

Some Applications of the Poisson Process

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Abstract

The Poisson process is a stochastic process that models many real-world phenomena. We present the definition of the Poisson process and discuss some facts as well as some related probability distributions. Finally, we give some new applications of the process.

Keywords

Poisson Processes, Gamma Distribution, Inter-Arrival Time, Marked Poisson Processes

1. Introduction

Poisson process is used to model the occurrences of events and the time points at which the events occur in a given time interval, such as the occurrence of natural disasters and the arrival times of customers at a service center. It is named after the French mathematician Siméon Poisson (1781-1840). In this paper, we first give the definition of the Poisson process (Section 2). Then we stated some theorems related to the Poisson process (Section 3). Finally, we give some examples and compute the relevant quantities associated with the process (Section 4).

2. What Is Poisson Process?

A Poisson process with parameter (rate) $\lambda > 0$ is a family of random variables $\{N_t, t \geq 0\}$ satisfying the following properties:

- 1) $N_0 = 0$.
- 2) $N_{t_1} - N_{t_0}, N_{t_2} - N_{t_1}, \dots, N_{t_n} - N_{t_{n-1}}$ are independent random variables where $0 = t_0 < t_1 < \dots < t_n$.
- 3) $P(N_t - N_s = n) = \frac{e^{-\lambda(t-s)}}{n!} (\lambda(t-s))^n$ for $t > s$.

$N_t = N(0, t]$ can be thought of the number of arrivals up to time t or the number of occurrences up to time t .

3. Some Facts about the Poisson Process

We give some properties associated with the Poisson process. The proofs can be found in [1] or [2]. If we let $W_n, n \geq 1$ be the time of the n^{th} arrival ($W_0 = 0$), and we let $X_{n+1} = W_{n+1} - W_n, n \geq 1$, be the interarrival time ($X_1 = W_1$). Then we have the following theorems:

Theorem 1 The n^{th} arrival time has the Γ -distribution with density function $f_{W_n}(x) = \frac{\lambda(\lambda x)^{n-1}}{(n-1)!} e^{-\lambda x}$, for

$x > 0$.

Theorem 2 The interarrival times X_1, X_2, \dots are independently exponentially distributed random variables with parameter λ .

Theorem 3 Conditioned on $N_t = n$, the random variables W_1, W_2, \dots, W_n have the joint density probability function

$$f_{W_1, \dots, W_n | N_t = n}(w_1, \dots, w_n) = \frac{n!}{t^n} \text{ for } 0 < w_1 < \dots < w_n \leq t.$$

Theorem 4 If Y_k is a random variable associated with the k^{th} event in a Poisson process with parameter λ . We assume that Y_1, Y_2, \dots are independent, independent of the Poisson process, and share the common distribution function $G(y) = P(Y_k \leq y)$. The sequence of pairs $(W_1, Y_1), (W_2, Y_2), \dots$ is called a **marked Poisson process**. The $(W_1, Y_1), (W_2, Y_2), \dots$ form a two-dimensional nonhomogeneous Poisson point process in the (t, y) plane, where the mean number of points in a region A is given by

$$\mu(A) = \iint_A \lambda g(y) dy dt.$$

The marked Poisson processes have been applied in some geometric probability area [3].

4. Examples of Poisson Processes

1) Suppose the number of calls to a phone number is a Poisson process $N_t, t \geq 0$ with parameter λ and $\tau \sim \exp(\mu)$ is the duration of each call. It is reasonable to assume that τ is independent of the Poisson process. What is the probability p that the $(n+1)^{\text{st}}$ call gets a busy signal, i.e. it comes when the user is still responding to the n^{th} call?

For a fixed τ ,

$$\begin{aligned} P(W_n + \tau > W_{n+1} | \tau) &= P(W_{n+1} - W_n < \tau | \tau) = P(X_{n+1} < \tau | \tau) = \int_0^\tau \lambda e^{-\lambda x} dx = 1 - e^{-\lambda \tau} \\ p &= \int_0^\infty P(W_n + \tau > W_{n+1} | \tau) f(\tau) d\tau = \int_0^\infty P(W_n + \tau > W_{n+1} | \tau) \mu e^{-\mu \tau} d\tau \\ &= \int_0^\infty (1 - e^{-\lambda \tau}) \mu e^{-\mu \tau} d\tau = 1 - \mu \int_0^\infty e^{-(\lambda + \mu)\tau} d\tau = \frac{\lambda}{\lambda + \mu} \end{aligned}$$

2) On average, how many calls arrive when the user is on the phone?

Suppose the user is talking on the n^{th} call,

$$\begin{aligned} E[N(W_n, W_n + \tau) | \tau] &= E[N(0, \tau) | \tau] = E[N_\tau | \tau] = \lambda \tau \\ E[N(W_n, W_n + \tau)] &= E[\lambda \tau] = \lambda E[\tau] = \frac{\lambda}{\mu} \end{aligned}$$

3) In a single server system, customers arrive in a bank according to a Poisson process with parameter λ and each customer spends $\tau \sim \exp(\mu)$ time with the one and only one bank teller. If the teller is serving a customer, the new customers have to wait in a queue till the teller finishes serving. How long on average does the teller serves the customers up to time T ? (i.e. How long is the server unavailable?)

$$\begin{aligned} E\left[\sum_{n=1}^{N_T} \tau_n\right] &= \sum_{j=0}^{\infty} E\left[\sum_{n=1}^{N_T} \tau_n \mid N_T = j\right] P(N_T = j) = \sum_{j=0}^{\infty} E\left[\sum_{n=1}^j \tau_n \mid N_T = j\right] \frac{e^{-\lambda T} (\lambda T)^j}{j!} \\ &= \sum_{j=0}^{\infty} E\left[\sum_{n=1}^j \tau_n\right] \frac{e^{-\lambda T} (\lambda T)^j}{j!} = \sum_{j=0}^{\infty} \frac{j}{\mu} \frac{e^{-\lambda T} (\lambda T)^j}{j!} = \frac{\lambda}{\mu} T e^{-\lambda T} \sum_{j=1}^{\infty} \frac{1}{(j-1)!} (\lambda T)^{j-1} = \frac{\lambda}{\mu} T e^{-\lambda T} e^{\lambda T} = \frac{\lambda}{\mu} T \end{aligned}$$

4) Suppose team A and team B are engaging in a sport competition. The points scored by team A follows a Poisson process M_t with parameter λ and the points scored by team B follows a Poisson process N_t with parameter μ . Assume that M_t and N_t are independent, what is the probability that the game ties? Team A wins? Team B wins?

Let T be the duration of the competition.

$$\begin{aligned} P(\text{game ties}) &= P(M_T = N_T) = \sum_{k=0}^{\infty} P(M_T = k, N_T = k) \\ &= \sum_{k=0}^{\infty} P(M_T = k) P(N_T = k) = \sum_{k=0}^{\infty} \frac{e^{-\lambda T} (\lambda T)^k}{k!} \frac{e^{-\mu T} (\mu T)^k}{k!} \\ P(\text{A wins}) &= P(M_T > N_T) = \sum_{k=0}^{\infty} \sum_{\ell=1}^{\infty} P(M_T = k + \ell, N_T = k) \\ &= \sum_{k=0}^{\infty} \sum_{\ell=1}^{\infty} P(M_T = k + \ell) P(N_T = k) = \sum_{k=0}^{\infty} \sum_{\ell=1}^{\infty} \frac{e^{-\lambda T} (\lambda T)^{k+\ell}}{(k + \ell)!} \frac{e^{-\mu T} (\mu T)^k}{k!} \\ P(\text{B wins}) &= P(N_T > M_T) = \sum_{k=0}^{\infty} \sum_{\ell=1}^{\infty} P(N_T = k + \ell, M_T = k) \\ &= \sum_{k=0}^{\infty} \sum_{\ell=1}^{\infty} P(N_T = k + \ell) P(M_T = k) = \sum_{k=0}^{\infty} \sum_{\ell=1}^{\infty} \frac{e^{-\mu T} (\mu T)^{k+\ell}}{(k + \ell)!} \frac{e^{-\lambda T} (\lambda T)^k}{k!} \end{aligned}$$

5) Given that there are k points scored in a match (by both team A and team B), what is the probability that team A scores ℓ points, where $\ell \leq k$?

$$\begin{aligned} P(M_T = \ell | M_T + N_T = k) &= \frac{P(M_T = \ell, M_T + N_T = k)}{P(M_T + N_T = k)} \\ &= \frac{P(M_T = \ell, N_T = k - \ell)}{\sum_{j=0}^k P(M_T = j, N_T = k - j)} = \frac{P(M_T = \ell) P(N_T = k - \ell)}{\sum_{j=0}^k P(M_T = j) P(N_T = k - j)} \\ &= \frac{\frac{e^{-\lambda T} (\lambda T)^\ell}{\ell!} \frac{e^{-\mu T} (\mu T)^{k-\ell}}{(k-\ell)!}}{\sum_{j=0}^k \frac{e^{-\lambda T} (\lambda T)^j}{j!} \frac{e^{-\mu T} (\mu T)^{k-j}}{(k-j)!}} = \frac{\binom{k}{\ell} \lambda^\ell \mu^{k-\ell}}{\sum_{j=0}^k \binom{k}{j} \lambda^j \mu^{k-j}} = \frac{\binom{k}{\ell} \lambda^\ell \mu^{k-\ell}}{(\lambda + \mu)^k} \end{aligned}$$

6) When does a car accident happen? Suppose a street is from west to east and another is from south to north, the two streets intersect at a point O . Cars going from west to east arrives at O follows a Poisson process W_i with parameter λ and cars going from south to east arrives at O follows a Poisson process \widetilde{W}_j with parameter μ . It is reasonable to assume that these two processes are independent. If the cars don't slow down and stop at the intersection O , then collision happens. The j^{th} car going from south to north hits the i^{th} car going from south to east if and only if $W_i \leq \widetilde{W}_j \leq W_i + \tau$, where τ is the time it takes for the car's tail to reach O , τ has density function $f_\tau(t)$.

$$\begin{aligned} P(W_i \leq \widetilde{W}_j \leq W_i + \tau | \tau) &= \int_0^\infty \int_x^{x+\tau} \frac{\lambda (\lambda x)^{i-1} e^{-\lambda x}}{(i-1)!} \frac{\mu (\mu y)^{j-1} e^{-\mu y}}{(j-1)!} dy dx \\ &P(j^{\text{th}} \text{ car from south to north hits } i^{\text{th}} \text{ car from west to east}) \\ &= \int_0^\infty P(W_i \leq \widetilde{W}_j \leq W_i + \tau | \tau) f_\tau(t) dt \\ &= \int_0^\infty \left[\int_0^\infty \int_x^{x+\tau} \frac{\lambda (\lambda x)^{i-1} e^{-\lambda x}}{(i-1)!} \frac{\mu (\mu y)^{j-1} e^{-\mu y}}{(j-1)!} dy dx \right] f_\tau(t) dt \end{aligned}$$

$$\begin{aligned}
P(\text{car collision}) &= P\left(\bigcup_{i,j} j^{\text{th}} \text{ car from south to north hits } i^{\text{th}} \text{ car from west to east}\right) \\
&\quad + P\left(\bigcup_{i,j} i^{\text{th}} \text{ car from west to east hits } j^{\text{th}} \text{ car from south to north}\right) \\
&= \sum_{i,j} \int_0^\infty \left[\int_0^{x+\tau} \frac{\lambda(\lambda x)^{i-1} e^{-\lambda x}}{(i-1)!} \frac{\mu(\mu y)^{j-1} e^{-\mu y}}{(j-1)!} dy dx \right] f_\tau(t) dt \\
&\quad + \sum_{i,j} \int_0^\infty \left[\int_0^{y+\tau} \frac{\mu(\mu y)^{j-1} e^{-\mu y}}{(j-1)!} \frac{\lambda(\lambda x)^{i-1} e^{-\lambda x}}{(i-1)!} dx dy \right] f_\tau(t) dt
\end{aligned}$$

7) Occurrences of natural disasters follow a Poisson process with parameter λ . Suppose that the time it takes to recover and rebuild after the n^{th} disaster is Y_n , assume that Y_1, Y_2, \dots are independent random variables having the common distribution functions $G(y) = P(Y_k \leq y)$. There are N_T disasters up to time T , what is the probability that everything is back to normal at time T ? This can also be used as a model for insurance claims. W_k is the time for the insurance company to receive the k^{th} claim and Y_k is the time the insurance company takes to settle it. What is the probability that the insurance company is not working on any claim at time T ?

$$\begin{aligned}
P\left(\max_{1 \leq i \leq N_T} \{W_i + Y_i\} < T\right) &= \sum_{n=0}^{\infty} P\left(\max_{1 \leq i \leq N_T} \{W_i + Y_i\} < T \mid N_T = n\right) P(N_T = n) \\
&= \sum_{n=0}^{\infty} P\left(\max_{1 \leq i \leq n} \{W_i + Y_i\} < T \mid N_T = n\right) \frac{e^{-\lambda T} (\lambda T)^n}{n!} \\
&= \sum_{n=0}^{\infty} P(W_1 + Y_1 < T, \dots, W_n + Y_n < T \mid N_T = n) \frac{e^{-\lambda T} (\lambda T)^n}{n!} \\
&= \sum_{n=0}^{\infty} n! P(U_1 + Y_1 < T, \dots, U_n + Y_n < T) \frac{e^{-\lambda T} (\lambda T)^n}{n!} \\
&= \sum_{n=0}^{\infty} P(U_1 + Y_1 < T, \dots, U_n + Y_n < T) e^{-\lambda T} (\lambda T)^n
\end{aligned}$$

where U_1, \dots, U_n are independent and uniformly distributed on $(0, T]$.

$$\begin{aligned}
P\left(\max_{1 \leq i \leq N_T} \{W_i + Y_i\} < T\right) &= \sum_{n=0}^{\infty} \left[P(U_1 + Y_1 < T) \right]^n e^{-\lambda T} (\lambda T)^n \\
&= \sum_{n=0}^{\infty} \left[\int_0^T P(U_1 + Y_1 < T \mid U_1 = u) \frac{1}{T} du \right]^n e^{-\lambda T} (\lambda T)^n \\
&= \sum_{n=0}^{\infty} \left[\int_0^T P(Y_1 < T - u \mid U_1 = u) \frac{1}{T} du \right]^n e^{-\lambda T} (\lambda T)^n \\
&= \sum_{n=0}^{\infty} \left[\int_0^T P(Y_1 < T - u) \frac{1}{T} du \right]^n e^{-\lambda T} (\lambda T)^n \\
&= \sum_{n=0}^{\infty} \left[\frac{1}{T} \int_0^T G(T - u) du \right]^n e^{-\lambda T} (\lambda T)^n \\
&= e^{-\lambda T} \sum_{n=0}^{\infty} \left[\lambda \int_0^T G(z) dz \right]^n = \frac{e^{-\lambda T}}{1 - \lambda \int_0^T G(z) dz}
\end{aligned}$$

8) Suppose that W_k is the time an insurance company receives the k^{th} claim and Y_k is the time the company takes to settle the claim. What is the average time to settle all claims received before time T ?

The average time to settle all claims received before T is

$$E\left[\max_{1 \leq k \leq N_T} \{W_k + Y_k\}\right].$$

Suppose $\tau \geq T$,

$$\begin{aligned} P\left(\max_{1 \leq k \leq N_T} \{W_k + Y_k\} < \tau\right) &= \sum_{n=0}^{\infty} P\left(\max_{1 \leq k \leq N_T} \{W_k + Y_k\} < \tau \mid N_T = n\right) P(N_T = n) \\ &= \sum_{n=0}^{\infty} P\left(\max_{1 \leq k \leq n} \{W_k + Y_k\} < \tau \mid N_T = n\right) \frac{e^{-\lambda T}}{n!} (\lambda T)^n \\ &= \sum_{n=0}^{\infty} P(W_1 + Y_1 < \tau, \dots, W_n + Y_n < \tau \mid N_T = n) \frac{e^{-\lambda T}}{n!} (\lambda T)^n \\ &= \sum_{n=0}^{\infty} n! P(U_1 + Y_1 < \tau, \dots, U_n + Y_n < \tau) \frac{e^{-\lambda T}}{n!} (\lambda T)^n \end{aligned}$$

where U_1, \dots, U_n are independent and uniformly distributed on $(0, T]$.

$$\begin{aligned} P\left(\max_{1 \leq k \leq N_T} \{W_k + Y_k\} < \tau\right) &= \sum_{n=0}^{\infty} [P(U_1 + Y_1 < \tau)]^n e^{-\lambda T} (\lambda T)^n \\ &= \sum_{n=0}^{\infty} \left[\int_0^T P(U_1 + Y_1 < \tau \mid U_1 = u) \frac{1}{T} du \right]^n e^{-\lambda T} (\lambda T)^n \\ &= \sum_{n=0}^{\infty} \left[\int_0^T P(Y_1 < \tau - u \mid U_1 = u) \frac{1}{T} du \right]^n e^{-\lambda T} (\lambda T)^n \\ &= \sum_{n=0}^{\infty} \left[\frac{1}{T} \int_0^T P(Y_1 < \tau - u) du \right]^n e^{-\lambda T} (\lambda T)^n \\ &= \sum_{n=0}^{\infty} \left[\frac{1}{T} \int_0^T G(\tau - u) du \right]^n e^{-\lambda T} (\lambda T)^n \\ &= \sum_{n=0}^{\infty} \left[\frac{1}{T} \int_{\tau-T}^{\tau} G(z) dz \right]^n e^{-\lambda T} (\lambda T)^n \\ &= e^{-\lambda T} \sum_{n=0}^{\infty} \left[\lambda \int_{\tau-T}^{\tau} G(z) dz \right]^n = \frac{e^{-\lambda T}}{1 - \lambda \int_{\tau-T}^{\tau} G(z) dz} \end{aligned}$$

Clearly, $P\left(\max_{1 \leq k \leq N_T} \{W_k + Y_k\} < \tau\right) = 0$ for $\tau < T$.

$$\begin{aligned} E\left[\max_{1 \leq k \leq N_T} \{W_k + Y_k\}\right] &= \int_0^{\infty} P\left(\max_{1 \leq k \leq N_T} \{W_k + Y_k\} > \tau\right) d\tau \\ &= T + \int_T^{\infty} P\left(\max_{1 \leq k \leq N_T} \{W_k + Y_k\} > \tau\right) d\tau \\ &= T + \int_T^{\infty} \left(1 - \frac{e^{-\lambda T}}{1 - \lambda \int_{\tau-T}^{\tau} G(z) dz}\right) d\tau \end{aligned}$$

9) Customers arrive at a shopping mall follows a Poisson process with parameter λ . The time the customers spend in the store Y_1, Y_2, \dots are independent random variables having the common distribution function $G(y) = P(Y_k \leq y)$. Let M_t be the number of customers exist up to the closing time t . What is the expected number of customers in the mall at time t ?

Condition on $N_t = n$ and let $W_1, \dots, W_n \leq t$ be the arrival time of the customers. Then customer k exists in the mall at time t if and only if $W_k + Y_k \geq t$. Let the random variable

$$\mathbb{I}\{W_k + Y_k \geq t\} = \begin{cases} 1 & \text{if } W_k + Y_k \geq t, \\ 0 & \text{if } W_k + Y_k < t. \end{cases}$$

Then $\mathbb{I}\{W_k + Y_k \geq t\} = 1$ if and only if the k^{th} customer exists in the mall at time t . Thus

$$\begin{aligned} P(M_t = m | N_t = n) &= P\left(\sum_{k=1}^{N_t} \mathbb{I}\{W_k + Y_k \geq t\} = m | N_t = n\right) \\ &= P\left(\sum_{k=1}^n \mathbb{I}\{W_k + Y_k \geq t\} = m | N_t = n\right) = P\left(\sum_{k=1}^n \mathbb{I}\{U_k + Y_k \geq t\} = m\right) \end{aligned}$$

where U_1, U_2, \dots, U_n are independent and uniformly distributed on $(0, t]$. $P\left(\sum_{k=1}^n \mathbb{I}\{U_k + Y_k \geq t\} = m\right)$ is the binomial distribution in which

$$\begin{aligned} p &= P(U_k + Y_k \geq t) = \int_0^t P(U_k + Y_k \geq t | U_k = u) \frac{1}{t} du \\ &= \int_0^t P(Y_k \geq t - u | U_k = u) \frac{1}{t} du = \frac{1}{t} \int_0^t P(Y_k \geq t - u) du \\ &= \frac{1}{t} \int_0^t [1 - G(t - u)] du = \frac{1}{t} \int_0^t [1 - G(z)] dz \end{aligned}$$

Hence,

$$\begin{aligned} P(M_t = m) &= \sum_{n=m}^{\infty} P(M_t = m | N_t = n) P(N_t = n) \\ &= \sum_{n=m}^{\infty} \frac{n!}{m!(n-m)!} p^m (1-p)^{n-m} \frac{(\lambda t)^n e^{-\lambda t}}{n!} \\ &= e^{-\lambda t} \frac{(\lambda p t)^m}{m!} \sum_{n=m}^{\infty} \frac{(1-p)^{n-m} (\lambda t)^{n-m}}{(n-m)!} \\ &= e^{-\lambda t} \frac{(\lambda p t)^m}{m!} e^{\lambda t(1-p)} = \frac{e^{-\lambda p t} (\lambda p t)^m}{m!} \end{aligned}$$

That is, the number of customers existing at time t has a Poisson distribution with mean

$$\lambda p t = \lambda \int_0^t [1 - G(y)] dy.$$

The average number of customers exist at the mall closing time is

$$E[M_t] = \frac{1}{\lambda \int_0^t [1 - G(y)] dy}.$$

10) Customers arriving at a service counter follows a Poisson process with parameter λ . Let M_t be the number of customers served longer than τ up to time t . What is the distribution of M_t ?

Condition on $N_t = n$ and let $W_1, \dots, W_n \leq t$ be the arrival time of the customers. Let the random variable

$$\mathbb{I}\{Y_k > \tau\} = \begin{cases} 1 & \text{if } Y_k > \tau, \\ 0 & \text{if } Y_k \leq \tau. \end{cases}$$

Then $\mathbb{I}\{Y_k > \tau\} = 1$ if and only if the k^{th} customer served longer than τ . Thus

$$\begin{aligned} P(M_t = m | N_t = n) &= P\left(\sum_{k=1}^{N_t} \mathbb{I}\{Y_k > \tau\} = m | N_t = n\right) \\ &= P\left(\sum_{k=1}^n \mathbb{I}\{Y_k > \tau\} = m | N_t = n\right) \\ &= P\left(\sum_{k=1}^n \mathbb{I}\{Y_k > \tau\} = m\right), \end{aligned}$$

which is the binomial distribution with $p = P(Y_k > \tau) = 1 - G(\tau)$. Hence,

$$\begin{aligned} P(M_t = m) &= \sum_{n=m}^{\infty} P(M_t = m | N_t = n) P(N_t = n) \\ &= \sum_{n=m}^{\infty} \frac{n!}{m!(n-m)!} p^m (1-p)^{n-m} \frac{(\lambda t)^n e^{-\lambda t}}{n!} \\ &= e^{-\lambda t} \frac{(\lambda p t)^m}{m!} \sum_{n=m}^{\infty} \frac{(1-p)^{n-m} (\lambda t)^{n-m}}{(n-m)!} \\ &= e^{-\lambda t} \frac{(\lambda p t)^m}{m!} e^{\lambda t(1-p)} = \frac{e^{-\lambda p t} (\lambda p t)^m}{m!} \end{aligned}$$

That is, the number of customers served longer than τ has a Poisson distribution with mean

$$\lambda p t = \lambda(1 - G(\tau))t.$$

5. Conclusion

Poisson process is one of the most important tools to model the natural phenomenon. Some important distributions arise from the Poisson process: the Poisson distribution, the exponential distribution and the Gamma distribution. It is also used to build other sophisticated random process.

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