbf{x}_i = (x_{i1}, x_{i2}, \dots, x_{is})$ and the velocity vector $\mathbf{v}_i = (v_i, v_i, \dots, v_s)$. For the PTSS, the segmentation vector $\mathbf{q}_i = (q_{i1}, q_{i2}, \dots, q_{is})$ of the time series T can be taken as the position variable of the i th particle. The velocity variable \mathbf{v}_i of the i th particle is usually initialized to be zero vector. In addition to these two state variables of the i th particle, another state variable $\mathbf{p}_i = (p_i, p_i, \dots, p_i)$ is utilized to describe the best position the i th particle ever reached, which represents the experience of the i th particle itself. The initial best position variable $\mathbf{p}_i = (p_i, p_i, \dots, p_i)$ of the i th particle is commonly set to $\mathbf{p}_i = \mathbf{x}_i$ and can be updated by the following rule when the aim of optimization is to obtain the minimum value of objective function.

$$\mathbf{p}_i(t+1) = \begin{cases} \mathbf{p}_i(t) & \text{if } J(\mathbf{x}_i(t+1)) \geq J(\mathbf{p}_i(t)) \\ \mathbf{x}_i(t+1) & \text{if } J(\mathbf{x}_i(t+1)) < J(\mathbf{p}_i(t)) \end{cases} \quad (11)$$

where t denotes the number of generations and $J(\cdot)$ denotes objective function.

In SPSO, another very important variable is the global best position variable \mathbf{p}_g , which describes the best position among all the positions that all particles ever reached and represents the social shared information. The global best position \mathbf{p}_g is updated in every generation by the following rule.

$$\mathbf{p}_g(t) = \arg \min_{\mathbf{p}_i(t)} J(\mathbf{p}_i(t)) \quad (12)$$

4.2.2. Evolutionary Rules of SPSO.

With the above concepts, the evolutionary rules of SPSO can be described as

$$\begin{cases} \mathbf{v}_{ij}(t+1) = w\mathbf{v}_{ij}(t) + c_1\varphi_1(\mathbf{p}_{ij}(t) - \mathbf{x}_{ij}(t)) + c_2\varphi_2(\mathbf{p}_{gj}(t) - \mathbf{x}_{ij}(t)) \\ \mathbf{x}_{ij}(t+1) = \mathbf{x}_{ij}(t) + \mathbf{v}_{ij}(t+1) \end{cases} \quad (13)$$

where i denotes the i th particle; j denotes the j th dimension; t denotes the t th generation; w denotes the inertia weight, which often is set to be linear decrease in a interval (e.g. $[0.4, 0.9]$); and c_1, c_2 are two acceleration constants (often set in the interval $(0, 2]$); φ_1 and φ_2 are two random numbers in the interval $[0, 1]$. When a segmentation point vector \mathbf{q}_i is taken as a position vector \mathbf{x}_i in the SPSO, the constraint conditions

$$\mathbf{x}_{ij}(t+1) = \text{round}(\mathbf{x}_{ij}(t+1)) \quad (14)$$

$$\mathbf{x}_{ij}(t+1) = \begin{cases} \mathbf{x}_{ij}(t+1) & \text{if } \mathbf{x}_{ij}(t+1) > \mathbf{x}_{i(j-1)}^{\text{current}} \text{ and } \mathbf{x}_{ij}(t+1) < \mathbf{x}_{i(j+1)}^{\text{current}} \\ \mathbf{x}_{ij}(t) & \text{otherwise} \end{cases} \quad (15)$$

$x_{ij} \in \{1, 2, \dots, n\}$, $x_{ij} < x_{i(j+1)}$, ($j = 1, \dots, s-1$), $x_{i1} > 1$, $x_{is} < n$ must be satisfied, where n is the length of the time series to be segmented and s is the number of segmentation points of a segmentation point vector, *i.e.* the dimensional number of x_i . For the constraint conditions in PTSS, we need to make further processing on $x_{ij}(t+1)$ obtained by (14). where $\text{round}(a)$ denotes the nearest integer to a ; x_{ij}^{current} denotes the current value of x_{ij} ; if x_{ij}^{current} has been updated in the t th generation, then $x_{ij}^{\text{current}} = x_{ij}(t+1)$, otherwise, $x_{ij}^{\text{current}} = x_{ij}(t)$, meanwhile, for simplicity, we set $x_{i0}^{\text{current}} = 1$, $x_{i(s+1)}^{\text{current}} = n$.

Based on the above conceptions and evolutionary rules of the SPSO, a detailed PTSS algorithm based on the CI-model +SPSO is presented in **Table 2**.

4.2.3. Some Discussions

In the above subsection, we present a PTSS algorithm based on the CI-model. In fact, these two algorithms are only two feasible schemes and can be furthermore improved by different tactics.

In [11], an evolutionary PTSS algorithm is proposed for financial time series segmentation and the corresponding improved versions are presented in [12]. Here, we give a brief discussion about the relationship between these PTSS algorithms in [11,12] and the proposed CI-model based PTSS algorithms in this study. In essence, the algorithm in [11,12] optimizes the fitness objective function given in (16) by a GA optimization method with the segmentation point set of the time series as the solution.

Table 1. General CI-model based PTSS algorithm.

	1) Given the time series to be segmented and the pattern time series set.
Step1	2) Select a specific optimization objective function (e.g. the objective function of FCM clustering) and the corresponding update rules of the related variables (e.g. fuzzy membership variables in the FCM objective function). 3) Select a matching measure of time series and the corresponding data processing operations. 4) Set the desired approximate segment length $dlen$ and initialize the segmentation point set with $dlen$. 5) Select the optimization method.
Step2	Use the selected optimization method to optimize the objective function and gain the optimal segmentation point set.
Step3	Use the obtained optimal segmentation point set to get the set of time series segments.

Table 2. PTSS algorithm based on CI-model + SPSO.

	1) Given the time series to be segmented and the pattern time series set.
Step1	2) Set the approximately desired segment length $dlen$. 3) Initialize the state variables of the population. 4) Select the objective function and the corresponding update rules of the variables in this objective function.
Step2	1) Select the matching measure and the corresponding data processing operation. 2) Transform the pattern time series into the corresponding prototype vectors by a data processing operation. 3) Set the termination conditions of the SPSO.
Step3	Obtain the time series segments sets associated with different individuals, and then transform them into the corresponding data sets.
Step4	Update the corresponding variables (e.g. the FCM membership variables).
Step5	Compute the objective function values of all individuals
Step6	If the termination conditions of the SPSO are satisfied, then terminate the learning of the SPSO and go to Step 8; Otherwise, go to Step 7
Step7	Generate the next generation population with the evolutionary rules of the SPSO in (11)-(15); Then, go to Step 3.
Step8	Obtain the optimal individual, <i>i.e.</i> the optimal segmentation point vector. Furthermore, get the set of time series segments associated with the optimal segmentation point vector.

$$\text{fitness}(D_s) = \frac{1}{k} \sum_{j=1}^k \text{fitness}(S_j) \quad (16)$$

$$\text{fitness}(S_j) = \min_{\forall P_i} \{ \text{Dis}(P_i, S_j) \} \quad (17)$$

where S_j ($j = 1, 2, \dots, k$), P_i ($i = 1, 2, \dots, c$) are the obtained time series segments and the pattern time series, respectively, $\text{Dis}(\cdot)$ denotes the dissimilarity distance measure. Substituting (17) into (16), (16) can be reformulated as

$$\text{fitness}(D_s) = \frac{1}{k} \sum_{i=1}^c \sum_{j \in D_{P_i}} \text{Dis}(P_i, S_j) \quad (18)$$

$$D_{P_i} = \left\{ S_j \mid \text{Dis}(S_j, P_i) = \min_{h=1,2,\dots,c} \text{Dis}(S_j, P_h) \right\}, i = 1, 2, \dots, c \quad (19)$$

By comparing (18) with (1) (*i.e.* the objective function of K-means clustering), we find that the two objective functions are very similar if the same dissimilarity measure is adopted. The only difference is the coefficient $1/k$ in (18). In fact, the variable k only fluctuates in a narrow range by some parameter controls [11,12]. So the presented algorithm in [11] can be approximately regarded as a special case of the proposed CI-model based PTSS algorithms when the objective function of K-means clustering and GA optimization method are adopted for CI-model.

In the exiting time series segmentation algorithms, the

Gath-Geva fuzzy clustering algorithm is a representative one that has introduced the clustering technique for time series segmentation [4]. In our work, the clustering techniques are also introduced for this purpose. However, the two methods are very different. For the Gath-Geva clustering based method, the representative time series patterns are unknown. By the clustering procedure the representative time series patterns and the corresponding segmentation results are obtained. However, in our work, the proposed time series segmentation algorithms are specially designed for the pattern based time series segmentation (PTSS), where the representative patterns have been known and the aim of time series segmentation is to get the similar time series segments which are similar to a certain pattern time series in the given pattern template set. Especially, the Gath-Geva clustering based method is to segment the time series by clustering procedure and the clustering centers can be obtained as the representative patterns simultaneously, while the proposed method can be taken as the inverse procedure of clustering and the clustering centers, *i.e.* the representative patterns, are given ahead.

5. Experimental Studies

In this section, the experimental study of the proposed CI-model is carried out. To effectively investigate the performance of the CI-model, we present a performance index in (20) to evaluate the segmentation results.

$$J_{eva} = \frac{1}{k} \sum_{i=1}^c \sum_{j=D_{p_i}} D_{eva}(P_i, S_j) \quad (20)$$

$$D_{p_i} = \left\{ S_j \mid \text{sim}(S_j, P_i) = \max_{h=1,2,\dots,c} \text{sim}(S_j, P_h) \right\} \quad (21)$$

where $D_{eva} = D_{dtw}/p_l$ and p_l is the length of the warping path in the DTW measure; c and k are the number of the pattern time series and the obtained time series segments, respectively. The purpose of setting $D_{eva} = D_{dtw}/p_l$ is to effectively reduce the influence of the difference in the length of different time series segments.

At present, there is no performance index that can be proved to be absolutely fair in all cases for evaluating the segmentation results. For example, given two segmented results of a time series in a practical application, the result with the worse performance index may be considered much better by the expert. Therefore, a more elastic and appropriate evaluation index deserves further studying in future. In this study, all the experiments were carried out with the MATLAB code in the computer with 1 G ROM and 1.66 GHz CPU.

5.1. Segmentation Results Analysis

In this subsection, to demonstrate the effectiveness of the

proposed CI-model, we report segmentation results of the CI-model based PTSS algorithm on a real-world stock time series. First, the real-world stock time series are briefly described, and then the segmentation results are reported and discussed.

5.1.1. The Real-World Stock Time Series

The adopted real-world stock time series R01 is shown in **Figure 4(a)** and a pattern template set is given in **Figure 4(b)**. Here the real-world stock time series is adopted from [12]. For the real-world time series the pattern template set is used due to the fact that these pattern templates are the important technique templates to segment the stock/index time series for the trend analysis of stock market.

5.1.2. Analyses of Segmentation Results

Here, the segmentation results obtained by the CI-model based PTSS algorithm with the FCM objective function, the D_{pip} measure and the SPSO optimization are adopted for analysis purpose. In **Figure 5**, the obtained time series segments are labeled with the corresponding patterns. Each series segment is associated with one pattern in **Figure 4(b)**. With the segmentation result, the

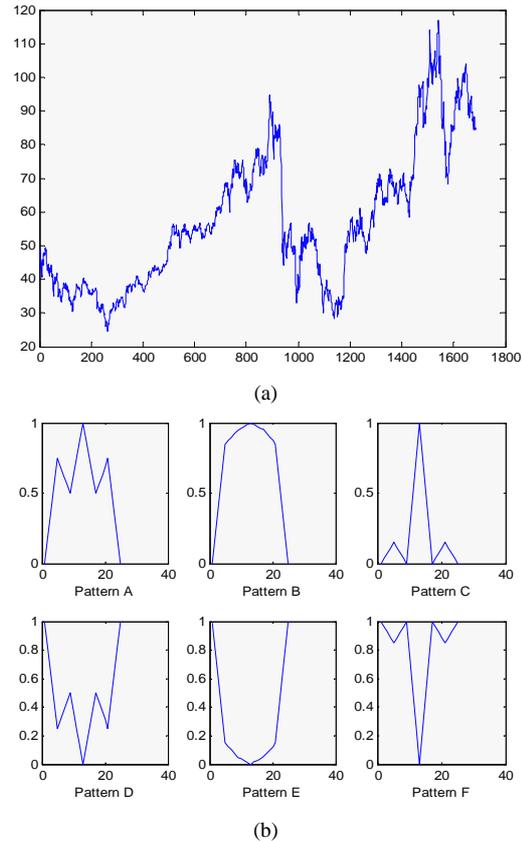


Figure 4. The real-world stock times series and the pattern template set. (a) Real-world stock time series R01; (b) the pattern template set.

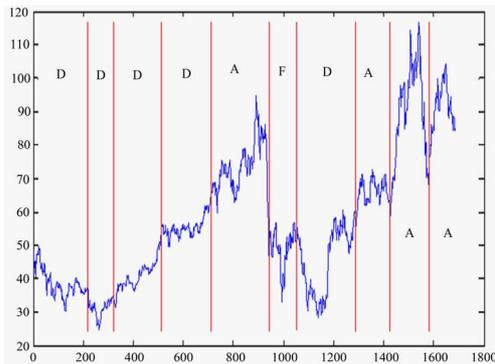


Figure 5. Segmentation results of the time series R01 with $dlen = 180$.

obtained time series mainly belong to the three classes associated with the pattern template A, D and F, respectively. From **Table 3** we can see that although some time series are classified into the same class, their membership values are different. More higher the membership value, more possible the time segment belongs to the corresponding class. The obtained segmentation result is also quite valuable for further analysis. For example, the expert may analyze the trend of stock market by these time series segments.

5.5. Image Segmentation Application

In this subsection, we give an application of the CI-model based PTSS algorithm to gray image segmentation. Image thresholding is one of the important image segmentation methods, which can find some thresholds in

the histogram of a gray image. In fact, image thresholding can be taken as a PTSS problem when the histogram of a gray image is viewed as a time series. Especially, a histogram time series usually contains the following representative technique patterns: peak and valley. The peaks and valleys usually indicate the existence of the sooth areas and edges. Therefore, a relative independent region of a gray image should correspond to a histogram time series segment which appears convex and is similar to one of pattern templates in **Figure 6**. By taking the image thresholding as a PTSS problem, we propose a PTSS based image thresholding algorithm with the following steps. 1) Obtain the histogram of a gray image; 2) Take the gray histogram as a time series and present some representative template patterns; 3) Segment the time series with the CI-model based PTSS algorithm; 4) Take the obtained time series segmentation points as the thresholds for image thresholding.

Two gray images, as shown in the left column of **Figure 7** are adopted to test the proposed image segmentation algorithm. All the images have the gray level from 0 to 255. The length of histogram time series of each image is 256, as shown in the middle column of **Figure 7**. In our experiment, the pattern template set in **Figure 6** is adopted for PTSS. In fact, some other similar pattern template set also can be adopted for the histogram time series segmentation. By large amounts of experiments, we find that with the similar pattern template sets, the segmentation results are usually approximately equivalent. In this experiment, the SPSO, the objective function

Table 3. Segmentation results of the time series R01 with $dlen = 18$.

Obtained segments			Membership function						Labels
S_i			u_{ij}						of
No.	b_i	e_i	Pattern	Pattern	Pattern	Pattern	Pattern	Pattern	clusters
			A	B	C	D	E	F	
1	1	217	0.1417	0.0142	0.0111	0.7518	0.0391	0.0419	D
2	218	321	0.0005	9.23e-005	3.59e-005	0.9757	0.0024	0.0210	D
3	322	514	0.0272	0.0014	0.0285	0.7967	0.1432	0.0028	D
4	515	710	0.0010	6.03e-005	0.0013	0.9148	0.0824	0.0003	D
5	711	942	0.9584	0.0409	0.0003	0.0002	1.68e-005	0.0001	A
6	943	1053	0.0003	0.0002	8.28e-006	0.0150	0.0002	0.9842	F
7	1054	1287	0.0036	0.0006	0.0008	0.9217	0.0503	0.0228	D
8	1288	1426	0.8792	0.1193	0.0003	0.0005	3.69e-005	0.0006	A
9	1427	1581	0.9647	0.0350	0.0002	4.55e-005	4.05e-006	2.25e-005	A
10	1582	1685	0.9918	0.0079	7.67e-005	2.19e-005	2.13e-006	1.03e-005	A

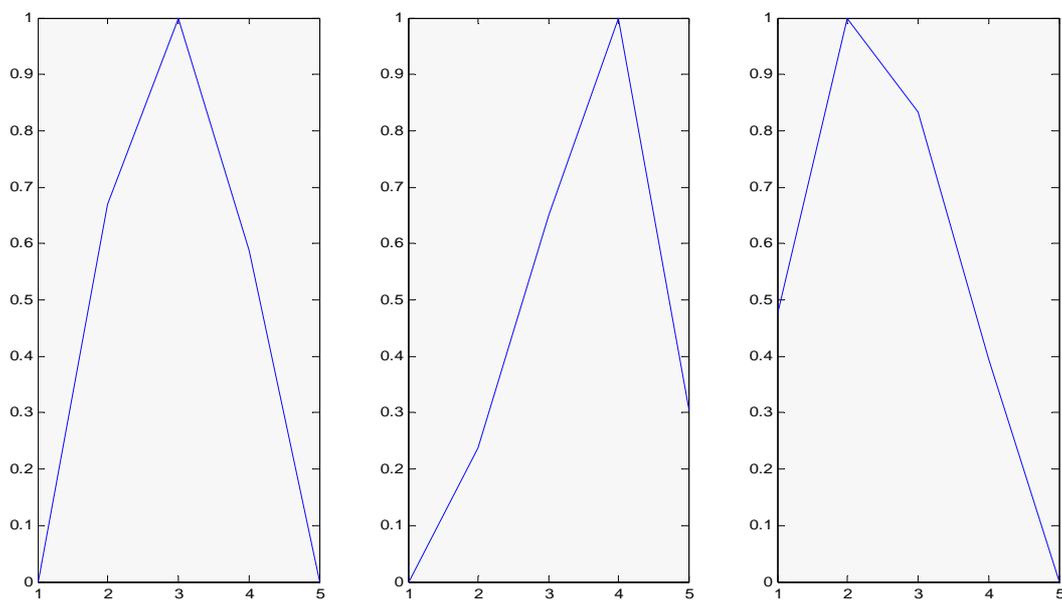


Figure 6. Proposed pattern template set for the histogram time series segmentation.

of FCNN ($\beta=10$), the D_{pdt} measure with $(r_1=1, r_2=1.5)$, and $dlen = \lceil 255/Snum \rceil$ are adopted for the proposed image segmentation algorithm. Using $Snum$ to denote the desired number of different image sections, the adopted images can be segmented into two sections with $Snum=2$. The right column of **Figure 7** shows segmentation results of the four images. We can see that the

obtained segmentation results are encouraging. As a novel method for image thresholding, the proposed algorithm is very promising.

6. Conclusions and Future Work

In this study, a new interpretation for PTSS is presented and then a generalized CI-model is proposed. A detailed

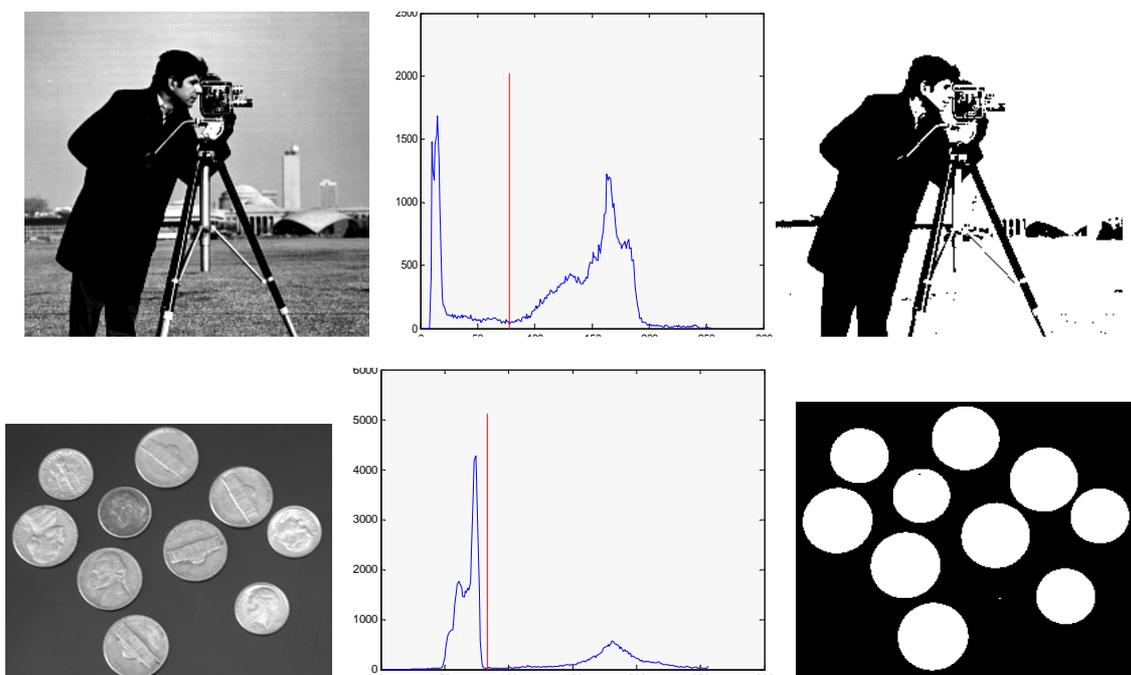


Figure 7. Segmentation results of the four gray images by the proposed CI-model based PTSS algorithm.

algorithm is proposed to implement this model. The proposed CI-model deserves furthermore studying on many aspects in future, such as the objective functions, the optimization methods, and so on. Moreover, it is also very attractive to apply the proposed CI-model based PTSS algorithms to other research fields. For example, by integrating CI-model with the biomedicine knowledge, the proposed algorithms can be adopted to analyze the biomedicine signal.

Although the proposed CI-model for PTSS has shown a promising performance, it still has the following disadvantage. The proposed CI-model based PTSS algorithms usually need more parameters to implement time series segmentation. For example, when the D_{pdt} measure is adopted two parameters for control the number of the selected PISs are required. In order to make the proposed CI-model based PTSS algorithms more efficient, the further study for the choices of these parameters is very valuable.

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