

Evaluation of Kinetic Properties of Dendritic Potassium Current in Ghostbursting Model of Electrosensory Neurons

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Abstract

A ghostbursting model is a mathematical model (a system of coupled nonlinear ordinary differential equations) that is based on the Hodgkin-Huxley formalism. The ghostbursting model describes bursting similar to the *in vitro* bursting of electrosensory neurons of weakly electric fish. Doiron and coworkers have focused on two system parameters of the model: maximal conductance of the dendritic potassium current ($g_{Dr,d}$) and the current injected into the somatic compartment (I_s).

They performed bifurcation analysis and revealed that the ($g_{Dr,d}, I_s$)-parameter space was divided into three dynamical states: quiescence, periodic tonic spiking, and bursting. The present study focused on a third system parameter: the time constant of dendritic potassium current inactivation (τ_{pd}). A computer simulation of the model revealed how the dynamical states of the ($g_{Dr,d}, I_s$)-parameter space changed in response to variations of τ_{pd} .

Keywords

Mathematical Model, Bifurcation, Ghostbursting, Time Constant

1. Introduction

Hodgkin and Huxley [1] proposed a mathematical model that is composed of a system of four-coupled nonlinear ordinary differential equations (page 518 in [1]) and that describes the action potential regeneration of the squid giant axon and the biophysical mechanisms underlying the action potential generation. Various types of mathematical models describing the electrical excitability of neurons and endocrine cells have been developed on the

basis of the concepts proposed by Hodgkin and Huxley [1], and analyses of these models, including the RPeD1 neuron model in [2], various bursting models in Chapter 5 of [3], and pituitary lactotroph bursting model in [4], are important research areas in the field of applied mathematics. The concepts proposed by Hodgkin and Huxley [1] are also important in the fields of theoretical physics [5] and mathematical physics [6]. The Hodgkin-Huxley model is also used in drug-disease modeling (see Chapter 5.2.2 in [7]).

A ghostbursting model [8], which is a mathematical model based on the concepts proposed by Hodgkin and Huxley [1], describes a system of six-coupled nonlinear ordinary differential equations [see Equations (1) to (6) in Section 2]. This model exhibits bursting similar to that observed in *in vitro* recordings of pyramidal cells in the electrosensory lateral line lobe (ELL) of the weakly electric fish *Apteronotus leptorhynchus*. This model consists of two compartments: the somatic compartment [see Equations (1) and (2) in Section 2] and the dendritic compartment [see Equations (3) to (6) in Section 2]. Doiron *et al.* have focused on two system parameters of the model: maximal conductance of the delayed-rectifying potassium current in the dendritic compartment ($g_{Dr,d}$) [see Equation (3)] and the current injected into the somatic compartment (I_s) [see Equation (1)]. They performed ($g_{Dr,d}, I_s$)-parameter bifurcation analysis of the model (see Figure 6 in [8]). This figure indicates that the organizing center of the ($g_{Dr,d}, I_s$)-parameter bifurcation diagram is a codimension-two bifurcation point and that unfolding the codimension-two bifurcation point yields two types of bifurcation manifolds: a curve for a saddle-node bifurcation of fixed points (SNFP curve) and a curve for a saddle-node bifurcation of limit cycles (SNLC curve). The SNFP and SNLC curves divide the ($g_{Dr,d}, I_s$)-parameter space into three dynamical states: quiescence, periodic tonic spiking, and bursting. When crossing the SNFP curve with an increase in I_s under a condition in which $g_{Dr,d}$ is fixed to a certain value smaller than the $g_{Dr,d}$ value at the codimension-two bifurcation point, the dynamical state changes from quiescence to bursting. When crossing the SNFP curve with an increase in I_s under a condition in which $g_{Dr,d}$ is fixed to a certain value larger than the $g_{Dr,d}$ value at the codimension-two bifurcation point, the dynamical state changes from quiescence to periodic tonic spiking. The periodic tonic spiking further changes into bursting when the SNLC curve is crossed with an increase in I_s . In addition, various bursting patterns are shown in Figure 13 in [8] and Figure 3 in [9].

Vo *et al.* have indicated that it is important to investigate the kinetic properties of ionic conductance for understanding the dynamics of pituitary cell models [10]. In other words, variations in the time constant values of ionic conductance can change the dynamical states of the cell model (Figure 4 in [10]). Doiron *et al.* have also suggested that the appropriate setting of the time constant value in dendritic potassium current inactivation is important for bursting dynamics (see the last paragraph of Section 3.3 in [8]). However, how variations in the time constant values affect the ($g_{Dr,d}, I_s$)-parameter space was not revealed in their study. Therefore, to contribute to an in-depth understanding of the kinetic properties of dendritic potassium current inactivation, in the present study, we performed numerical analysis and clarified the influence of time constant variations on the ($g_{Dr,d}, I_s$)-parameter space.

2. Materials and Methods

The ghostbursting model [Equations (1)-(6)] contains the following six state variables: the somatic membrane potential [V_s (mV)], activating variable of the somatic delayed-rectifying potassium current (n_s), dendritic membrane potential [V_d (mV)], inactivating variable of the dendritic sodium current (h_d), activating variable of the dendritic delayed-rectifying potassium current (n_d), and inactivating variable of the dendritic delayed-rectifying potassium current (p_d). The time evolution of these variables is described with the following equations:

$$C_m \frac{dV_s}{dt} = I_s - g_{Na,s} \left(\frac{1}{1 + e^{-(V_s - V_{ms})/k_{ms}}} \right)^2 (1 - n_s)(V_s - E_{Na}) - g_{Dr,s} n_s^2 (V_s - E_K) - g_L (V_s - E_L) - \frac{g_c}{\kappa} (V_s - V_d) \quad (1)$$

$$\frac{dn_s}{dt} = \frac{1}{\tau_{ns}} \left(\frac{1}{1 + e^{-(V_s - V_{ns})/k_{ns}}} - n_s \right) \quad (2)$$

$$C_m \frac{dV_d}{dt} = -g_{Na,d} \left(\frac{1}{1 + e^{-(V_d - V_{md})/k_{md}}} \right)^2 h_d (V_d - E_{Na}) - g_{Dr,d} n_d^2 p_d (V_d - E_K) - g_L (V_d - E_L) - \frac{g_c}{1 - \kappa} (V_d - V_s) \quad (3)$$

$$\frac{dh_d}{dt} = \frac{1}{\tau_{hd}} \left(\frac{1}{1 + e^{-(V_d - V_{hd})/k_{hd}}} - h_d \right) \quad (4)$$

$$\frac{dn_d}{dt} = \frac{1}{\tau_{nd}} \left(\frac{1}{1 + e^{-(V_d - V_{nd})/k_{nd}}} - n_d \right) \quad (5)$$

$$\frac{dp_d}{dt} = \frac{1}{\tau_{pd}} \left(\frac{1}{1 + e^{-(V_d - V_{pd})/k_{pd}}} - p_d \right) \quad (6)$$

where the definitions and values of the above-mentioned parameters are listed in **Table 1**. Equation (1) indicates that the time evolution of the somatic membrane potential (V_s) is regulated by the fast inward sodium current

Table 1. Values of the parameters in Equations (1)-(6) from [8].

Parameter	Value	Unit	Definition
C_m	1	$\mu\text{F}/\text{cm}^2$	Membrane capacitance
I_s	5.6 - 6.6	mA/cm^2	Current injected into somatic compartment
$g_{Na,s}$	55	mS/cm^2	Maximal conductance of the somatic sodium current
$g_{Dr,s}$	20	mS/cm^2	Maximal conductance of the somatic potassium current
$g_{Na,d}$	5	mS/cm^2	Maximal conductance of the dendritic sodium current
$g_{Dr,d}$	11.2 - 14.0	mS/cm^2	Maximal conductance of the dendritic potassium current
g_L	0.18	mS/cm^2	Leak conductance
g_c	1	mS/cm^2	Coupling coefficient
κ	0.4		Ratio of the somatic-to-total surface area
E_{Na}	40	mV	Reversal potential for the sodium ion
E_K	-88.5	mV	Reversal potential for the potassium ion
E_L	-70	mV	Reversal potential of the leak current
V_{ms}	-40	mV	Voltage at the midpoint of the steady-state function of the somatic sodium current activating variable
k_{ms}	3	mV	Slope factor of the steady-state function of the somatic sodium current activating variable
V_{md}	-40	mV	Voltage at the midpoint of the steady-state function of the dendritic sodium current activating variable
k_{md}	5	mV	Slope factor of the steady-state function of the dendritic sodium current activating variable
V_{ns}	-40	mV	Voltage at the midpoint of the steady-state function of n_s
k_{ns}	3	mV	Slope factor of the steady-state function of n_s
V_{hd}	-52	mV	Voltage at the midpoint of the steady-state function of h_d
k_{hd}	-5	mV	Slope factor of the steady-state function of h_d
V_{nd}	-40	mV	Voltage at the midpoint of the steady-state function of n_d
k_{nd}	5	mV	Slope factor of the steady-state function of n_d
V_{pd}	-65	mV	Voltage at the midpoint of the steady-state function of p_d
k_{pd}	-6	mV	Slope factor of the steady-state function of p_d
τ_{ns}	0.39	ms	Time constant of n_s
τ_{hd}	1	ms	Time constant of h_d
τ_{nd}	0.9	ms	Time constant of n_d
τ_{pd}	4.2, 5.0, 5.8	ms	Time constant of p_d

(the 2nd term), outward delayed-rectifying potassium current (the 3rd term), leak current (the 4th term), and electrotonic diffusive current between the somatic and dendritic compartments (the 5th term). Similarly, Equation (3) indicates that the time evolution of the dendritic membrane potential (V_d) is regulated by the fast inward sodium current (the 1st term), outward delayed-rectifying potassium current (the 2nd term), leak current (the 3rd term), and electrotonic diffusive current between the somatic and dendritic compartments (the 4th term). Equations (2), (4), (5), and (6) indicate that the activating or inactivating variables approach the steady-state function $\frac{1}{1+e^{-(v_x-v_y)/k_y}}$ ($x = s, d, y = ns, hd, nd, pd$.) at a rate that depends on the time constant τ_y ($y = ns, hd, nd, pd$).

For detailed explanations of the model, see [8].

The free and open source software Scilab (<http://www.scilab.org/>) was used to numerically solve equations (1)-(6) under the following initial conditions: $V_s = -70$ mV, $n_s = 0.00005$, $V_d = -70$ mV, $h_d = 0.973$, $n_d = 0.002$, and $p_d = 0.697$. The response of the model to various $(g_{Dr,d}, I_s)$ values was investigated under different values of τ_{pd} . The total simulation time was 1.2 s, and the constant depolarizing current pulse (I_s) was injected between 0.1 s and 1.1 s. Otherwise, the injected current was zero.

3. Results

3.1. Reproduction of Previous Results

The ghostbursting model can show the three dynamical states: quiescence (**Figure 1(a)**), periodic tonic spiking (**Figure 1(b)**), and bursting (**Figure 1(c)**). The present study shows that the regions of these dynamical states in the $(g_{Dr,d}, I_s)$ -parameter space change in response to τ_{pd} variations (**Figure 2**). The results at low τ_{pd} are shown in **Figure 2(a)**, those at intermediate τ_{pd} are shown in **Figure 2(b)**, and those at high τ_{pd} are shown in **Figure 2(c)**. First, in the present study, we performed a simulation of the model with $(g_{Dr,d}, I_s)$ variable values set at $\tau_{pd} = 5.0$ ms (**Figure 2(b)**), which was the same condition as that used in Figure 6 in [8]. At a low I_s value ($5.6 \mu\text{A}/\text{cm}^2$), the dynamical state of the model was that of quiescence, irrespective of the $g_{Dr,d}$ value (\times in **Figure 2(b)**). An example of the time course of the somatic membrane potential during the quiescent state is shown in **Figure 1(a)**. At high I_s values ($\geq 5.8 \mu\text{A}/\text{cm}^2$), the dynamical state was that of periodic tonic spiking (\circ in **Figure 2(b)**) or bursting (\bullet in **Figure 2(b)**). In other words, when the $g_{Dr,d}$ value was small ($\leq 12.0 \text{ mS}/\text{cm}^2$), the dynamical state was that of bursting. In contrast, when the $g_{Dr,d}$ value was large ($\geq 12.2 \text{ mS}/\text{cm}^2$), the dynamical state was that of periodic tonic spiking at smaller I_s values and that of bursting at larger I_s values, and the I_s threshold between periodic tonic spiking and bursting increased as the $g_{Dr,d}$ value was increased. Examples of the time courses of the somatic membrane potential during periodic tonic spiking and bursting are shown in **Figure 1(b)** and **Figure 1(c)**, respectively. When the above-mentioned results were compared with previous findings (Figure 6 in [8]), the present numerical analysis could reproduce the previous results.

Based on the previous results (Figure 6 in [8]), SNFP was thought to occur at certain I_s values between \times and \bullet in **Figure 2(b)**. In addition, SNFP was thought to occur at certain I_s values between \times and \circ in **Figure 2(b)**. SNLC was thought to occur at certain I_s values between \circ and \bullet in **Figure 2(b)**. Codimension-two bifurcation was thought to occur at a certain $(g_{Dr,d}, I_s)$ value that is surrounded by \times , \circ , and \bullet in **Figure 2(b)**.

3.2. Effects of Changes in τ_{pd} on the $(g_{Dr,d}, I_s)$ -Parameter Space

The simulation results under conditions in which the τ_{pd} value was decreased and increased are shown in **Figure 2(a)** and **Figure 2(c)**, respectively. At a low I_s value ($5.6 \mu\text{A}/\text{cm}^2$), the dynamical state was that of quiescence, irrespective of the $g_{Dr,d}$ value (\times in **Figure 2(a)** or **Figure 2(c)**), which is the same as that shown in **Figure 2(b)**. The I_s threshold between quiescence and bursting, which is the boundary between \times and \bullet in **Figure 2(a)** and **Figure 2(c)**, is the same as that shown in **Figure 2(b)**. The I_s threshold between quiescence and periodic tonic spiking, which is the boundary between \times and \circ in **Figure 2(a)** and **Figure 2(c)**, is also the same as that shown in **Figure 2(b)**. These results suggested that changes in the τ_{pd} values did not affect SNFP.

At high I_s values ($\geq 5.8 \mu\text{A}/\text{cm}^2$), patterns similar to **Figure 2(b)** were observed. In other words, when the $g_{Dr,d}$ value was small ($\leq 12.8 \text{ mS}/\text{cm}^2$ in **Figure 2(a)** and $\leq 11.6 \text{ mS}/\text{cm}^2$ in **Figure 2(c)**), the dynamical state was that of bursting only (\bullet in **Figure 2(a)** and **Figure 2(c)**). In contrast, when the $g_{Dr,d}$ value was large ($\geq 13.0 \text{ mS}/\text{cm}^2$ in **Figure 2(a)** and $\geq 11.8 \text{ mS}/\text{cm}^2$ in **Figure 2(c)**), the dynamical state was that of periodic tonic

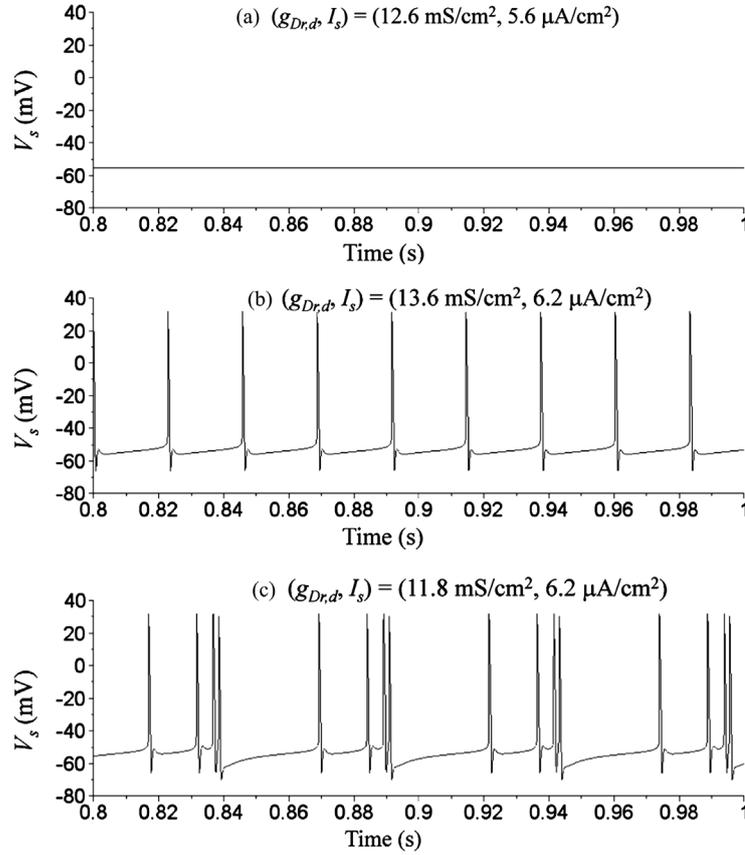


Figure 1. Examples of the time courses of the simulated somatic membrane potential (V_s) at different $g_{Dr,d}$ and I_s values at $\tau_{pd} = 5.0$ ms. (a) Quiescent state at $(g_{Dr,d}, I_s) = (12.6, 5.6)$; (b) Periodic tonic spiking state at $(g_{Dr,d}, I_s) = (13.6, 6.2)$; (c) Bursting state at $(g_{Dr,d}, I_s) = (11.8, 6.2)$.

spiking (\circ in **Figure 2(a)** and **Figure 2(c)**) at smaller I_s values and that of bursting at larger I_s values. The I_s threshold between periodic tonic spiking and bursting increased as the $g_{Dr,d}$ value increased, as illustrated in **Figure 2(a)** and **Figure 2(c)**. However, the I_s threshold between periodic tonic spiking and bursting differed among **Figure 2(a)**, **Figure 2(b)**, and **Figure 2(c)**. In other words, an increase in the τ_{pd} value with fixed $g_{Dr,d}$ values increased the I_s threshold between periodic tonic spiking and bursting. These results suggested that changes in the τ_{pd} values had a great impact on SNLC and changes in the τ_{pd} values had no influence on the I_s value of the codimension-two bifurcation point but had a great impact on the $g_{Dr,d}$ value of the codimension-two bifurcation point.

4. Discussion

In the field of dynamical systems, it is important to investigate the dependence of the solutions of ordinary differential equations on system parameters. The present study illustrates the dependence of the qualitative nature of the solutions of ordinary differential equations on the following system parameters: $g_{Dr,d}$, I_s , and τ_{pd} . In the ghost bursting model, there were three qualitatively different dynamical states: quiescence, spiking, and bursting. In particular, the present results revealed how the dynamical states of the two-dimensional $(g_{Dr,d}, I_s)$ -parameter space changed in response to variations in the third parameter τ_{pd} . These results are important in that they imply a relationship between τ_{pd} and bifurcation manifolds in the $(g_{Dr,d}, I_s)$ -parameter space. In other words, these findings suggested that an increase in the τ_{pd} value did not shift the SNFP curve in the $(g_{Dr,d}, I_s)$ -parameter space but rather shifted the SNLC curve upward. A very interesting finding in the present

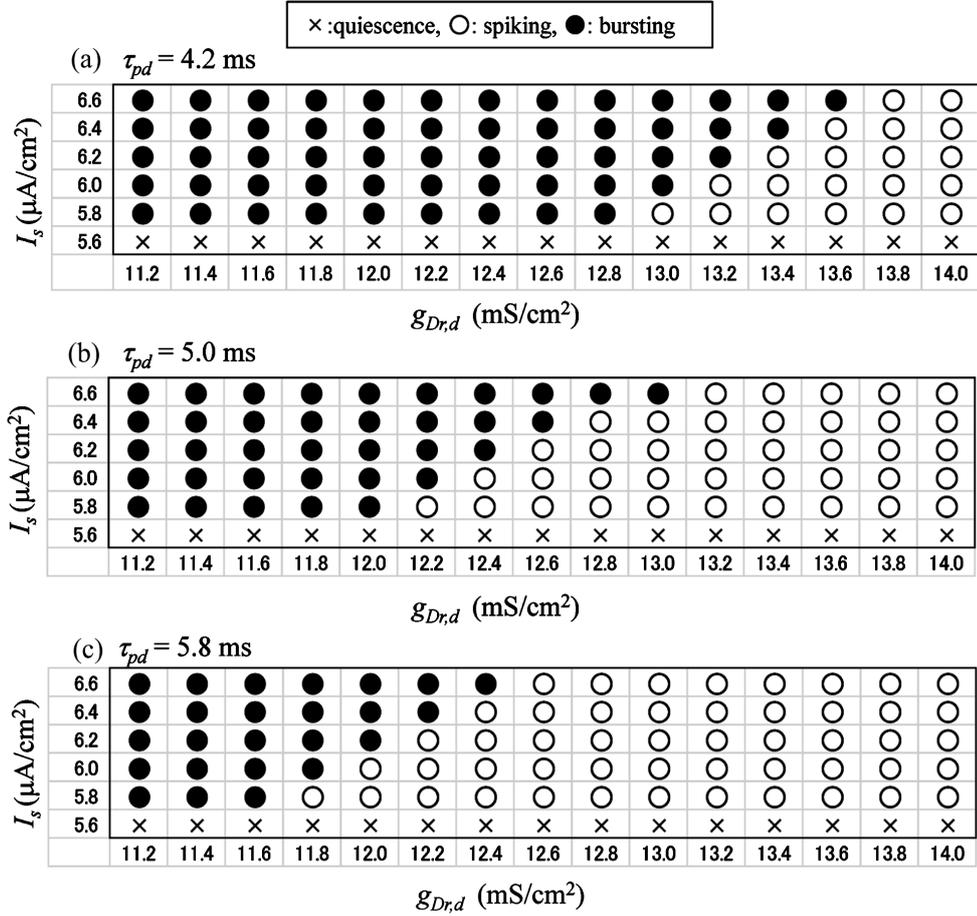


Figure 2. The effects of variations in the τ_{pd} value on the dynamical states in the two-dimensional $(g_{Dr,d}, I_s)$ -parameter space (a) $\tau_{pd} = 4.2$ ms ; (b) $\tau_{pd} = 5.0$ ms ; (c) $\tau_{pd} = 5.8$ ms . The symbols are × : quiescence, ○ : periodic tonic spiking, and ● : bursting.

study, which was not reported in the previous study [8], is that there was a nonlinear relationship between τ_{pd} and the area of the bursting state. In other words, although the amount of τ_{pd} decrease was the same (-0.8 ms) between the changes from **Figure 2(c)** to **Figure 2(b)** and the changes from **Figure 2(b)** to **Figure 2(a)**, the amount of increase in the area of the bursting state in the latter case was much larger than that in the former case.

Other examples that illustrate how the dynamical states of two-dimensional parameter space change in response to variations in the third parameter are (1) a model of CA1 pyramidal neuron spiking dynamics (Figure 12 in [11]) and (2) a compartmental model of Cheyne-Stokes respiration (Figure 5 in [12]). In analysis of the CA1 model, Bianchi *et al.* have focused on the following three parameters: the injected current (I_{inj}), half-activation voltage of the transient sodium current ($V_{1/2(\text{mNaT})}$), and half-activation voltage of the delay-rectifier potassium current ($V_{1/2(\text{mKDR})}$). Their findings revealed that the dynamical states of the two-dimensional $(V_{1/2(\text{mNaT})}, I_{inj})$ -parameter space hardly changed in response to variations in $V_{1/2(\text{mKDR})}$, while the dynamical states of the two-dimensional $(V_{1/2(\text{mKDR})}, I_{inj})$ -parameter space drastically changed in response to variations in $V_{1/2(\text{mNaT})}$. In analysis of the Cheyne-Stokes respiration model, Atamanyk and Langford focused on the following three parameters: the partial pressure of CO_2 in the inspired air (x_I), ventilation-perfusion ratio (V_A/F), and slope of the Hill function (μ). Their findings revealed that the two-dimensional $(V_A/F, \mu)$ -parameter space was divided into stable equilibria and unstable equilibria regions by a Hopf bifurcation curve and that an increase in x_I shifted the Hopf bifurcation curve upward, resulting in an expansion of the stable equilibria region.

Study [13] proposed an algorithm for the visualization of the bifurcation manifolds in the three-dimensional parameter space. In the three-dimensional parameter space, the parameter sets at which codimension one-bifurcation occurs are visualized as bifurcation surfaces. Higher codimension bifurcations are located at intersections of the bifurcation surfaces. For example, analyses of a socioeconomic model have revealed codimension-one bifurcation surfaces: a Hopf bifurcation surface and a saddle-node bifurcation surface (Figure 5 in [13]). In addition, the following codimension-two bifurcation curves were visualized: a Gavrilov-Guckenheimer bifurcation curve and a Takens-Bogdanov bifurcation curve. In contrast to the findings of the previous study [13], in the present study, we did not visualize bifurcation manifolds in the three-dimensional $(g_{Dr,d}, I_s, \tau_{pd})$ -parameter space. However, when considering the changes in the dynamical states of the two-dimensional $(g_{Dr,d}, I_s)$ -parameter space in response to variations in τ_{pd} (Figure 2), one can roughly imagine the bifurcation manifold in the three-dimensional $(g_{Dr,d}, I_s, \tau_{pd})$ -parameter space. In other words, in the three-dimensional parameter space that is defined as a three-dimensional orthogonal coordinate system with axis lines $g_{Dr,d}$, I_s and τ_{pd} , the parameter sets at which SNFP occurs are thought to form the surface of SNFP that is orthogonal to the $(g_{Dr,d}, I_s)$ plane, while the parameter sets at which SNLC occurs are thought to form the surface of SNLC that is not orthogonal to the $(g_{Dr,d}, I_s)$ plane. The parameter sets at which codimension-two bifurcation occurs are thought to form a bifurcation curve at the intersection of the surfaces of SNFP and SNLC.

5. Conclusion

In conclusion, the novelty of this paper is that it reveals in detail the influence of τ_{pd} variations on the dynamical states in the $(g_{Dr,d}, I_s)$ -parameter space of the ghostbursting model.

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